Mean Feld Therry

- a, h, a. Hantree - Fock Mathods

Reduce the many - body groblem to the groblem & a single gentricle moving in an effective mean field generated by all of the Filer gentricles.

Fundamental operapienation in condensed metter and nuclaw physics.

We will consider nomeletivistic men fuld methods.

- Petieles interest through an instantaneous getential;

 $V(\vec{x} - \vec{x}') = \sum_{\vec{q}} e^{i\vec{q}\cdot(\vec{x} - \vec{x}')} \tilde{V}(\vec{q})$ 

In the language of Second Quantization,

H = H + V

In The MEAN FIELD APPROXIMATION, the correction to the ground state energy is found by taking the vacuum (i.e., ground state) expectation value of v:

E -> E + <01V10> How to we calculate (01/10)? <0/2 at at a a 10) All of the terms left with a normal ordering of specitors will So, we are left with 

## = = = [13 × 13 4 × (2-2) < 4 (2) + (2) > < 4 (2) > < 4 (2) > <

Now consider

 $\times \sqrt{2} \int d^{3}x \, d^{3}x' \, d^{3}y \, d^{3}y' \, \langle \hat{V}(\vec{x}) \hat{V}(\vec{x}') \rangle \langle \hat{V}(\vec{y}) \hat{V}(\vec{y}') \rangle$   $\times e^{i(\vec{x}-\vec{y}) \cdot \vec{x}} e^{-i\vec{k} \cdot \vec{x}'} e^{i(\vec{k}+\vec{y}) \cdot \vec{y}} e^{-i\vec{y}^{2} \cdot \vec{y}'}$ 

 $\times \int_{a^{3}} \times d^{3} + (\vec{x}) \hat{\psi}(\vec{y}) > (\hat{\psi}) + (\vec{y}) \hat{\psi}(\vec{x}) > e^{i\vec{x}\cdot(\vec{x}-\vec{y})}$ 



Digramatic Analysis Remember om original diegeen for V= = を V(す) む む む む む む む で 2 - 1 k+2 The diagrams that consumed to VEV have no external lines -For the Hantier term we contract ( at a ) and ( at a ) and Dugiamentuly this conegorale to the grigh "TANPOLE" DIAGRAM For the Fock turn, we control ( a a ) and ( a a ).

1-1-12 7-12 " OYSTER" DIAGRAM

The sum wer to will of up to the Farmi momentum:

$$N = 2 \sqrt{\frac{1}{(2\pi)^3}} 4\pi \int_{0}^{k_F} k^2 dk = \frac{\sqrt{12}}{\pi^2} \frac{1}{3} k^3$$

Then

$$E = EN = \frac{3}{5}NE = N^{\frac{3}{2}}E$$

$$E = (\sqrt{15}N)^{1/2}/C$$

$$S = (\sqrt{$$

$$\Delta E^{(F)} = 2 \frac{1}{2} \left\{ \frac{1}{2} \left\{ \frac{e^2}{4\pi\epsilon_0} \right\} F\left(\frac{e^2}{8\pi}\right) \right\}$$

$$= -\frac{3}{2\pi} F \left( \frac{e^{2}}{4\pi\epsilon} \right) \int dx \, x^{2} F(x)$$

$$= -\frac{3\sqrt{8\pi}}{4\pi} \left(\frac{e^2}{4\pi6}\right)$$

Finilly

$$\frac{E}{N} = \left(\frac{2.2}{\pi^2} - \frac{0.916}{\pi_s}\right) \frac{Rydbugs}{sletton}$$