

Variable Selection

Cindy J. Pang

2025-03-18

```
rm(list=ls())
library(dplyr)

##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##   filter, lag
## The following objects are masked from 'package:base':
##
##   intersect, setdiff, setequal, union
library(survival)
library(survMisc)

data <- read.csv("../data/survDataCleaned.csv")
```

Which race variable should we use?

```
data.raceCleaned <- data %>% select(-race_collapsed)
data.raceCollapsed <- data %>% select(-race_cleaned)
```

Variable Selection.

Fit Cox-PH models for both the `data.raceCleaned` and `data.raceCollapsed`.

```
data.raceCleaned$race_cleaned <- relevel(factor(data.raceCleaned$race_cleaned), ref = "white")
data.raceCleaned$FIGO <- relevel(factor(data.raceCleaned$FIGO), ref = "Stage I")

fullCoxMod <- coxph(Surv(time, delta) ~ size.intermediate + factor(race_cleaned) + factor(FIGO)+age_at_
fullCoxMod

## Call:
## coxph(formula = Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
##   factor(FIGO) + age_at_diagnosis, data = data.raceCleaned)
##
##               coef exp(coef) se(coef)      z
## size.intermediate    0.151974  1.164130  0.147632  1.029
## factor(race_cleaned)asian   -0.914762  0.400612  0.413712 -2.211
## factor(race_cleaned)black    0.280853  1.324259  0.221897  1.266
## factor(race_cleaned)hispanic  0.093532  1.098046  0.384043  0.244
## factor(race_cleaned)unreported/other -0.896446  0.408017  0.383582 -2.337
```

```

## factor(FIGO)Stage II          0.578492  1.783347  0.660023  0.876
## factor(FIGO)Stage III        1.546288  4.694015  0.581007  2.661
## factor(FIGO)Stage IV         2.019321  7.533212  0.591642  3.413
## age_at_diagnosis             0.021200  1.021426  0.004712  4.499
##                               p
## size.intermediate            0.303286
## factor(race_cleaned)asian    0.027028
## factor(race_cleaned)black    0.205624
## factor(race_cleaned)hispanic 0.807583
## factor(race_cleaned)unreported/other 0.019437
## factor(FIGO)Stage II        0.380773
## factor(FIGO)Stage III       0.007782
## factor(FIGO)Stage IV        0.000642
## age_at_diagnosis            6.83e-06
##
## Likelihood ratio test=78.46  on 9 df, p=3.264e-13
## n= 598, number of events= 359

data.raceCollapsed$race_cleaned <- relevel(factor(data.raceCollapsed$race_collapsed), ref = "white")
data.raceCollapsed$FIGO <- relevel(factor(data.raceCollapsed$FIGO), ref = "Stage I")

fullCoxMod.r <- coxph(Surv(time, delta) ~ size.intermediate + factor(race_cleaned) + factor(FIGO)+age_at_diagnosis, data = data.raceCollapsed)

fullCoxMod.r

## Call:
## coxph(formula = Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
##       factor(FIGO) + age_at_diagnosis, data = data.raceCollapsed)
##
##               coef exp(coef) se(coef)      z
## size.intermediate    0.153985  1.166473  0.147402  1.045
## factor(race_cleaned)asian -0.913906  0.400955  0.413715 -2.209
## factor(race_cleaned)black/hisp.  0.232315  1.261517  0.195233  1.190
## factor(race_cleaned)other/unreported -0.896253  0.408096  0.383577 -2.337
## factor(FIGO)Stage II    0.583044  1.791483  0.659915  0.884
## factor(FIGO)Stage III   1.546116  4.693204  0.581015  2.661
## factor(FIGO)Stage IV    2.017950  7.522891  0.591655  3.411
## age_at_diagnosis        0.021367  1.021597  0.004697  4.549
##                               p
## size.intermediate        0.296180
## factor(race_cleaned)asian 0.027173
## factor(race_cleaned)black/hisp. 0.234071
## factor(race_cleaned)other/unreported 0.019462
## factor(FIGO)Stage II    0.376959
## factor(FIGO)Stage III   0.007790
## factor(FIGO)Stage IV    0.000648
## age_at_diagnosis        5.39e-06
##
## Likelihood ratio test=78.27  on 8 df, p=1.089e-13
## n= 598, number of events= 359

```

Above is proof that collapsing the race category doesn't improve or make inference any better. I will use the `data.raceCleaned` variable going forward.

