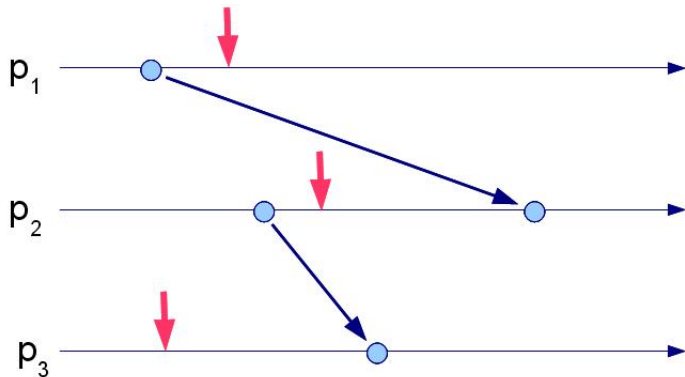


# Snapshot - shot of distributed computation



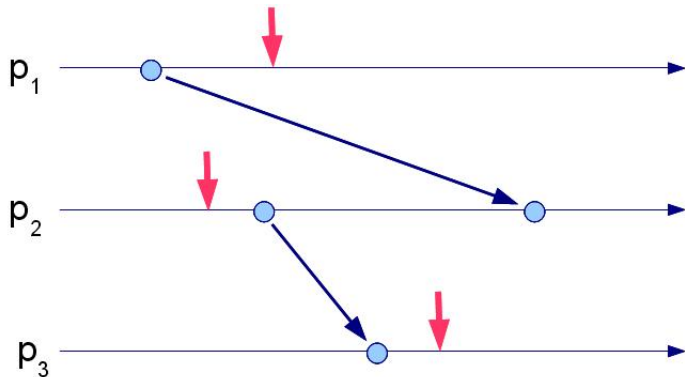
consistent shot



# Snapshot - shot of distributed computation



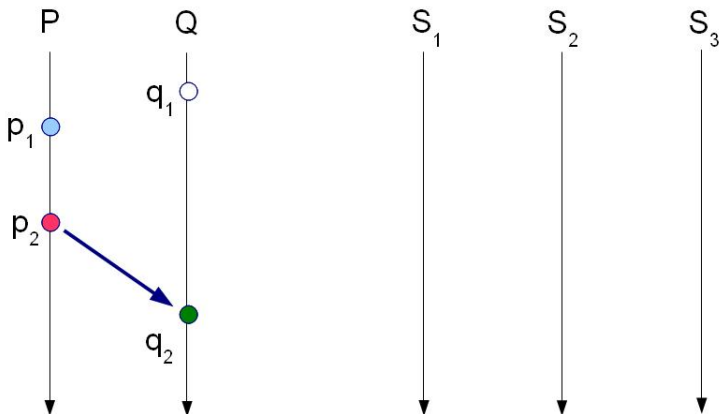
inconsistent shot



# Ordering of events



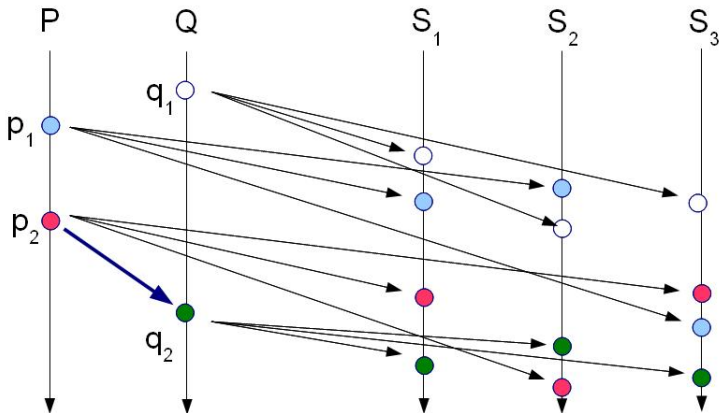
## sequential computing and communication



