

**Instituto de
Computação**

UNIVERSIDADE ESTADUAL DE CAMPINAS



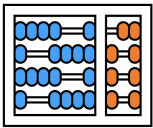
Capacitação profissional em tecnologias de Inteligência Artificial

Machine Learning Overview

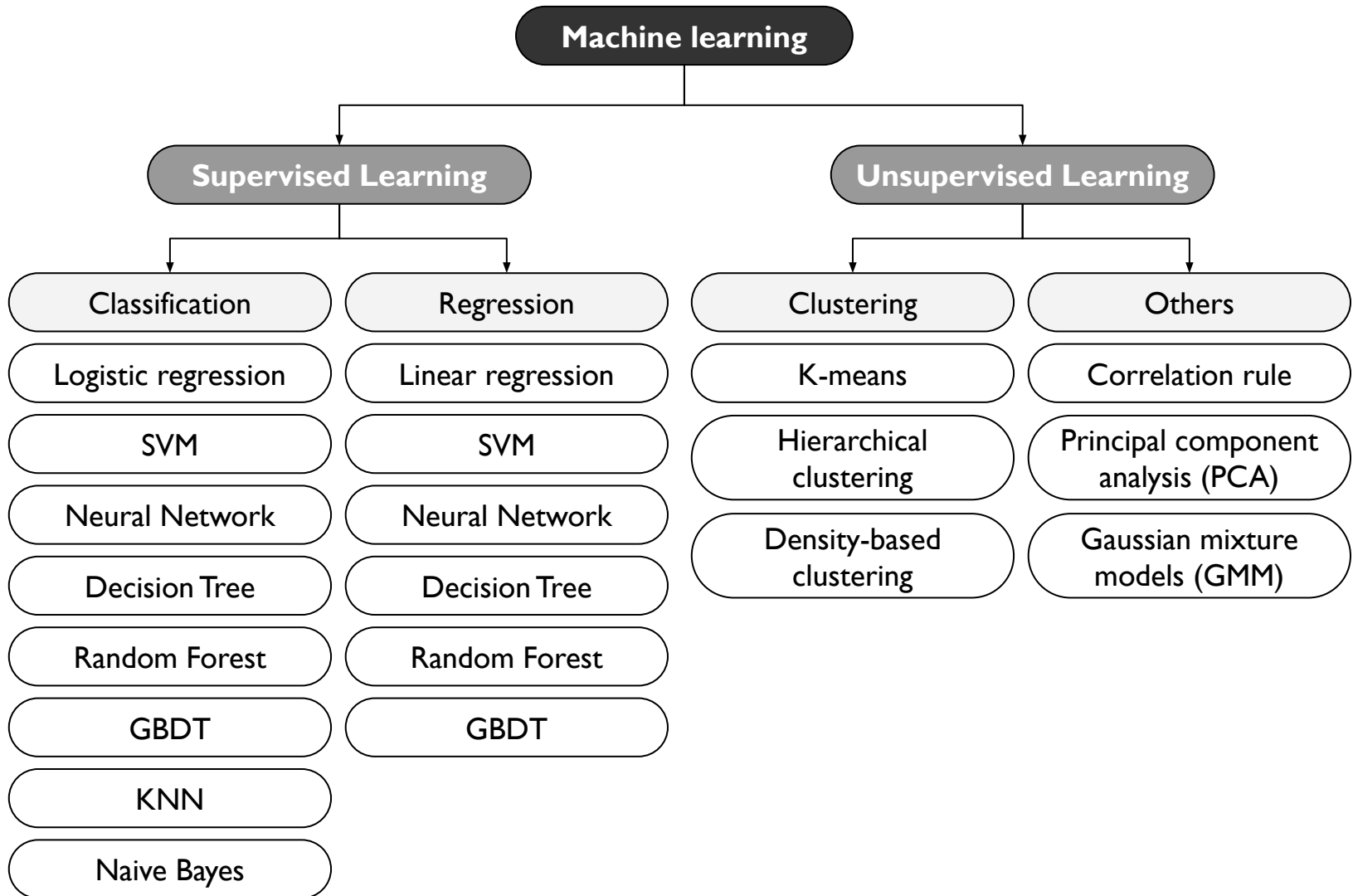
Prof. Edson Borin

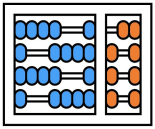
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Institute of Computing - UNICAMP