Stepwise AIC Selection.

```
# import package
library(MASS)

##
## Attaching package: 'MASS'

## The following object is masked from 'package:dplyr':
##
##      select

best.model.aic <- stepAIC(fullCoxMod, direction="both",
                        k=2, trace=1)

## Start:  AIC=4247.61
## Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
##      factor(FIG0) + age_at_diagnosis
##
##              Df    AIC
## - size.intermediate    1 4246.6
## <none>                  4247.6
## - factor(race_cleaned)  4 4255.3
## - age_at_diagnosis     1 4265.7
## - factor(FIG0)         3 4279.7
##
## Step:  AIC=4246.65
## Surv(time, delta) ~ factor(race_cleaned) + factor(FIG0) + age_at_diagnosis
##
##              Df    AIC
## <none>                  4246.6
## + size.intermediate     1 4247.6
## - factor(race_cleaned)  4 4254.9
## - age_at_diagnosis     1 4265.7
## - factor(FIG0)         3 4279.5

# Display the best model obtained by AIC
best.model.aic

## Call:
## coxph(formula = Surv(time, delta) ~ factor(race_cleaned) + factor(FIG0) +
##      age_at_diagnosis, data = data.raceCleaned)
##
##              coef exp(coef) se(coef)      z
## factor(race_cleaned)asian    -0.928315  0.395219  0.413392 -2.246
## factor(race_cleaned)black     0.287141  1.332613  0.221873  1.294
## factor(race_cleaned)hispanic   0.085670  1.089447  0.383921  0.223
## factor(race_cleaned)unreported/other -0.907432  0.403559  0.383402 -2.367
## factor(FIG0)Stage II          0.579955  1.785958  0.660003  0.879
## factor(FIG0)Stage III         1.544113  4.683814  0.580996  2.658
## factor(FIG0)Stage IV          2.035096  7.652983  0.591420  3.441
## age_at_diagnosis              0.021626  1.021861  0.004692  4.609
##
##              p
## factor(race_cleaned)asian    0.024729
## factor(race_cleaned)black     0.195606
## factor(race_cleaned)hispanic   0.823422
```

```
## factor(race_cleaned)unreported/other 0.017943
## factor(FIG0)Stage II 0.379556
## factor(FIG0)Stage III 0.007868
## factor(FIG0)Stage IV 0.000579
## age_at_diagnosis 4.04e-06
##
## Likelihood ratio test=77.43 on 8 df, p=1.608e-13
## n= 598, number of events= 359
```

Ok, AIC stepwise selection only selected `race_cleaned`, `FIG0` and `age_at_diagnosis`.

Stepwise BIC Selection.

```
n <- nrow(data) # number of rows
best.model.bic <- stepAIC(fullCoxMod, direction="both",
                          k=log(n), trace=1)

## Start: AIC=4287.15
## Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
##   factor(FIG0) + age_at_diagnosis
##
##               Df    AIC
## - factor(race_cleaned) 4 4277.3
## - size.intermediate    1 4281.8
## <none>                  4287.2
## - age_at_diagnosis     1 4300.8
## - factor(FIG0)         3 4306.0
##
## Step: AIC=4277.28
## Surv(time, delta) ~ size.intermediate + factor(FIG0) + age_at_diagnosis
##
##               Df    AIC
## - size.intermediate    1 4272.5
## <none>                  4277.3
## + factor(race_cleaned) 4 4287.2
## - age_at_diagnosis     1 4293.9
## - factor(FIG0)         3 4298.4
##
## Step: AIC=4272.49
## Surv(time, delta) ~ factor(FIG0) + age_at_diagnosis
##
##               Df    AIC
## <none>          4272.5
## + size.intermediate 1 4277.3
## + factor(race_cleaned) 4 4281.8
## - age_at_diagnosis     1 4290.5
## - factor(FIG0)         3 4294.6

best.model.bic

## Call:
## coxph(formula = Surv(time, delta) ~ factor(FIG0) + age_at_diagnosis,
##       data = data.raceCleaned)
##
##               coef exp(coef) se(coef)      z      p
```

```
## factor(FIG0)Stage II 0.543453 1.721942 0.658470 0.825 0.409186
## factor(FIG0)Stage III 1.534167 4.637460 0.580808 2.641 0.008256
## factor(FIG0)Stage IV 2.050814 7.774229 0.591210 3.469 0.000523
## age_at_diagnosis 0.022862 1.023125 0.004608 4.961 7e-07
##
## Likelihood ratio test=61.16 on 4 df, p=1.655e-12
## n= 598, number of events= 359
```

BIC selected FIG0 and age_at_diagnosis to obtain the best model.

