Perception

Some resources

- Stevens' power law
  - Appearance compensation, Perceptual Scaling of Map Symbols
- Colors
  - Value-Suppressing Uncertainty Palettes - an interesting example of exploiting the human color perception (see paper 2018-UncertaintyPalettes-CHI.pdf)
- Pre-attentive processing
- Christopher Healey: Perception in Visualization
- Further readings
  - Design principles for visual communication (see p60-agrawala.pdf)
  - Data visualization: A view of every Points of View column
  - Color coding (see nmeth0810-573.pdf)
  - Design of data figures (see nmeth0910-665.pdf)
  - Salience (see nmeth1010-773.pdf)
  - Gestalt principles (Part 1) (see nmeth1110-863.pdf)
  - Avoiding color (see nmeth.1642.pdf)
  - Crowdsourcing Graphical Perception: Using Mechanical Turk to Assess Visualization Design (see 2010-MTurk-CHI.pdf)

Perception

Perform a small experiment to test the perception of length and area.

In [24]:
```
import pandas as pd
import math
import matplotlib.pyplot as plt
%matplotlib inline
```

Vega datasets

Before going into the perception experiment, let's first talk about some handy datasets that you can play with.

It's nice to have clean datasets handy to practice data visualization. There is a nice small package called `vega-datasets`, from the altair project.

You can install the package by running

```
$ pip install vega-datasets
```

or

```
$ pip3 install vega-datasets
```

Once you install the package, you can import and see the list of datasets:

In [25]:
```
from vega_datasets import data

data.list_datasets()
```

Out[25]:
```
['7zip',
 'airports',
 'annual-precip',
 'anscombe',
 'barley',
 'birdstrikes',
 'budget',
 'budgets',
 'burtin',
 'cars',
 'climate',
 'co2-concentration',
 'countries',
 'crimea',
 'disasters',
 'driving',
 'earthquakes',
 'ffox',
 'flare',
 'flare-dependencies',
 'flights-10k',
 'flights-200k',
 'flights-20k',
 'flights-2k',
 'flights-3m',
 'flights-5k',
 'flights-airport',
 'gapminder',
 'gapminder-health-income',
 'gimp',
 'github',
 'graticule',
 'income',
 'iowa-electricity',
 'iris',
 'jobs',
 'la-riots',
 'londonBoroughs',
 'londonCentroids',
 'londonTubeLines',
```

```
 'lookup_groups',
 'lookup_people',
 'miserables',
 'monarchs',
 'movies',
 'normal-2d',
 'obesity',
 'ohlc',
 'points',
 'population',
 'population_engineers_hurricanes',
 'seattle-temps',
 'seattle-weather',
 'sf-temps',
 'sp500',
 'stocks',
 'udistrict',
 'unemployment',
 'unemployment-across-industries',
 'uniform-2d',
 'us-10m',
 'us-employment',
 'us-state-capitals',
 'volcano',
 'weather',
 'weball26',
 'wheat',
 'windvectors',
 'world-110m',
 'zipcodes']
```

or you can work with only smaller, local datasets.

In [26]:
```
from vega_datasets import local_data
local_data.list_datasets()
```

Out[26]:
```
['airports',
 'anscombe',
 'barley',
 'burtin',
 'cars',
 'crimea',
 'driving',
 'iowa-electricity',
 'iris',
 'la-riots',
 'ohlc',
 'seattle-temps',
 'seattle-weather',
 'sf-temps',
 'stocks',
 'us-employment',
 'wheat']
```

Ah, we have the `anscombe` data here! Let's see the description of the dataset.

In [27]:
```
local_data.anscombe.description
```

Out[27]:
```
"Anscombe's Quartet is a famous dataset constructed by Francis Anscombe [1]_. Common summary statistics are identical for eac
h subset of the data, despite the subsets having vastly different characteristics."
```

Anscombe's quartet dataset

How does the actual data look like? Very conveniently, calling the dataset returns a Pandas dataframe for you.

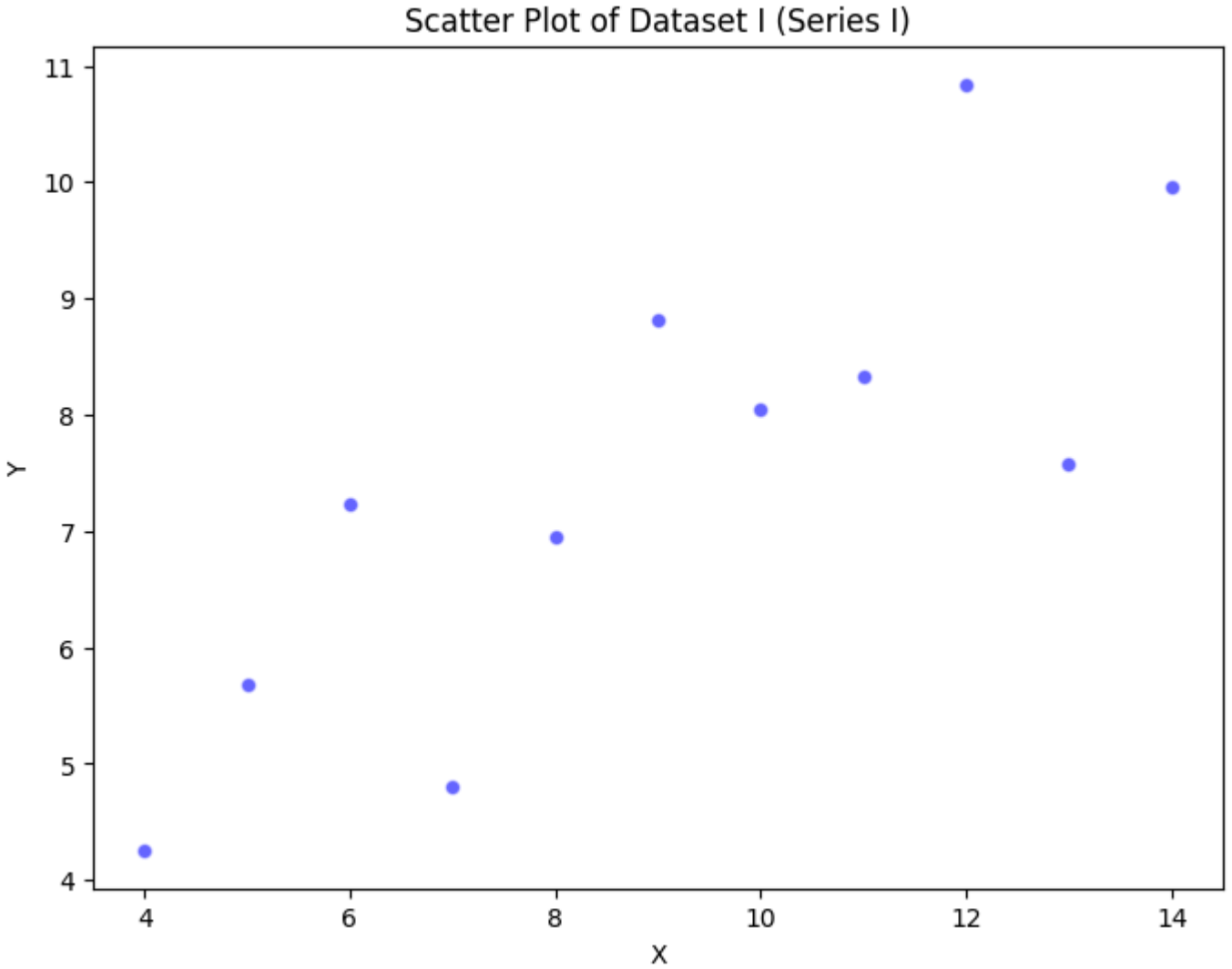
In [28]:
```
df = local_data.anscombe()
df.head()
```

Out[28]:

	Series	X	Y
0	I	10	8.04
1	I	8	6.95
2	I	13	7.58
3	I	9	8.81
4	I	11	8.33

Q1: can you draw a scatterplot of the dataset "I"? You can filter the dataframe based on the `Series` column and use `scatter` function that you used for the Snow's map.

In [29]:
```
filtered_df = df[df['Series'] == 'I']

plt.figure(figsize=(8, 6))
plt.scatter(filtered_df['X'], filtered_df['Y'],
            c='blue', alpha=0.6, edgecolors='w')

plt.xlabel('X')
plt.ylabel('Y')
plt.title('Scatter Plot of Dataset I (Series I)')
plt.show()
```



Some histograms with pandas

Let's look at a slightly more complicated dataset.

In [30]:
```
car_df = local_data.cars().astype({'Year':'object'})
car_df.head()
```

Out[30]:

	Name	Miles_per_Gallon	Cylinders	Displacement	Horsepower	Weight_in_lbs	Acceleration	Year	Origin
0	chevrolet chevelle malibu	18.0	8	307.0	130.0	3504	12.0	1970-01-01 00:00:00	USA
1	buick skylark 320	15.0	8	350.0	165.0	3693	11.5	1970-01-01 00:00:00	USA
2	plymouth satellite	18.0	8	318.0	150.0	3436	11.0	1970-01-01 00:00:00	USA
3	amc rebel sst	16.0	8	304.0	150.0	3433	12.0	1970-01-01 00:00:00	USA
4	ford torino	17.0	8	302.0	140.0	3449	10.5	1970-01-01 00:00:00	USA

Pandas provides useful summary functions. It identifies numerical data columns and provides you with a table of summary statistics.