Common ML Algorithms





Supervised Learning Algorithms



Linear Regression

Supervised Learning Algorithms

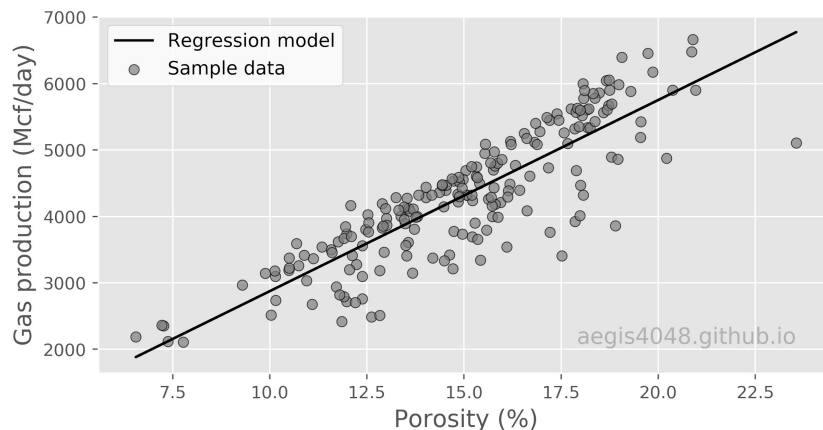
Linear Regression



Linear regression

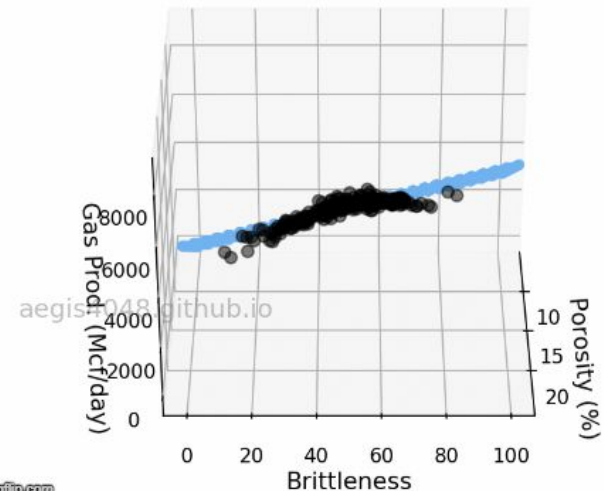
- Statistical analysis method to determine linear relationships between a scalar response (output variable or label) and one or more explanatory variables (input variables or features)

Univariate



Source: https://aegis4048.github.io/mutiple_linear_regression_and_visualization_in_python

Multivariate



Supervised Learning Algorithms

Linear Regression



Linear regression

Let:

- θ : Set of model parameters. $\theta = \{\theta_0, \theta_1, \dots, \theta_n\}$
- x : Set of input variables. $x = \{x_1, x_2, \dots, x_n\}$
- \hat{y} : model output (predicted value)
- $\hat{y} = \theta_0 + \theta_1 \cdot x_1 + \dots + \theta_n \cdot x_n$
- $\hat{y} = \theta_0 + \theta_1 \cdot x_1$
- $h_\theta(x) = \theta_0 + \theta_1 \cdot x_1 + \dots + \theta_n \cdot x_n$

Multivariate linear model

Univariate linear model

Also known has hypothesis!

Supervised Learning Algorithms

Linear Regression



Linear regression

Linear model

- $$h_{\theta}(x) = \theta_0 + \theta_1 \cdot x_1 + \dots + \theta_n \cdot x_n$$

Supervised Learning Algorithms

Linear Regression



Linear regression

Linear model

- $$h_{\theta}(x) = \theta_0 + \theta_1 \cdot x_1 + \dots + \theta_n \cdot x_n$$

Also explained as:

- $$h_w(x) = \mathbf{b} + \mathbf{w}_1 \cdot x_1 + \dots + \mathbf{w}_n \cdot x_n$$
- $$h(x) = \text{intercept} + \text{coef}_1 \cdot x_1 + \dots + \text{coef}_n \cdot$$

