

# Machine Health Monitoring Using Local Feature-based Gated Recurrent Unit Networks

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**Abstract**—In modern industries, machine health monitoring systems (MHMS) have been applied wildly with the goal of realizing predictive maintenance including failures tracking, downtime reduction and assets preservation. In the era of big machinery data, data-driven MHMS have achieved remarkable results in the detection of faults after the occurrence of certain failures (diagnosis) and prediction of the future working conditions and the remaining useful life (prognosis). The numerical representation for raw sensory data is the key stone for various successful MHMS. Conventional methods are labor-extensive as they usually depend on handcrafted features, which require expert knowledge. Inspired by the success of deep learning methods that redefine representation learning from raw data, we propose local feature-based gated recurrent unit networks (LFGRU). It is a hybrid approach that combines handcrafted feature design with automatic feature learning for machine health monitoring. Firstly, features from windows of input time series are extracted. Then, an enhanced bi-directional GRU network is designed and applied on the generated sequence of local features to learn the representation. A supervised learning layer is finally trained to predict machine condition. Experiments on three machine health monitoring tasks: tool wear prediction, gearbox fault diagnosis and incipient bearing fault detection verify the effectiveness and generalization of the proposed LFGRU.

**Index Terms**—Machine Health Monitoring, Fault Diagnosis, Tool Wear Prediction, Gated Recurrent Unit (GRU), Feature Engineering

## I. INTRODUCTION

THE development of advanced sensing technologies, wireless communications, and computing systems has generated a huge amount of data for manufacturing systems in recent years [1], [2]. Meanwhile, it motivates the research of data-driven machine health monitoring systems (MHMS) that are capable to detect faults and predict working conditions [2]–[4]. Data-driven MHMS train models based on

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historical measured data, and make decisions upon the online data collected from sensors of the monitored equipment. It demonstrates that data-driven MHMS can update themselves with on-line collected data in real time. As shown in Figure 1, data-driven MHMS includes two phases: one is training model based on historical sensor signals and the other one is applying the trained model on online sensor signals to make decisions. However, it is difficult to design a complete set of features to represent machine condition, considering these commonly adopted time, frequency and time-frequency domain analysis provide a broad range of measures. Therefore, feature extraction/selection methods as a kind of information fusion are usually conducted after handcrafted feature design. To learn a more discriminative feature space, feature extraction methods such as principal component analysis [5] and factor analysis [6] have been used to transform original features into a novel informative feature space, while feature selection including fisher ratio [7] and distance measures [8] attempts to select subsets of features. Then, the derived features are fed into machine learning models, e.g., support vector machine and linear regression models, to make predictions of machine condition. For example, Widod [9] presented an overview of machine condition monitoring and fault diagnosis based on support vector machine. Prieto et al. [10] extracted significant statistical-time features firstly and then apply a hierarchical neural network for bearing fault classification. Yang et al. [11] extracted energy features at various vital frequencies and trained a random forest classifier for induction motor fault diagnosis. He et al. [12] constructed a k-nearest neighbor (kNN) classifier on time domain features extracted by empirical mode decomposition for bearing faults detection as one submodule. Regardless of which kind of machine learning models are applied, it is shown that the representation determines the upper-bound performances of machine learning algorithms [13]. However, the above pipeline system may have some potential concerns as follows:

- 1) **Expert Knowledge:** Handcrafted feature design and adaptation of appropriate feature extraction/selection methods all require prior domain-knowledge and expert expertise, which may not be met in all scenarios.
- 2) **Joint Optimization:** Considering feature learning and machine learning models that work in a cascaded way, it is impossible to jointly optimize them. One part should be fixed, and the other part can be adjusted.
- 3) **Temporal Information:** The machinery data are usually

sampled by sensors and expressed in a sequential form. And the sequential information behind sensor data is quite vital to represent machine condition. However, the hand-crafted feature design usually extract measures from the whole range of time-series data, which may not capture its intrinsic temporal information.

As a branch of machine learning models, deep learning (DL) provides a powerful solution to these above concerns [14], [15]. Deep learning is featured by its capability of extracting hierarchical representations from input data by building deep neural networks with multiple layers of non-linear transformations. Intuitively, one layer operation can be regarded as a transformation from input values to output values. The state-of-arts of various application areas including computer vision, automatic speech recognition, natural language processing, audio recognition and bioinformatics have been achieved by DL techniques. In the past few years, many deep learning models including stacked autoencoder (SAE) and deep belief network (DBN) have been developed in the field of machine health monitoring [16]. Generally, DL-based MHMS as an end-to-end system has the capability of learning features from raw input directly, which do not require extensive expert knowledge. Since feature learning and target prediction are incorporated into the whole neural network, all model parameters can be trained and optimized jointly. Some researchers focused on the pretraining of deep neural network (DNN). Stacked auto-encoder (SAE) [17] and deep belief networks (DBN) [18] are adopted to facilitate the training of DNN and learn discriminative representation for machinery data. Although these pretrained DNN models can directly work on raw sensory time-series data, input dimensionality is easily over hundred, even one thousand, which will increase model size [19]. The huge number of model parameters may lead to heavy computational cost and overfitting problems. To control the model size, features in a low-dimensional space are usually fed into pretrained DNN models. For example, Jia et al. [20] firstly extracted the frequency spectra features of time-series data, and then fed them into SAE-DNN for rotating machinery fault diagnosis. Guo et al. [21] designed multi-domain statistical features including time domain features, frequency domain features and time-frequency domain features and built a SAE-DNN upon them for bearing fault diagnosis. In [22], Ma et al. adopted a DBN-DNN framework for degradation assessment under an accelerated bearing life test, in which the raw input consists of statistical feature, root mean square (RMS) fitted by Weibull distribution and the frequency domain features. Chen et al. [23] fed a feature vector consisting of load and speed measure, time domain features and frequency domain features into DBN-DNN for gearbox fault diagnosis. Therefore, to relief the above concerns, we focus on DL-based machine health monitoring methods here.