In [31]:
```
car_df.describe()
```

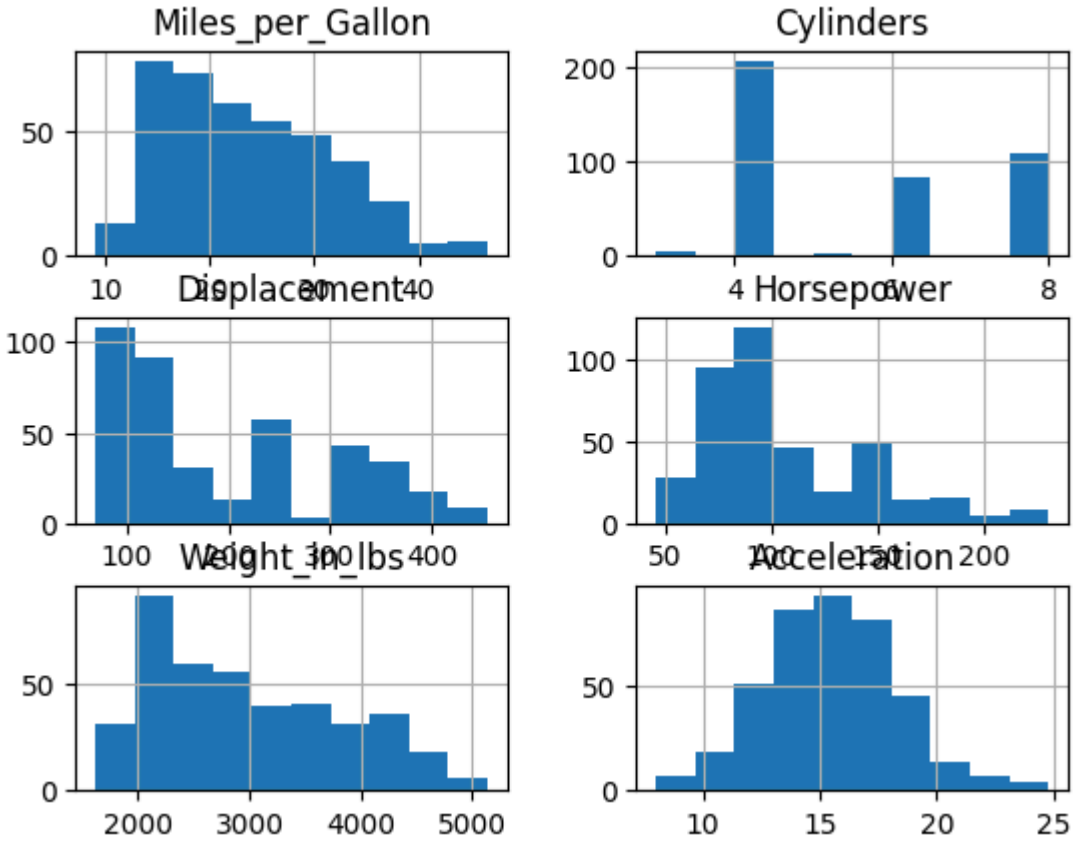
Out[31]:

	Miles_per_Gallon	Cylinders	Displacement	Horsepower	Weight_in_lbs	Acceleration
count	398.000000	406.000000	406.000000	400.000000	406.000000	406.000000
mean	23.514573	5.475369	194.779557	105.082500	2979.413793	15.519704
std	7.815984	1.712160	104.922458	38.768779	847.004328	2.803359
min	9.000000	3.000000	68.000000	46.000000	1613.000000	8.000000
25%	17.500000	4.000000	105.000000	75.750000	2226.500000	13.700000
50%	23.000000	4.000000	151.000000	95.000000	2822.500000	15.500000
75%	29.000000	8.000000	302.000000	130.000000	3618.250000	17.175000
max	46.600000	8.000000	455.000000	230.000000	5140.000000	24.800000

If you ask to draw a histogram, you get all of them.

In [32]:
```
car_df.hist()
```

Out[32]:
```
array([[<Axes: title={'center': 'Miles_per_Gallon'}>,
        <Axes: title={'center': 'Cylinders'}>],
       [<Axes: title={'center': 'Displacement'}>,
        <Axes: title={'center': 'Horsepower'}>],
       [<Axes: title={'center': 'Weight_in_lbs'}>,
        <Axes: title={'center': 'Acceleration'}>]], dtype=object)
```

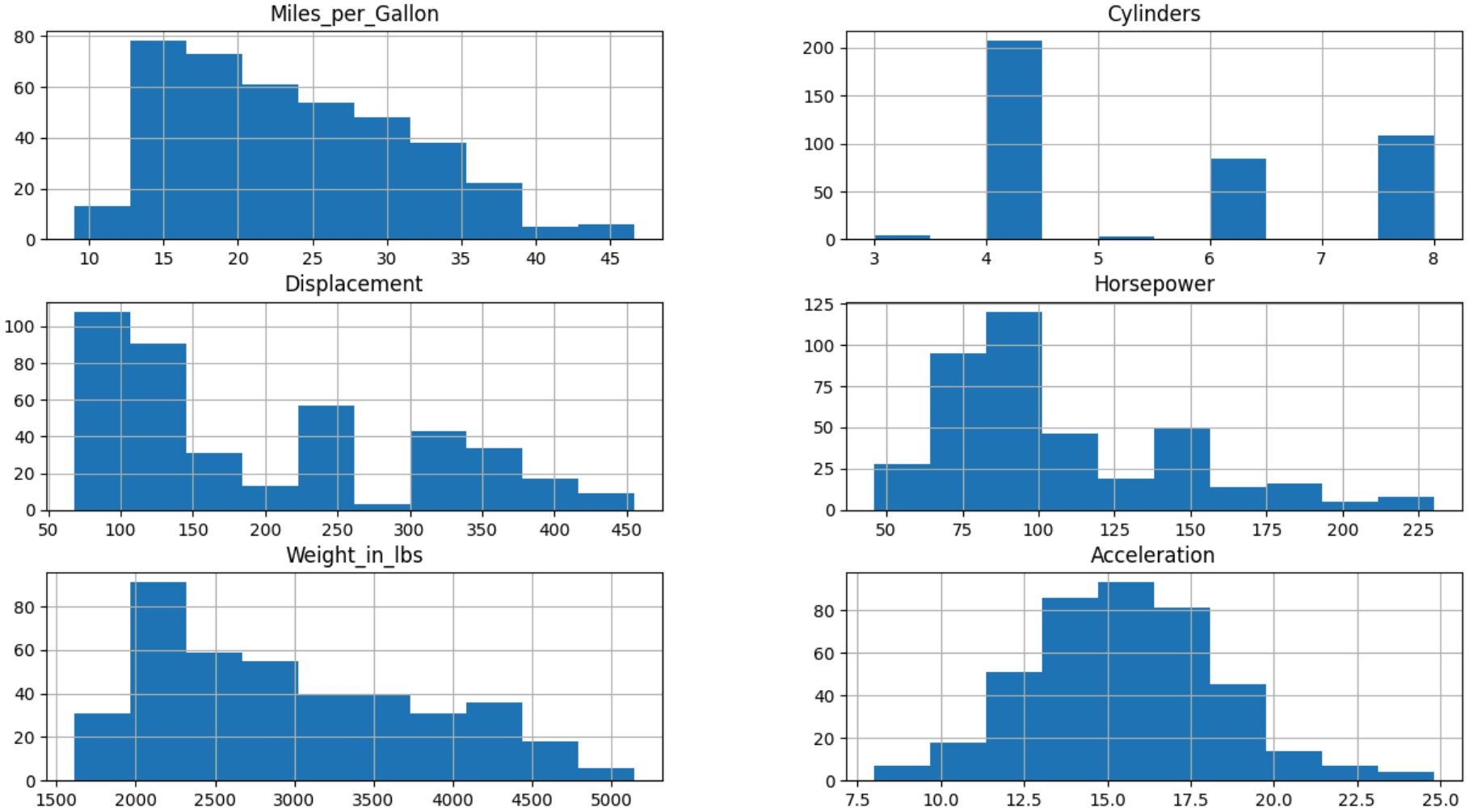


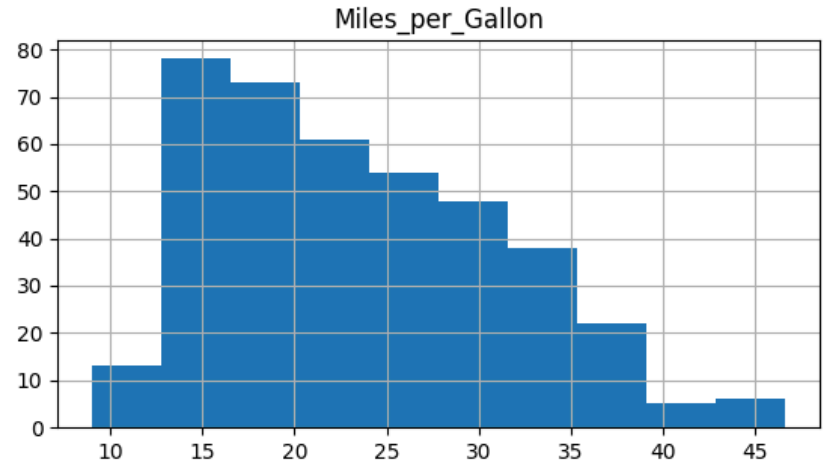
This is too small. You can check out the documentation and change the size of the figure.

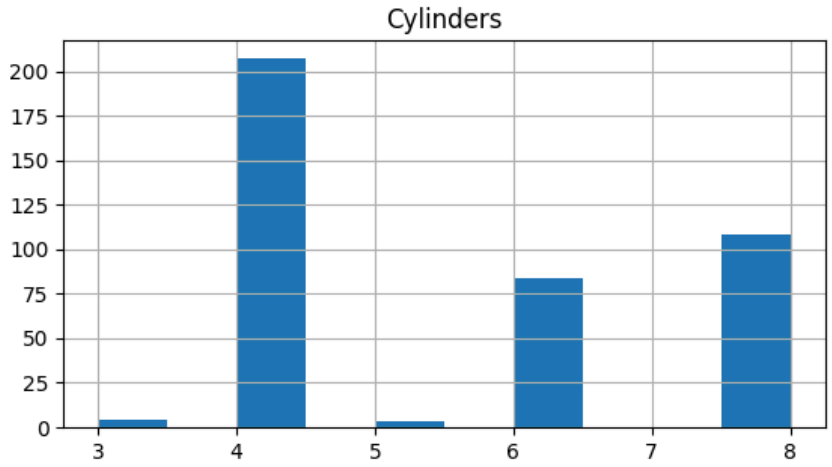
Q2: by consulting the documentation, can you make the figure larger so that we can see all the labels clearly? And then make the layout 2 x 3 not 3 x 2, then change the number of bins to 20?

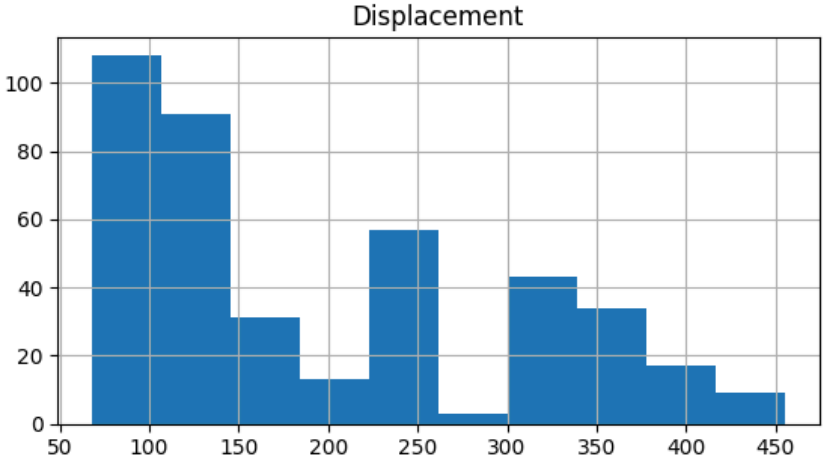
In [33]:
```
car_df.hist(figsize=(15,8))
car_df.hist(figsize=(15,12), layout=(3,2))
car_df.hist(figsize=(15,12), layout=(3,2), bins=20)
```

