# student-success-analysis

#### Data loading and getting the feeling of the dataset

```
students_org <- readxl::read_excel("student_data.xlsx")</pre>
# 370 rows, 39 columns
dim(students org)
## [1] 370 39
# Show column names
names(students_org)
                        "sex"
    [1] "school"
                                        "age"
                                                       "address"
                                                                       "famsize"
##
   [6] "Pstatus"
                        "Medu"
                                        "Fedu"
                                                       "Mjob"
                                                                       "Fjob"
                                                       "studytime"
                                                                       "failures_mat"
## [11] "reason"
                        "guardian"
                                        "traveltime"
                                                       "paid_mat"
## [16] "failures_por" "schoolsup"
                                        "famsup"
                                                                       "paid_por"
                        "nursery"
                                        "higher"
                                                       "internet"
                                                                       "romantic"
## [21] "activities"
## [26] "famrel"
                                                       "Dalc"
                                                                       "Walc"
                        "freetime"
                                        "goout"
## [31] "health"
                                                                       "G2_mat"
                        "absences_mat"
                                       "absences_por"
                                                       "G1 mat"
## [36] "G3 mat"
                        "G1 por"
                                        "G2 por"
                                                       "G3 por"
# Show first few rows
head(students_org)
## # A tibble: 6 x 39
                    age address famsize Pstatus Medu Fedu Mjob
                                                                        Fjob
##
     school sex
                                                                               reason
##
     <chr> <chr> <dbl> <chr>
                                 <chr>
                                          <chr>
                                                  <dbl> <dbl> <chr>
                                                                        <chr>
                                                                               <chr>>
## 1 GP
                     18 U
                                 GT3
                                                             4 at_home
                                                                        teach~ course
## 2 GP
            F
                      17 U
                                 GT3
                                          Т
                                                             1 at_home
                                                                        other
                                                                               course
                                                      1
            F
                                          Т
## 3 GP
                      15 U
                                 LE3
                                                             1 at_home
                                                                        other
                                                                               other
                                                      1
## 4 GP
                      15 U
            F
                                 GT3
                                         Т
                                                      4
                                                             2 health
                                                                        servi~ home
## 5 GP
            F
                      16 U
                                 GT3
                                          Т
                                                      3
                                                             3 other
                                                                        other
## 6 GP
            Μ
                      16 U
                                 LE3
                                         Τ
                                                             3 services other reputa~
## # ... with 28 more variables: guardian <chr>, traveltime <dbl>,
       studytime <dbl>, failures_mat <dbl>, failures_por <dbl>, schoolsup <chr>,
       famsup <chr>, paid mat <chr>, paid por <chr>, activities <chr>,
       nursery <chr>, higher <chr>, internet <chr>, romantic <chr>, famrel <dbl>,
## #
## #
       freetime <dbl>, goout <dbl>, Dalc <dbl>, Walc <dbl>, health <dbl>,
## #
       absences_mat <dbl>, absences_por <dbl>, G1_mat <dbl>, G2_mat <dbl>,
       G3_mat <dbl>, G1_por <dbl>, G2_por <dbl>, G3_por <dbl>
# Show details for each column
summary(students_org)
       school
                                                               address
##
                            sex
                                                 age
##
   Length: 370
                        Length: 370
                                            Min.
                                                   :15.00
                                                             Length: 370
    Class :character
                        Class :character
                                            1st Qu.:16.00
                                                             Class : character
    Mode :character
                        Mode :character
                                            Median :17.00
                                                             Mode :character
##
                                                  :16.58
##
                                            Mean
```

```
3rd Qu.:17.00
##
##
                                            Max.
                                                    :22.00
                                                                Fedu
##
      famsize
                          Pstatus
                                                  Medu
                                                    :0.0
##
    Length: 370
                        Length: 370
                                            Min.
                                                           Min.
                                                                   :0.000
##
    Class : character
                        Class : character
                                            1st Qu.:2.0
                                                           1st Qu.:2.000
##
    Mode :character
                        Mode :character
                                            Median:3.0
                                                           Median :3.000
##
                                            Mean :2.8
                                                           Mean
                                                                   :2.557
##
                                            3rd Qu.:4.0
                                                           3rd Qu.:3.750
##
                                            Max.
                                                    :4.0
                                                           Max.
                                                                   :4.000
##
                            Fjob
        Mjob
                                                reason