# Ordering of events



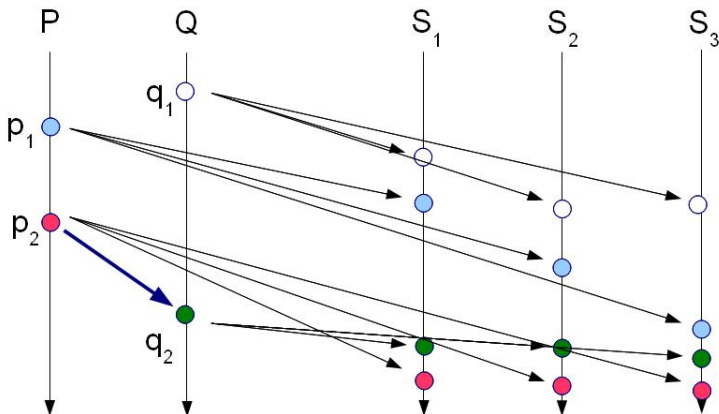
## influence of communication



# Ordering of events



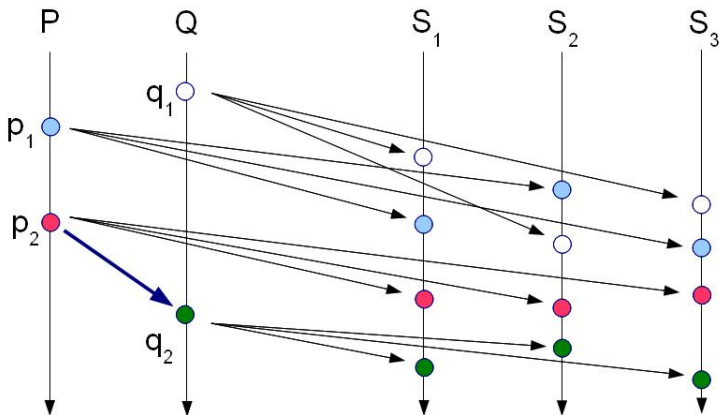
full ordering



# Ordering of events



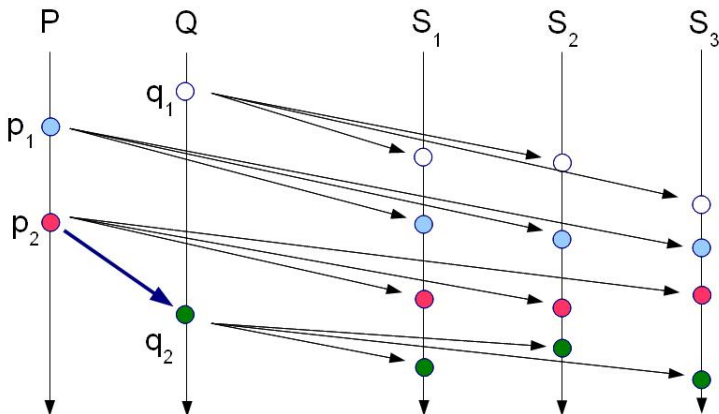
## causal ordering



# Ordering of events



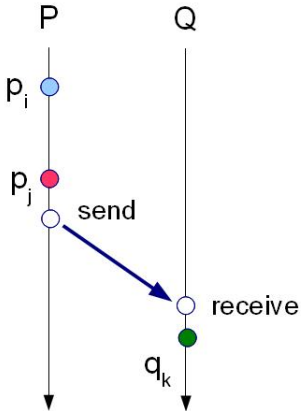
full and causal ordering





# Logic clock

## relation



## Interprocess

$$p_i \xrightarrow{!} p_j$$

## communication

$$p_j \xrightarrow{!} q_k$$





## relation

**transitive**

$$(a \rightarrow b) \wedge (b \rightarrow c) \implies a \rightarrow c$$

**asymmetric**

$$(a \rightarrow b) \not\Rightarrow (b \rightarrow a)$$

**concurrency**

$$\text{Df: } (a \not\rightarrow b) \wedge (b \not\rightarrow a)$$