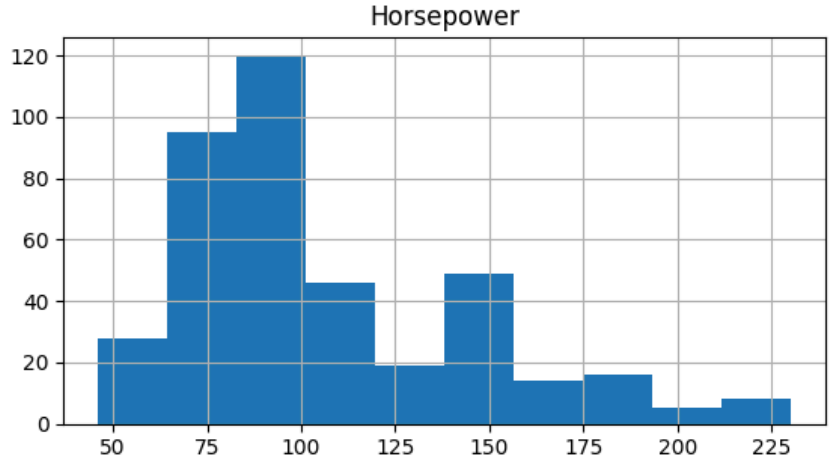
Out[33]:
```
array([[<Axes: title={'center': 'Miles_per_Gallon'}>,
        <Axes: title={'center': 'Cylinders'}>],
       [<Axes: title={'center': 'Displacement'}>,
        <Axes: title={'center': 'Horsepower'}>],
       [<Axes: title={'center': 'Weight_in_lbs'}>,
        <Axes: title={'center': 'Acceleration'}>]], dtype=object)
```

