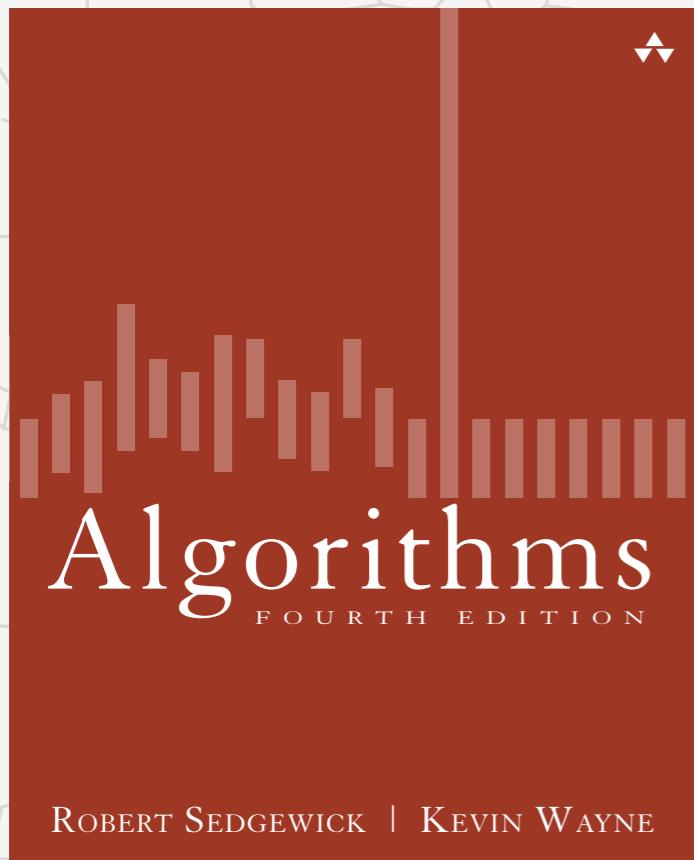


# Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE



## ALGORITHMS, PARTS I AND II

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- ▶ **overview**
- ▶ ***why study algorithms?***
- ▶ **resources**

<http://algs4.cs.princeton.edu>

# Course overview

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## What is this course?

- Intermediate-level survey course.
- Programming and problem solving, with applications.
- **Algorithm:** method for solving a problem.
- **Data structure:** method to store information.

topic	data structures and algorithms	
data types	stack, queue, bag, union-find, priority queue	
sorting	quicksort, mergesort, heapsort	part 1
searching	BST, red-black BST, hash table	
graphs	BFS, DFS, Prim, Kruskal, Dijkstra	
strings	radix sorts, tries, KMP, regexps, data compression	part 2
advanced	B-tree, suffix array, maxflow	

# Why study algorithms?

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Their impact is broad and far-reaching.

Internet. Web search, packet routing, distributed file sharing, ...

Biology. Human genome project, protein folding, ...

Computers. Circuit layout, file system, compilers, ...

Computer graphics. Movies, video games, virtual reality, ...

Security. Cell phones, e-commerce, voting machines, ...

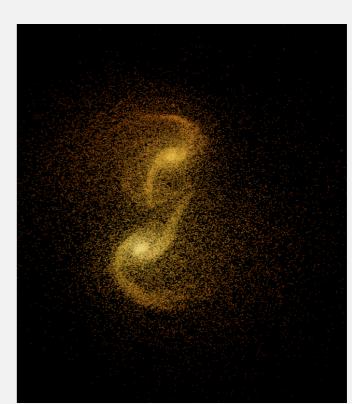
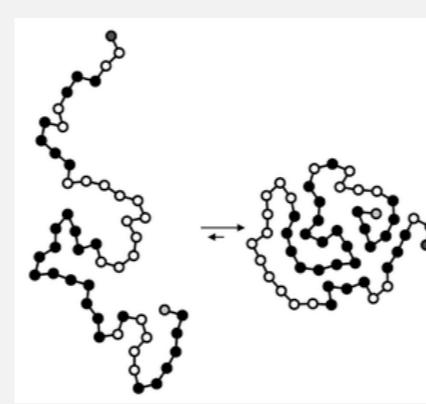
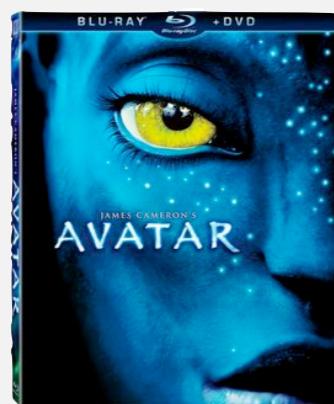
Multimedia. MP3, JPG, DivX, HDTV, face recognition, ...