                                                                   guardian
##
    Length: 370
                        Length: 370
                                            Length: 370
                                                                Length: 370
##
    Class : character
                        Class : character
                                                                Class : character
                                            Class :character
##
    Mode :character
                        Mode :character
                                            Mode :character
                                                                Mode
                                                                      :character
##
##
##
##
                       studytime
                                       failures_mat
      traveltime
                                                         failures_por
##
    Min.
           :1.000
                     Min.
                            :1.000
                                      Min.
                                              :0.0000
                                                        Min.
                                                                :0.0000
    1st Qu.:1.000
                     1st Qu.:1.000
                                      1st Qu.:0.0000
                                                        1st Qu.:0.0000
##
                     Median :2.000
                                      Median :0.0000
##
    Median :1.000
                                                        Median: 0.0000
##
    Mean
           :1.446
                     Mean
                            :2.043
                                      Mean
                                              :0.2784
                                                        Mean
                                                                :0.1324
##
    3rd Qu.:2.000
                     3rd Qu.:2.000
                                      3rd Qu.:0.0000
                                                        3rd Qu.:0.0000
                            :4.000
                                                                :3.0000
##
    Max.
           :4.000
                     Max.
                                      Max.
                                             :3.0000
                                                        Max.
##
     schoolsup
                           famsup
                                              paid mat
                                                                   paid_por
##
    Length: 370
                        Length: 370
                                            Length: 370
                                                                Length: 370
    Class : character
                        Class : character
                                            Class : character
                                                                 Class : character
##
    Mode :character
                        Mode :character
                                            Mode :character
                                                                Mode :character
##
##
##
##
     activities
                          nursery
                                               higher
                                                                   internet
##
    Length: 370
                        Length: 370
                                            Length:370
                                                                Length: 370
##
    Class : character
                        Class : character
                                            Class : character
                                                                 Class : character
##
    Mode :character
                        Mode : character
                                            Mode :character
                                                                Mode :character
##
##
##
##
      romantic
                            famrel
                                            freetime
                                                              goout
##
    Length: 370
                        Min.
                               :1.000
                                         Min.
                                                 :1.000
                                                                  :1.000
                                                          Min.
##
    Class : character
                        1st Qu.:4.000
                                         1st Qu.:3.000
                                                          1st Qu.:2.000
##
    Mode : character
                        Median :4.000
                                         Median :3.000
                                                          Median :3.000
##
                        Mean
                               :3.935
                                         Mean
                                                :3.224
                                                          Mean
                                                                  :3.116
                        3rd Qu.:5.000
                                         3rd Qu.:4.000
                                                          3rd Qu.:4.000
##
##
                                :5.000
                                                 :5.000
                        Max.
                                         Max.
                                                          Max.
                                                                  :5.000
##
         Dalc
                          Walc
                                          health
                                                        absences mat
                                                               : 0.000
##
           :1.000
                            :1.000
                                             :1.000
                                                       Min.
    Min.
                     Min.
                                      Min.
##
    1st Qu.:1.000
                     1st Qu.:1.000
                                      1st Qu.:3.000
                                                       1st Qu.: 0.000
##
    Median :1.000
                     Median :2.000
                                      Median :4.000
                                                       Median : 4.000
##
    Mean
           :1.484
                     Mean
                            :2.295
                                      Mean
                                            :3.562
                                                       Mean
                                                              : 5.381
##
    3rd Qu.:2.000
                     3rd Qu.:3.000
                                      3rd Qu.:5.000
                                                       3rd Qu.: 8.000
##
    Max.
           :5.000
                            :5.000
                                             :5.000
                                                              :75.000
                     Max.
                                      Max.
                                                       Max.
##
     absences por
                          G1_mat
                                           G2_mat
                                                            G3_mat
##
   Min.
           : 0.000
                            : 3.00
                                       Min. : 0.00
                                                        Min.
                                                               : 0.00
                      Min.
   1st Qu.: 0.000
                      1st Qu.: 8.00
                                       1st Qu.: 9.00
                                                        1st Qu.: 8.00
```