In this paper, we present a new framework named local feature-based gated recurrent units networks (LFGRU) as a generalized machine health monitoring system. Gated recurrent units networks as a variant of recurrent neural network is able to process memories of sequential data by storing previous inputs in the internal state of networks and map

from the entire history of previous inputs to target vectors in principal. In our proposed framework, local features are firstly extracted from segments or windows of time-series data. Then, an enhanced GRU networks: bidirectional GRU networks with weighted local features averaging has been proposed to learn representation from the sequence of local features. Supervised learning layer is added on the top to map the learned representation to targets. In our framework, deep learning models are applied to handcrafted features design instead of raw time series data, considering the model size can be controlled. Different from previous DL-based MHMS that built upon extracted features of the whole range of time series data, our proposed LFGRU extracts local features from consecutive windows of time-series data, which can keep the order information among windows. What is more, this kind of local feature extraction are suitable for multi-sensory data. The features extracted from synchronized segments of multiple sensory data can be concatenated to summarize the information of all sensors at the same time step. Gated recurrent units was proposed to relief the problem of gradient exploding or vanishing in RNN with a controlled model complexity compared to another RNN variant: Long-short term memory network [24]–[26]. In our proposed LFGRU, the bi-directional recurrent structure has been incorporated, which can access the sequential data in two directions including forward and backward ones with two separate hidden layers so that our model can fully explore the context of the input, i.e., the past and future information at each state. The averaging local feature is able to generate representation of sequential data without capturing ordering information, which can provide a supplementary to representation generated by bi-directional GRU. Considering information in the middle of the sequence might be easily lost in the bi-directional GRU, the weighted average of local features is adopted here that assigns large weights to features located in the middle. To verify the effectiveness and generalizability of our proposed LFGRU, three different machine health monitoring tasks including tool wear sensing, gearbox fault diagnosis and incipient fault diagnosis of rolling element bearings are introduced. Several state-of-the-art models are compared with our proposed model. The main contributions of our work can be summarized as follows:

- 1) Our proposed framework can be considered as a hybrid approach of handcrafted feature design and automatic feature learning by DL model. The local feature extraction scheme can reduce the model size of the applied enhanced GRU networks. And the enhanced GRU networks are able to encode the temporal information on the generated sequence of local features. Therefore, in our proposed framework, not only the model size of GRU can be controlled to prevent overfitting, but also the handcrafted feature design is not required to be at expert level.
- 2) An enhanced GRU networks has been proposed. Bi-directional recurrent structure is firstly incorporated to GRU network to capture the future and past context jointly. Next, the center-biased feature averaging operation can provide a direct representation of the input sequence without considering order information, which can be supplementary

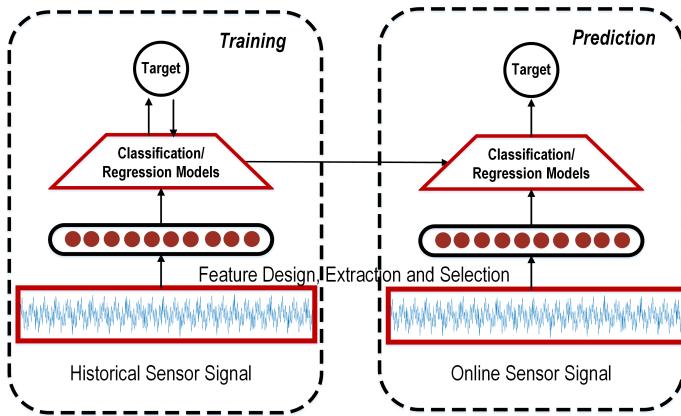


Fig. 1: Illustration of Data-driven Machine Health Monitoring System.

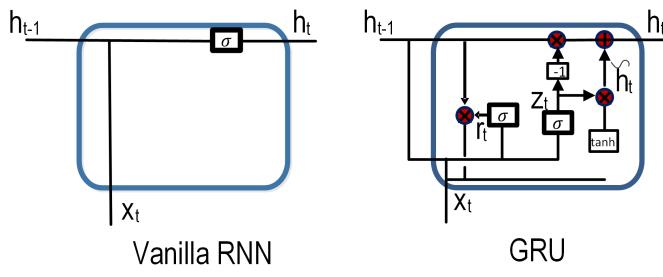


Fig. 2: The illustrations of Vanilla RNN and GRU models.

to the output of bi-directional GRU. The concatenated vector is regarded as the final representation learned by our proposed enhanced GRU networks.

- 3) This approach is suitable for multi-sensory scenario, which is illustrated in the following Section III-A and verified in the experimental part.
- 4) Comprehensive experimental studies including three case studies including tool wear prediction, gearbox fault diagnosis and incipient bearing fault detection are conducted. The effectiveness and generalization capability behind our proposed framework have been verified.

This paper is organized as follows. In Section II, RNN and GRU models are reviewed. Then, our proposed LFGRU is presented in Section III. After that, experimental results are illustrated in the following Section IV. Finally, concluding remarks are provided in Section V.

## II. RECURRENT NEURAL NETWORKS AND GATED RECURRENT UNITS NETWORKS

Recurrent neural networks (RNN) including GRU is related to our work. In the section, a brief introduction to RNN and GRU is given.

