

Applied Cryptography

CPEG 472/672

Lecture 8B

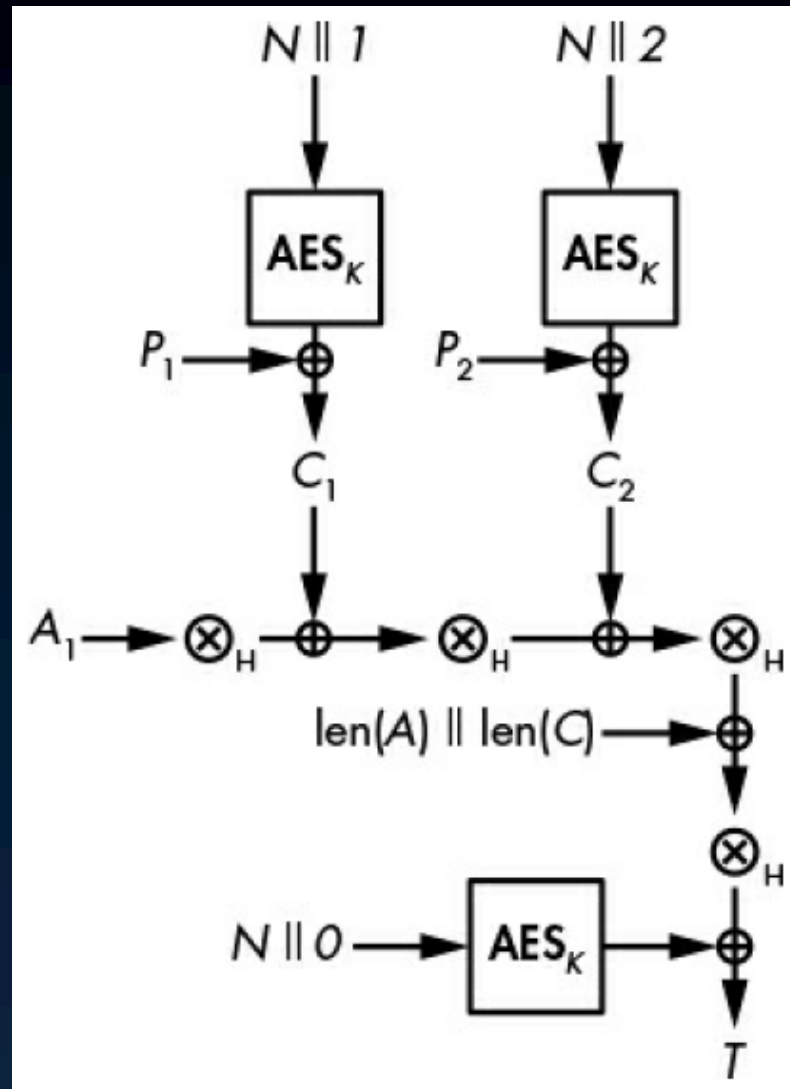
Instructor: Nektarios Tsoutsos

AES-GCM

NIST SP800-38D

- ◉ Most widely used authenticated cipher
 - ◉ AES CTR mode + C-W MAC (EtM)
 - ◉ Associated data
 - ◉ Secret key K (128 bits), nonce N (96 bits)
 - ◉ Encryption CTR starts at 1 (not 0)
- ◉ C-W MAC
 - ◉ Tag = GHASH xor PRF
 - ◉ The PRF is AES(K, N || 0x00)
 - ◉ GHASH: UH using GF(2) polmul and XORs
 - ◉ CLMUL instruction in x86

AES-GCM construction



GCM security and efficiency

- ◉ Security

- ◉ Fragile if nonce is reused
 - ◉ $T = GH(AES(K,0), A, C) \text{ xor } AES(K, N || 0)$
- ◉ Can recover $GH(A1, C1) \text{ xor } GH(A2, C2)$
 - ◉ Can leak GH key which is $AES(K,0)$

- ◉ Efficiency

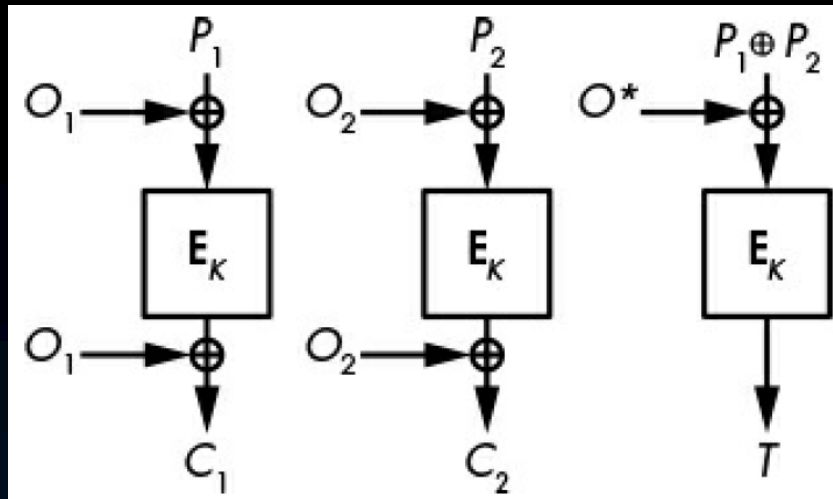
- ◉ Encryption & decryption **parallelizable**
- ◉ MAC **not parallelizable**
 - ◉ Associated data processed first
- ◉ Streamable (two layers)