x_n

Supervised Learning Algorithms

Linear Regression



Linear regression

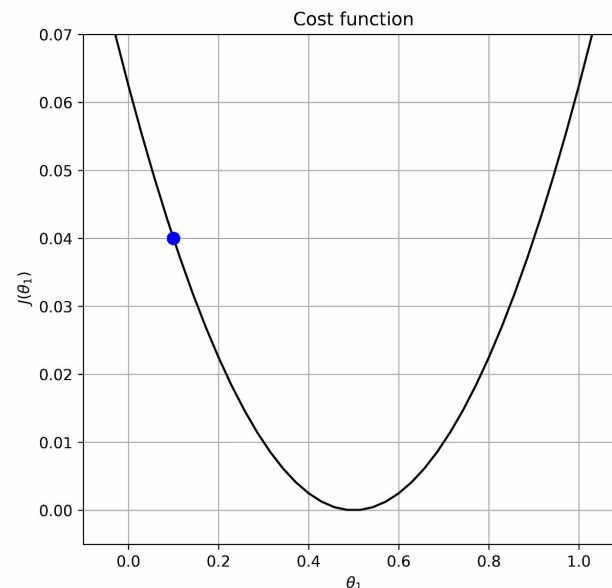
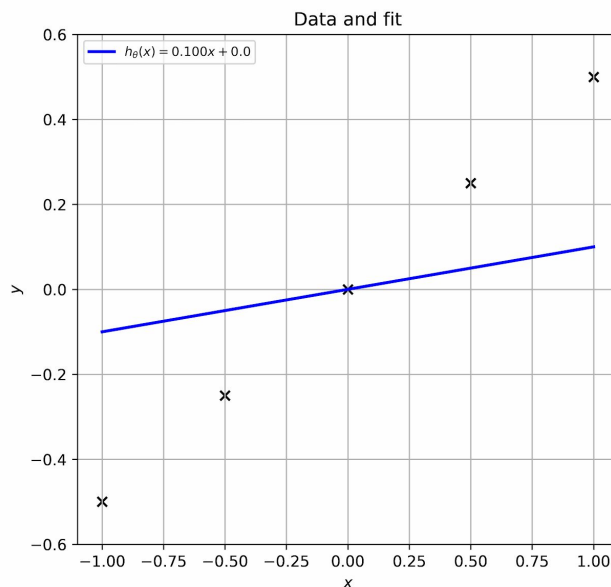
Linear model

- $$h_{\theta}(x) = \theta_0 + \theta_1 \cdot x_1 + \dots + \theta_n \cdot x_n$$

Training

Select θ so that the cost function is minimized

Gradient Descent: First $\theta_1=0.10$, $\alpha=0.80$, # steps = 0



Supervised Learning Algorithms

Linear Regression



Linear regression

Linear model

- $$h_{\theta}(x) = \theta_0 + \theta_1 \cdot x_1 + \dots + \theta_n \cdot x_n$$

Cost function:

- Usually the Mean Squared Error (MSE)

$$J(\theta) = \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

$\underbrace{\hspace{10em}}_{\text{MSE}(X, h_{\theta})}$

Supervised Learning Algorithms

Linear Regression



Linear regression

Linear model

- $$h_{\theta}(x) = \theta_0 + \theta_1 \cdot x_1 + \dots + \theta_n \cdot x_n$$

Cost function:

- Usually the Mean Squared Error (MSE)

$$J(\theta) = \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

MSE(X, h_{θ})

Can also be the Mean Absolute Error (MAE)

Supervised Learning Algorithms

Linear Regression



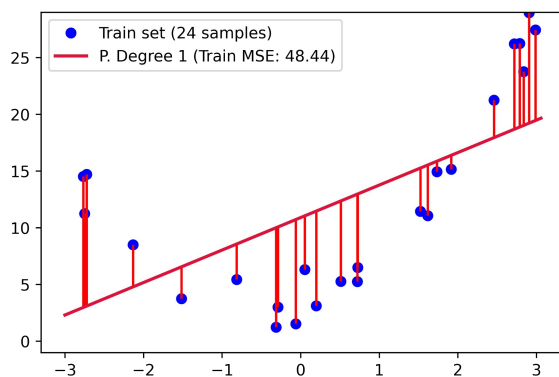
Polynomial regression

Similar to linear regression.