As stated in [14], recurrent neural networks (RNN) are able to memorize arbitrary-length sequences of input patterns by building connections between units from a directed cycle. The key component in RNN is the transition function in each time step  $t$  which takes the current time information  $x_t$  and the

previous hidden output  $h_{t-1}$  and updates the current hidden output as follows:

$$h_t = \mathbb{H}(x_t, h_{t-1}) \quad (1)$$

where  $\mathbb{H}$  defines a nonlinear and differentiable transformation function. Due to the recurrent structure,  $h_{t-1}$  in Eq. (1) can be regarded as a memory of previous inputs, i.e., RNN can keep the memory of previous inputs in the network's internal state. Therefore, after processing the whole sequence, the hidden output at the last time step i.e.  $h_T$  can be regarded as a vector encoding the original sequential data. Supervised learning layer is added on top to map the obtained representation  $h_T$  to targets and the model can be trained via backpropagation through time [27]. Different formulations of transition functions derive different RNN models. Vanilla RNN adopts a linear transformation function with a non-linear activation function as follows:

$$h_t = \varphi(\mathbf{W}x_t + \mathbf{H}h_{t-1} + \mathbf{b}) \quad (2)$$

where  $\mathbf{W} \in \mathbb{R}^{d \times k}$  and  $\mathbf{H} \in \mathbb{R}^{d \times d}$  represent transformation matrices and  $\mathbf{b} \in \mathbb{R}^d$  is the bias vector. And  $\varphi$  is the nonlinear activation function such as sigmoid and tanh functions. Due to the vanishing gradient problem during backpropagation for model training, vanilla RNN may not capture long-term dependencies. It means that  $h_t$  may forget the information in the early stage of sequential data. To alleviate this issue, long short-term memory networks were firstly presented by introducing gates function in the design of transition function [25]. In our paper, we adopt another RNN variant: gated recurrent units (GRUs) that can be regarded as a simpler version of LSTMs [24], [28]. In GRU, two gates including a reset gate  $r$  that adjusts the incorporation of new input with the previous memory and an update gate  $z$  that controls the preservation of the previous memory are introduced. The transition functions in hidden units of GRU are given as follows:

$$\begin{aligned} z_t &= \sigma(\mathbf{W}^z x_t + \mathbf{V}^z h_{t-1} + \mathbf{b}^z), \\ r_t &= \sigma(\mathbf{W}^r x_t + \mathbf{V}^r h_{t-1} + \mathbf{b}^r), \\ \tilde{h}_t &= \tanh(\mathbf{W}^c x_t + \mathbf{V}^c(r_t \odot h_{t-1})), \\ h_t &= (1 - z_t) \odot h_{t-1} + z_t \odot \tilde{h}_t. \end{aligned} \quad (3)$$

where model parameters including all  $\mathbf{W} \in \mathbb{R}^{d \times k}$ ,  $\mathbf{V} \in \mathbb{R}^{d \times d}$  and  $\mathbf{b} \in \mathbb{R}^d$  are shared by all time steps and learned during model training,  $\odot$  denotes the element-wise product,  $k$  is a hyper-parameter that represents the dimensionality of hidden vectors. For an intuitive illustration, if the update gate is closed, i.e.,  $z_t = 0$ , the information in the initial time step can be kept no matter how long the sequence is. The illustration of vanilla RNN and GRU has been given in Figure 2.

In our proposed framework, an enhanced GRU networks has been proposed with bi-directional structure and weighted feature averaging scheme. Firstly, a bi-directional structure is applied to the capture of future and previous context, which can improve the expressiveness of the GRU model. The adopted weighted feature averaging simply derives the mean vector of representations in each time step with a center-biased weighting scheme. The final representation consists of two

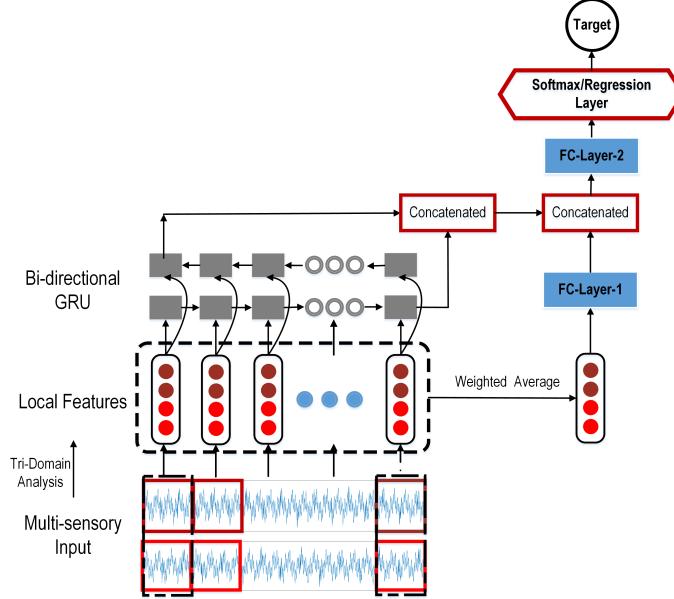


Fig. 3: The architecture of our proposed LFGRU. As an end-to-end system, this framework is able to predict target from multi-sensor input.

parts: one is the output of bi-directional GRU and the other is the weighted mean feature, which are supplementary to each other.

### III. LOCAL FEATURE-BASED GATED RECURRENT UNITS NETWORKS

In this section, our proposed LFGRU networks will be presented in the scenario of multi-sensory machine monitoring. As shown in Figure 3, The enhanced GRU network is applied on the sequence of local features extracted from raw sensor inputs to learn representation of machine condition and predict the corresponding target.

We assume each data collected from monitored machine consists of one sensor input which is time-series data denoted as  $\mathbf{x} = [x_1, x_2, \dots, x_l]$  that  $l$  is the length of data sample and training data has a corresponding target value such as fault type or tool wear that are defined in the specific applications.

