



PES University, Bengaluru
(Established under Karnataka Act No. 16 of 2013)

UE14EE353

MAY 2017: END SEMESTER ASSESSMENT (ESA) B.TECH. VI SEMESTER

UE14EE353- DIGITAL SIGNAL PROCESSING

Time: 3 Hrs

Answer All Questions

Max Marks: 100

1.	a)	The input sequence $x(n)$ of length 100 is convolved with a unit sample sequence of length 64 using 128-point DFT. Indicate I) number of zeros appended if convolution preferred is circular. II) Length of linear convolution and is there an aliasing? III) for what index values n circular and linear convolution results are same?	06
	b)	Find the inverse DFT of $Y(k) = X(k) ^2$ where $X(k)$ is the 6 point DFT of $x(n) = u(n) - u(n-4)$.	06
	c)	Use known standard DFT's to compute 10 point DFT of $x(n) = \delta(n) + \frac{1}{5} + \cos(\frac{3\pi n}{5})$. $0 \leq n \leq 9$. Also mention any property used.	08
2.	a)	Give 2 – point DFT computational equation if time and frequency variables are independently decimated and show pictorial representation highlighting multiplication and additions involved.	06
	b)	A long input data sequence of length 2000 is to be filtered using impulse sequence of length 250. Suppose a 256 point DFT – IDFT is employed, compute the number of DFT & IDFT necessary by overlap save and overlap add methods.	06
	c)	Apply radix – 2 DIT – FFT technique to compute 8 – point DFT of 8 – point <i>circularly even</i> real sequence given the first five samples as $x(n) = \{1, 0, 1, 0, 0\}$.	08
3.	a)	In each of the following filter functions identify the <i>type</i> , <i>order</i> of filter and associated <i>frequencies</i> and <i>magnitude at dc frequency</i> , if applicable. i) $H(s) = \frac{s^2 + 100^2}{(s + 100)^2}$ ii) $H(s) = \frac{s}{s + 60}$	06
	b)	Use examples to prove that angle of separation between poles is a function of filter order in analog Butterworth filter.	06
	c)	Design a low pass analog filter to satisfy the following requirements: ➤ Monotonic response in pass band and stop band ➤ –3 dB attenuation in pass band at an edge frequency of 100 rad/s ➤ –20 dB stop band attenuation at an edge frequency of 400 rad/s	08
4.	a)	Realize the filter function given in adjacent box in direct form 2 & cascaded form with least number of delays. $H(z) = \frac{(1 + z^{-1})^2}{(1 + \frac{1}{2}z^{-1})(1 + \frac{5}{4}z^{-1} + \frac{1}{4}z^{-2})}$	06

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	b)	Causal digital filter function obtained by Bilinear transformation with $T = 2$ s is $\frac{5z^2 + 4z - 1}{8z^2 + 4z}$. Determine the parent analog transfer function.	06
	c)	Design a first order digital highpass Butterworth filter to satisfy the requirement of -3 dB ripple in pass band at a cutoff frequency of 3000Hz. Assume 8000Hz as the sampling frequency. Use Bilinear transformation.	08
5.	a)	Suggest a suitable window and calculate window length, assuming a transition frequency of 500 Hz & sampling frequency of 5000 Hz, given: <ul style="list-style-type: none"> i. Attenuation of near 0 dB in pass band & 70 dB in stop band ii. Attenuation of near 1 dB in pass band & 25 dB in stop band iii. Attenuation of near 0.02 dB in pass band & 55 dB in stop band 	06
	b)	Find order N & control parameter β of Kaiser window given the frequency specifications: <ul style="list-style-type: none"> ▪ Cutoff frequency 2200π rad/s ▪ Transition width 900π rad/s ▪ Sampling frequency 12000Hz ▪ Pass band ripple 0.015dB ▪ Maximum stop band attenuation 50dB. 	06
	c)	Design a lowpass linear phase FIR filter using Hamming window to satisfy following requirements: Passband edge frequency: 1.3 kHz Stopband edge frequency: 4.5 kHz Sampling frequency: 8 kHz.	08