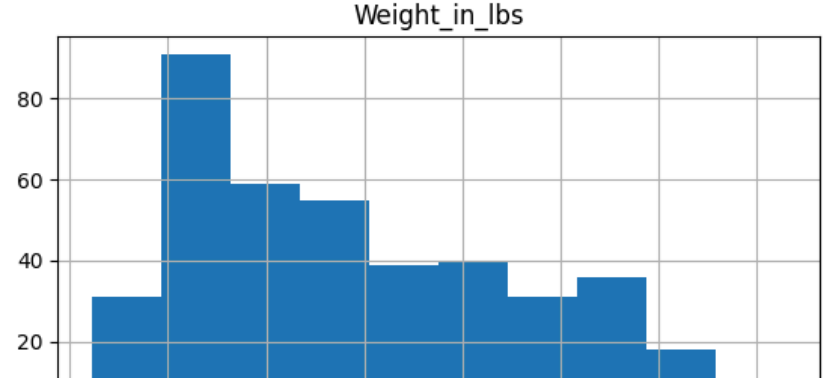


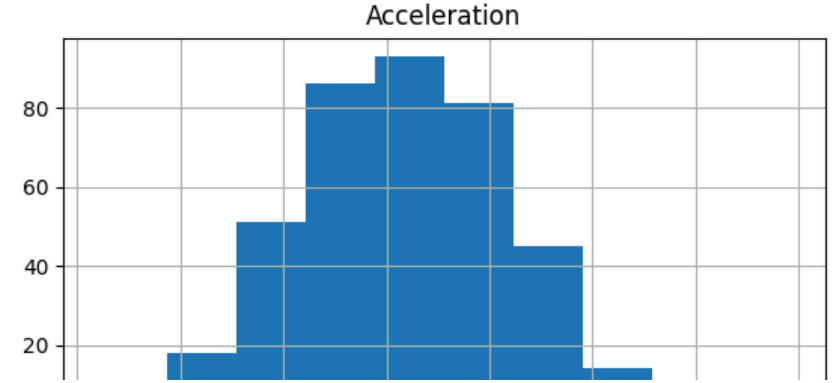

Miles_per_Gallon
80
70
60
50
40
30
20
10
0
10
15
20
25
30
35
40
45

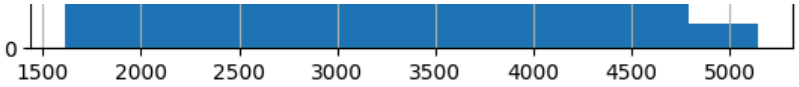

Cylinders
200
175
150
125
100
75
50
25
0
3
4
5
6
7
8

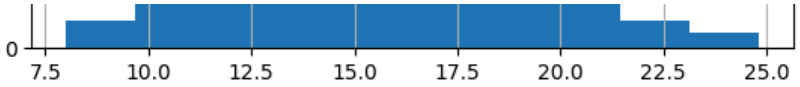

Displacement
100
80
60
40
20
0
50
100
150
200
250
300
350
400
450

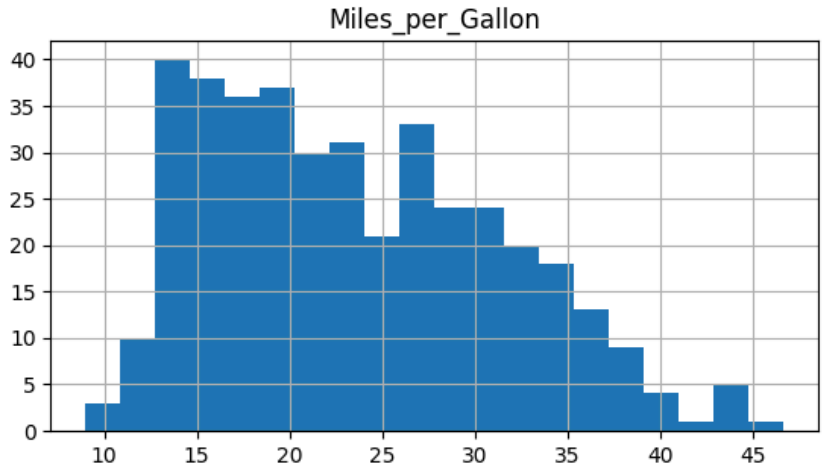

Horsepower
120
100
80
60
40
20
0
50
75
100
125
150
175
200
225

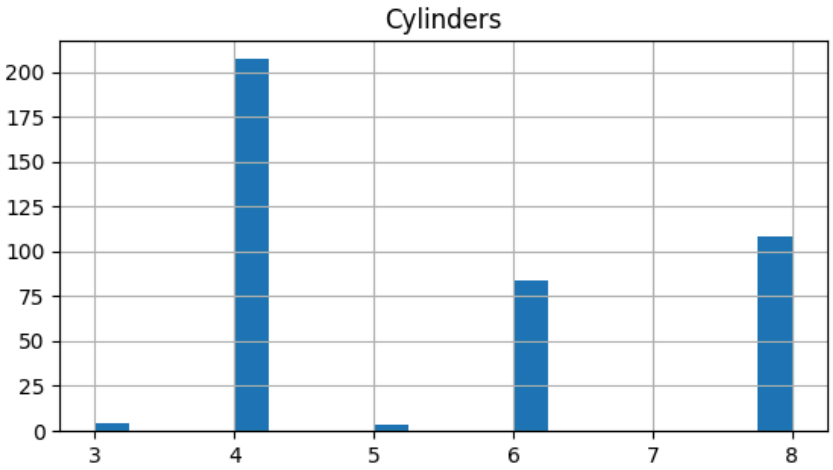

Weight_in_lbs
80
60
40
20

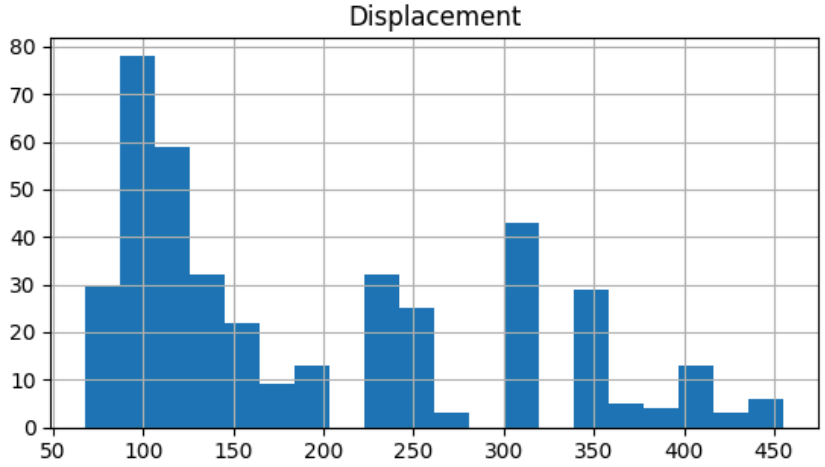

Acceleration
80
60
40
20

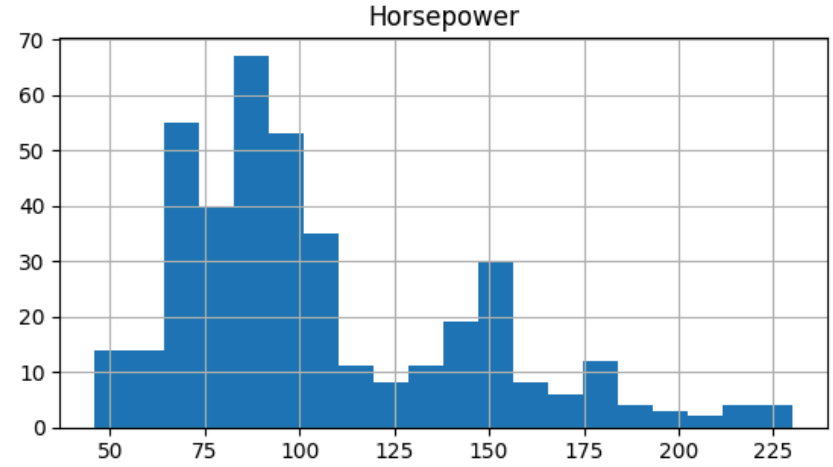

0
1500
2000
2500
3000
3500
4000
4500
5000

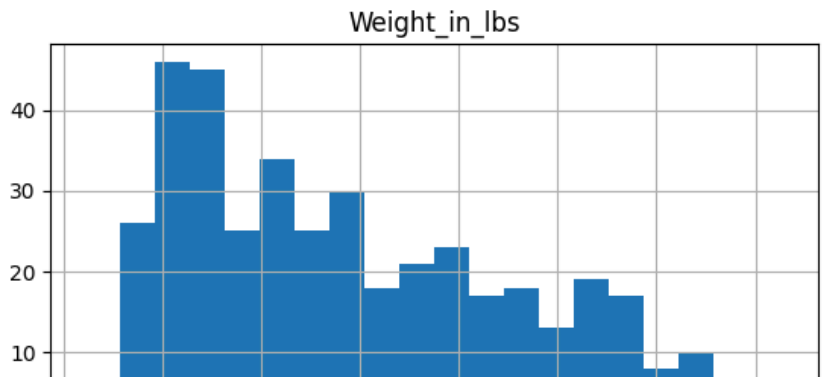

0
7.5
10.0
12.5
15.0
17.5
20.0
22.5
25.0

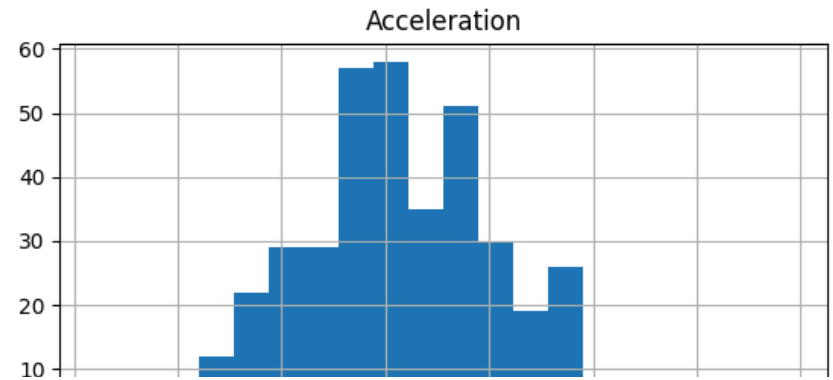

Miles_per_Gallon
0 5 10 15 20 25 30 35 40
10 15 20 25 30 35 40 45

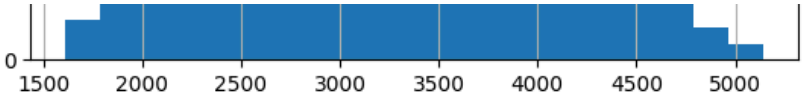

Cylinders
0 25 50 75 100 125 150 175 200
3 4 5 6 7 8

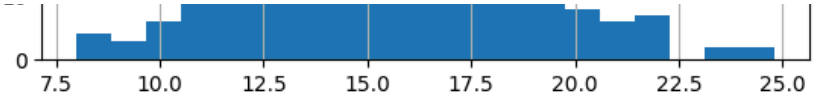

Displacement
0 10 20 30 40 50 60 70 80
50 100 150 200 250 300 350 400 450


Horsepower
0 10 20 30 40 50 60 70
50 75 100 125 150 175 200 225


Weight_in_lbs
10 20 30 40


Acceleration
10 20 30 40 50 60





Your own psychophysics experiment!

Let's do an experiment! The procedure is as follows:

1. Generate a random number between [1, 10];
2. Use a horizontal bar to represent the number, i.e., the length of the bar is equal to the number;
3. Guess the length of the bar by comparing it to two other bars with length 1 and 10 respectively;
4. Store your guess (perceived length) and actual length to two separate lists;
5. Repeat the above steps many times;
6. How does the perception of length differ from that of area?.

First, let's define the length of a short and a long bar. We also create two empty lists to store perceived and actual length.

In [83]:
```
import random
import time
import numpy as np

l_short_bar = 1
l_long_bar = 10

perceived_length_list = []
actual_length_list = []
```

Perception of length

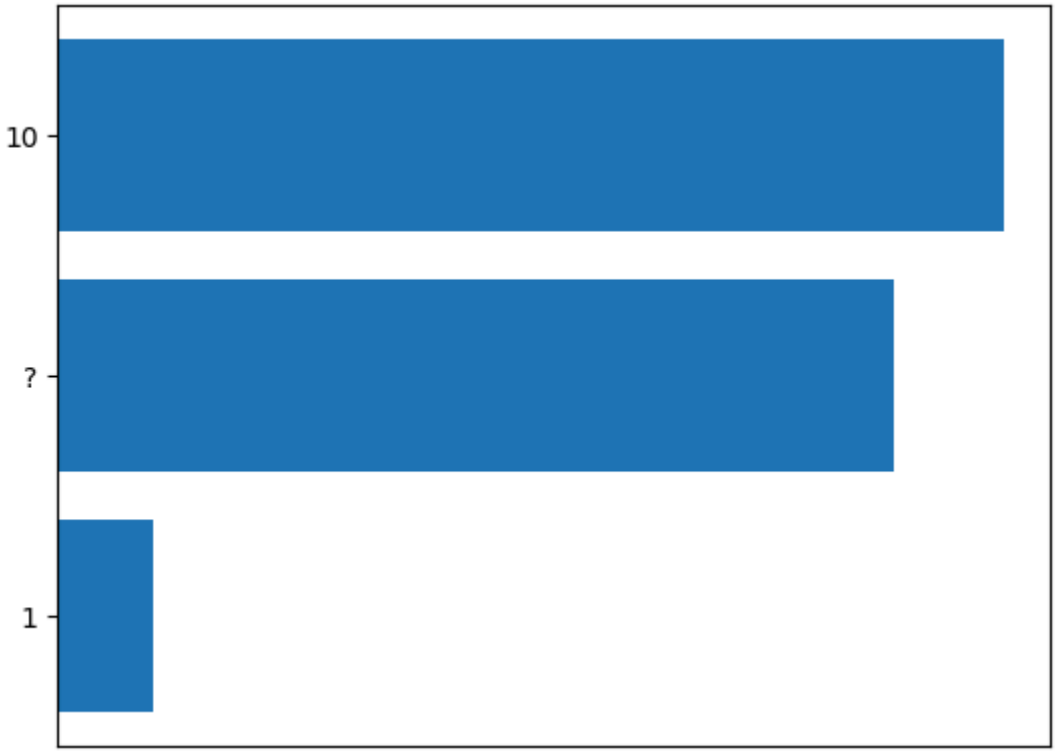
Let's run the experiment.

The `random` module in Python provides various random number generators, and the `random.uniform(a,b)` function returns a floating point number in [a,b].

We can plot horizontal bars using the `pyplot.barh()` function. Using this function, we can produce a bar graph that looks like this:

In [84]:
```
mystery_length = random.uniform(1, 10)  # generate a number between 1 and 10. this is the *actual* length.

plt.barh(np.arange(3), [l_short_bar, mystery_length, l_long_bar], align='center')
plt.yticks(np.arange(3), ('1', '?', '10'))
plt.xticks([]) # no hint!
```

Out[84]:
```
([], [])
```

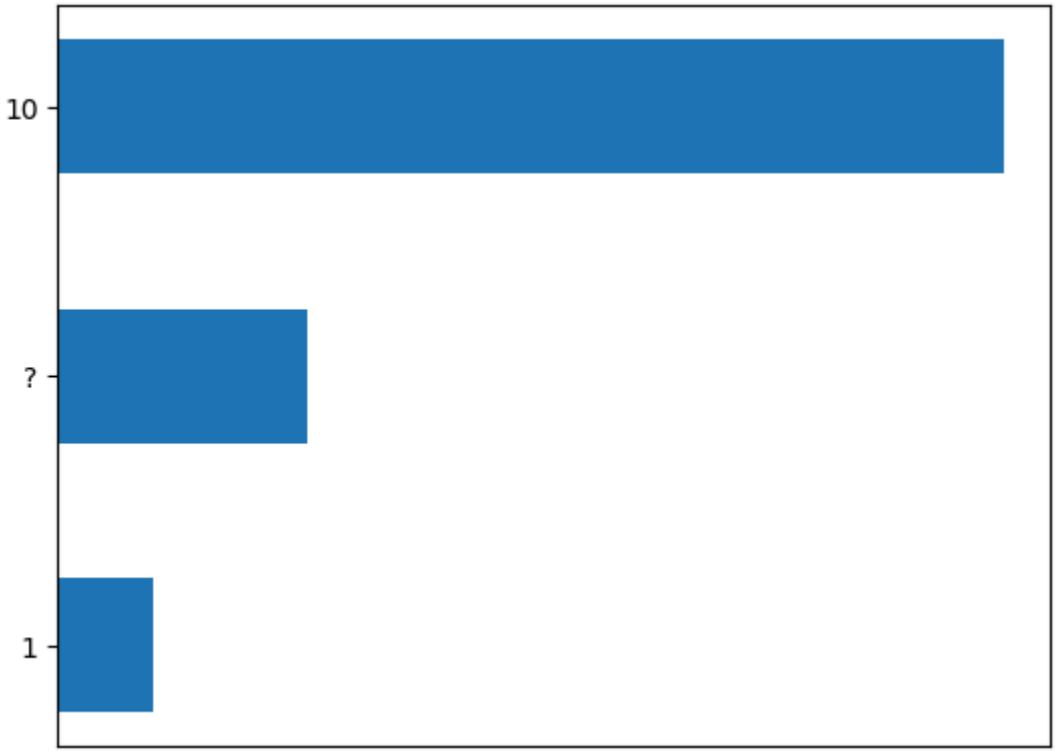


Now let's define a function to perform the experiment once. When you run this function, it picks a random number between 1.0 and 10.0 and show the bar chart. Then it asks you to input your estimate of the length of the middle bar. It then saves that number to the `perceived_length_list` and the actual answer to the `actual_length_list`.

In [86]:
```
def run_exp_once():
    mystery_length = random.uniform(1, 10)  # generate a number between 1 and 10.

    plt.barh(np.arange(3), [l_short_bar, mystery_length, l_long_bar], height=0.5, align='center')
    plt.yticks(np.arange(3), ('1', '?', '10'))
    plt.xticks([]) # no hint!
    plt.show()

    try:
        perceived_length_list.append( float(input()) )
    except:
        print("This should only fail in workflow. If you are running this in browser, this won't fail.")
```

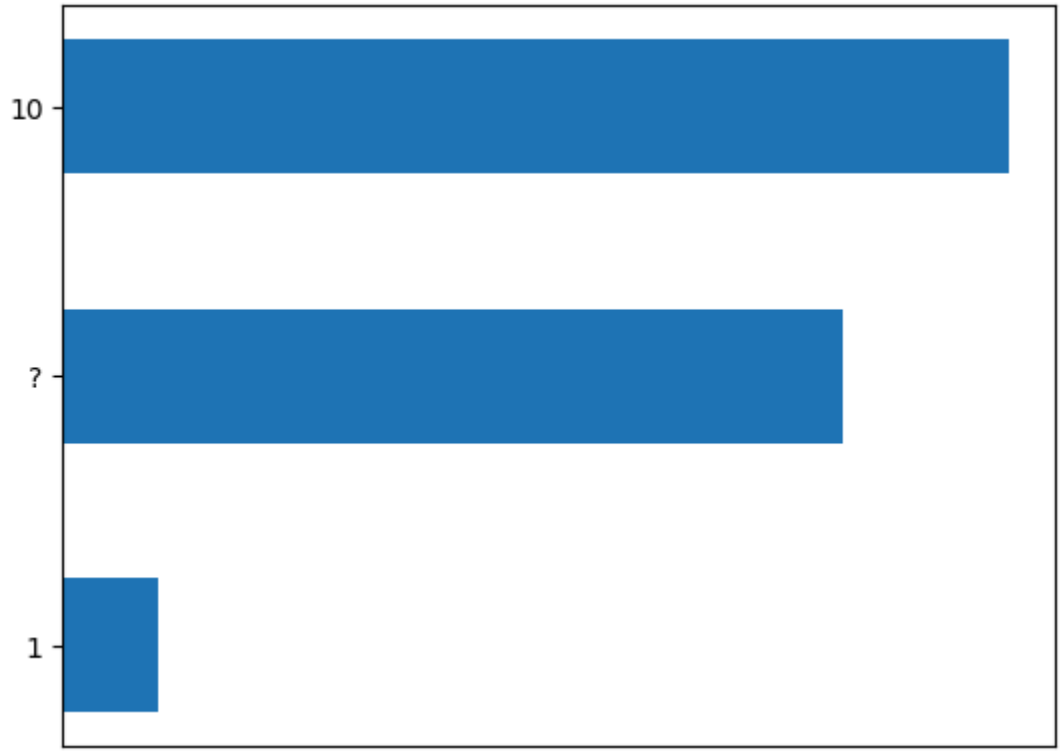
```
        pass
    actual_length_list.append(mystery_length)
    print(perceived_length_list)
    print(actual_length_list)
```