Social networks. Recommendations, news feeds, advertisements, ...

Physics. N-body simulation, particle collision simulation, ...

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Google  
YAHOO!<sup>®</sup>  
bing<sup>™</sup>

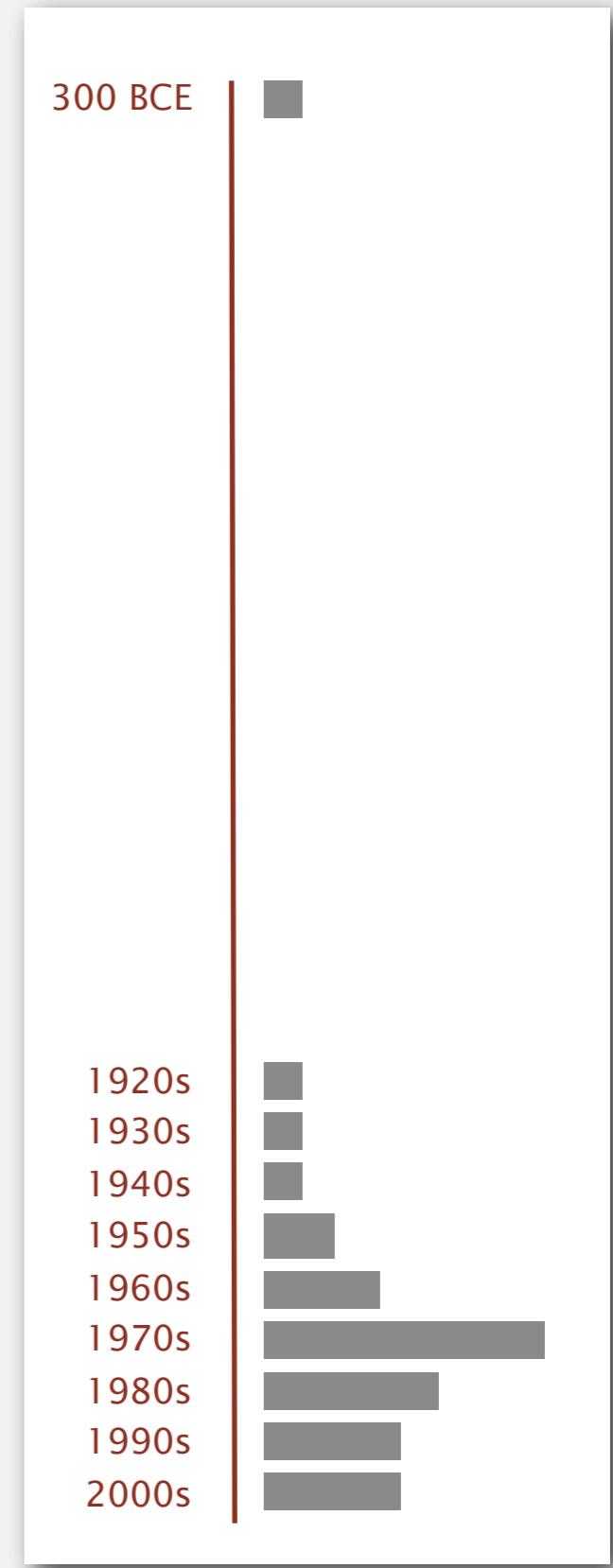


# Why study algorithms?

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## Old roots, new opportunities.

- Study of algorithms dates at least to Euclid.
- Formalized by Church and Turing in 1930s.
- Some important algorithms were discovered by undergraduates in a course like this!

