

Homework 4: Due Friday February 24th recitation. Late homework will not be accepted.

**Write on only one side of each page. Staple all work.**

1. My friend earns more 30 % more than me. Together we make \$39, 348 per year. What is my annual salary? Round to the nearest dollar.
2. I would like to figure out the dimensions of our classroom. I am simply concerned with the dimensions of the floor, which we assume is a rectangle and has area  $450 \text{ ft}^2$ . Moreover, assume that the length is  $10 \text{ ft}$  longer than the width. Find the dimensions. Round to the nearest foot.
3. Determine the values of  $x$  for which the expression  $\sqrt{2x^2 + 3x - 2}$  is a real number.
4. Solve the inequality for  $x$

$$\left| \frac{bx + c}{a} \right| > 5a.$$

Assume that  $a, b, c$  are positive constants.

5. In my spare time I like to sell math books. The books that I sell are not obtained for free unfortunately, I buy them in lots of 100. I pay  $C$  dollars where  $C = 2000 + 8x + .00025x^2$ . Here  $x$  is number of lots purchased. For every lot I sell, I generate a revenue of  $R$  dollars where  $R = 20x$ .
  - (a) How many lots should I sell to see a profit of at least \$2400.
  - (b) Interpret the slope of the revenue  $R$ .
6. When we say  $y$  is directly proportional to  $x$ , we write  $y = kx$  where  $k$  is some constant. Suppose we have a spring and we stretch it a distance of  $x$  beyond its natural length. Hooke's law says that the force required to hold the spring  $x$  units beyond its natural length is directly proportional to  $x$ .
  - (a) A force of  $40N$  is required to hold a spring that has been stretched from its natural length of  $10\text{cm}$  to  $15\text{cm}$ . Denote the force by  $y$ . Find an equation for  $y$ .
  - (b) Find the force needed to hold a spring from its natural length to  $18\text{cm}$ .
7. Find the domain of  $f(x)$  where
  - (a)  $f(x) = \frac{1}{x^{18}-8}$ .
  - (b)  $f(x) = \frac{1}{\sqrt{x^6-1}}$ .