In [ ]:
```
#run_exp_once()
```

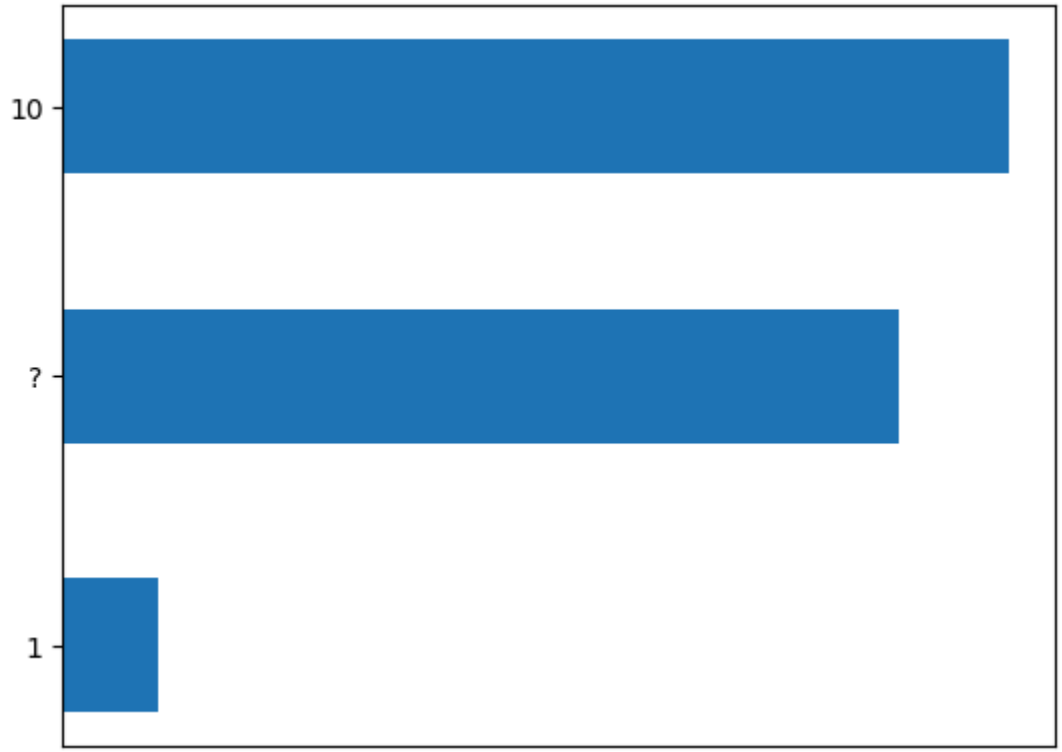


Now, run the experiment many times to gather your data. Check the two lists to make sure that you have the proper dataset. The length of the two lists should be the same.

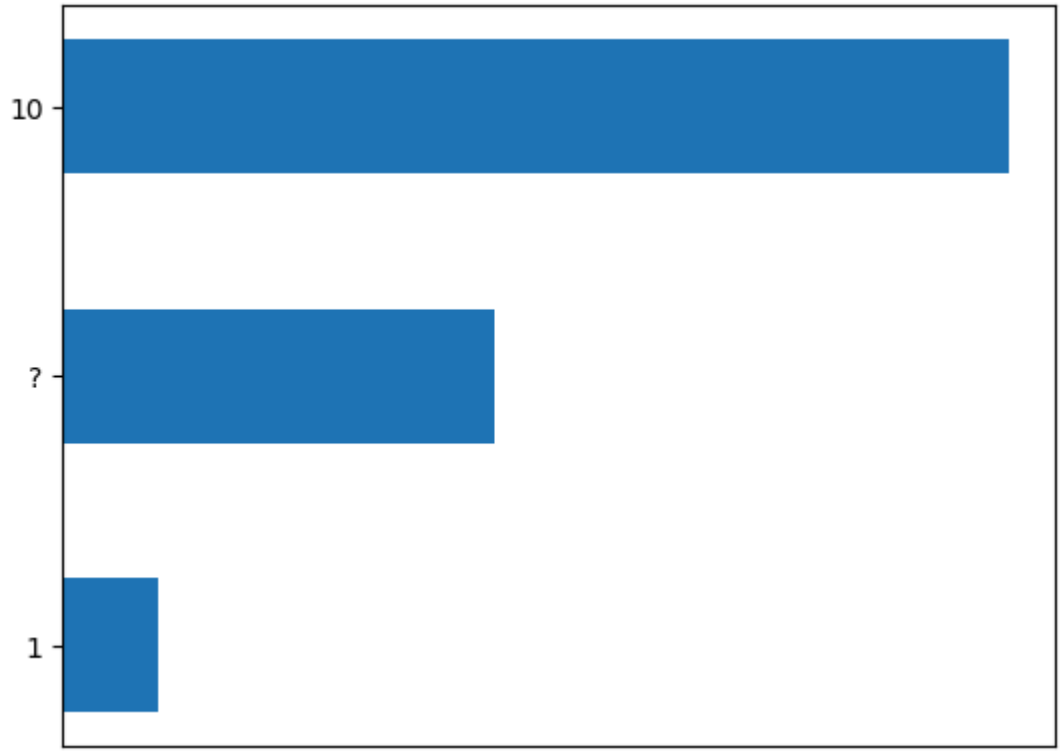
In [87]:
```
for i in range (0,5):
    run_exp_once()
```



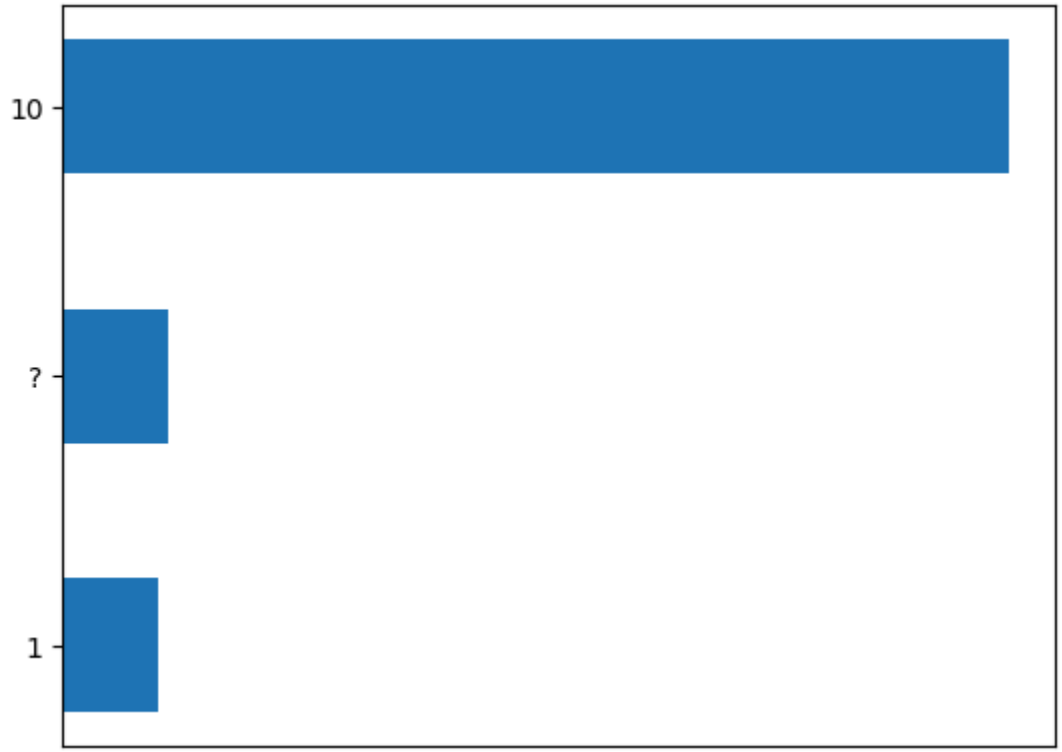

```
[7.0]
[8.251836692042774]
```



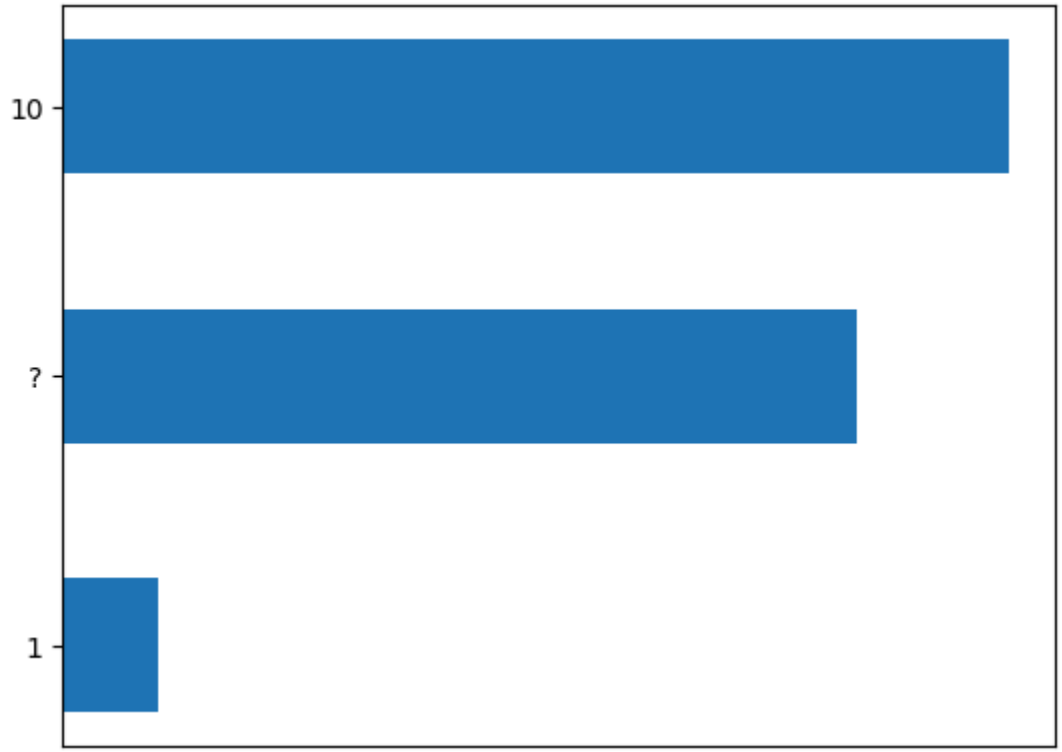

```
[7.0, 8.25]
[8.251836692042774, 8.851705366517024]
```




```
[7.0, 8.25, 4.3]
[8.251836692042774, 8.851705366517024, 4.5635280938757425]
```




```
[7.0, 8.25, 4.3, 1.1]
[8.251836692042774, 8.851705366517024, 4.5635280938757425, 1.114906838253339]
```