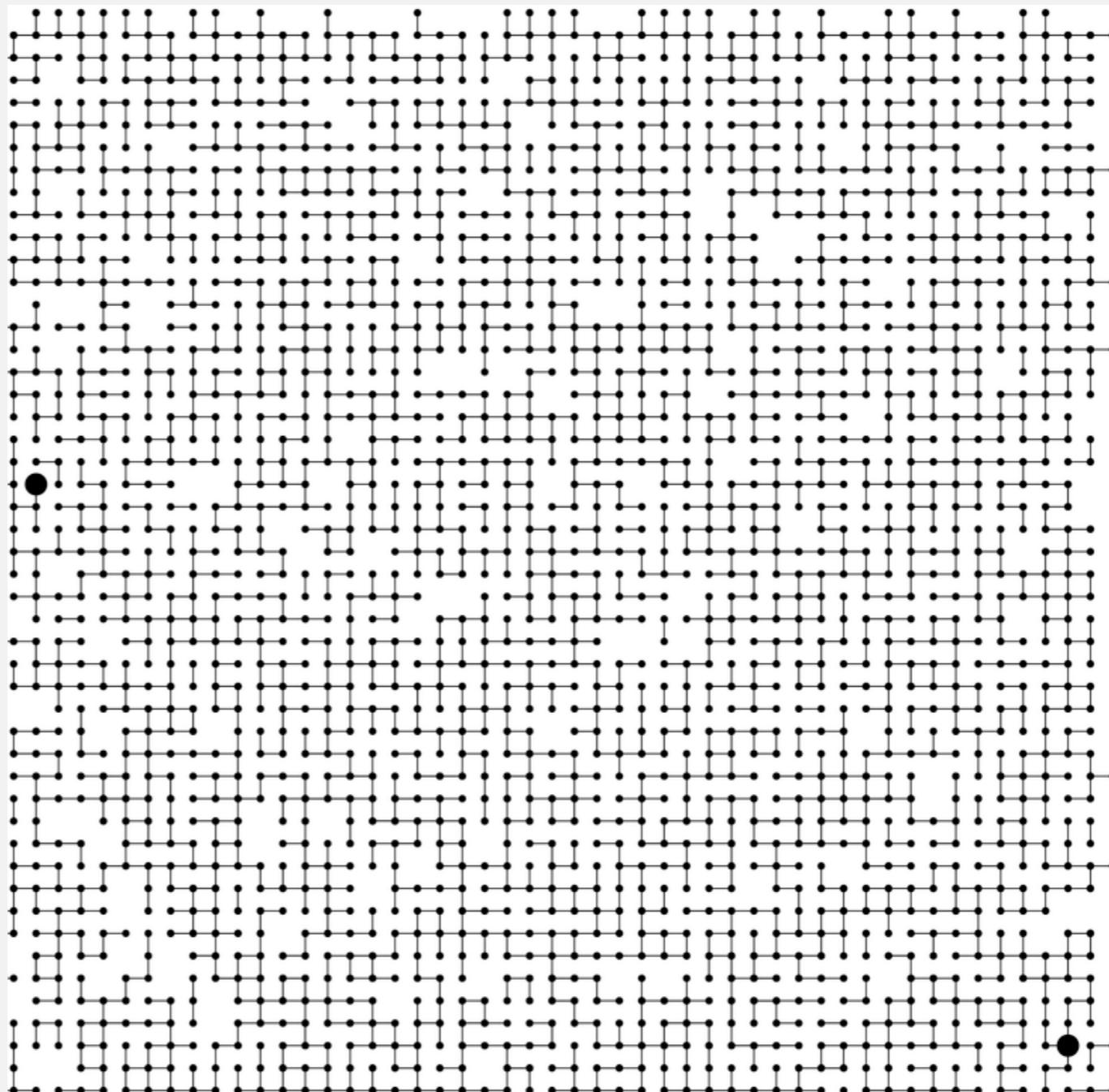


# Why study algorithms?

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To solve problems that could not otherwise be addressed.