## scalar time stamps - Lamport's clock

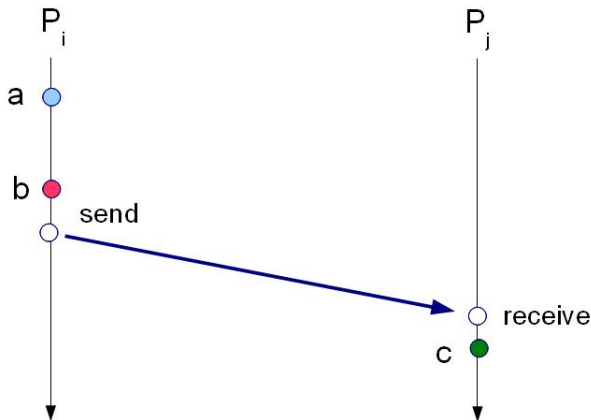
**Df:**  $C : a \rightarrow C(a)$

$\forall a, b : a \rightarrow b \Rightarrow C(a) < C(b)$

# Logic clock



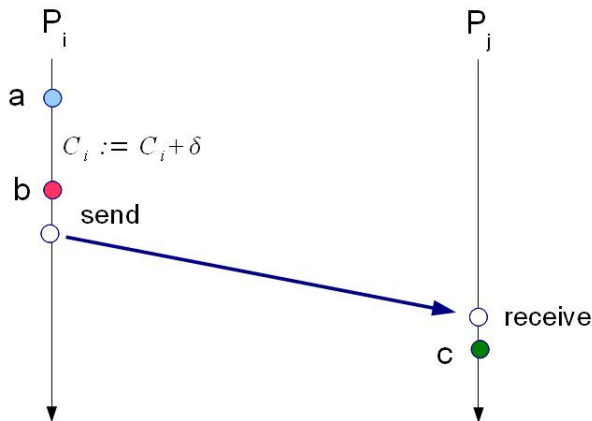
## scalar time stamps - Lamport's clock



# Logic clock



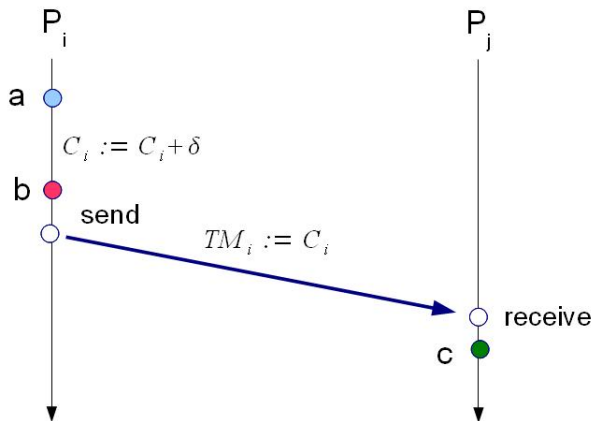
scalar time stamps - Lamport's clock



# Logic clock



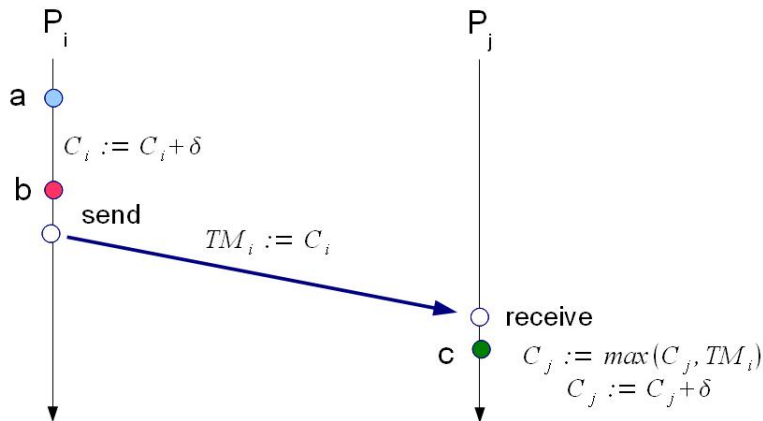
## scalar time stamps - Lamport's clock



# Logic clock



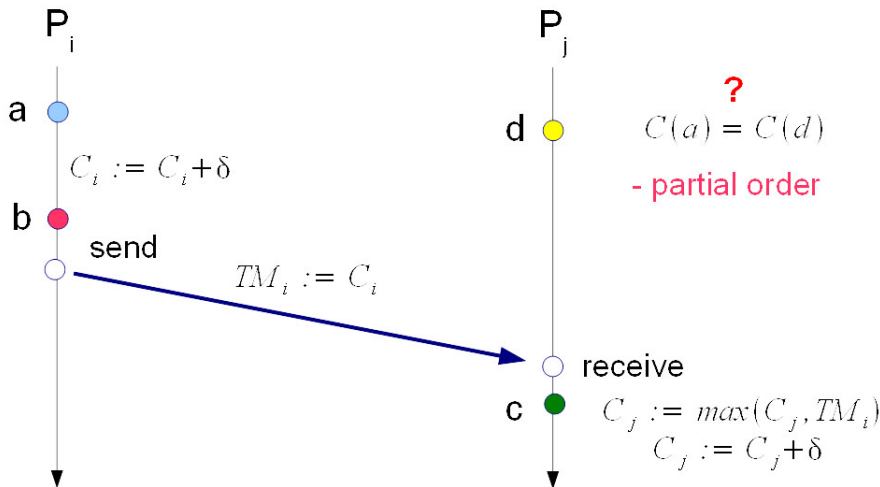
## scalar time stamps - Lamport's clock





# Logic clock

## scalar time stamps - Lamport's clock





## scalar time stamps - Lamport's clock

completion to full ordering

$$a \Rightarrow b$$

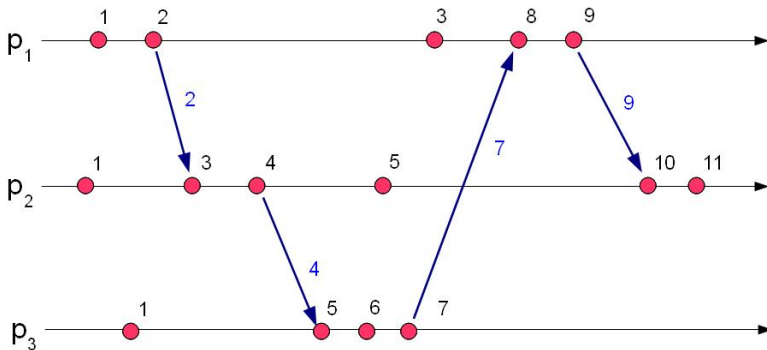
1.  $C(a) < C(b)$
2.  $(C_i(a) = C_j(b)) \wedge (i < j)$