Polynomial model

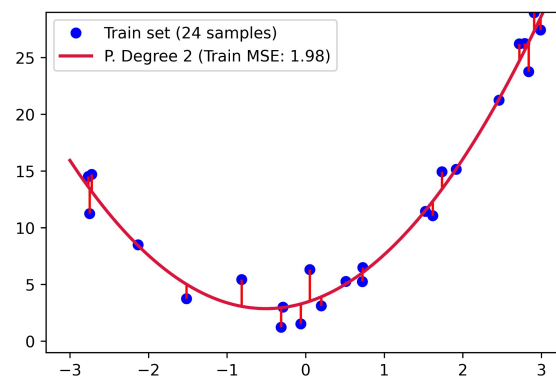
- $$h_{\theta}(x) = \theta_0 + \theta_1 \cdot x_1 + \theta_2 \cdot x_1^2 + \theta_3 \cdot x_1^3 + \dots + \theta_n \cdot x_1^n$$

Linear model



$$f(x) = 10.895022 + 2.863998 x$$

Poly. degree = 2



$$f(x) = 3.403875 + 2.122188 x + 2.099980 x^2$$

Supervised Learning Algorithms

Linear Regression

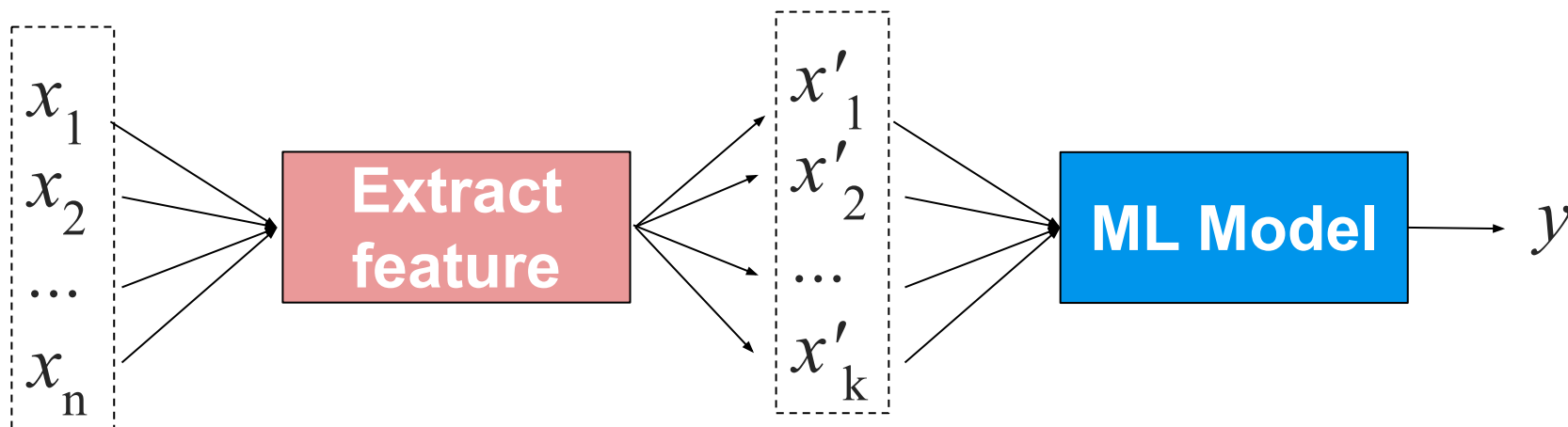


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Polynomial model

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Supervised Learning Algorithms

Linear Regression

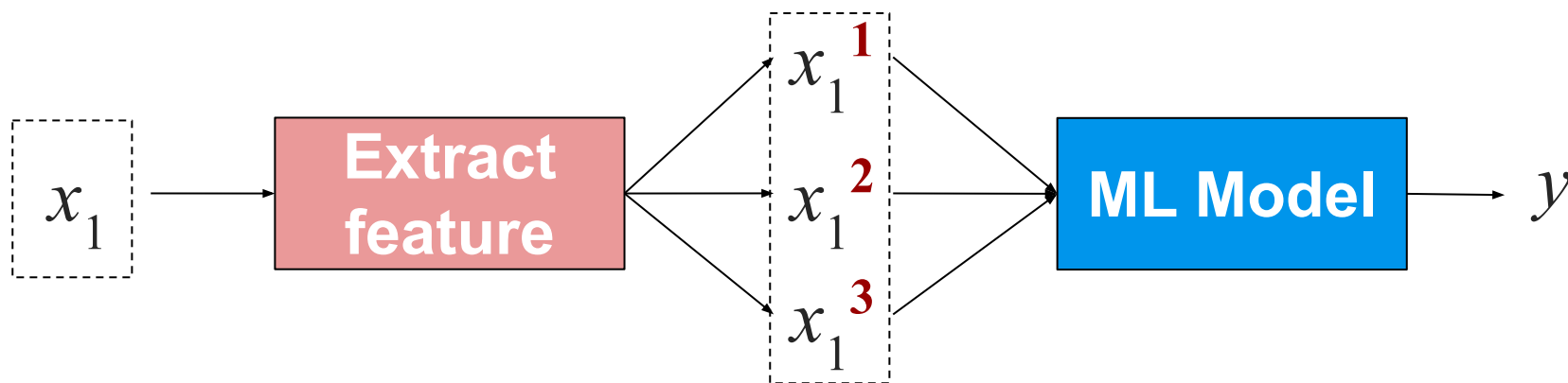


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Supervised Learning Algorithms