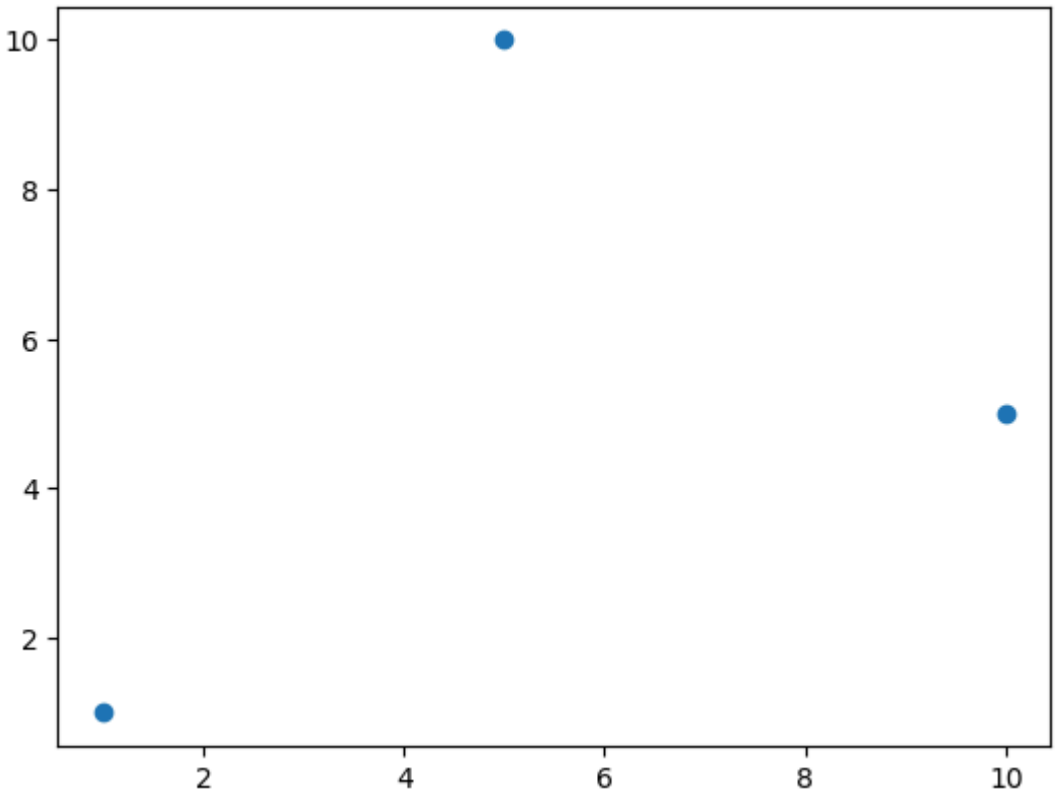

```
[7.0, 8.25, 4.3, 1.1, 8.76]
[8.251836692042774, 8.851705366517024, 4.5635280938757425, 1.1149068382533339, 8.396526833385407]
```

Plotting the result

Now we can draw the scatter plot of perceived and actual length. The `matplotlib` 's **`scatter()`** function will do this. This is the backend of the pandas' scatterplot. Here is an example of how to use `scatter` :

In [88]:
```
plt.scatter(x=[1,5,10], y=[1,10, 5])
```

Out[88]:
```
<matplotlib.collections.PathCollection at 0x203ff274200>
```

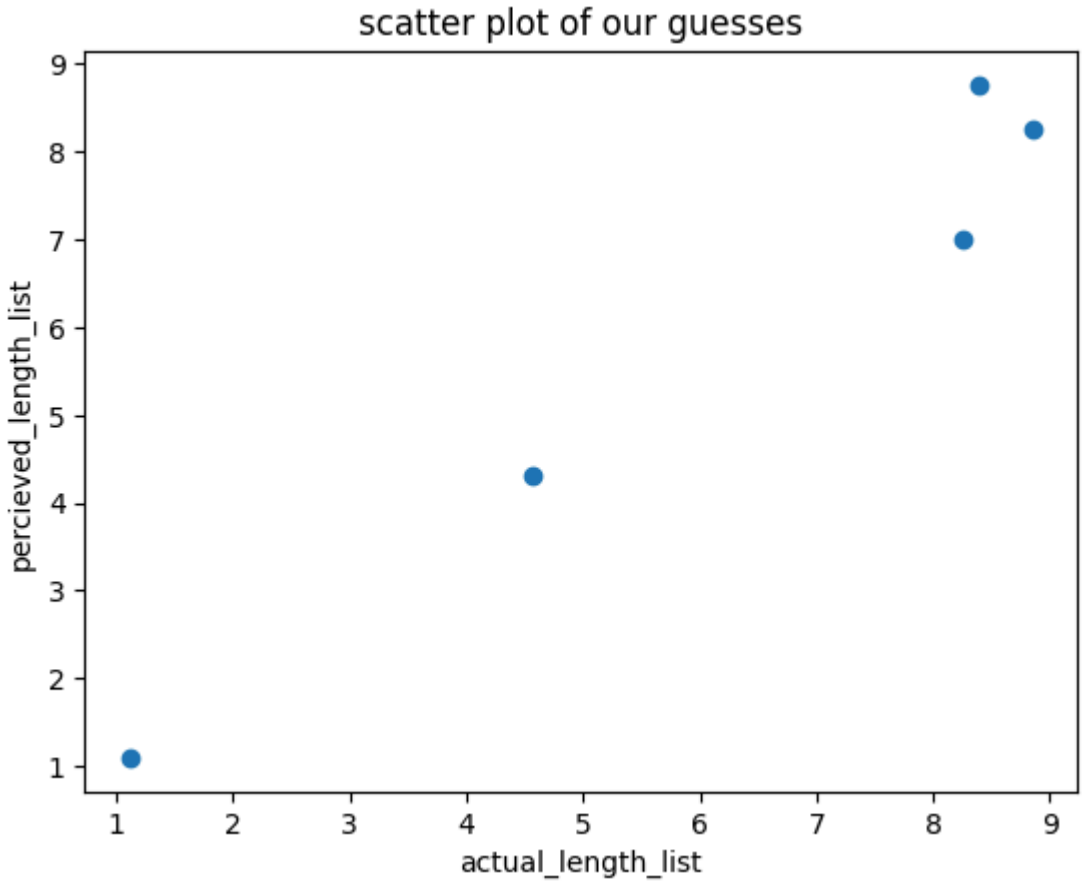


Q3: Now plot your result using the `scatter()` function. You should also use `plt.title()`, `plt.xlabel()`, and `plt.ylabel()` to label your axes and the plot itself.

In [89]:
```
print(actual_length_list)
print(perceived_length_list)

plt.title("scatter plot of our guesses")
plt.xlabel("actual_length_list")
plt.ylabel("percieved_length_list")
plt.scatter(x=actual_length_list, y=perceived_length_list)
```

```
[8.251836692042774, 8.851705366517024, 4.5635280938757425, 1.1149068382533339, 8.396526833385407]
[7.0, 8.25, 4.3, 1.1, 8.76]
```

Out[89]: `<matplotlib.collections.PathCollection at 0x203ff085580>`



After plotting, let's fit the relation between actual and perceived lengths using a polynomial function. We can easily do it using `curve_fit(f, x, y)` in Scipy, which is to fit x and y using the function `f`. In our case, $f = a * x^b + c$. For instance, we can check whether this works by creating a fake dataset that follows the exact form:

In [90]:
```
from scipy.optimize import curve_fit

def func(x, a, b, c):
    return a * np.power(x, b) + c

x = np.arange(20)  # [0,1,2,3, ..., 19]
y = np.power(x, 2) # [0,1,4,9, ... ]
```

```
popt, pcov = curve_fit(func, x, y)
print('{:.2f} x^{:.2f} + {:.2f}'.format(*popt))
```

```
1.00 x^2.00 + -0.00
```

In order to plot the function to check the relationship between the actual and perceived lenghts, you can use two variables `x` and `y` to plot the relationship where `x` equals to a series of continuous numbers. For example, if your x axis ranges from 1 to 9 then the variable `x` could be equal to `np.linspace(1, 10, 50)`. The variable `y` will contain the equation that you get from `popt`. For example, if you get equation `1.00 x^2.00 + 0.00` then the variable `y` would be equal to `1.0 * x**2.0 + 0`.

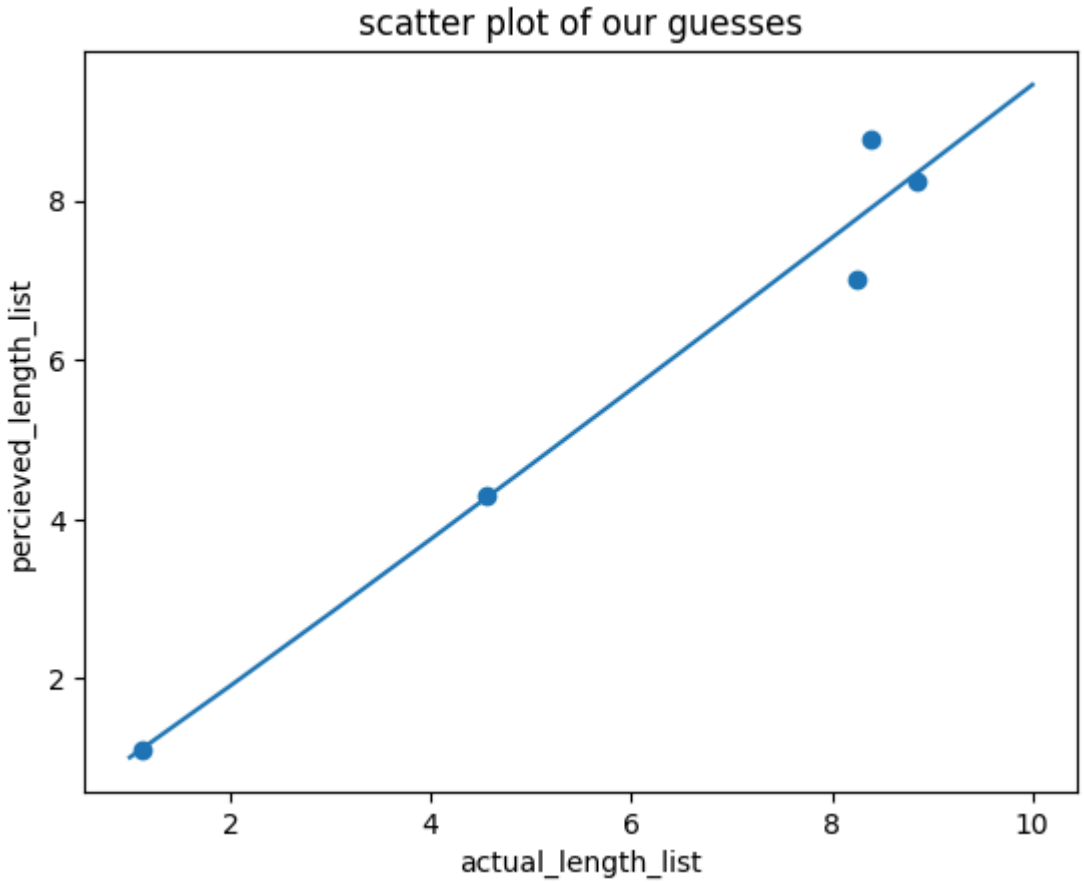
After assigning `x` and `y` variables you will plot them in combination with the scatter plot of actual and perceived values to check if you get a linear relationship or not.

