## PEKING UNIVERSITY

## 统计力学及应用作业 3

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证明 Metropolis 方法产生的随机数列分布为  $\rho(x)$ , 若  $\frac{A_{xx'}}{A_{x'x}} = \frac{\rho(x')}{\rho(x)}$ .

讲过长时间的发展后, 处于某一状态 x 的概率都为一常数. 考虑 x, x' 两点间转化的概率, 不妨设  $\rho(x) > \rho(x')$ .

$$T(x \to x') = \omega_{xx'} A_{xx'} = \omega_{xx'} \frac{\rho(x')}{\rho(x)}, \tag{1.1}$$

$$T(x' \to x) = \omega_{x'x} A_{x'x} = \omega_{x'x}. \tag{1.2}$$

由于

$$T(x \to x')\rho(x) = \omega_{xx'}\frac{\rho(x')}{\rho(x)}\rho(x) = \omega_{xx'}\rho(x') = \omega_{x'x}\rho(x') = T(x' \to x)\rho(x'), \quad (1.3)$$

所以其达到了细致平衡,也就是说系统达到的平衡是 x 数列分布满足  $\rho(x)$  概率密度的平衡.