

$$a_n = (2n-1)^2$$

$$\sum_{k=1}^n a_k$$

$$= \sum_{k=1}^n 4k^2 - \sum_{k=1}^n 4k + \sum_{k=1}^n 1$$

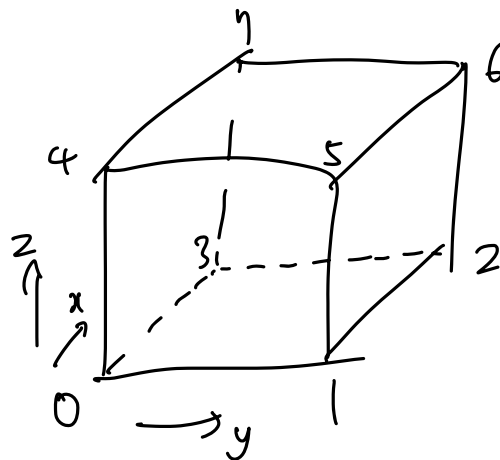
$$= \frac{2}{3} n(n+1)(2n+1) - 2n(n+1) + n$$

$$\left(\frac{4}{3}n + \frac{2}{3} - 2\right) n(n+1) + n$$

$$\frac{4}{3}n - \frac{4}{3}$$

$$\frac{4}{3} n(n^2-1) + n$$

$$= \frac{4}{3} n^3 - \frac{1}{3} n$$



$$a_n = \frac{1 \cdot (2^n - 1)}{2 - 1} = 2^n - 1$$

$$\sum_{k=1}^n a_k = \sum_{k=1}^n (2^k - 1)$$

$$= 2 + 2^2 + \dots + 2^n - n$$

$$\frac{2(2^{n+1} - 1)}{2 - 1} - n$$

$$2^{n+1} - 2 - n$$

$$1 \rightarrow 3 \times \sum_{k=1}^n 10^{k-1} = a_n$$

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$$\frac{10^n - 1}{9} = a_n$$

$$\sum_{k=1}^8 a_k = \sum_{k=1}^8 \frac{10^k - 1}{9}$$

$$a_k = k \cdot (n+1-k)$$

$$\frac{(n+1)n(n+1)}{2} - \frac{1}{6} n(n+1)(2n+1)$$

$$= \frac{n(n+1)}{6} (3n+3) - \frac{1}{6} n(n+1)(2n+1)$$

$$\begin{matrix} 1 & 2 & 3 & 4 & \dots & n \end{matrix} \rightarrow 1 \cdot n$$

$$\begin{matrix} 1 & 2 & \vdots & \vdots & \dots & n-1 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 1 & 2 & \vdots & \vdots & \vdots & \vdots \end{matrix} \rightarrow \begin{matrix} n \cdot n-1 \\ n \cdot n-2 \\ n \cdot n-3 \\ \vdots \\ n \cdot 2 \end{matrix}$$

$$= \frac{n(n+1)(n+2)}{6}$$

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$$a_k = \frac{k(k+1)}{2} \quad \sum_{i=1}^k \frac{1}{2}$$

$$\sum_{k=1}^n \frac{1}{2}(k^2) + \frac{1}{2}(k)$$

$$\frac{n(n+1)(2n+1)}{12} + \frac{n(n+1)}{4}$$

$$\frac{n(n+1)(2n+4)}{12} = \frac{n(n+1)(n+2)}{6}$$

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$$1+2$$

$$1+2+3$$

$$1+2+3+4$$

⋮

$$\sum_{i=1}^n \left( \sum_{k=1}^i k \right) = \sum_{i=1}^n \frac{i(i+1)}{2}$$

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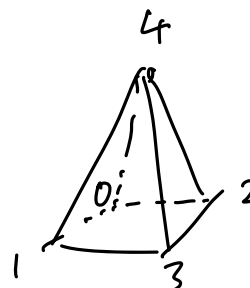
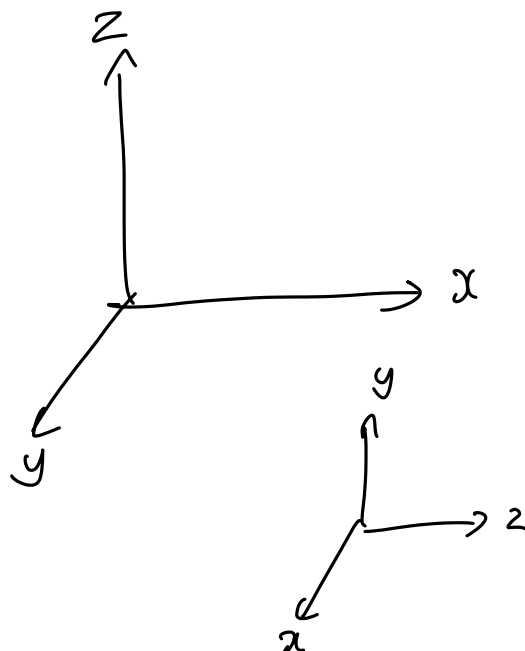
$$\sum_{k=1}^n \frac{k^2}{2} = \frac{n(n+1)(2n+1)}{6}$$