Linear Regression

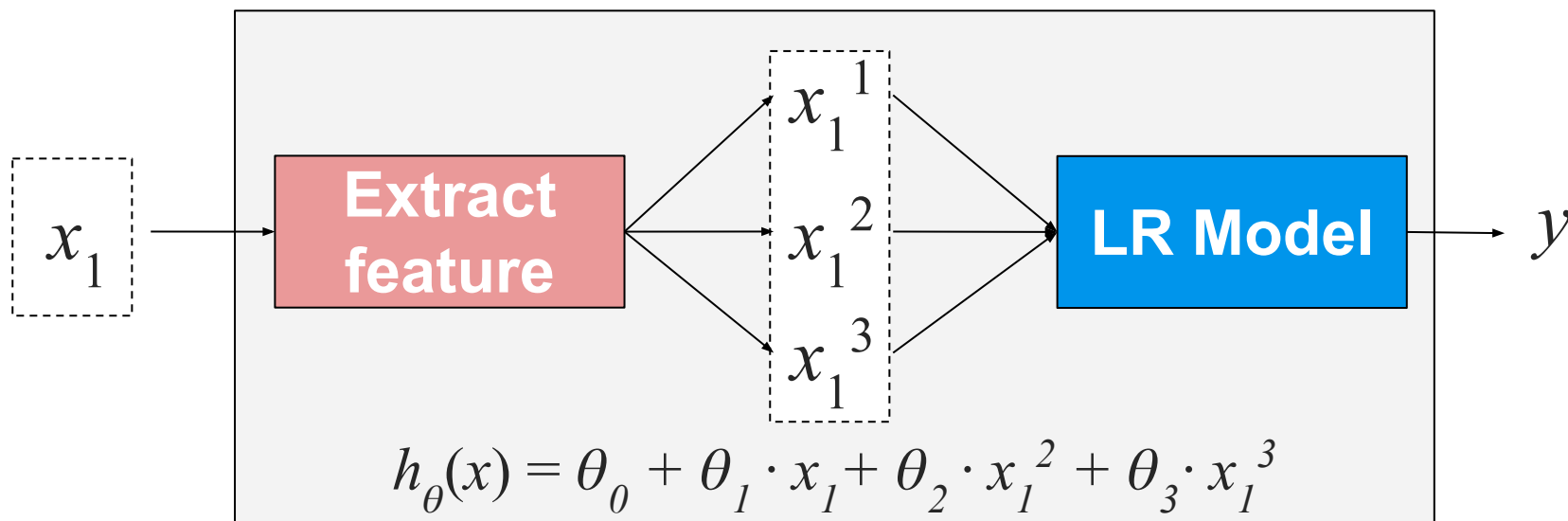


Polynomial regression

Similar to linear regression.

Polynomial model

- $$h_{\theta}(x) = \theta_0 + \theta_1 \cdot x_1 + \theta_2 \cdot x_1^2 + \theta_3 \cdot x_1^3 + \dots + \theta_n \cdot x_1^n$$