OCB mode

Offset codebook (2001)

- ◉ Faster than GCM

- ◉ Patented, free for non military use



- ◉ Blends encryption & auth in 1 layer

- ◉ Only one secret key K

- ◉ $C = E(K, P \text{ xor } O) \text{ xor } O$

- ◉ Offset O depends on key K and nonce N

- ◉ $T = E(K, (\text{xor of all } P \text{ blks}) \text{ xor } O^*)$

- ◉ Can auth associated data as well

- ◉ $T = T \text{ xor } E(K, A_i \text{ xor } O_i)$

OCB security

- ◉ Less fragile to nonce reuse than GCM
 - ◉ Reusing nonce help identify if two ctxt blocks at the **same index** encrypt the same ptxt blk
 - ◉ **Smaller impact vs GCM**
- ◉ Reusing nonce breaks authentication
 - ◉ Combine blocks from another two msgs
 - ◉ Create fake message with same **checksum**
 - ◉ But: attacker **can't recover MAC key**

OCB efficiency

- ◉ Parallelizable
- ◉ Streamable
- ◉ 1 processing layer
- ◉ Essentially: Calls to cipher and XORs
 - ◉ Less expensive compared to GHASH
- ◉ OCB needs both encryption & decryption
 - ◉ GCM needs only encryption

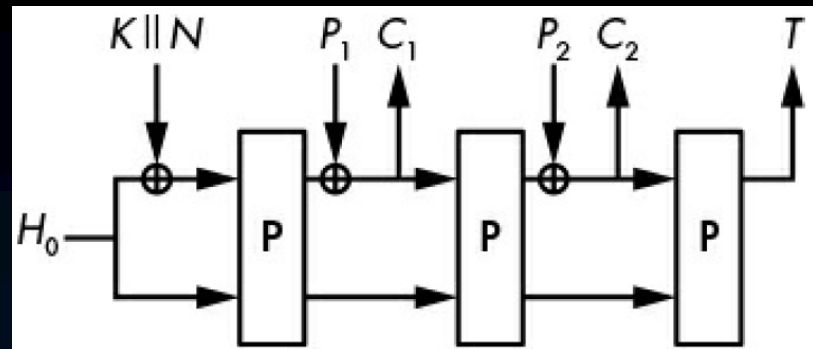
SIV

Synthetic IV

- ◉ Authenticated cipher mode
 - ◉ Mostly used with AES, 2 keys, nonce for tag
 - ◉ More robust to nonce reuse vs GCM, OCB
 - ◉ Attacker learns if same ptxt is encrypted twice
 - ◉ Can't tell if n'th block is the same
- ◉ Combines cipher + PRF
 - ◉ Tag = PRF(K1, Nonce || ptxt)
 - ◉ Ctxt = E(K2, Tag, ptxt)
 - ◉ The nonce of E is the tag
- ◉ Not streamable

Permutation-based AEAD

- ◉ Uses a permutation P
 - ◉ E.g., AES with fixed key
- ◉ Initial state H_0 , K , N
 - ◉ P updates the internal state
- ◉ XOR ptx blk, get ctxt blk
 - ◉ Finally get state bits as tag T
 - ◉ Needs correct padding
- ◉ More nonce resistant than GCM and OCB
 - ◉ Security depends on number of non-XORed bits of the state
 - ◉ Reveals if ptxt prefix is the same
- ◉ Single layer, streamable, non-parallelizable



AES-GCM security

- ◉ GHASH internals

- ◉ $X_i = (X_{i-1} \text{ xor } C_i) \text{ polymul } H$
- ◉ $H = \text{AES}(K, 0x00)$
- ◉ $X_0 = 0x00$
- ◉ $X_n = C_1 \text{ xor } H^n \text{ xor } C_2 \text{ xor } H^{n-1} \text{ xor } \dots \text{ xor } C_n \text{ xor } H^1$

- ◉ Weak hash keys \Rightarrow forgery

- ◉ $H=0 \Rightarrow X_n=0$
- ◉ $H=1 \Rightarrow$ tag is xor of ctxt blocks (can reorder)
- ◉ $H^e=H \Rightarrow$ short cycles (can swap blocks)

- ◉ Small auth tags in AES-GCM

- ◉ n-bit tags, 2^m blks $\Rightarrow \text{Prob}(\text{forgery}) = 2^{(m-n)}$

Hands-on exercises

- ◉ Polymul
- ◉ OCB mode
- ◉ SIV

Reading for next lecture

- ◉ Aumasson: Chapter 9 (until end of chapter)
 - ◉ We will have a short quiz on the material