AFT Models.

Exponential AFT.

```
full.expAFT <- survreg(Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
  factor(FIG0) + age_at_diagnosis, data = data.raceCleaned, dist = "exponential")

expAFT.aic <- stepAIC(full.expAFT, direction = "both", k=2, trace=1)
```

```
## Start: AIC=6673.96
## Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
##   factor(FIG0) + age_at_diagnosis
##
##           Df      AIC
## <none>          6674.0
## - size.intermediate    1 6674.9
## - factor(race_cleaned)  4 6687.1
## - age_at_diagnosis     1 6692.7
## - factor(FIG0)         3 6717.2
```

```
expAFT.aic
```

```
## Call:
## survreg(formula = Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
##   factor(FIG0) + age_at_diagnosis, data = data.raceCleaned,
##   dist = "exponential")
##
## Coefficients:
##           (Intercept)                size.intermediate
##           11.5786835                -0.2600141
##   factor(race_cleaned)asian      factor(race_cleaned)black
##           0.9821891                -0.3971982
##   factor(race_cleaned)hispanic  factor(race_cleaned)unreported/other
##          -0.1746070                1.0148055
##   factor(FIG0)Stage II          factor(FIG0)Stage III
##          -0.6588743                -1.7113719
##   factor(FIG0)Stage IV          age_at_diagnosis
##          -2.2627941                -0.0213537
##
## Scale fixed at 1
##
## Loglik(model)= -3327   Loglik(intercept only)= -3377.4
##   Chisq= 100.91 on 9 degrees of freedom, p= <2e-16
## n= 598
```

```
expAFT.bic <- stepAIC(full.expAFT, direction = "both", k=log(n), trace=1)
```

```
## Start: AIC=6717.9
## Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
##   factor(FIG0) + age_at_diagnosis
##
##               Df    AIC
## - factor(race_cleaned)  4 6713.5
## - size.intermediate    1 6714.5
## <none>                  6717.9
## - age_at_diagnosis     1 6732.2
## - factor(FIG0)         3 6748.0
##
## Step: AIC=6713.49
## Surv(time, delta) ~ size.intermediate + factor(FIG0) + age_at_diagnosis
##
##               Df    AIC
## - size.intermediate    1 6711.3
## <none>                  6713.5
## + factor(race_cleaned)  4 6717.9
## - age_at_diagnosis     1 6731.0
## - factor(FIG0)         3 6746.6
##
## Step: AIC=6711.3
## Surv(time, delta) ~ factor(FIG0) + age_at_diagnosis
##
##               Df    AIC
## <none>          6711.3
## + size.intermediate    1 6713.5
## + factor(race_cleaned)  4 6714.5
## - age_at_diagnosis     1 6731.1
## - factor(FIG0)         3 6746.3
```

```
expAFT.bic
```

```
## Call:
## survreg(formula = Surv(time, delta) ~ factor(FIG0) + age_at_diagnosis,
##   data = data.raceCleaned, dist = "exponential")
##
## Coefficients:
##      (Intercept)  factor(FIG0)Stage II factor(FIG0)Stage III
##      11.52387703          -0.64591491          -1.71559843
## factor(FIG0)Stage IV      age_at_diagnosis
##      -2.32689756          -0.02338033
##
## Scale fixed at 1
##
## Loglik(model)= -3339.7   Loglik(intercept only)= -3377.4
##  Chisq= 75.54 on 4 degrees of freedom, p= 1.53e-15
## n= 598
```