# Logic clock



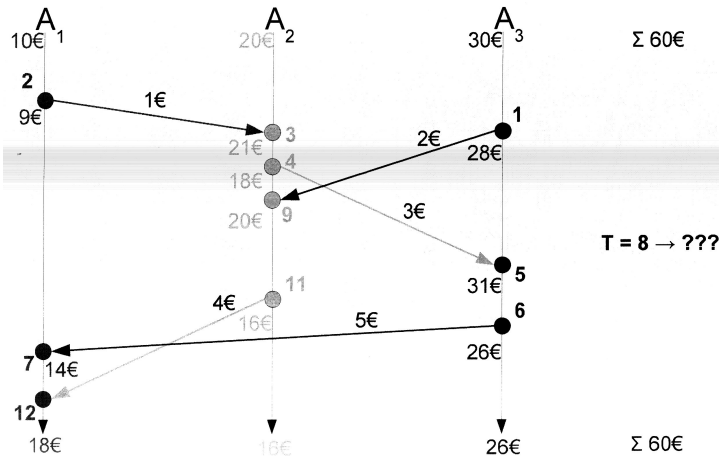
## scalar time stamps - Lamport's clock



# Logic clock



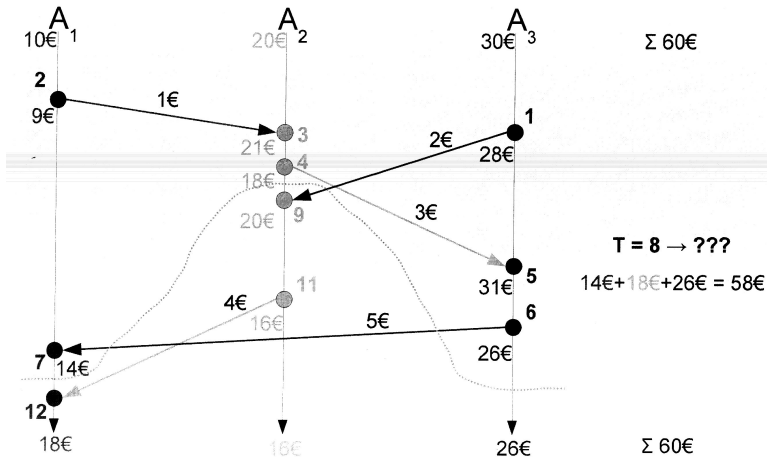
## usage in banking



# Logic clock



## usage in banking



# Logic clock



scalar time stamps - Lamport's clock

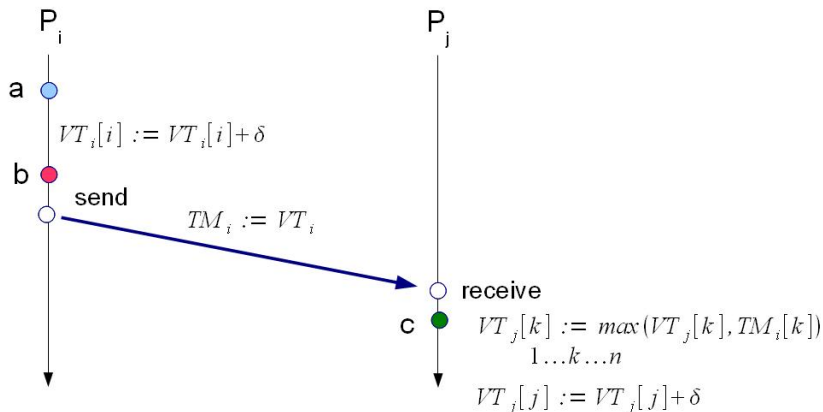
no strong consistency

$$C(a) < C(b) \not\Rightarrow a \rightarrow b$$

# Logic clock



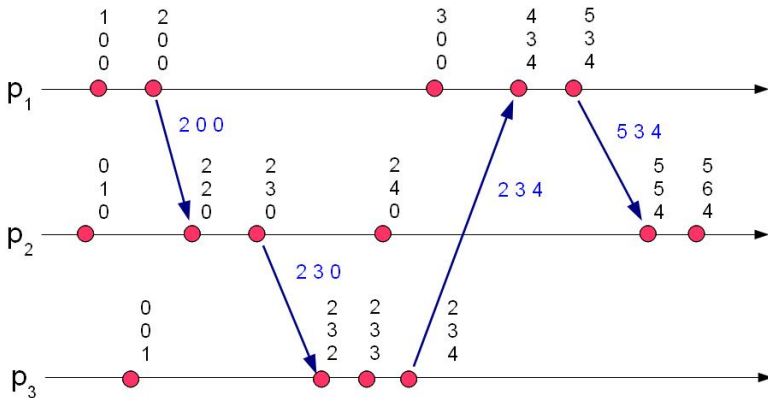
## vector time stamps - vector clock



# Logic clock



## vector time stamps - vector clock





## vector time stamps - vector clock

### isomorphism

events ordering  $\Leftrightarrow$  ordering of time stamps