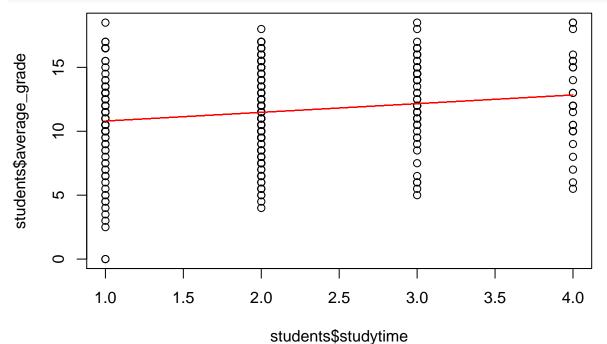
```
## Median : 2.000
                     Median :11.00
                                      Median :11.00
                                                       Median :11.00
                            :10.89
                                      Mean :10.75
   Mean : 3.632
##
                     Mean
                                                       Mean
                                                              :10.46
    3rd Qu.: 6.000
                     3rd Qu.:13.00
                                      3rd Qu.:13.00
                                                       3rd Qu.:14.00
           :32.000
   Max.
                     Max.
                             :19.00
                                      Max.
                                             :19.00
                                                       Max.
                                                              :20.00
##
##
        G1 por
                        G2_por
                                         G3_por
##
          : 0.00
                    Min. : 5.00
                                     Min. : 0.00
   \mathtt{Min}.
   1st Qu.:10.00
                    1st Qu.:11.00
                                     1st Qu.:11.00
                    Median :12.00
                                     Median :13.00
##
  Median :12.00
## Mean :12.14
                    Mean :12.27
                                     Mean :12.55
## 3rd Qu.:14.00
                    3rd Qu.:14.00
                                     3rd Qu.:14.00
## Max.
           :19.00
                    Max.
                           :19.00
                                     Max.
                                            :19.00
# Check the class of the column. "numeric", "character"...
sapply(students_org, class)
##
         school
                                                              famsize
                                                                            Pstatus
                                                 address
                                       age
    "character"
                 "character"
                                                          "character"
##
                                 "numeric"
                                            "character"
                                                                        "character"
##
           Medii
                        Fedu
                                      Mjob
                                                    Fjob
                                                               reason
                                                                           guardian
##
      "numeric"
                   "numeric"
                               "character"
                                             "character"
                                                          "character"
                                                                        "character"
##
     traveltime
                   studytime failures_mat failures_por
                                                            schoolsup
                                                                             famsup
##
      "numeric"
                   "numeric"
                                 "numeric"
                                              "numeric"
                                                          "character"
                                                                        "character"
##
       paid mat
                    paid_por
                                activities
                                                nursery
                                                               higher
                                                                           internet
##
    "character"
                 "character"
                               "character"
                                            "character"
                                                          "character"
                                                                        "character"
##
       romantic
                      famrel
                                  freetime
                                                  goout
                                                                 Dalc
                                                                               Walc
##
    "character"
                   "numeric"
                                 "numeric"
                                              "numeric"
                                                            "numeric"
                                                                          "numeric"
##
         health absences_mat absences_por
                                                                            G3_mat
                                                 G1_mat
                                                               G2_mat
##
      "numeric"
                   "numeric"
                                 "numeric"
                                              "numeric"
                                                            "numeric"
                                                                          "numeric"
##
         G1_por
                      G2_por
                                    G3_por
##
      "numeric"
                   "numeric"
                                 "numeric"
# Let's check if any columns exceed the maximum or minumum values specified in the pdf
# This makes sense only for numerical values
colMax <- students_org %>%
  select(where(is.numeric)) %>%
  sapply(., max, na.rm = TRUE)
colMax
##
                        Medu
                                      Fedu
                                             traveltime
                                                            studytime failures_mat
            age
##
             22
                            4
                                         4
                                                       4
                                                                    4
                                                                                  3
## failures_por
                                                                 Dalc
                                                                               Walc
                      famrel
                                  freetime
                                                  goout
##
              3
                                         5
                                                                                  5
                           5
                                                       5
                                                                    5
##
         health absences mat absences por
                                                               G2 mat
                                                                             G3 mat
                                                  G1 mat
##
                                                      19
                                                                                 20
              5
                          75
                                        32
                                                                   19
##
         G1_por
                       G2_por
                                    G3 por
##
             19
                           19
                                        19
# Every column has normal maximum value
# Are there any na values?
students_org %>% filter(is.na(.))
## # A tibble: 0 x 39
## # ... with 39 variables: school <chr>, sex <chr>, age <dbl>, address <chr>,
       famsize <chr>, Pstatus <chr>, Medu <dbl>, Fedu <dbl>, Mjob <chr>,
       Fjob <chr>, reason <chr>, guardian <chr>, traveltime <dbl>,
## #
       studytime <dbl>, failures_mat <dbl>, failures_por <dbl>, schoolsup <chr>,
```

```
famsup <chr>, paid_mat <chr>, paid_por <chr>, activities <chr>,
## #
      nursery <chr>, higher <chr>, internet <chr>, romantic <chr>, famrel <dbl>,
## #
       freetime <dbl>, goout <dbl>, Dalc <dbl>, Walc <dbl>, health <dbl>, ...
sum(apply(students_org, 2, is.nan))
## [1] 0
students_org %>% filter(is.null(.))
## # A tibble: 0 x 39
## # ... with 39 variables: school <chr>, sex <chr>, age <dbl>, address <chr>,
      famsize <chr>, Pstatus <chr>, Medu <dbl>, Fedu <dbl>, Mjob <chr>,
## #
      Fjob <chr>, reason <chr>, guardian <chr>, traveltime <dbl>,
## #
       studytime <dbl>, failures_mat <dbl>, failures_por <dbl>, schoolsup <chr>,
      famsup <chr>, paid_mat <chr>, paid_por <chr>, activities <chr>,
       nursery <chr>, higher <chr>, internet <chr>, romantic <chr>, famrel <dbl>,
## #
## #
      freetime <dbl>, goout <dbl>, Dalc <dbl>, Walc <dbl>, health <dbl>, ...
# Drop these values just in case they show up with another dataset
# We will continue using "student" variable
students <- students_org %>% filter_all(all_vars(!is.na(.) & !is.nan(.) & !is.null(.)))
```