#### A. Local Feature Extraction

Each sensory input is firstly divided into  $T$  local segments and each segment is a window of original signal with a length of  $\frac{l}{T}$ . For example, the  $j$ -th local window is a segment starting from time step  $(j-1)\frac{l}{T}$  to  $(j-1)\frac{l}{T} + \frac{l}{T} - 1$  denoted as  $\mathbf{x}_{(j-1)\frac{l}{T}:(j-1)\frac{l}{T} + \frac{l}{T}-1}$ . Then, tri-domain features including time, frequency and time-frequency ones are extracted from each local window. The details of these handcraft features design will be elaborated in the following experiments. Therefore, the original sensory input can be transformed to a sequence of local features as:

$$\mathbf{c} = [\mathbf{c}_1, \mathbf{c}_2, \dots, \mathbf{c}_T] \quad (4)$$

where  $\mathbf{c}_j \in \mathbb{R}^m$  consists of  $m$  features extracted from the  $j$ -th local window. It is shown that this operation can be

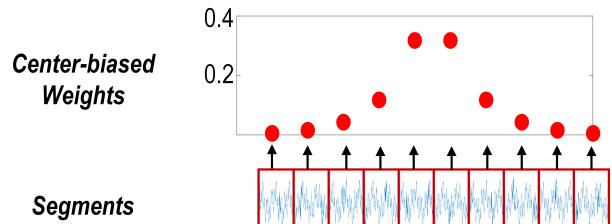


Fig. 4: Visualization of center-biased weights for a sequence of 10 local features.

easily extended to multi-sensory scenario. Local features can be extracted from synchronized windows of multiple sensor signals, respectively and concatenated together into one feature vector as  $\mathbf{c}_i$ .

After local feature extraction, the sequence of feature vectors  $\mathbf{c}$  with a length of  $T$  can be generated. Compared to the original time series  $\mathbf{x}$ , the local feature sequence is much shorter and can convey more discriminative information compared to the noisy original signal. Compared to conventional feature extraction conducted in MHMS that may abandon sequential characteristic, local features are designed and extracted from windows of the original noisy signal, which are arranged in order to form a sequence.

#### B. Bi-directional GRU with Weighted Feature Averaging

Then, GRU is applied on the generated local feature sequence to learn representation. Here, an enhanced GRU model has been proposed named bi-directional GRU with weighted feature averaging.

**Bi-directional GRU:** The incorporated bi-directionality of recurrent structure can increase the model capacity and flexibility. As shown in Figure 3, the bidirectional recurrent structure can enable GRU to process the sequence input in two directions including forward and backward ways with two individual hidden layers. Therefore, each hidden layer at one certain time step can capture past (forward direction) and future (backward direction) context jointly. In addition, the bi-directional structure can reinforce the memory of the beginning and the end stages of the raw time-series input. In bi-directional GRU, the complete hidden element representation  $\mathbf{h}^T$  at the last time step is the concatenated vector of the outputs of forward and backward processes as follows:

$$\mathbf{h}_T = \overrightarrow{\mathbf{h}}_T \oplus \overleftarrow{\mathbf{h}}_1 \quad (5)$$

where  $\rightarrow$  and  $\leftarrow$  denote forward and backward process and the corresponding hidden vector is updated as follows:

$$\begin{aligned} \overrightarrow{\mathbf{h}}_t &= \overrightarrow{\mathbb{H}}(\mathbf{x}_t, \overrightarrow{\mathbf{h}}_{t-1}) \\ \overleftarrow{\mathbf{h}}_t &= \overleftarrow{\mathbb{H}}(\mathbf{x}_t, \overleftarrow{\mathbf{h}}_{t+1}). \end{aligned} \quad (6)$$

In bi-directional GRU, the function  $\mathbb{H}$  is defined by Eq. (3).

**Weighted Feature Averaging:** The hidden output of the bi-directional GRU at the last time step  $\mathbf{h}_T$  can be regarded as the representation of the raw sensor signal. However, information

in the middle range of the sequence might be lost in bi-directional GRU. Considering the beginning and end ranges of sequence contribute a lot to the outputs of backward GRU and forward GRU, respectively. Therefore, weighted feature averaging is introduced to provide another view of the sequence of local features  $\mathbf{c}$ . The average feature vector  $\bar{\mathbf{c}}$  is given as

$$\bar{\mathbf{c}} = \sum_{k=1}^T w_k \mathbf{c}_k \quad (7)$$

where  $k$  denote the index for time step. To highlight the impact of the middle local features, weights are designed as follows:

$$w_k = \frac{\exp(q(k))}{\sum_{j=1}^T \exp(q(j))} \quad (8)$$

where

$$q(k) = \min(k - 1, T - k) \quad (9)$$

To give a clear illustration of the above equations, the weights derived by Eq. (8) for a length-10 sequence of local features are illustrated in Fig. 4. Then, the weighted average of local features is fed into a fully-connected dense layer  $F_1$ , and the output of this dense layer is concatenated to  $\mathbf{h}_T$  generated by bi-directional GRU to derive the final representation  $\mathbf{u}$ .

$$\mathbf{u} = \mathbf{h}_T \oplus F_1(\bar{\mathbf{c}}) \quad (10)$$

### C. Supervised Learning Layer

At last, the learned final representation  $\mathbf{u}$  is passed into another fully-connected dense layer  $F_2$  and supervised learning layer. If the targets are discrete labels such as fault types, the supervised learning layer can be softmax layer, which is defined as

$$P\left(\tilde{y} = j \mid F_2(\mathbf{u})\right) = \frac{e^{F_2(\mathbf{u})^T \mathbf{w}_j}}{\sum_{k=1}^K e^{F_2(\mathbf{u})^T \mathbf{w}_k}} \quad (11)$$

where  $K$  is the number of labels and  $\mathbf{w}$  denotes parameters of softmax layer. If the targets are continuous values such as RUL estimation and tool wear depth, the supervised learning layer can be a liner-regression layer given by

$$\tilde{y} = \mathbf{W} F_2(\mathbf{u}) + b \quad (12)$$

where  $\mathbf{W}$  and  $b$  denote transformation matrix and bias value in the liner regression layer. The error between predicted values and ground truth values in training data can be calculated and backpropagated to train the parameters in the whole model. Then, the trained model can be applied on the unseen input data to make prediction about machine condition. The whole framework has been illustrated in Figure 3.