Ex. Network connectivity. [stay tuned]

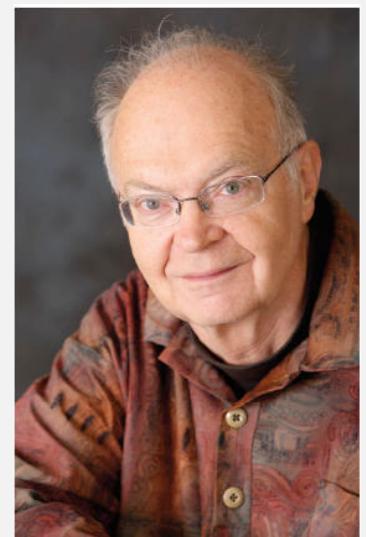


# Why study algorithms?

## For intellectual stimulation.

*“For me, great algorithms are the poetry of computation. Just like verse, they can be terse, allusive, dense, and even mysterious. But once unlocked, they cast a brilliant new light on some aspect of computing.” — Francis Sullivan*

*“ An algorithm must be seen to be believed. ” — Donald Knuth*



FROM THE  
EDITORS

# THE JOY OF ALGORITHMS

Frances Sullivan, Associate Editor-in-Chief

**T**HE THEME OF THIS FIRST-OF-THE-CENTURY ISSUE OF COMPUTING IN SCIENCE & ENGINEERING IS ALGORITHMS. IN FACT, WE WERE BOLD ENOUGH—AND PERHAPS FOOLISH ENOUGH—TO CALL THE 10 EXAMPLES WE’VE SELECTED “THE TOP 10 ALGORITHMS OF THE CENTURY.”

Computational algorithms are probably as old as civilization. Sumerian cuneiform, one of the most ancient written records, contains partly of algebraic descriptions for calculating in base 60. And the Chinese, Greeks, Indians, and Babylonians were estimating the sum of series that is embodied in Stirling’s formula. (That’s really hard, however!)

Like most other topics that technology affects, algorithms have been in vogue and unexpected ways since the 20th century—at least it looks that way to us now. The algorithms that we use today are everywhere: in communications, health care, manufacturing, economics, weather prediction, defense, and fundamental science. Consider, for example, the area of search engines. At the Maryland Shore where someone asked, “Who first ate a sandwich?” Google’s algorithm was the first to respond. Speculations about the observed behavior of gel galaxies, someone gave what must be the right answer—“A very hungry person.”

The flip side to “necessity is the mother of invention” is “invention creates its own necessity.” Our need for powerful mathematics, for example, has led to the development of new computation brings insights that suggest the next, usually much larger, computation to be done. New algorithms are an integral part of our culture. We are so used to them that we hardly notice them. We’ve become accustomed to gaining the Moore’s Law factor of two every 18 months. In effect, Moore’s Law is a consequence of the fact that computation is a function of time. Important new algorithms do not come along every 1.5 years, but when they do, they can change the world.

For me, great algorithms are the poetry of computation. Just like verse, they can be terse, allusive, dense, and even

mysterious. But once unlocked, they cast a new light on some aspect of computing. A colleague recently claimed that he’d done only 15 minutes of productive work in his office over the past year. I asked him what he had done. He responded that while he sketched out a fundamental optimization algorithm, he regarded the previous years of work as “research in progress” at a scale that might or might not have paid off.

Researchers have cracked many hard problems since 1 January 2000. One of the most interesting is the problem of the next century. In spite of a lot of good work, the question of how to extract information from extremely large masses of data is still a difficult challenge. Another is the problem of finding more efficient ways to tasks, too. For example, we need efficient methods to tell when the result of a large computation is correct. This is a problem that goes to the very heart of what a function does. The added computational cost is very small, but the added confidence in the answer is large.

Another problem is the need for better ways to do “iterative optimization.” At an even deeper level is the issue of reasonable methods for solving specific cases of “impossible” problems. For example, how do we find the best solution to a problem by attempting to answer many similar questions? Are there efficient ways to attack them?

As we move forward, things will be ripe for another revolution in our understanding of the basis of computational theory. Questions already arising from quantum computing, for example, are forcing us to reconsider the notion of random numbers seem to require that we somehow tie theories of computing, logic, and the nature of the

The new century is going to be very useful for us, but it is not going to be dull either! ■

2 COMPUTING IN SCIENCE & ENGINEERING

# Why study algorithms?

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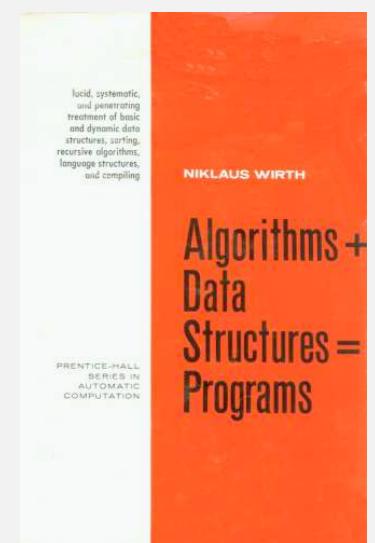
To become a proficient programmer.