## Petar Dragojević

```
students$average_grade <- (students$G3_mat + students$G3_por)/2

fit.studytime = lm(average_grade~studytime,data=students)
plot(students$studytime,students$average_grade)
lines(students$studytime,fit.studytime$fitted.values,col='red')</pre>
```



#Pearsonov korelacijski koeficijent
cor(students\$studytime,students\$average\_grade)

```
## [1] 0.175217
```

```
cor.test(students$studytime,students$average_grade)
```

```
##
## Pearson's product-moment correlation
##
## data: students$studytime and students$average_grade
## t = 3.4141, df = 368, p-value = 0.0007113
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## 0.07459575 0.27230630
## sample estimates:
##
       cor
## 0.175217
summary(fit.studytime)
##
## Call:
## lm(formula = average_grade ~ studytime, data = students)
## Residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                           Max
## -10.8003 -1.9801
                      0.0199
                               2.1997
                                        7.6997
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 10.1205
                           0.4404 22.981 < 2e-16 ***
                           0.1991 3.414 0.000711 ***
## studytime
                0.6798
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.243 on 368 degrees of freedom
## Multiple R-squared: 0.0307, Adjusted R-squared: 0.02807
## F-statistic: 11.66 on 1 and 368 DF, p-value: 0.0007113
#procjena modela s dummy varijablama
students.d = dummy_cols(students,select_columns='studytime')
#procjena modela s dummy varijablama
fit.multi.d = lm(average_grade ~ studytime_1 + studytime_2, students.d)
summary(fit.multi.d)
##
## lm(formula = average_grade ~ studytime_1 + studytime_2, data = students.d)
##
## Residuals:
##
                      Median
       Min
                 1Q
                                   3Q
                                           Max
## -10.7653 -1.9432
                      0.0568 2.2347
                                        7.7347
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 12.4885
                        0.3475 35.942 < 2e-16 ***
                           0.4774 -3.610 0.000349 ***
## studytime_1 -1.7232
```

```
## studytime_2 -1.0453     0.4213 -2.481 0.013550 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.241 on 367 degrees of freedom
## Multiple R-squared: 0.03468, Adjusted R-squared: 0.02942
## F-statistic: 6.592 on 2 and 367 DF, p-value: 0.00154
```

