

## Big O Analysis

In the context of Big O analysis, it is well-established that **Merge Sort** has a time complexity of  $O(n \log n)$ , while **Bubble Sort** exhibits a time complexity of  $O(n^2)$ . To experimentally validate these complexities, I utilized a custom `SystemTick` interrupt to measure the execution time required to perform these sorting algorithms.

As illustrated in the accompanying figures, the time taken for sorting arrays of various lengths is recorded in a tabulated format for both algorithms. For **Merge Sort**, the data demonstrates a clear proportionality to an  $n \log n$  function, with the constant factor derived and presented. In the case of **Bubble Sort**, the observed times align closely with a quadratic function ( $n^2$ ), and a best-fit quadratic equation was calculated to minimize the error between theoretical and observed values.

In summary, as the array length increases, the measured execution times for these algorithms adhere to their respective theoretical growth rates. The results confirm that the runtime of **Merge Sort** is proportional to  $n \log n$  while the runtime of **Bubble Sort** grows quadratically with the input size.

$x_2$	$y_2$	$x_2$	$y_2$
5	5	5	4
10	14	10	15
15	24	15	34
20	34	20	60
25	46	25	95
30	57	30	141
35	69	35	192
40	82	40	249
45	96	45	317
50	111	50	391
55	122	55	469
60	137	60	561
65	151	65	654
70	165	70	761
75	179	75	868
80	193	80	989
85	210	85	1119
90	225	90	1250
95	241	95	1392
100	256	100	1541