*“I will, in fact, claim that the difference between a bad programmer and a good one is whether he considers his code or his data structures more important. Bad programmers worry about the code. Good programmers worry about data structures and their relationships. ”*

— Linus Torvalds (creator of Linux)



“Algorithms + Data Structures = Programs.” — Niklaus Wirth



# Why study algorithms?

They may unlock the secrets of life and of the universe.

Computational models are replacing math models in scientific inquiry.

$$E = mc^2$$

$$F = ma$$

$$\left[ -\frac{\hbar^2}{2m} \nabla^2 + V(r) \right] \Psi(r) = E \Psi(r)$$

20<sup>th</sup> century science  
(formula based)

$$F = \frac{Gm_1 m_2}{r^2}$$

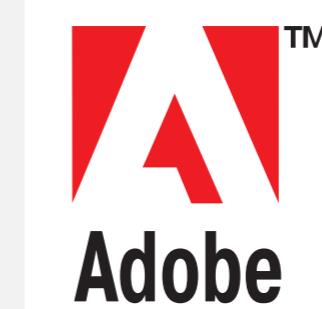
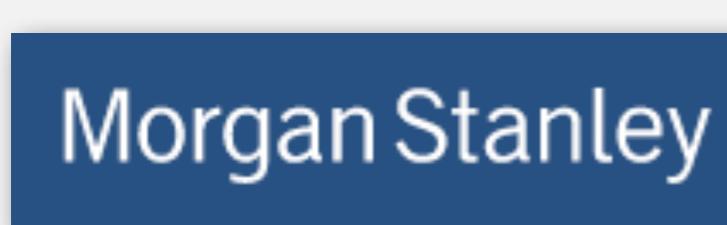
```
for (double t = 0.0; true; t = t + dt)
    for (int i = 0; i < N; i++)
    {
        bodies[i].resetForce();
        for (int j = 0; j < N; j++)
            if (i != j)
                bodies[i].addForce(bodies[j]);
    }
```

21<sup>st</sup> century science  
(algorithm based)

“Algorithms: a common language for nature, human, and computer.” — Avi Wigderson

# Why study algorithms?

For fun and profit.



# Why study algorithms?

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- Their impact is broad and far-reaching.
- Old roots, new opportunities.
- To solve problems that could not otherwise be addressed.
- For intellectual stimulation.
- To become a proficient programmer.
- They may unlock the secrets of life and of the universe.
- For fun and profit.

Why study anything else?

