

 $\sup_{w \in \mathcal{W}_S} G_S(w) \lesssim \sqrt{\frac{(\text{Topological complexity}) + \text{IT} + \log(1/\zeta)}{n}}$