

STACKS

RECALL:

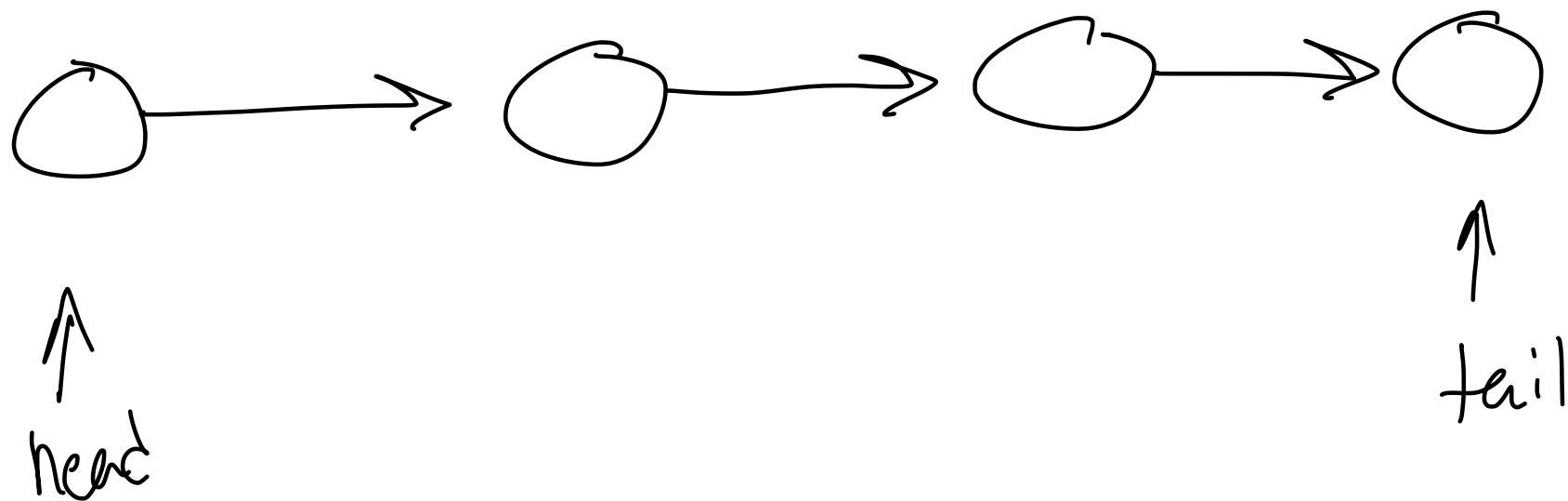
- Collection of objects
- Last in - first out (LIFO)
- Primary operations:
 - push (add to top)
 - pop (remove from top)

IMPELEMNTATIONS:

- Separate from the ADT
- The details of how we create the stack data structure
- Options:
 - Linked list based
 - Array based

LINKED LIST BASED

- Store stack as linked list
- How could we best represent stack using linked list for operations to be as efficient as possible?
 - Can `push` be $O(1)$?
 - Can `pop` be $O(1)$?
 - Possible to implement so they are both $O(1)$?



Stack:
need head
don't need the tail

LINKED LIST BASED

- Think about what operations with linked list were $O(1)$:
 - adding to start
 - adding to end (if there's a `tail`)
 - computing size (if `size` is stored as instance variable)
 - removing from start
- LIFO: want to remove the last one we added

ARRAY BASED

- Store stack using an array
- How can we represent to be as efficient as possible?
 - Can `push` be $O(1)$?
 - Can `pop` be $O(1)$?
 - Possible to implement so they are both $O(1)$?

ARRAY BASED

- Just keep filling elements
 - Keep track of index representing top
 - Setting value of element is $O(1)$
- Problem: everytime we resize need to create new and copy over
 - Don't resize everytime we add
 - Grab a chunk more (typically 2x) when we need to resize
 - $O(n)$, but happens rarely


```
for (int i=0; i<4; i++) {
    int j=0;
    while (j<N) {
```

$$\frac{n}{2} * n = \frac{n^2}{2}$$

```
        j+=2;
```

```
        int k=0 {
```

```
            while (k < N/2 * N) {
```

```
                k++;
```

```
                //some statement
```

$\Theta(1)$

```
            }
```

```
        }
```

```
    }
```

$\Theta(n)$

$\Theta(n^2)$

$\Theta(n^3)$

$\Theta(n^4)$

$$\left(\frac{n^2}{2} + 1\right) \frac{n}{2} 4$$

$$4n^2 - 8n + 6$$

$$\frac{1}{2}n^2 + 8n + 3$$