

$$\begin{array}{ccc}
 \mathcal{P}_k(W) & \hookrightarrow & \mathcal{P}_L(W_L) \\
 \downarrow \ell & \nearrow \sim & \\
 \mathcal{P}_k(W)_L & & 
 \end{array}$$