## IV. EXPERIMENTS

To test the performances of our proposed LFGRU machine health monitoring system, three real-life case studies including tool wear prediction, gearbox fault diagnosis and incipient fault diagnosis of rolling element bearings are conducted.

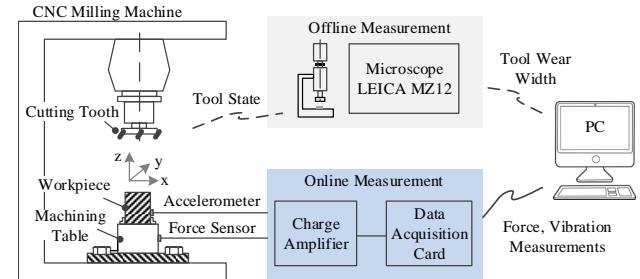


Fig. 5: Schematic of the experimental setup for tool wear prediction [6].

### A. Descriptions of Datasets

**Tool Wear Prediction:** This dataset was collected from a high speed CNC machine operated under dry milling operations [29]. The schematic diagram of experimental platform has been shown in Figure 5. The operation parameters are as follows: the running speed of the spindle was 10,400 rpm; the feed rate in x direction was 1,555 mm/min; The depth of cut (radial) in y direction was 0.125 mm; the depth of cut (axial) in z direction was 0.2 mm. To acquire online data related to this CNC machine's operation condition, a Kistler quartz 3-component platform dynamometer was mounted between the workpiece and the machining table to measure cutting forces, while three Kistler Piezo accelerometers were mounted on the workpiece to measure the machine tool vibration in x, y, z directions, respectively. DAQ NI PCI1200 was adopted to perform in-process measurements including force and vibration in three directions (x,y,z) with a continuous sampling frequency of 50 KHz during the tool wear test. Therefore, the sensory data consists of seven channels: force in three directions, vibration in three directions and AE-RMS. The corresponding flank wear of each individual flute was measured offline using a LEICA MZ12 microscope after finishing each surface which is considered to be one cut number in the following data analysis, which will be the target value. The task is defined as the prediction of the actual flank wear (offline measurement) from the seven-channel sensory data (online measurement). Finally, three individual cutter records named  $c1$ ,  $c4$  and  $c6$  were selected as our dataset. Each test contains 315 data samples, while each data sample has a corresponding flank wear. For training/testing splitting, a three-fold setting is adopted that two tests are used as training domain and the rest one is used as testing domain. Therefore, three different testing cases can be created, which are denoted as C1, C4 and C6. For example, the training/testing splitting scenario C1 is referred to the case that  $c4$  and  $c6$  are adopted as training data and  $c1$  is used as testing data.

**Gearbox Fault Diagnosis:** This experiment was conducted in the Drivetrain Dynamics Simulator (DDS). The DDS is composed of four units including the motor, the planetary gearbox, the parallel gearbox and brake as shown in Figure 6. In the experiment, the faults of gear and bearing were investigated under two different operating conditions where rotating speed and load configuration are set as 20HZ-0V and 30HZ-2V. These two fault locations have their own fault types

TABLE I: Fault Types of Bearing and Gear Components

Component	Types	Description
Bearing	ball	A crack occurs in the ball
	combo	A crack occurs in both inner and outer ring.
	inner	A crack occurs in the inner ring.
	outer	A crack occurs in the outer ring.
Gear	chipped	A crack occurs in the feet.
	miss	One of feet is missing.
	root	A crack occurs in the root of feet.
	surface	The wear occurs in the surface.

as described in Table I, where the real images of these fault types and locations are shown in Figure 7. Therefore, four different fault diagnosis datasets are created and each of them is a five-class categorization task (four fault conditions and one health condition). The sensing configuration is described as follows: seven vibrating 608A11 sensors whose frequency range, measuring range and accuracy are 0.5Hz-10kHz,  $\pm 50$ g and 100mV/g were adopted in the surface of DDS test-bed. Three of them measured the vibration of planetary gearbox in three directions: x, y and z, other three of them measured the three direction vibrations of the gear box, and the rest one was used to measure the driving motor. A torque sensor (model: FT293; measuring range:  $\pm 5$ V; accuracy: 4Nm/V) was mounted between the motor and the planetary gearbox to measure the load. And a compact spectra PAD data acquisition instrument (Max 20 channels) was adopted for signal collecting with 1024Hz sampling frequency and 512s sampling window.

**Incipient Fault Diagnosis of Rolling Element Bearings:** This testing scenario is introduced to verify the performance of our model in the area of incipient fault diagnosis. Here, we used the experimental data from the bearing data center in the Case Western Reserve University (CWRU)<sup>1</sup> following the procedures adopted in [30] that vibration data under the smallest damage radius 7mils are selected. Due to page limits, the description of CWRU experimental platform and data acquisition system are skipped, which can be referred in [30]. Here, we create a four-class classification task. The corresponding classes include health condition, inner fault, ball fault and outer fault and each class contains 800 data samples. Each data sample is the vibration signal acquired on fan end whose length is fixed to 20000.