Supervised Learning Algorithms

Linear Regression



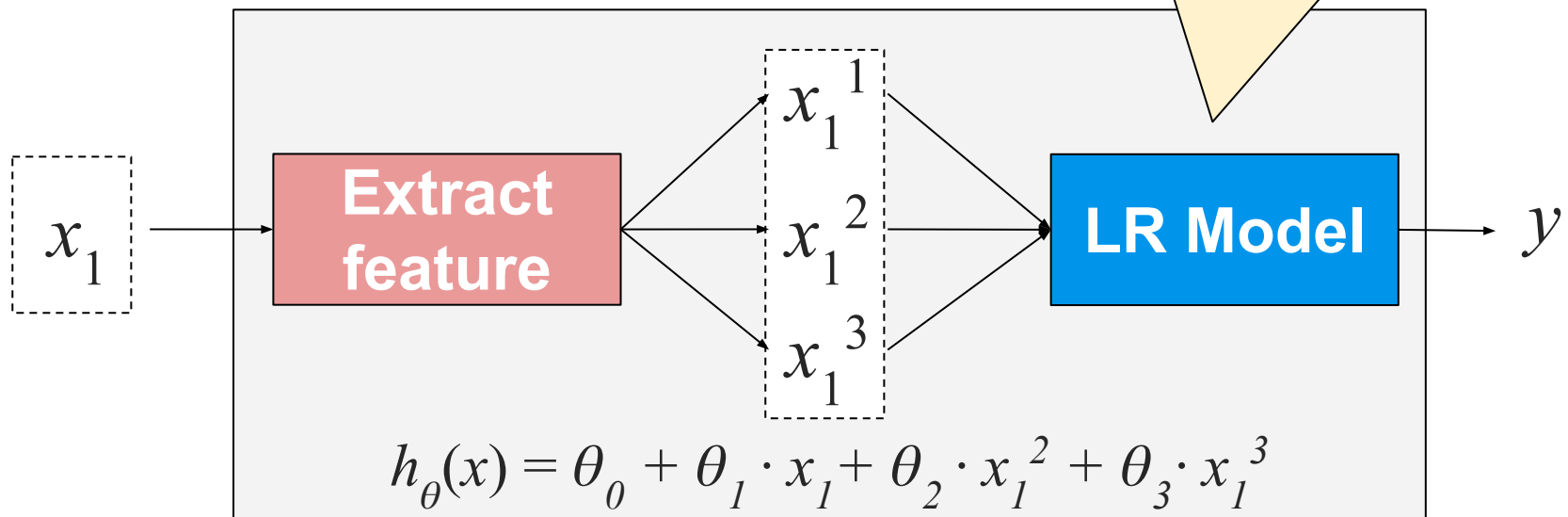
Polynomial regression

Similar to linear regression

Polynomial model

- $h_{\theta}(x) = \theta_0 + \theta_1 \cdot x_1 + \theta_2 \cdot x_1^2 + \theta_3 \cdot x_1^3 + \dots + \theta_n$

Train in the same way we train linear regression models!



Supervised Learning Algorithms

Linear Regression



Polynomial regression

Similar to linear regression

Polynomial model

- $h_{\theta}(x) = \theta_0 + \theta_1 \cdot x_1 + \theta_2 \cdot x_1^2 + \theta_3 \cdot x_1^3 + \dots + \theta_n$

Train in the same way we train linear regression models!

Polynomial regression belongs to linear regression as the relationship between its parameters θ is still linear while its nonlinearity is reflected in the feature dimension.