Q4: Now fit your data! Do you see roughly linear relationship between the actual and the perceived lengths? It's ok if you don't!

In [91]:
```
popt_data, _ = curve_fit(func, actual_length_list, perceived_length_list,maxfev=5000)
xs = np.linspace(1,10,10)
ys = popt_data[0] * xs ** popt_data[1] + popt_data[2]

print(popt_data)

plt.title("scatter plot of our guesses")
plt.xlabel("actual_length_list")
plt.ylabel("percieved_length_list")
plt.scatter(x=actual_length_list, y=perceived_length_list)
plt.plot(xs, ys)
```

```
[0.85196332 1.03822017 0.151749  ]
```

Out[91]:
```
[<matplotlib.lines.Line2D at 0x203ff2d2f90>]
```



Perception of area

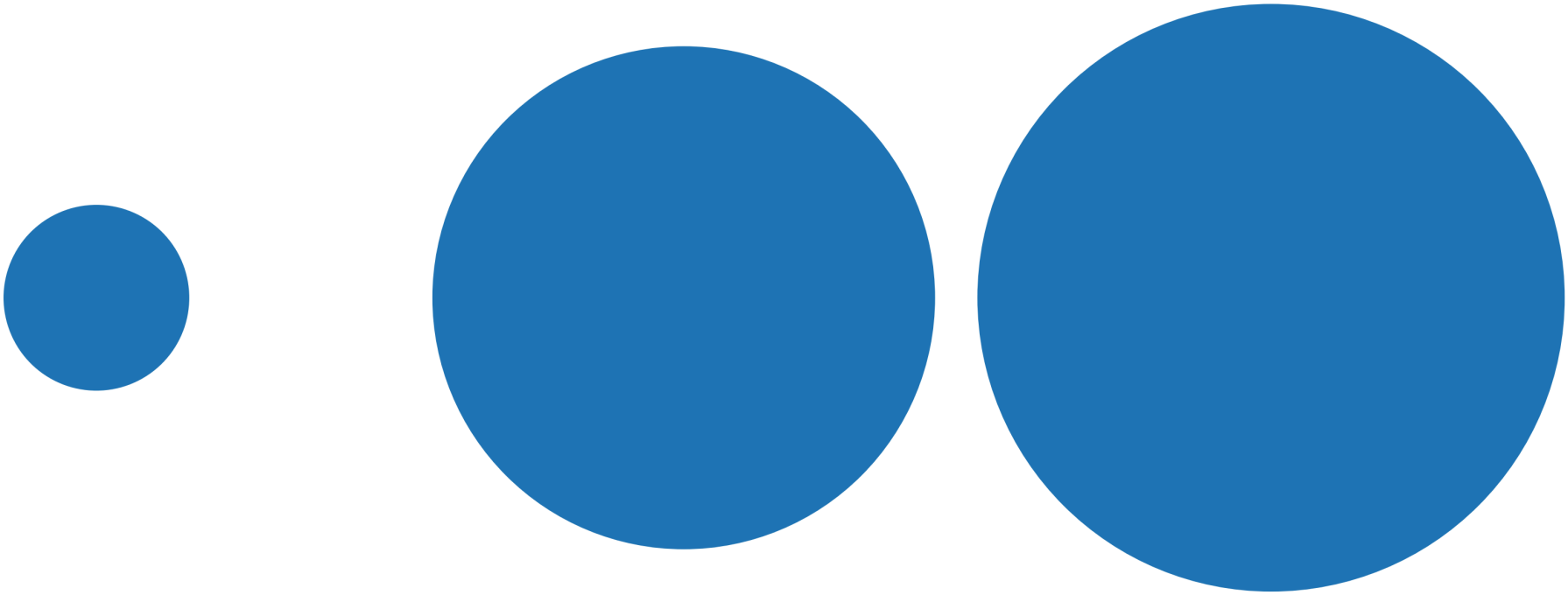
Similar to the above experiment, we now represent a random number as a circle, and the area of the circle is equal to the number.

First, calculate the radius of a circle from its area and then plot using the **`Circle()`** function. `plt.Circle((0,0), r)` will plot a circle centered at (0,0) with radius `r`.

In [ ]:
```
n1 = 0.005
n2 = 0.05

radius1 = np.sqrt(n1/np.pi) # area = pi * r * r
```

```
radius2 = np.sqrt(n2/np.pi)
random_radius = np.sqrt(n1*random.uniform(1,10)/np.pi)

plt.axis('equal')
plt.axis('off')
circ1 = plt.Circle( (0,0),          radius1, clip_on=False )
circ2 = plt.Circle( (4*radius2,0), radius2, clip_on=False )
rand_circ = plt.Circle((2*radius2,0), random_radius, clip_on=False )

plt.gca().add_artist(circ1)
plt.gca().add_artist(circ2)
plt.gca().add_artist(rand_circ)
```

Out[ ]: <matplotlib.patches.Circle at 0x1fe8f7b8a70>



Let's have two lists for this experiment.

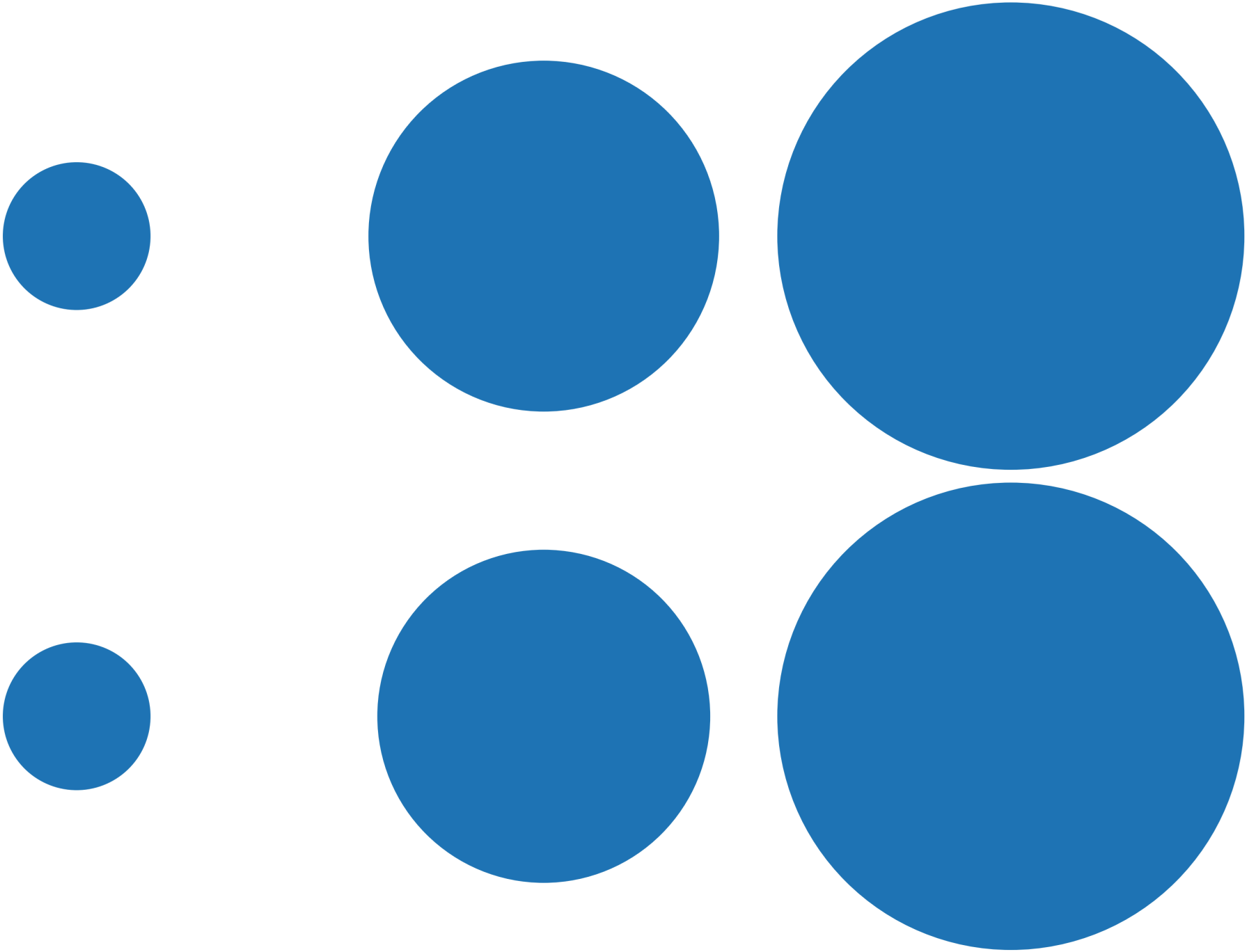
In [92]:
```
perceived_area_list = []
actual_area_list = []
```