Weibull AFT

```
full.weibullAFT <- survreg(Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
  factor(FIGO) + age_at_diagnosis, data = data.raceCleaned, dist = "weibull")

weibullAFT.aic <- stepAIC(full.weibullAFT, direction = "both", k=2, trace=1)
```

```
## Start: AIC=6640.12
## Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
##   factor(FIGO) + age_at_diagnosis
##
##               Df      AIC
## <none>                6640.1
## - size.intermediate    1 6640.4
## - factor(race_cleaned)  4 6650.7
## - age_at_diagnosis     1 6656.5
## - factor(FIGO)         3 6676.7
```

```
weibullAFT.aic
```

```
## Call:
## survreg(formula = Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
##   factor(FIGO) + age_at_diagnosis, data = data.raceCleaned,
##   dist = "weibull")
##
## Coefficients:
##               (Intercept)                size.intermediate
##               12.36301594                -0.28985830
##   factor(race_cleaned)asian      factor(race_cleaned)black
##               1.22733827                -0.44097742
##   factor(race_cleaned)hispanic factor(race_cleaned)unreported/other
##               -0.20784887                1.24874844
##   factor(FIGO)Stage II          factor(FIGO)Stage III
##               -0.82430720                -2.11463119
##   factor(FIGO)Stage IV          age_at_diagnosis
##               -2.76756691                -0.02613169
##
## Scale= 1.294644
##
## Loglik(model)= -3309.1   Loglik(intercept only)= -3352.5
##   Chisq= 86.94 on 9 degrees of freedom, p= 6.68e-15
## n= 598
```

```
weibullAFT.bic <- stepAIC(full.weibullAFT, direction = "both", k=log(n), trace=1)
```

```
## Start: AIC=6688.45
## Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
##   factor(FIGO) + age_at_diagnosis
##
##               Df      AIC
## - factor(race_cleaned)  4 6681.4
## - size.intermediate    1 6684.3
## <none>                6688.4
## - age_at_diagnosis     1 6700.4
## - factor(FIGO)         3 6711.8
##
## Step: AIC=6681.41
```

```
## Surv(time, delta) ~ size.intermediate + factor(FIG0) + age_at_diagnosis
##
##              Df      AIC
## - size.intermediate      1 6678.2
## <none>                    6681.4
## + factor(race_cleaned)    4 6688.4
## - age_at_diagnosis        1 6696.2
## - factor(FIG0)            3 6707.3
##
## Step:  AIC=6678.2
## Surv(time, delta) ~ factor(FIG0) + age_at_diagnosis
##
##              Df      AIC
## <none>                    6678.2
## + size.intermediate      1 6681.4
## + factor(race_cleaned)    4 6684.3
## - age_at_diagnosis        1 6694.8
## - factor(FIG0)            3 6705.6
```

```
weibullAFT.bic
```

```
## Call:
## survreg(formula = Surv(time, delta) ~ factor(FIG0) + age_at_diagnosis,
##         data = data.raceCleaned, dist = "weibull")
##
## Coefficients:
##      (Intercept) factor(FIG0)Stage II factor(FIG0)Stage III
##      12.35580783      -0.80343728      -2.13537950
## factor(FIG0)Stage IV      age_at_diagnosis
##      -2.86714404      -0.02884478
##
## Scale= 1.311245
##
## Loglik(model)= -3319.9   Loglik(intercept only)= -3352.5
##  Chisq= 65.22 on 4 degrees of freedom, p= 2.31e-13
## n= 598
```

Log-Logistic AFT.

```
full.loglogisticAFT <- survreg(Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
  factor(FIG0) + age_at_diagnosis, data = data.raceCleaned, dist = "loglogistic")
loglogisticAFT.aic <- stepAIC(full.loglogisticAFT, direction = "both", k=2, trace=1)
```

```
## Start:  AIC=6595.7
## Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
##         factor(FIG0) + age_at_diagnosis
##
##              Df      AIC
## - size.intermediate      1 6594.6
## <none>                    6595.7
## - factor(race_cleaned)    4 6605.0
## - age_at_diagnosis        1 6618.7
## - factor(FIG0)            3 6630.9
##
```



```

## Step: AIC=6594.55
## Surv(time, delta) ~ factor(race_cleaned) + factor(FIGO) + age_at_diagnosis
##
##              Df      AIC
## <none>              6594.6
## + size.intermediate    1 6595.7
## - factor(race_cleaned)  4 6604.2
## - age_at_diagnosis      1 6618.3
## - factor(FIGO)          3 6630.5
loglogisticAFT.aic

## Call:
## survreg(formula = Surv(time, delta) ~ factor(race_cleaned) +
##         factor(FIGO) + age_at_diagnosis, data = data.raceCleaned,
##         dist = "loglogistic")
##
## Coefficients:
##              (Intercept)              factor(race_cleaned)asian
##              11.75168203              1.24102582
##         factor(race_cleaned)black      factor(race_cleaned)hispanic
##              -0.48585138              -0.17884472
## factor(race_cleaned)unreported/other      factor(FIGO)Stage II
##              1.09502164              -0.72098231
##              factor(FIGO)Stage III      factor(FIGO)Stage IV
##              -1.96859618              -2.69683380
##              age_at_diagnosis
##              -0.03253153
##
## Scale= 0.9524551
##
## Loglik(model)= -3287.3   Loglik(intercept only)= -3330.7
## Chisq= 86.94 on 8 degrees of freedom, p= 1.94e-15
## n= 598
loglogisticAFT.bic <- stepAIC(full.loglogisticAFT, direction = "both", k=log(n), trace=1)

## Start: AIC=6644.03
## Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
##         factor(FIGO) + age_at_diagnosis
##
##              Df      AIC
## - factor(race_cleaned)  4 6635.7
## - size.intermediate    1 6638.5
## <none>              6644.0
## - age_at_diagnosis      1 6662.6
## - factor(FIGO)          3 6666.1
##
## Step: AIC=6635.75
## Surv(time, delta) ~ size.intermediate + factor(FIGO) + age_at_diagnosis
##
##              Df      AIC
## - size.intermediate    1 6630.6
## <none>              6635.7
## + factor(race_cleaned)  4 6644.0