LR Model

y

$$\theta_2 \cdot x_1^2 + \theta_3 \cdot x_1^3$$

Supervised Learning Algorithms

Linear Regression



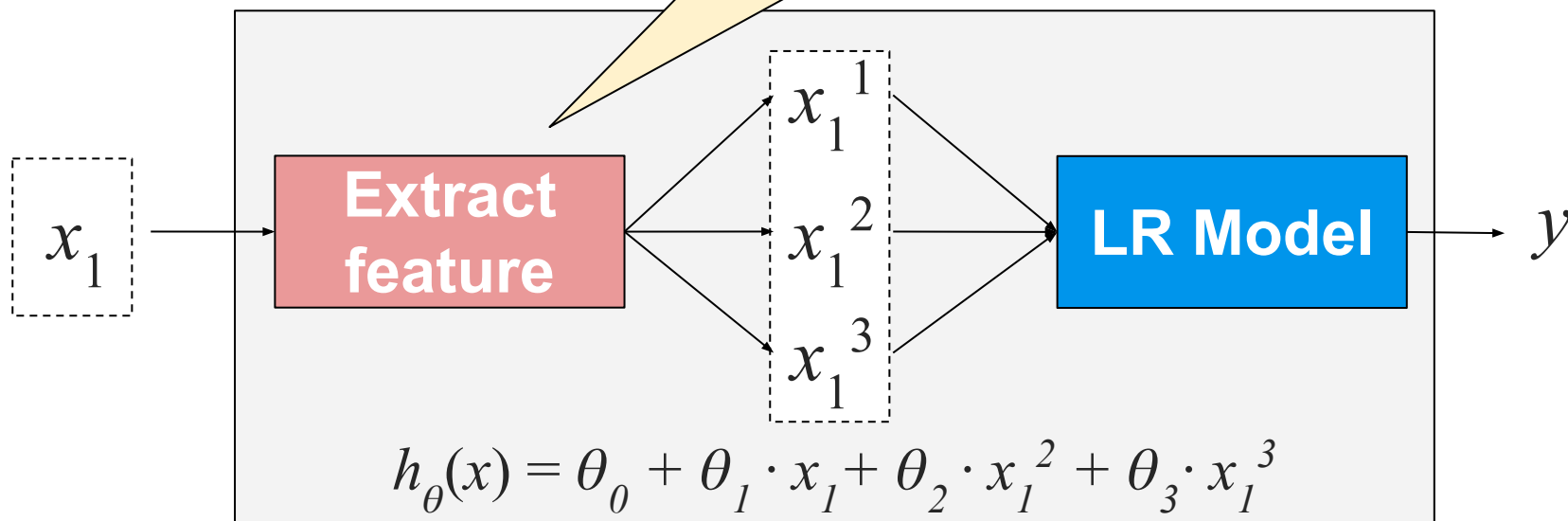
Polynomial regression

Similar to linear regression

Polynomial model

- $$h_{\theta}(x) = \theta_0 + \theta_1 \cdot x_1 + \theta_2 \cdot x_1^2 + \theta_3 \cdot x_1^3 + \dots + \theta_n \cdot x_1^n$$

Scikit Learn
PolynomialFeatures module



Supervised Learning Algorithms

Linear Regression



Ridge/Lasso regression

In linear (and polynomial) regression, the more input variables, the more parameters the model will have, and the greater the chance of overfitting the training data

Supervised Learning Algorithms

Linear Regression



Ridge/Lasso regression

In linear (and polynomial) regression, the more input variables, the more parameters the model will have, and the greater the chance of overfitting the training data

An approach to minimize overfit is to tweak the training process to produce a model with small parameter (θ) values

Supervised Learning Algorithms

Linear Regression



Ridge/Lasso regression

In linear (and polynomial) regression the more input variables, the more parameters we have, and the greater the risk of overfitting the training data

This is called regularization!

An approach to minimize overfit is to tweak the training process to produce a model with small parameter (θ) values

Supervised Learning Algorithms

Linear Regression



Ridge/Lasso regression

How do we tweak the training process to produce a model with small parameter (θ) values?



Supervised Learning Algorithms

Linear Regression



Ridge/Lasso regression

How do we tweak the training process to produce a model with small parameter (θ) values?

- By penalizing the cost function with θ values!

$$J(\theta) = \underbrace{\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2}_{\text{MSE}(X, h_{\theta})} + (\theta_1^2 + \theta_2^2 + \dots + \theta_n^2)$$

Supervised Learning Algorithms

Linear Regression



Ridge/Lasso regression

How do we tweak the training process to produce a model with small parameter (θ) values?

- By penalizing the cost function with θ values!

θ_0 (a.k.a. bias) is not penalized

$$J(\theta) = \underbrace{\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2}_{\text{MSE}(X, h_{\theta})} + (\theta_1^2 + \theta_2^2 + \dots + \theta_n^2)$$

Supervised Learning Algorithms

Linear Regression



Ridge/Lasso regression

How do we tweak the training process to produce a model with small parameter (θ) values?

- By penalizing the cost function with θ values!

$$J(\theta) = \underbrace{\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2}_{\text{MSE}(X, h_{\theta})} + \alpha \cdot (\theta_1^2 + \theta_2^2 + \dots + \theta_n^2)$$

α : hyperparameter

Supervised Learning Algorithms

Linear Regression



Ridge/Lasso regression

How do we tweak the training function to train a model with small parameters?

- By penalizing the cost function

Assuming $w = \{\theta_1, \dots, \theta_n\}$,
then, $(\theta_1^2 + \theta_2^2 + \dots + \theta_n^2) = \|w\|_2^2$

$$J(\theta) = \underbrace{\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2}_{\text{MSE}(X, h_{\theta})} + \alpha \cdot (\theta_1^2 + \theta_2^2 + \dots + \theta_n^2)$$

Supervised Learning Algorithms

Linear Regression



Ridge/Lasso regression

How do we tweak the training procedure to train a model with small parameters?