#### Tomislay Prhat

```
1. Jesu li učenici uspješniji u matematici ili glavnom jeziku?
students_org %>% summarise(
          Mean.G1_mat = mean(G1_mat),
          Mean.G2_mat = mean(G2_mat),
          Mean.G3_mat = mean(G3_mat),
          Mean.G1_por = mean(G1_por),
          Mean.G2_por = mean(G2_por),
          Mean.G3_por = mean(G3_por),
            ) -> summary.result1
summary.result1
## # A tibble: 1 x 6
     Mean.G1_mat Mean.G2_mat Mean.G3_mat Mean.G1_por Mean.G2_por Mean.G3_por
##
           <dbl>
                        <dbl>
                                    <dbl>
                                                 <dbl>
                                                             <dbl>
                                                                          <dbl>
## 1
            10.9
                        10.8
                                     10.5
                                                  12.1
                                                              12.3
                                                                           12.6
students_org %>% summarise(
          Med.G1_mat = median(G1_mat),
          Med.G2_mat = median(G2_mat),
          Med.G3 mat = median(G3 mat),
          Med.G1_por = median(G1_por),
          Med.G2_por = median(G2_por),
          Med.G3_por = median(G3_por),
            ) -> summary.result2
summary.result2
## # A tibble: 1 x 6
     Med.G1_mat Med.G2_mat Med.G3_mat Med.G1_por Med.G2_por Med.G3_por
##
          <dbl>
                     <dbl>
                                 <dbl>
                                             <dbl>
                                                        <dbl>
                                                                   <dbl>
## 1
                                                           12
             11
                         11
                                    11
                                                12
                                                                       13
students_org %>% summarise(
          Mean.G1_mat = mean(G1_mat, trim = 0.1),
          Mean.G2_mat = mean(G2_mat, trim = 0.1),
          Mean.G3_mat = mean(G3_mat, trim = 0.1),
          Mean.G1_por = mean(G1_por, trim = 0.1),
          Mean.G2_por = mean(G2_por, trim = 0.1),
          Mean.G3_por = mean(G3_por, trim = 0.1),
            ) -> summary.result3
summary.result3
## # A tibble: 1 x 6
    Mean.G1_mat Mean.G2_mat Mean.G3_mat Mean.G1_por Mean.G2_por Mean.G3_por
##
           <dbl>
                       <dbl>
                                    <dbl>
                                                 <dbl>
                                                             <dbl>
                                                                          <dbl>
## 1
            10.8
                        10.9
                                     10.9
                                                  12.1
                                                              12.2
                                                                           12.6
```

```
(1 - summary.result3/summary.result1)*100
     Mean.G1_mat Mean.G2_mat Mean.G3_mat Mean.G1_por Mean.G2_por Mean.G3_por
##
                                -4.016012
                                             0.1670379
## 1
        1.085608
                     -1.08723
                                                           0.715859 -0.7265877
Kao što je vidljivo iz podataka, učenici su malo uspješniji u glavnom jeziku (portugalskom), ali ako gleda
prema samoj ocjeni obje skupine spadaju u ocjenu "C". Čak i ako uzmemo podrezanu srednju vrijednost
(10\%), rezultat se promijeni za ~1%.
students_org %>% summarise(
          IQR.G1_mat = IQR(G1_mat),
          IQR.G2_mat = IQR(G2_mat),
          IQR.G3_mat = IQR(G3_mat),
          IQR.G1_por = IQR(G1_por),
          IQR.G2_por = IQR(G2_por),
          IQR.G3_por = IQR(G3_por),
            ) -> summary.result4
summary.result4
## # A tibble: 1 x 6
     IQR.G1_mat IQR.G2_mat IQR.G3_mat IQR.G1_por IQR.G2_por IQR.G3_por
##
          <dbl>
                      <dbl>
                                 <dbl>
                                             <dbl>
                                                         <dbl>
                                                                    <dbl>
## 1
                                                             3
students_org %>% summarise(
          Var.G1_mat = var(G1_mat),
          Var.G2_mat = var(G2_mat),
          Var.G3_mat = var(G3_mat),
          Var.G1_por = var(G1_por),
          Var.G2_por = var(G2_por),
          Var.G3_por = var(G3_por),
            ) -> summary.result5
summary.result5
## # A tibble: 1 x 6
     Var.G1_mat Var.G2_mat Var.G3_mat Var.G1_por Var.G2_por Var.G3_por
##
##
          <dbl>
                      <dbl>
                                 <dbl>
                                             <dbl>
                                                         <dbl>
                                                                    <dbl>
## 1
           11.2
                       14.4
                                   21.2
                                              6.51
                                                          6.08
                                                                     8.67
students_org %>% summarise(
          sd.G1_mat = sd(G1_mat),
          sd.G2 mat = sd(G2 mat),
          sd.G3_mat = sd(G3_mat),
          sd.G1_por = sd(G1_por),
          sd.G2_por = sd(G2_por),
          sd.G3_por = sd(G3_por),
            ) -> summary.result6
summary.result6
```

```
## # A tibble: 1 x 6
##
     sd.G1_mat sd.G2_mat sd.G3_mat sd.G1_por sd.G2_por sd.G3_por
##
         <dbl>
                    <dbl>
                               <dbl>
                                          <dbl>
                                                     <dbl>
                                                               <dbl>
## 1
          3.35
                     3.80
                                4.61
                                           2.55
                                                      2.47
                                                                2.94
```

Ako gledamo raspršenost varijabli vidimo da ocjene iz portugalskog jezika imaju manje sve tri mjere (IQR, varijanca i standardna devijacija) vidimo da se ocjene iz portugalskog manje manje odmiču od srednje vrijednosti nego ocjene iz matematike.