```

```
## - age_at_diagnosis      1 6657.3
## - factor(FIG0)          3 6659.9
##
## Step: AIC=6630.58
## Surv(time, delta) ~ factor(FIG0) + age_at_diagnosis
##
##              Df      AIC
## <none>                6630.6
## + size.intermediate    1 6635.7
## + factor(race_cleaned)  4 6638.5
## - age_at_diagnosis      1 6653.1
## - factor(FIG0)          3 6655.7
```

```
loglogisticAFT.bic
```

```
## Call:
## survreg(formula = Surv(time, delta) ~ factor(FIG0) + age_at_diagnosis,
##         data = data.raceCleaned, dist = "loglogistic")
##
## Coefficients:
##      (Intercept) factor(FIG0)Stage II factor(FIG0)Stage III
##      11.93419596      -0.69099201      -1.98625823
## factor(FIG0)Stage IV      age_at_diagnosis
##      -2.75224858      -0.03446027
##
## Scale= 0.9666854
##
## Loglik(model)= -3296.1  Loglik(intercept only)= -3330.7
## Chisq= 69.27 on 4 degrees of freedom, p= 3.24e-14
## n= 598
```

Log-Normal AFT

```
full.lognormalAFT <- survreg(Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
  factor(FIG0) + age_at_diagnosis, data = data.raceCleaned, dist = "lognormal")
```

```
lognormalAFT.aic <- stepAIC(full.lognormalAFT, direction = "both", k=2, trace=1)
```

```
## Start: AIC=6604.08
## Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
##      factor(FIG0) + age_at_diagnosis
##
##              Df      AIC
## - size.intermediate    1 6602.9
## <none>                6604.1
## - factor(race_cleaned)  4 6611.1
## - age_at_diagnosis      1 6629.1
## - factor(FIG0)          3 6638.9
##
## Step: AIC=6602.87
## Surv(time, delta) ~ factor(race_cleaned) + factor(FIG0) + age_at_diagnosis
##
##              Df      AIC
## <none>                6602.9
## + size.intermediate    1 6604.1
```

```

## - factor(race_cleaned) 4 6610.4
## - age_at_diagnosis      1 6628.8
## - factor(FIG0)          3 6638.3
lognormalAFT.aic

## Call:
## survreg(formula = Surv(time, delta) ~ factor(race_cleaned) +
##     factor(FIG0) + age_at_diagnosis, data = data.raceCleaned,
##     dist = "lognormal")
##
## Coefficients:
##              (Intercept)                factor(race_cleaned)asian
##              11.60283189                1.32670368
##      factor(race_cleaned)black      factor(race_cleaned)hispanic
##              -0.60372256                -0.21390418
## factor(race_cleaned)unreported/other      factor(FIG0)Stage II
##              0.71779553                -0.27403185
##              factor(FIG0)Stage III      factor(FIG0)Stage IV
##              -1.53718723                -2.39908988
##              age_at_diagnosis
##              -0.03567528
##
## Scale= 1.698155
##
## Loglik(model)= -3291.4   Loglik(intercept only)= -3333.2
##  Chisq= 83.54 on 8 degrees of freedom, p= 9.43e-15
## n= 598
lognormalAFT.bic <- stepAIC(full.lognormalAFT, direction = "both", k=log(n), trace=1)

## Start:  AIC=6652.41
## Surv(time, delta) ~ size.intermediate + factor(race_cleaned) +
##     factor(FIG0) + age_at_diagnosis
##
##              Df      AIC
## - factor(race_cleaned) 4 6641.9
## - size.intermediate    1 6646.8
## <none>                  6652.4
## - age_at_diagnosis     1 6673.0
## - factor(FIG0)         3 6674.0
##
## Step:  AIC=6641.89
## Surv(time, delta) ~ size.intermediate + factor(FIG0) + age_at_diagnosis
##
##              Df      AIC
## - size.intermediate    1 6636.8
## <none>                  6641.9
## + factor(race_cleaned) 4 6652.4
## - factor(FIG0)         3 6663.8
## - age_at_diagnosis     1 6664.4
##
## Step:  AIC=6636.78
## Surv(time, delta) ~ factor(FIG0) + age_at_diagnosis
##