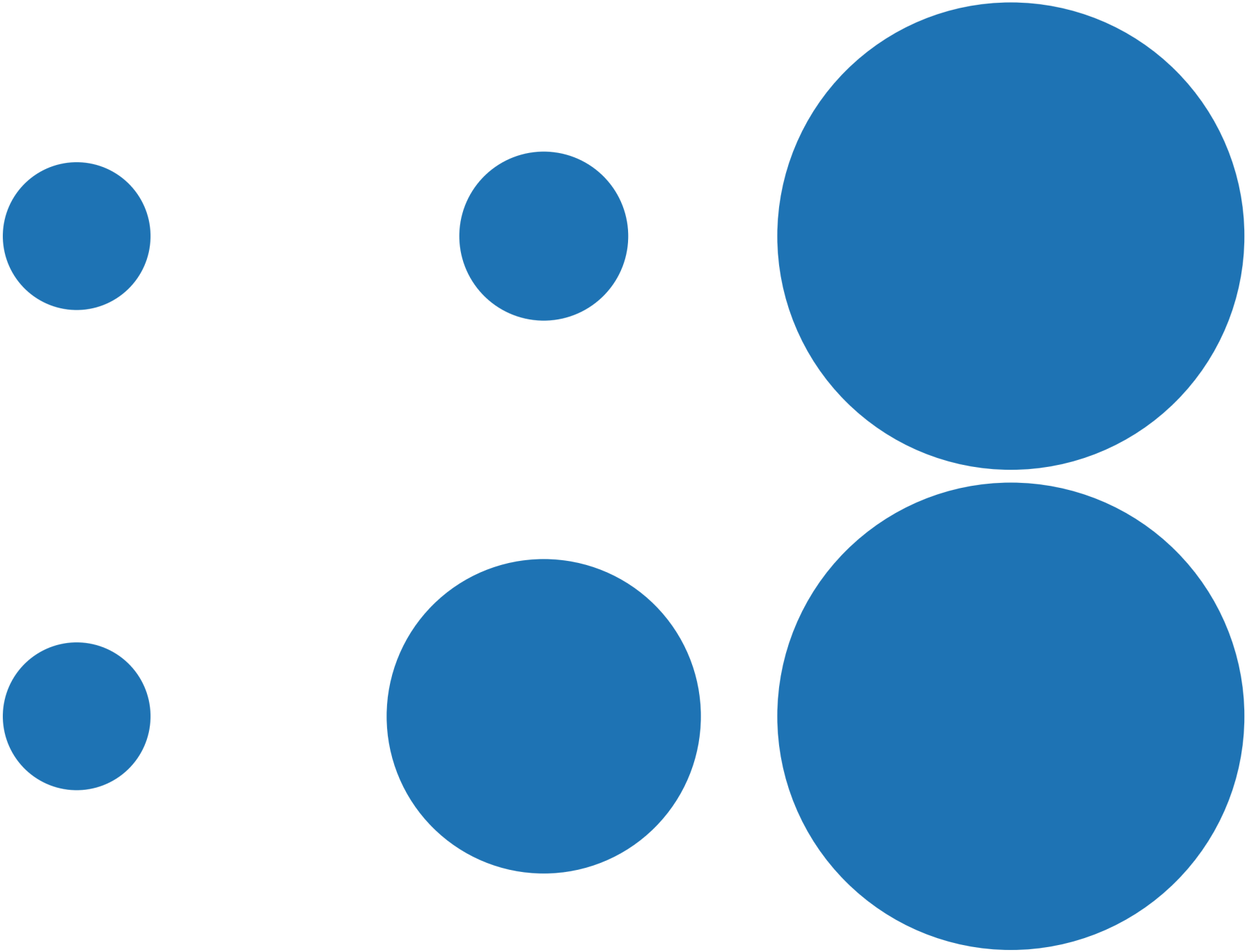
And define a function for the experiment.

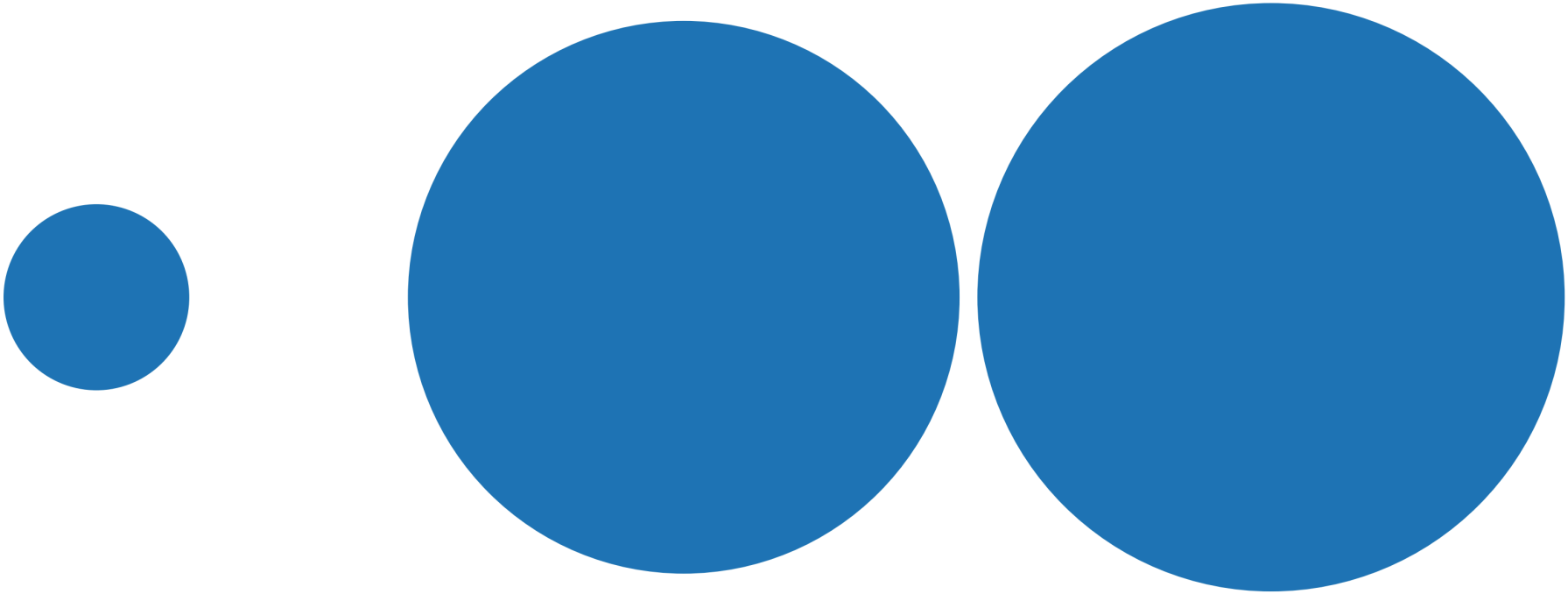
In [93]:
```
def run_area_exp_once(n1=0.005, n2=0.05):
    radius1 = np.sqrt(n1/np.pi) # area = pi * r * r
    radius2 = np.sqrt(n2/np.pi)

    mystery_number = random.uniform(1,10)
    random_radius = np.sqrt(n1*mystery_number/math.pi)

    plt.axis('equal')
    plt.axis('off')
    circ1 = plt.Circle( (0,0),         radius1, clip_on=False )
    circ2 = plt.Circle( (4*radius2,0), radius2, clip_on=False )
    rand_circ = plt.Circle((2*radius2,0), random_radius, clip_on=False )
    plt.gca().add_artist(circ1)
    plt.gca().add_artist(circ2)
    plt.gca().add_artist(rand_circ)
    plt.show()

    perceived_area_list.append( float(input()) )
    actual_area_list.append(mystery_number)
```

Q5: Now you can run the experiment many times, plot the result, and fit a power-law curve!

In [94]:
```
for i in range (0,5):
    run_area_exp_once()
```





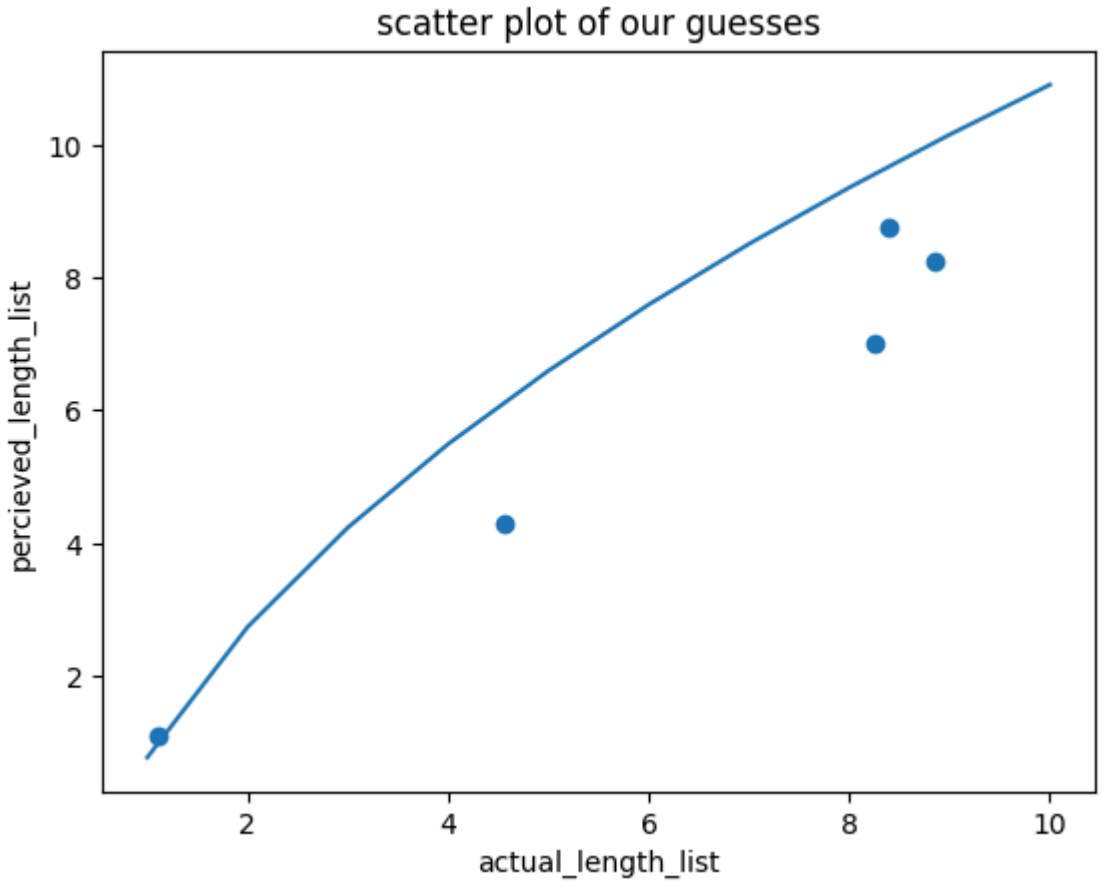


In [ ]:
```
print(actual_area_list)
```

In [96]:
```
popt_data, _ = curve_fit(func, actual_area_list, perceived_area_list ,maxfev=5000)
xs = np.linspace(1,10,10)
ys = popt_data[0] * xs ** popt_data[1] + popt_data[2]

print(popt_data)

plt.title("scatter plot of our guesses")
plt.xlabel("actual_length_list")
plt.ylabel("percieved_length_list")
plt.scatter(x=actual_length_list, y=perceived_length_list)
plt.plot(xs, ys)
```

```
[ 4.88097063  0.48761373 -4.10049916]
```

Out[96]:
```
[<matplotlib.lines.Line2D at 0x203f2351910>]
```



What is your result? How are the exponents different from each other?

Bars (b≈1.04)

An exponent essentially equal to 1 means perceived bar-length grows linearly with actual length. If you double the bar's true length, observers on average see it as about twice as long.

Circles (b≈0.49)

An exponent near 0.5 means perceived “size” of the circles grows like the square-root of the true stimulus. In other words, doubling the circle’s diameter (or area) makes it look only ≈√2 (≈1.4×) larger, so large circles are systematically under-perceived relative to small ones.

Why they differ

Length vs. area channels

- **Bars** encode data along a one-dimensional (length) channel, which people judge almost veridically ($b \approx 1$).
- **Circles** encode via two-dimensional area, and area judgments are notoriously sublinear: you need a disproportionate increase in physical size to get the same perceived jump in “bigness.”