- By penalizing the coefficients

Assuming $w = \{\theta_1, \dots, \theta_n\}$,
then, $(|\theta_1| + |\theta_2| + \dots + |\theta_n|) = ||w||_1$

$$J(\theta) = \underbrace{\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2}_{\text{MSE}(X, h_{\theta})} + \alpha \cdot (|\theta_1| + |\theta_2| + \dots + |\theta_n|)$$

Supervised Learning Algorithms

Linear Regression



Ridge/Lasso regression

$$J(\theta) = \underbrace{\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2}_{\text{MSE}(X, h_{\theta})} + \alpha \cdot (\theta_1^2 + \theta_2^2 + \dots + \theta_n^2)$$

Ridge regression

$$J(\theta) = \underbrace{\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2}_{\text{MSE}(X, h_{\theta})} + \alpha \cdot (|\theta_1| + |\theta_2| + \dots + |\theta_n|)$$

Lasso regression

Supervised Learning Algorithms



Linear

Ridge/Lasso regression

Tends to produce small parameter values (close to zero), but not zero.

$$J(\theta) = \underbrace{\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2}_{\text{MSE}(X, h_{\theta})} + \alpha \cdot (\theta_1^2 + \theta_2^2 + \dots + \theta_n^2)$$

Ridge regression

$$J(\theta) = \underbrace{\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2}_{\text{MSE}(X, h_{\theta})} + \alpha \cdot (|\theta_1| + |\theta_2| + \dots + |\theta_n|)$$

Tends to zero-out parameters associated with non-informative features! Can be used to simplify models!

$$h_{\theta}(x) = \theta_0 + \theta_1 \cdot x_1 + \dots + \theta_n \cdot x_n$$

Supervised Learning Algorithms

Linear Regression



Ridge/Lasso regression

$$J(\theta) = \underbrace{\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2}_{\text{MSE}(X, h_{\theta})} + \alpha \cdot (\theta_1^2 + \theta_2^2 + \dots + \theta_n^2)$$



Make sure you perform
feature scaling if using
Ridge/Lasso regression

Supervised Learning Algorithms

Linear Regression



Elastic Net regression

- Combines both Ridge and Lasso regression
- Hyperparameter r : mix ratio

$$J(\theta) = \underbrace{\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2}_{\text{MSE}(X, h_{\theta})} + \underbrace{r \cdot \alpha \cdot \sum_{i=1}^n |\theta_i|}_{\substack{\text{Lasso} \\ \text{Regularization} \\ \text{Term}}} + \underbrace{(1-r) \cdot \alpha \cdot \sum_{i=1}^n (\theta_i)^2}_{\substack{\text{Ridge} \\ \text{Regularization} \\ \text{Term}}}$$

r : mix ratio

Supervised Learning Algorithms

Linear Regression



General recommendations

- It is usually preferable to have at least a little bit of regularization: Avoid plain LR!
- Make sure you perform feature scaling if using Ridge/Lasso/Elastic Net regression
- Ridge is a good default, but if you suspect only a few features are actually useful, you should prefer Lasso or Elastic Net
 - Both tend to reduce the useless features' weights down to zero.

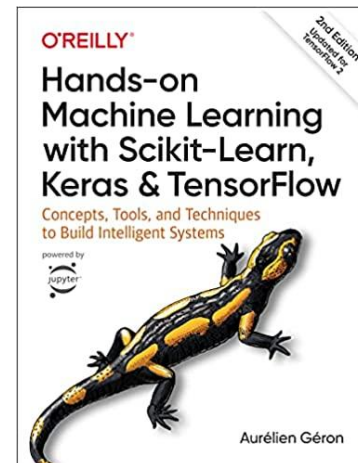
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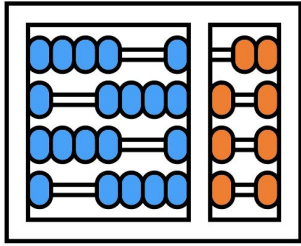
Linear Regression



References

- Aurelien Geron. Hands-on Machine Learning with Scikit-Learn, Keras, and TensorFlow: Concepts, Tools, and Techniques to Build Intelligent Systems - 2019
 - Chapter 4
- Logistic Regression on the scikit-learn website:
 - https://scikit-learn.org/stable/modules/linear_model.html





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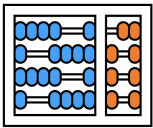
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Video Index



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| | | 0:03:30 | 0:02:35 | Linear Regression |
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| | | 0:08:31 | 0:05:23 | Polynomial Regression |
| | | 0:13:54 | 0:06:27 | Ridge/Lasso regression |
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