$$\sum_{k=1}^5 2k^2 + 2k + 8 = 110 + 30 + 40$$

$$a_{2k} \rightarrow k^2 - 2k + 4 = 180$$

$$a_{2k-1} \rightarrow (k+3)^2 = k^2 + 4k + 4$$

$$\sum_{k=1}^5 a_{2k-1} + a_{2k} = \sum_{n=1}^{10} a_n$$



$$ab - a - b + 1 \rightarrow \underbrace{(a-1)}_1 \underbrace{(b-1)}_2 = 2^n$$

$$\begin{array}{cc} \downarrow 2 & 1 \\ -1 & -2 \\ -2 & -1 \end{array}$$

$$n+1 \begin{pmatrix} 1 \\ 2 \\ \vdots \\ 2^n \end{pmatrix} \quad c_n = 2(n+1)$$

$$f\left(\frac{2n}{3}\right) = 2^{2n} = 4^n$$

$$\frac{1}{1 \cdot 2} + \frac{1}{2 \cdot 3} + \frac{1}{3 \cdot 4} + \dots + \frac{1}{9 \cdot 10}$$

$$\frac{1}{n(n+1)} = \left( \frac{1}{n} - \frac{1}{n+1} \right)$$

$$\begin{array}{l} a \\ a+3d \\ a+6d \\ \vdots \\ a+21d \\ \hline 10a+135d \end{array}$$

$$a_n = 3 \ 4 \ 5 \ 6 \ \dots$$

$$b_n \rightarrow$$

$$\begin{aligned} a_n &= S_n - S_{n-1} \\ &= \frac{3n^2 + 2n}{1} - \frac{3(n^2 - 2n + 1) - 2(n-1)}{1} \\ &= 6n - 1 \quad (n \geq 2) \end{aligned}$$

$$a_1 = S_1$$

$$a_1 - \cancel{a_2} + \cancel{a_2} - \cancel{a_3} + \dots + \cancel{a_n} - a_{n+1}$$

$$a_1 - a_{n+1}$$

$$\frac{1}{2} \left( \frac{1}{n} - \frac{1}{n+2} \right) = \frac{1}{2} \left( \frac{n+2-n}{n(n+2)} \right) = \frac{2}{n(n+2)}$$

$$\downarrow$$

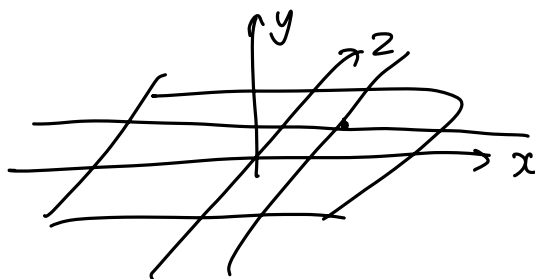
$$\frac{1}{n(n+2)}$$

$$\sum_{k=1}^{10} \frac{1}{S_k} - \frac{1}{S_{k+1}} = \frac{S_{k+1} - S_k}{S_k S_{k+1}} \rightarrow a_{k+1}$$

$$S_n = \frac{3}{2} n(n+1) \quad \frac{n(n+1)}{2}$$

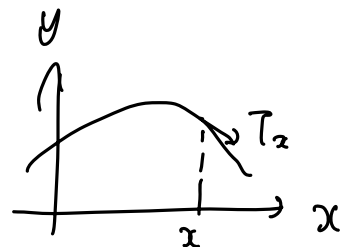
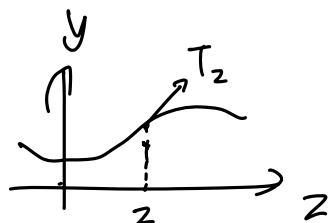
$$a_n = 3n$$

$$C_n = a_n b_n$$



$$(x, 2) \text{ or } (1, 1) \text{ or } (2, 1)$$

$$= n = T_2 \times T_x$$



$$T_2 \uparrow \quad T_2 \rightarrow \quad n = T_2 \times T_x$$

$$T_2 = \left( 0, \frac{\partial y}{\partial z}, 1 \right) \quad T_x = \left( 1, \frac{\partial y}{\partial x}, 0 \right)$$

$$n = T_z \times T_x = \left( -\frac{\partial y}{\partial x}, 1, -\frac{\partial y}{\partial z} \right)$$

$$y = 0.3(z \sin(0.1x) + x \cos(0.1z))$$

$$n = -0.3 \cdot 0.1z \cdot \cos(0.1x) - 0.3 \cos(0.1z),$$

$$1, \\ -0.3 \sin(0.1x) + 0.3x \cdot 0.1 \sin(0.1z)$$