$$h \rightarrow k \Leftrightarrow VT_h < VT_k \\ \forall 1 \leq i \leq n (VT_h[i] \leq VT_k[i])$$

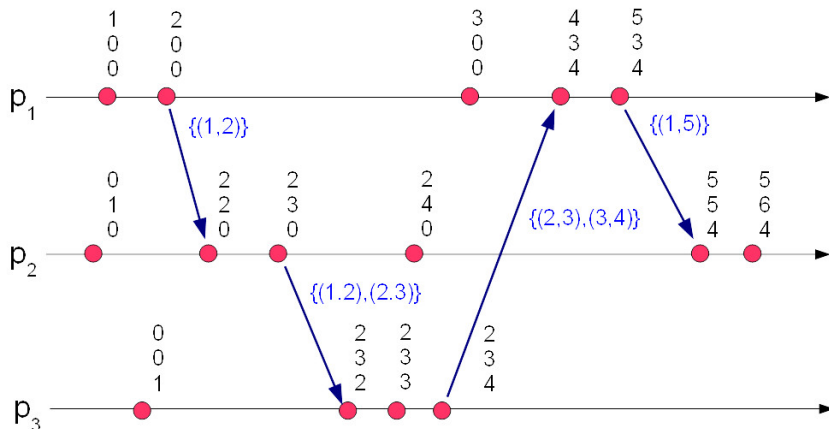
### usage

establishing of replicated data consistency

# Logic clock



## Singhal-Kshemkalyani's differential technique

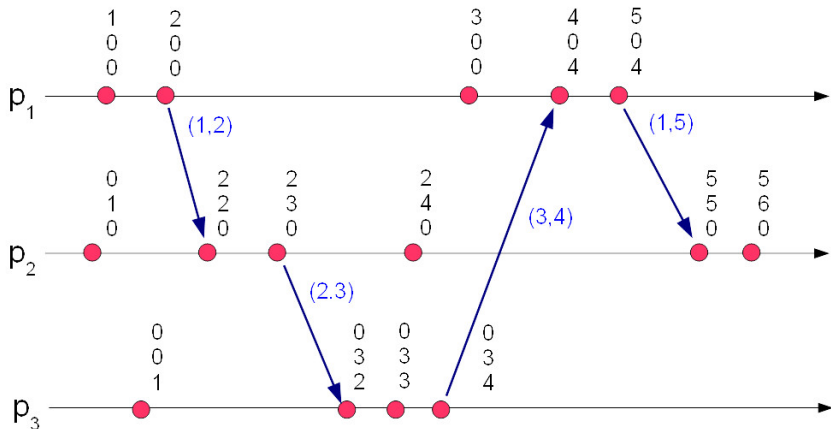






# Logic clock

## Fowler-Zwaenepoel's direct-dependency technique



information about causal relations in processes



## matrix time stamps - tensor clock

### matrix

the process has full information about knowledge of its local time in other processes

$$\min_{\forall(k,l)} [mt_i[k, l]] \geq t_i$$

### usage

establishing of replicated data robustness for processor faults