### B. Experimental Setup

In our experiments, several methods are compared as follows:

- SVM/SVR: Support Vector Machine/Regression with rbf kernel;
- MLP: Neural Network with two hidden layers;
- KNN: k-Nearest Neighbors
- SAE-DNN:

<sup>1</sup>The dataset has been kindly provided at <http://csegroups.case.edu/bearingdatacenter/home>

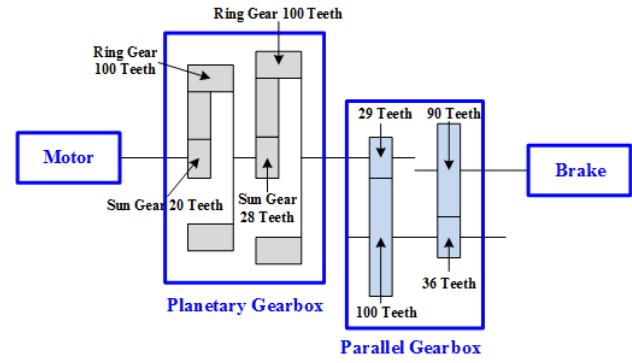
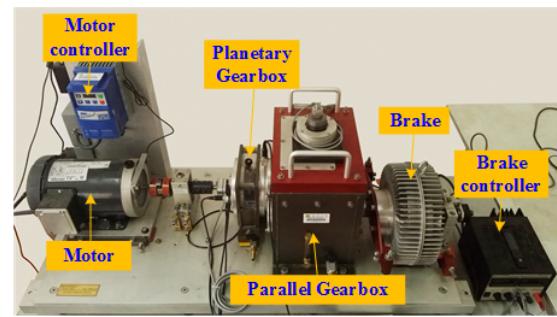


Fig. 6: Schematic of the experimental setup for gearbox fault diagnosis.

- ◊ RNN: Vanilla RNN
- ◊ GRU: Gated Recurrent Units Networks
- ◊ BiGRU: Bi-directional Gated Recurrent Units Networks
- ◊ LFGRU: Our proposed local featured-based Gated Recurrent Units

Here  $\bullet$  denotes the handcrafted feature from the whole range of raw signal and  $\diamond$  denotes the local feature extraction following the steps illustrated in Section III-A.

In tool wear prediction tasks, considering the multi-sensory input contain seven channels, the dimensionality of the hand-crafted feature vector is 70, which includes time domain, frequency domain and time-frequency domain features as illustrated in Table II. Here, the wavelet energy feature is the energy of a 8-level wavelet packet decomposition using  $db1$ , which corresponds to the wavelet coefficient with higher energy that is related to the characteristic frequency of the machine. In SVR, we search the best regularization parameter from  $[0.001, 0.01, 0.1, 1, 10]$ . In KNN, we search the best neighbor neighbors from  $[3, 5, 7, 9]$ . The layer sizes behind MLP and SAE-DNN are unified to be  $[140, 200]$  and their top layer is a linear regression layer to predict tool wear depth. For the last four methods, the shape of the input sequence of local features is  $20 \times 70$ . And the sizes of hidden recurrent layer in these four recurrent neural networks are unified to be the same as 100. In our proposed method, the sizes of FC-Layer 1  $F_1$  and FC-Layer 2  $F_2$  are set to be 100 and 400, respectively. One of gradient descent optimization algorithms: RMSprop is adopted to train these four models [31]. The other hyperparameters including learning rates and epoch number are all searched via validation dataset. To quantify the performance of all compared methods, two measures to



Fig. 7: Fault Types Illustrations.

evaluate regression loss are used including mean absolute error (MAE) and root mean squared error (RMSE). MAE is the average value of the absolute values of the errors. RMSE is the square root of the average of the square of all of the errors. The corresponding equations for the calculations of these two measures over  $n$  testing samples are given as follows:

$$MAE = \frac{1}{n} \sum_{i=1}^n |\tilde{y}_i - y_i| \quad (13)$$

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (\tilde{y}_i - y_i)^2} \quad (14)$$

where  $y_i$  and  $\tilde{y}_i$  are true and predicted tool wear depth.

In gearbox fault diagnosis tasks, the dimensionality of the handcrafted feature vector is 27 that the first 9 features described in Table II are extracted for three sensors on three directions. In SVM and KNN, we select their best hyperparameters using the same setting discussed above. MLP and SAE-DNN share the same structure of DNN in finetuning phase that the layer size is [54, 108] and the top layer is a softmax layer to classify machine conditions. In SAE-DNN, before finetuning, unsupervised training is performed by a stacked denoising autoencoder. The nonlinear activation function is set to be tanh. For the last four methods, the number of segments is  $T = 20$ , and thus the shape of the input sequence of local features is  $20 \times 27$ . And the sizes of hidden recurrent layer in these four recurrent neural networks are unified to be the same as 50. In our proposed method, the sizes of FC-Layer 1  $F_1$  and FC-Layer 2  $F_2$  are set to be 50 and 200, respectively. The RMSprop is adopted to train these four models and the other hyperparameters including learning rates and epoch number are all searched based on validation dataset. To quantify the performance of all compared methods,

TABLE II: Handcrafted Feature Sets for Gearbox Fault Diagnosis and Tool Wear Prediction

Quantity	Equations
RMS	$z_{rms} = \sqrt{\frac{1}{n} \sum_{i=1}^n z_i^2}$
Variance	$\frac{1}{n} \sum_{i=1}^n (z_i - \bar{z})^2$
Maximum	$\max(z)$
Skewness	$E[(\frac{z-\mu}{\sigma})^3]$
Kurtosis	$E[(\frac{z-\mu}{\sigma})^4]$
Peak-to-Peak	$\max(z) - \min(z)$
Spectral Skewness	$\sum_{i=1}^k (\frac{f_i - \bar{f}}{\sigma})^3 S(f_i)$
Spectral Kurtosis	$\sum_{i=1}^k (\frac{f_i - \bar{f}}{\sigma})^4 S(f_i)$
Spectral Power	$\sum_{i=1}^k (f_i)^3 S(f_i)$
Wavelet Energy	$\sum_{i=1}^N w_{\phi}^2(i)/N$

the classification accuracy over 5-fold training/testing splitting is reported.