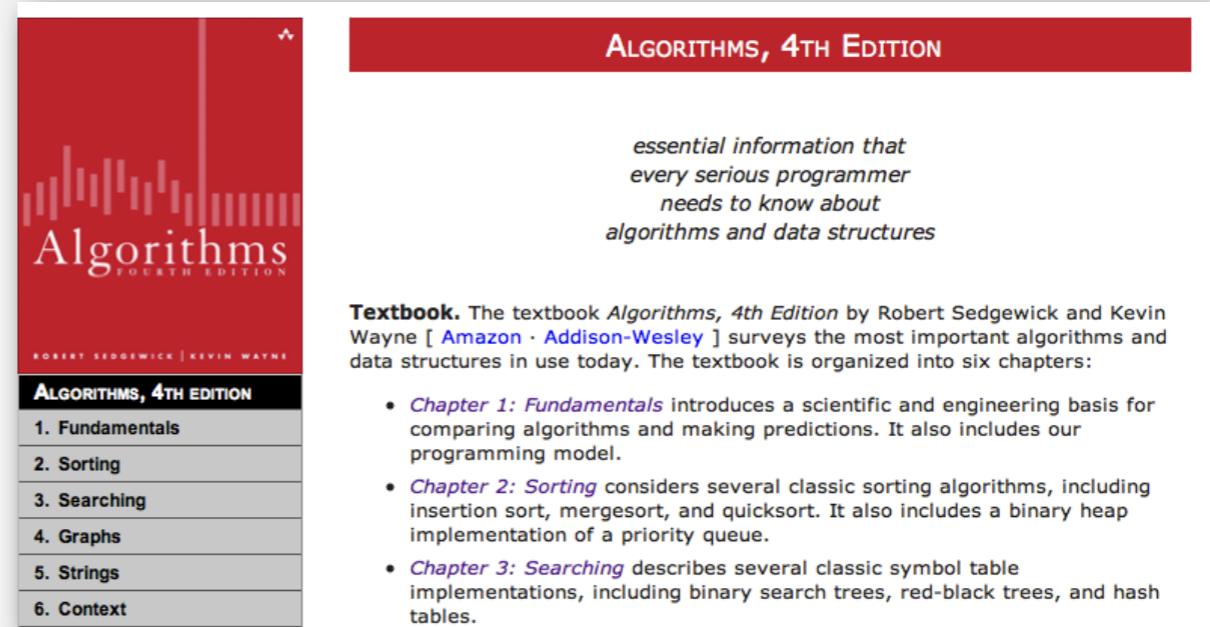


# Resources

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## Booksite.

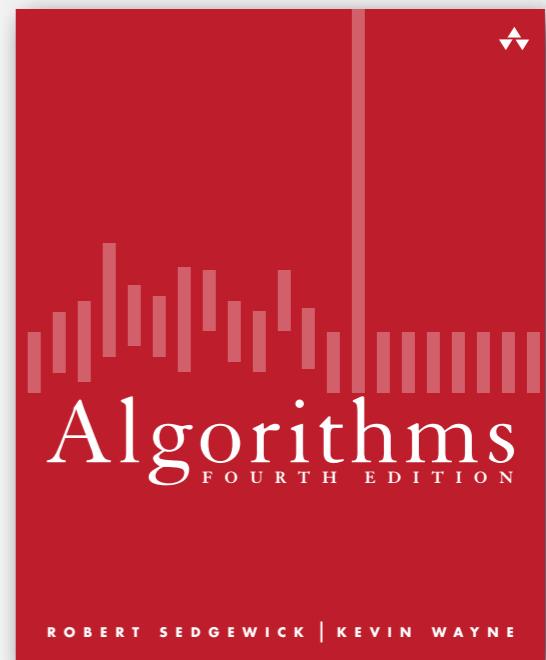
- Lecture slides.
- Download code.
- Summary of content.



<http://algs4.cs.princeton.edu>

## Textbook (optional).

- *Algorithms, 4<sup>th</sup> edition* by Sedgewick and Wayne.
- More extensive coverage of topics.
- More topics.



ISBN 0-321-57351-X

# Prerequisites

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## Prerequisites.

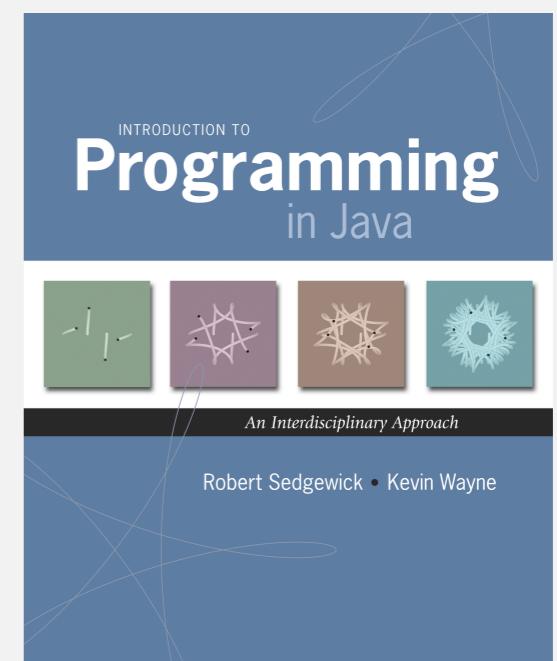
- Programming: loops, arrays, functions, objects, recursion.
- Java: we use as expository language.
- Mathematics: high-school algebra.

## Review of prerequisite material.

- Quick: Sections 1.1 and 1.2 of *Algorithms, 4<sup>th</sup> edition*.
- In-depth: *An Introduction to programming in Java: an interdisciplinary approach* by Sedgewick and Wayne.

## Programming environment.

- Use your own, e.g., Eclipse.
- Download ours (see instructions on web).



Quick exercise. Write a Java program.

ISBN 0-321-49805-4

<http://introcs.cs.princeton.edu>