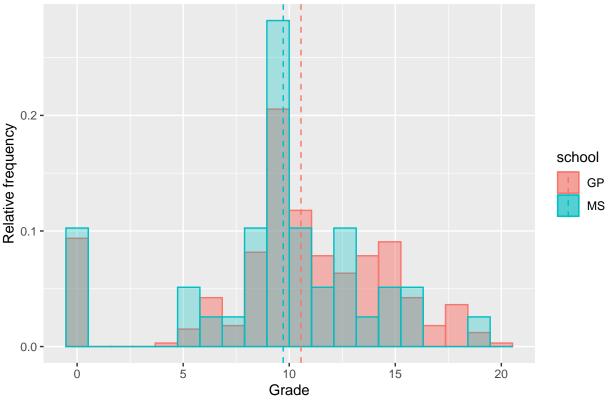
#### Matej Ciglenečki

```
# Show average grade for all schools
schools <- students %>%
  select("school") %>%
  distinct(.)
schools # [GP, MS]
## # A tibble: 2 x 1
##
     school
     <chr>>
##
## 1 GP
## 2 MS
subject_final_grade_names <- names(students)[grepl("G3", names(students))]</pre>
subject_final_grade_names
## [1] "G3_mat" "G3_por"
students_final_grade <- students %>% select("school", subject_final_grade_names)
## Note: Using an external vector in selections is ambiguous.
## i Use `all_of(subject_final_grade_names)` instead of `subject_final_grade_names` to silence this mes
## i See <https://tidyselect.r-lib.org/reference/faq-external-vector.html>.
## This message is displayed once per session.
# Select only the subject grade and school
gp_mat <- students_final_grade %>%
  filter(school == "GP") %>%
  select(G3_mat, school)
gp_por <- students_final_grade %>%
  filter(school == "GP") %>%
  select(G3_por, school)
ms_mat <- students_final_grade %>%
  filter(school == "MS") %>%
  select(G3_mat, school)
ms_por <- students_final_grade %>%
  filter(school == "MS") %>%
  select(G3_por, school)
# Rename all columns to "grade"
gp_mat <- gp_mat %>% rename(grade = G3_mat)
gp_por <- gp_por %>% rename(grade = G3_por)
ms_mat <- ms_mat %>% rename(grade = G3_mat)
ms_por <- ms_por %>% rename(grade = G3_por)
# TODO: can this data be grouped and used dynamically? (support multiple schools and mutliple subjects)
# scale_this <- function(x){</pre>
  (x - mean(x, na.rm=TRUE)) / sd(x, na.rm=TRUE)
# }
# gp_mat_scaled <- gp_mat %>% mutate(G3_mat = scale_this(G3_mat))
# gp_por_scaled <- gp_por %>% mutate(G3_por = scale_this(G3_por))
```

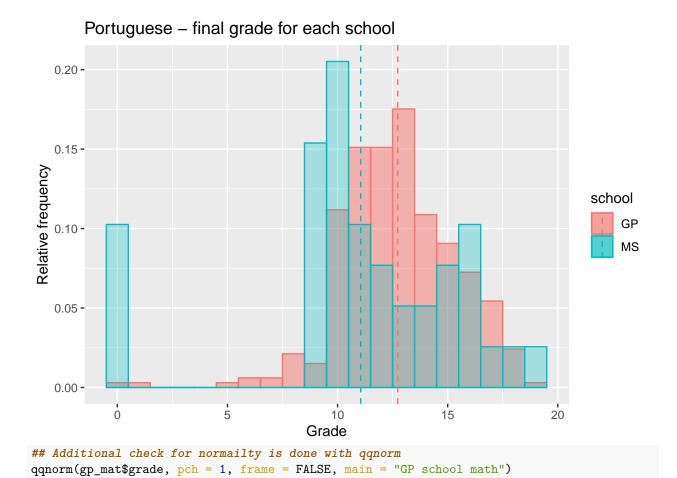
```
# ms_mat_scaled <- ms_mat %>% mutate(G3_mat = scale_this(G3_mat))
# ms_por_scaled <- ms_por %>% mutate(G3_por = scale_this(G3_por))

# Plot math -- final grade
ggplot(gp_mat, aes(x = grade, y = (..count.. / sum(..count..)))) +
    geom_histogram(bins = 20, aes(color = school, fill = school), alpha = 0.5) +
    geom_histogram(data = ms_mat, bins = 20, aes(color = school, fill = school), alpha = 0.3) +
    geom_vline(data = gp_mat, aes(xintercept = mean(grade), color = school), linetype = "dashed") +
    geom_vline(data = ms_mat, aes(xintercept = mean(grade), color = school), linetype = "dashed") +
    xlab("Grade") +
    ylab("Relative frequency") +
    labs(title = "Mathematics - final grade for each school")
```