In incipient fault diagnosis task, the dimensionality of the handcrafted feature vector is 10 as the one-channel vibration data is used. The layer size in MLP and SAE-DNN is [20, 40]. For the last four methods, the number of segments is  $T = 20$  so that the shape of the input sequence of local features is  $20 \times 10$ . And the sizes of hidden recurrent layer in these four recurrent neural networks are unified to be the same as 20. In our proposed method, the sizes of FC-Layer 1  $F_1$  and FC-Layer 2  $F_2$  are set to be 20 and 80, respectively. The other settings for all comparative methods and training/testing splitting scheme are kept the same as reported in the above gearbox fault diagnosis tasks.

### C. Experimental Results

In tool wear prediction tasks which is more challenging compared to fault diagnosis tasks, two measures including

MAE and RMSE are reported in Table III. It is shown that our proposed LFGRU achieves the lowest regression error among all compared methods. Compared to the most competitive model: BiGRU, the enhanced GRU networks concatenates the weighted averaging of local features and the output of BiGRU. Therefore, the experimental results have verified the effectiveness of the weighted feature averaging operation in our proposed model. And recurrent models based on local features especially three GRU variants outperform the rest models, which have demonstrated that the temporal information encoded by GRU can boost the tool wear prediction. At last, we found most of compared models perform slightly worse in dataset C6 than that in the rest two datasets. It may be explained by the fact that the distribution of  $c6$  is different from the other two datasets  $c1$  and  $c4$ . However, our proposed LFGRU model presents a robust performance over dataset C6. It further verifies the effectiveness of the hybrid combination of local feature extraction and the enhanced GRU networks. Finally, to qualitatively demonstrate the effectiveness of our proposed model, the predicted tool wears under different datasets are illustrated in Fig 8. The actual tool wear conditions measured offline by a microscope are also displayed, respectively. It is found that the predicted tool wear overall are able to follow the trend of the truth data well.

In gearbox fault diagnosis tasks and incipient fault detection task, the results are shown in Table IV. We compare our proposed method with several state-of-the-art methods. The first observation is that recurrent models including RNN, GRU, BiGRU and our proposed LFGRU that encode temporal information over the sequence of local features perform better than conventional data-driven models including SVM, KNN and MLP and the deep learning model: SAE-DNN. Therefore, the importance of modeling the temporal dependency in fault diagnosis has been verified. Among all recurrent models based on local features, our proposed model outperforms other models. It should be explained by the introduction of bi-directional recurrent structure and center-biased feature averaging scheme. As shown in Table IV, the robust performance achieved by our proposed method in the above two fault diagnosis tasks verify the generalization capability of our method over various fault severity and machinery equipments.

In addition, the robustness of our system on the quality of handcrafted design was investigated. We vary the number of adopted handcrafted features in the range [10, 15, 20, 25, 27] into SVM model and our proposed LFGRU. And the classification accuracies on one dataset: bearing (20HZ-0V) are shown in Figure 9. It is clear that even with 10 hand-crafted features, the accuracy achieved by our method can be as high as 0.8, which significantly outperforms SVM model. To illustrate the effectiveness of our proposed method intuitively, the learned representation by our model has been visualized in Figure 10. Here, we only report the results in gear dataset under a rotating speed of 30HZ and a load of 2V. t-SNE algorithm [32] is adopted to project the high-dimensional representation into a 2D space. The separability demonstrates the capability of our model to learn discriminative and informative representation from mechanical signals.

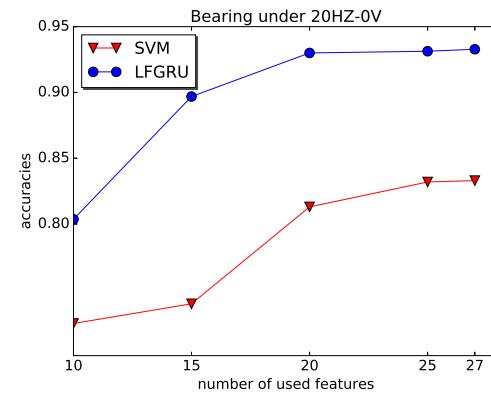


Fig. 9: Performances of SVM and LFGRU under different subsets of input features.

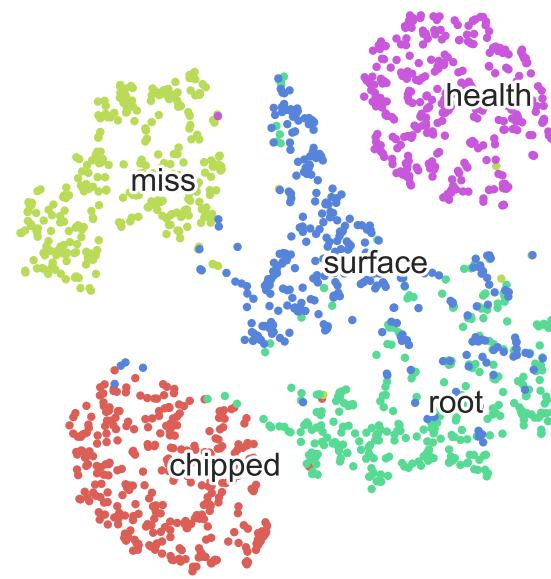


Fig. 10: 2D Projection of Gear Dataset. The representation is learned by LFGRU.

At last, all of our experiments are conducted using four Nvidia GTX GPUs 1080 on a Linux Server with a 3.60GHz Intel CPU. The testing time for each sample of our algorithm is only 0.009s, which is suitable for real-time monitoring.

