MILLLER'S THEOREM

$$K = \frac{V_o}{V_{gs}} = -g_m R_L'; \qquad C_1 = C_{gd} \left(1 - K \right) = C_{gd} \left(1 + g_m R_L' \right); \qquad C_2 = C_{gd} \left(1 - \frac{1}{K} \right) = C_{gd} \left(1 + \frac{1}{g_m R_L'} \right)$$

FET EQUATIONS

$$I_{D} = \frac{1}{2} k_{n}' \frac{W}{L} \left(v_{GS1} - V_{t} \right)^{2} = \frac{1}{2} k_{n}' \frac{W}{L} V_{OV}^{2}; \qquad f_{T} = \frac{g_{m}}{2\pi \left(C_{gs} + C_{gd} \right)}; \quad g_{m} = \frac{2I_{D}}{V_{OV}}; \quad r_{o} = \frac{\left| V_{A} \right|}{I_{D}}$$

BJT EQUATIONS

$$\begin{split} I_{C} &= I_{S} e^{-v_{BE}/V_{T}} \; ; & \alpha &= \beta / (\beta + 1) \; ; & I_{C} &= \alpha I_{E} \; ; & v_{BE2} &= v_{BE1} + V_{T} \ln \left(\frac{i_{C2}}{i_{C1}} \right) \\ g_{m} &= \frac{I_{C}}{V_{T}} \; ; & r_{\pi} &= \frac{\beta}{g_{m}} \; ; & r_{e} &= \frac{V_{T}}{I_{E}} \; ; & r_{o} &= \frac{V_{A}}{I_{C}} \; ; \; f_{T} &= \frac{g_{m}}{2\pi \left(C_{\pi} + C_{\mu} \right)} \; ; \; f_{\beta} &= \frac{1}{2\pi \left(C_{\pi} + C_{\mu} \right) r_{\pi}} = \frac{f_{T}}{\beta_{0}} \end{split}$$

MISCELLANEOUS EQUATIONS

$$f_{H} = \frac{1}{\sqrt{\frac{1}{f_{Pi}^{2}} + \frac{1}{f_{Po}^{2}} - \frac{2}{f_{Z}}}}$$

OPEN CIRCUIT TIME CONSTANTS

Determining R_{gd}

$$I_{x} = -V_{gs} \left(R_{G} \parallel R_{sig} \right) = -V_{gs} R'_{sig} \Rightarrow V_{gs} = -I_{x} R'_{sig}$$

$$I_{x} = g_{m} \left(-I_{x} R'_{sig} \right) + \frac{\left(-I_{x} R'_{sig} \right) + V_{x}}{R'_{L}} = \frac{-I_{x} g_{m} R'_{sig} R'_{L}}{R'_{L}} + \frac{V_{x} - I_{x} R'_{sig}}{R'_{L}}$$

$$I_{x} R'_{L} = -I_{x} g_{m} R'_{sig} R'_{L} - I_{x} R'_{sig} + V_{x} \Rightarrow V_{x} = I_{x} R'_{L} + I_{x} g_{m} R'_{sig} R'_{L} + I_{x} R'_{sig}$$

$$R_{gd} \equiv \frac{V_{x}}{I_{x}} = R'_{L} + g_{m} R'_{sig} R'_{L} + R'_{sig}$$

$$= R'_{sig} \left(1 + g_{m} R'_{L} \right) + R'_{L}$$

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