```

```
##                                Df      AIC
## <none>                        6636.8
## + size.intermediate          1 6641.9
## + factor(race_cleaned)       4 6646.8
## - factor(FIG0)               3 6659.4
## - age_at_diagnosis           1 6660.5

lognormalAFT.bic

## Call:
## survreg(formula = Surv(time, delta) ~ factor(FIG0) + age_at_diagnosis,
##         data = data.raceCleaned, dist = "lognormal")
##
## Coefficients:
##             (Intercept)  factor(FIG0)Stage II factor(FIG0)Stage III
##             11.6248024          -0.1457258          -1.4340866
## factor(FIG0)Stage IV      age_at_diagnosis
##             -2.3211559          -0.0371437
##
## Scale= 1.716158
##
## Loglik(model)= -3299.2   Loglik(intercept only)= -3333.2
##  Chisq= 68 on 4 degrees of freedom, p= 6.01e-14
## n= 598
```

Conclusions.

For both the AIC and BIC Stepwise selection models, FIG0 and `age_at_diagnosis` were selected. In both models, the Biopsy size variable `size.intermediate` was not considered significant. Going forward, it would be prudent to **use the BIC chosen model** since there is a larger penalty which adjusts for the large sample size (n=598).

Model Diagnostics.

Cox-Snell Residual Plot.

```
plotCoxSnellCPH<- function(survFit, delta, fitType){

  # get Cox-Snell Residual based on Martingale Residuals
  mg.residual <- resid(survFit, type = "martingale")

  cs.residual <- delta - mg.residual

  # Graphical Plot
  fit.cs <- survfit(Surv(cs.residual, delta) ~ 1) # get KM estimates
  H.cs <- cumsum(fit.cs$n.event/fit.cs$n.risk)

  plot(fit.cs$time, H.cs, type='s', col='blue',
       main = paste0('Cox-PH - ', fitType),
       xlab = 'Residual', ylab = 'Nelson-Aalen Cum. Hazard')
  #Note here that 'time' is the value of the Cox-Snell residual
  abline(0, 1, col='red', lty = 2)
}
```

```

plotCSExpAFT <- function(survFit, data, fitType){