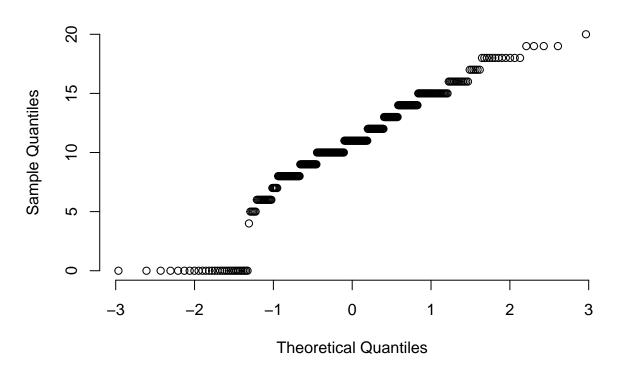
## Mathematics – final grade for each school



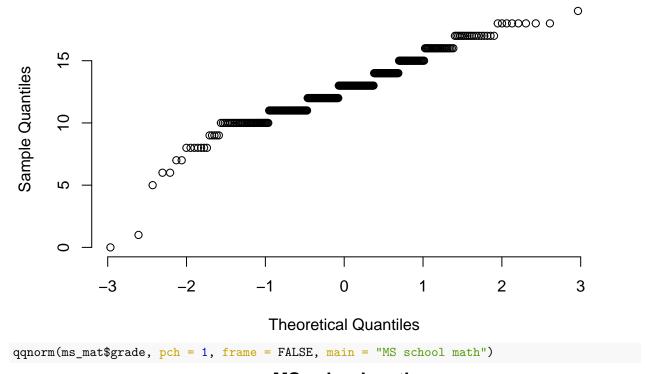
```
# Plot portug -- final grade
ggplot(gp_por, aes(x = grade, y = (..count.. / sum(..count..)))) +
  geom_histogram(bins = 20, aes(color = school, fill = school), alpha = 0.5) +
  geom_histogram(data = ms_por, bins = 20, aes(color = school, fill = school), alpha = 0.3) +
  geom_vline(data = gp_por, aes(xintercept = mean(grade), color = school), linetype = "dashed") +
  geom_vline(data = ms_por, aes(xintercept = mean(grade), color = school), linetype = "dashed") +
  xlab("Grade") +
  ylab("Relative frequency") +
  labs(title = "Portuguese - final grade for each school")
```



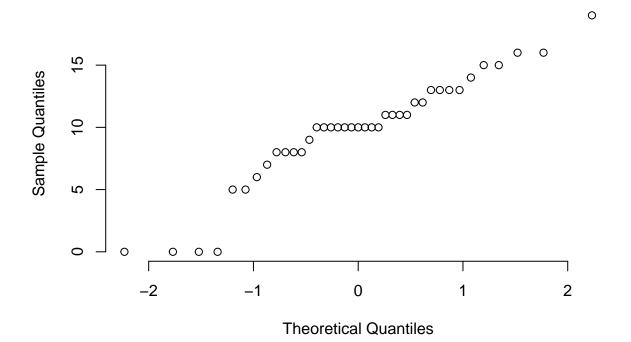
# **GP** school math



# **GP** school portuguese

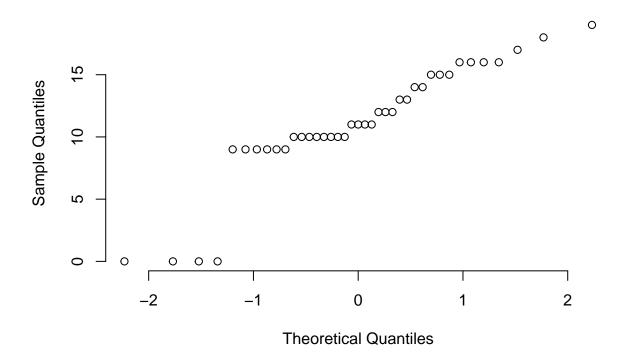


# MS school math





#### MS school portuguese



### F-test of variance equality

# HO - Variance of GP\_MAT and MS\_MAT are equal

Argument order for F-test of variance equality doesn't matter but in general:

$$\frac{\sigma_1^2}{\sigma_2^2}, \quad \sigma_1^2 > \sigma_2^2$$

 $p^-$  probability that under the null hypothesis of obtaining the value (of the test statistic) that's as extreme (or more extreme) than the value we got computed from the sample we have

If  $p < \alpha$  we are rejecting the hypothesis H0 in favor of H1 - falls under right tail => rejection

```
# Let's check variances just as a sanity check:
cat("Mathematics variances", var(gp_mat$grade), var(ms_mat$grade))

## Mathematics variances 21.38735 19.89204
cat("Portugeuse variances", var(gp_por$grade), var(ms_por$grade))

## Portugeuse variances 6.839605 22.1552

# At first glance, it seems that we will probably reject HO hypothesis for F-test in the case of Portugalpha <- 0.05</pre>
```

# H1 - not H0
mat\_f\_test <- var.test(gp\_mat\$grade, ms\_mat\$grade, alternative = "two.sided") # F = 1.0752, p = 0.817
mat\_f\_test</pre>

```
##
## F test to compare two variances
## data: gp_mat$grade and ms_mat$grade
## F = 1.0752, num df = 330, denom df = 38, p-value = 0.817
## alternative hypothesis: true ratio of variances is not equal to 1
## 95 percent confidence interval:
## 0.6349798 1.6605741
## sample estimates:
## ratio of variances
             1.075171
\# HO - Variance of GP_POR and MS_MAT are equal
# H1 - not H0
por_f_test <- var.test(gp_por$grade, ms_por$grade, alternative = "two.sided") # F = 1.0752, p = 0.817
por_f_test
## F test to compare two variances
##
## data: gp_por$grade and ms_por$grade
## F = 0.30871, num df = 330, denom df = 38, p-value = 1.217e-08
## alternative hypothesis: true ratio of variances is not equal to 1
## 95 percent confidence interval:
## 0.1823214 0.4767997
## sample estimates:
## ratio of variances
           0.3087133
# This part won't be outputed as code in PDF
cat_reject_h0 <- function(prefix_message, is_h0_rejected) {</pre>
  cat(prefix_message, "\n")
  if (is_h0_rejected) cat("\tWe are rejecting the HO hypothesis in favor of hypothesis H1\n") else cat(
}
var_equal_mat <- if (mat_f_test$p.value < alpha) FALSE else TRUE</pre>
cat_reject_h0("For mathemathics variance test:", !var_equal_mat)
## For mathemathics variance test:
## We are not rejecting the HO hypothesis
var_equal_por <- if (por_f_test$p.value < alpha) FALSE else TRUE</pre>
cat_reject_h0("For Portuguese variance test:", !var_equal_por)
## For Portuguese variance test:
## We are rejecting the HO hypothesis in favor of hypothesis H1
T-test for grade equality
var_equal_mat
```

## [1] TRUE
var\_equal\_por
## [1] FALSE

```
# HO - GP school has equal grades to in mathematics to MS (GP=MS)
# H1 - GP>MS
mat_t_test <- t.test(gp_mat$grade, ms_mat$grade, alt = "greater", var.equal = var_equal_mat)
is_gp_mat_better <- if (mat_t_test$p.value < alpha) TRUE else FALSE
cat_reject_h0("Mathemathics T-test test:", is_gp_mat_better)
## Mathemathics T-test test:
## We are not rejecting the HO hypothesis

# HO - GP school has equal grades to in Portuguese to MS (GP=MS)
# H1 - GP>MS
por_t_test <- t.test(gp_por$grade, ms_por$grade, alt = "greater", var.equal = var_equal_por)
is_gp_por_better <- if (por_t_test$p.value < alpha) TRUE else FALSE
cat_reject_h0("Portuguese T-test test:", is_gp_por_better)
## Portuguese T-test test:
## We are rejecting the HO hypothesis in favor of hypothesis H1</pre>
```