TABLE III: MAE(a) and RMSE(b) Achieved by Compared Methods in Tool Wear Prediction Tasks. Bold Face Indicates Best Performances

Algorithms	(a)			(b)			
	C1	C4	C6	C1	C4	C6	
SVR	6.9	10.0	31.1	SVR	9.6	12.4	34.3
KNN	10.3	12.7	28.7	KNN	13.0	15.4	31.6
MLP	11.2	11.6	30.1	MLP	13.7	14.1	31.9
SAE-DNN	10.9	9.5	29.5	SAE-DNN	13.7	11.8	31.2
RNN	8.6	8.1	10.1	RNN	10.8	10.7	25.5
GRU	5.9	7.0	11.6	GRU	7.9	8.8	12.9
BiGRU	5.5	7.4	9.4	BiGRU	6.8	9.2	11.1
<b>LFGRU</b>	<b>4.0</b>	<b>6.9</b>	<b>5.8</b>	<b>LFGRU</b>	<b>5.4</b>	<b>8.3</b>	<b>8.2</b>

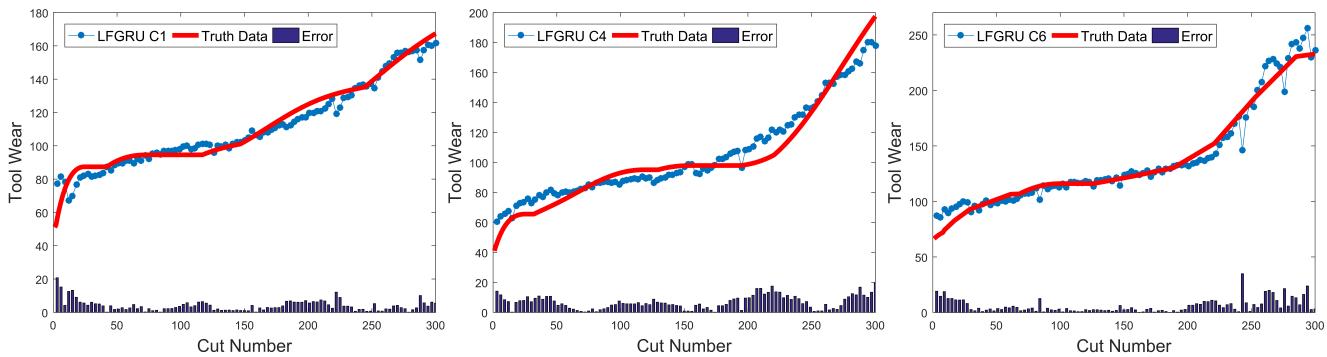


Fig. 8: Regression Analysis of tool wear predicted by LFGRU.

TABLE IV: Classification Accuracy achieved by Compared Methods in Gearbox Diagnosis Tasks and Incipient Fault Diagnosis. Bold Face Indicates Best Performances.

Algorithms	Bearing		Gear		Incipient Faults
	20-0	30-2	20-0	30-2	
SVM	0.833	0.886	0.944	0.901	0.972
KNN	0.808	0.864	0.932	0.892	0.956
MLP	0.865	0.905	0.843	0.906	0.968
SAE-DNN	0.875	0.921	0.927	0.919	0.974
RNN	0.929	0.920	0.923	0.893	0.956
GRU	0.912	0.924	0.938	0.905	0.981
BiGRU	0.930	0.936	0.938	0.907	0.985
<b>LFGRU</b>	<b>0.932</b>	<b>0.940</b>	<b>0.948</b>	<b>0.958</b>	<b>0.996</b>

#### D. Sensitivity Analysis on Number of Segments

Number of segments  $T$  is a hyperparameter to control the length of the sequential input into our proposed LFGRU model. It is clear that a small  $T$  will make the size of local segments large so that the too much sequential information may be lost. Under a large  $T$ , the small size of local segment may not be able to derive discriminative local features and the computational burden is increased at the same time. To verify the above statement empirically, we tested our proposed LFGRU under five additional different numbers of segments:  $T = [5, 10, 50, 100, 200]$  and our previous setting  $T = 20$  over one tool prediction task C1. The other parameters of our proposed LFGRU are kept unchanged as reported before. The RMSE and MAE are compared and shown in Figure 11. It can be shown that very large and small  $T$  both hinder the performance of our proposed LFGRU. Under moderate numbers of segments such as 10 and 20, our proposed LFGRU model is able to achieve optimal performance.

#### V. CONCLUSION

A new deep learning based machine health monitoring system, i.e., LFGRU has been proposed. After local feature extraction, a sequence of local features can be generated which does not require a high-level expert knowledge. Then, an enhanced GRU networks is adopted to learn representation of the sequence of local features. In three real machine health

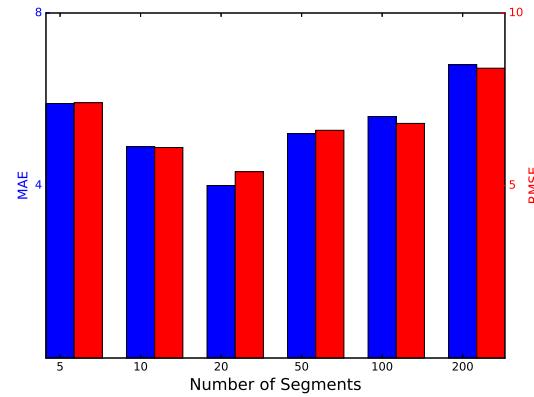


Fig. 11: Performances of our LFGRU under different number of segments.

monitoring tasks, the effectiveness and robustness of our proposed LFGRU model has been verified.

In the future work, we are going to explore the performance of our framework in the prognosis tasks. For example, the estimation of remaining useful life (RUL) can be casted into a regression problem [33], then our proposed technique may be adopted to predict the target RUL value from raw input signal.

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