  sigma <- survFit$scale
  eta <- -survFit$linear.predictors/sigma

  r.exp <- data$time * exp(eta)

  fit <- survfit(Surv(r.exp, data$delta) ~ 1)
  H.exp <- cumsum(fit$n.event / fit$n.risk)

  plot(H.exp ~ fit$time, type = 'l', main = paste0('Exponential AFT - ', fitType),
       ylab = 'Estimated Cumulative Hazard', xlab = 'Cox-Snell Residual')
  abline(0, 1, col='red', lty=2)
}

plotCSWeibullAFT <- function(survFit, data, fitType){
  sigma <- survFit$scale
  alpha <- 1 / sigma
  eta <- -survFit$linear.predictors / sigma

  r.wb <- data$time^alpha * exp(eta)

  fit <- survfit(Surv(r.wb, data$delta) ~ 1)
  H.wb <- cumsum(fit$n.event/fit$n.risk)

  plot(H.wb ~ fit$time, type = 'l', main = paste0('Weibull AFT - ', fitType),
       ylab = 'Estimated Cumulative Hazard', xlab = 'Cox-Snell Residual')
  abline(0, 1, col='red', lty=2)
}

plotCSLogLogisticAFT <- function(survFit, data, fitType){
  sigma <- data$scale
  alpha <- 1 / sigma
  eta <- -data$linear.predictors / sigma

  r.ll <- -log(1/(1 + data$time^alpha*exp(eta)))

  fit <- survfit(Surv(r.ll, data$delta) ~ 1)
  H.ll <- cumsum(fit$n.event / fit$n.risk)

  plot(H.ll ~ fit$time, type = 'l', main = paste0('Log-Logistic AFT- ', fitType),
       ylab = 'Estimated Cumulative Hazard', xlab = 'Cox-Snell Residual')
  abline(0, 1, col='red', lty=2)
}

plotCSLogNormalAFT <- function(survFit, data, fitType){
  eta <- -survFit$linear.predictors / survFit$scale
  r.ln <- -log(1 - pnorm((log(data$time) - survFit$linear.predictors) / survFit$scale))

  fit <- survfit(Surv(r.ln, data$delta) ~ 1)
  H.ln <- cumsum(fit$n.event/fit$n.risk)

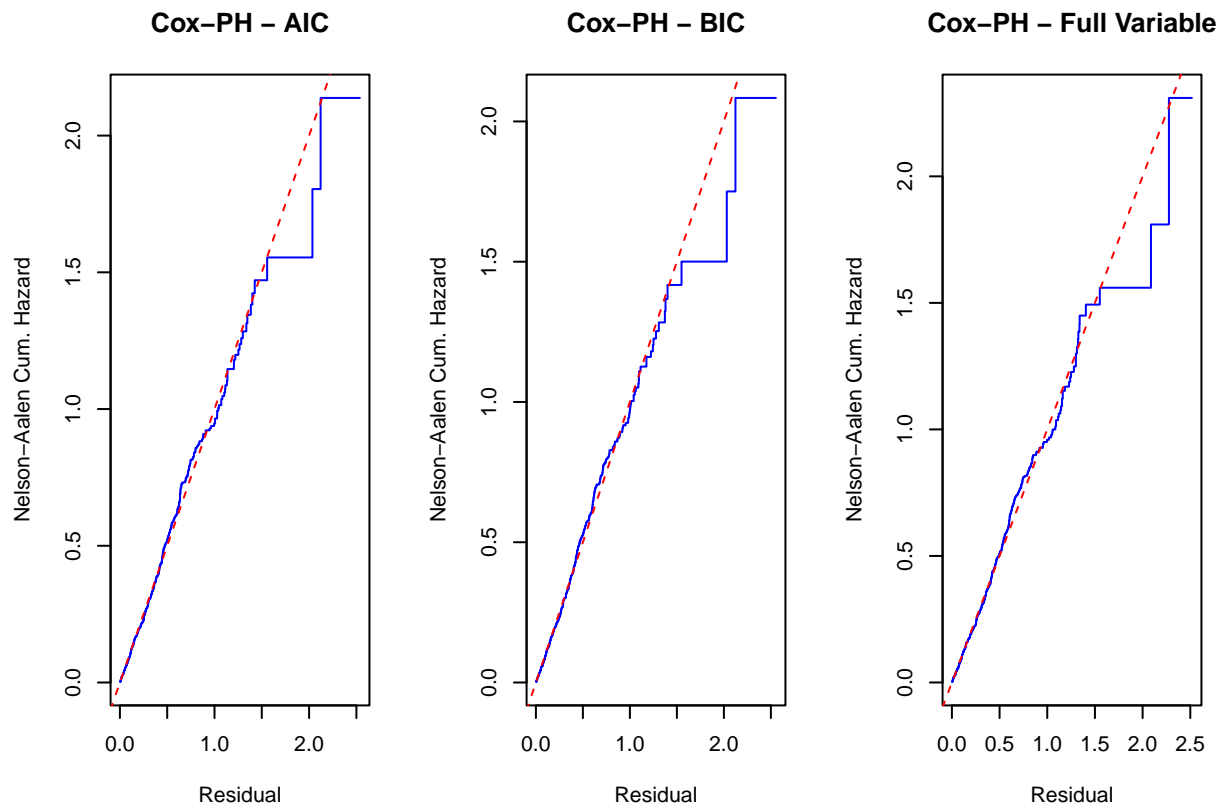
  plot(H.ln ~ fit$time, type = 'l', main = paste0('Log-Normal AFT - ', fitType),
       ylab = 'Estimated Cumulative Hazard', xlab = 'Cox-Snell Residual')
  abline(0, 1, col='red', lty = 2)
}

```

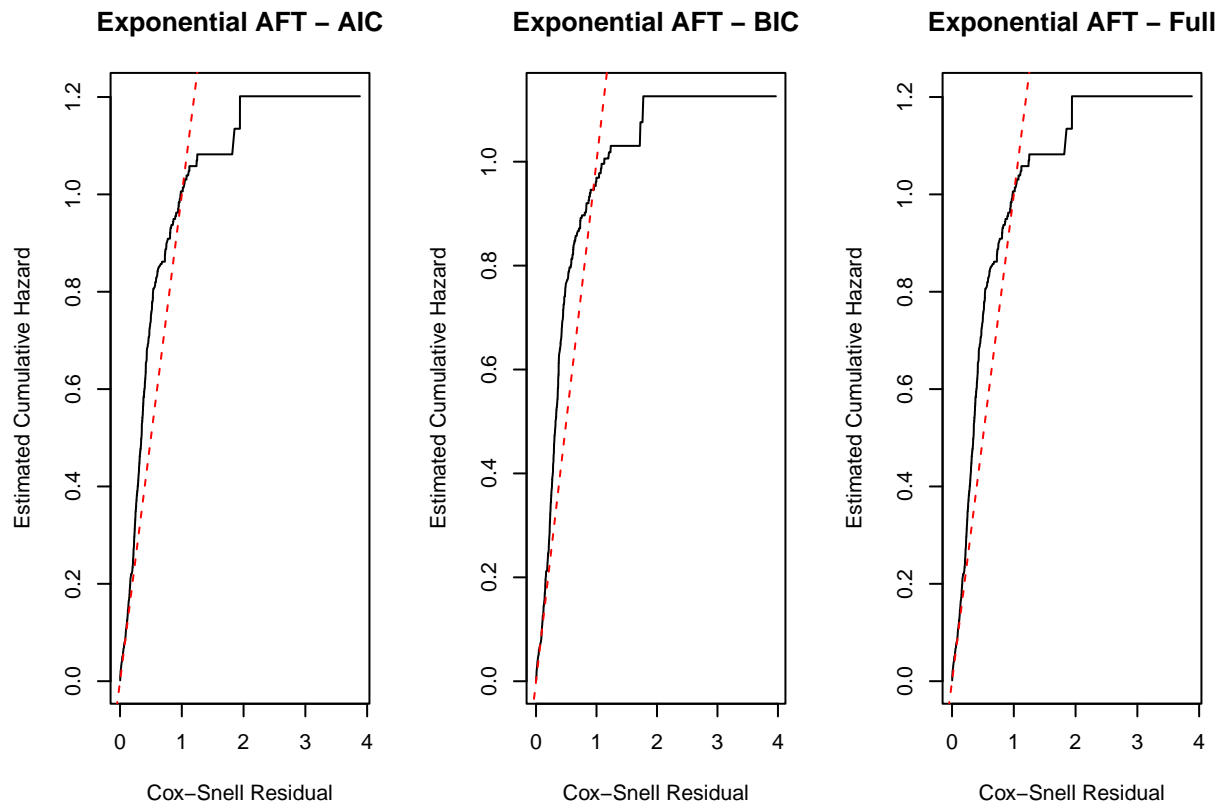
```
}
```

```
bic.modfit <- coxph(Surv(time, delta)~factor(FIGO)+age_at_diagnosis, data = data.raceCleaned, method =  
aic.modfit <- coxph(Surv(time,delta)~factor(race_cleaned)+factor(FIGO)+age_at_diagnosis, data = data.ra
```

```
par(mfrow = c(1,3))  
plotCoxSnellCPH(aic.modfit, data.raceCleaned$delta, "AIC")  
plotCoxSnellCPH(bic.modfit, data.raceCleaned$delta, "BIC")  
plotCoxSnellCPH(fullCoxMod, data.raceCleaned$delta, "Full Variable")
```



```
par(mfrow = c(1,3))  
plotCSExpAFT(expAFT.aic, data.raceCleaned, "AIC")  
plotCSExpAFT(expAFT.bic, data.raceCleaned, "BIC")  
plotCSExpAFT(full.expAFT, data.raceCleaned, "Full")
```



Ok both models fit similarly, which isn't helpful.