

Stacks

Abstract Data Type

- Model of a data structure
 - NOT the actual implementation
- Describes:
 - set of data values
 - the operations that can be performed
 - what the operations do (not how they do them...)
- Language independent
 - Helpful for approach/algorithm

Stack

- Collection of objects
- Last in - first out (LIFO)
- Primary operations:
 - push (add to top)
 - pop (remove from top)

Real life examples:

- Piles of items at grocery stores
- Shopping cart corral
- Stack of plates
- Pez dispenser

When to use?

- Depends on the problem
- Not useful for all problems
- But -- Really useful for some problems
- Something to consider before you start coding
 - algorithm stage -- which ADT makes sense to use

Application: Post-Fix Notation

- Infix:
 - what you're used to
 - $\langle \text{operand} \rangle \langle \text{operator} \rangle \langle \text{operand} \rangle$
 - relies on order of operations and parentheses
 - Ex: $3 + 2 * 4$
- Postfix:
 - $\langle \text{operator} \rangle \langle \text{operator} \rangle \langle \text{operand} \rangle$
 - Ex: $3\ 2\ 4\ * +$

Application: Post-Fix Notation

- Computer has to parse math expressions
- Postfix is easier
- How could we write parser to turn expression into code?

Coding Applications - Others

- Reversing a string
- Back button in browser
- Undo/redo
- Balanced parentheses
- Maze solving
- Function call stack

Implementations:

- Separate from the ADT
- The details of how we create the stack data structure
- Options:
 - Linked-list based
 - Array based (recall -- python lists are implemented on arrays)

Linked List Based

- Store stack as linked list
- How could we best represent stack using linked list for operations to be as efficient as possible?
 - Can **push** be $O(1)$?
 - Can **pop** be $O(1)$?
 - Possible to implement so they are both $O(1)$?

Linked List Based

- Think about what operations with linked list were $O(1)$:
 - adding to start
 - adding to end (if there's a `tail`)
 - computing size (if `size` is stored as instance variable)
 - removing from start
- LIFO: want to remove the last one we added

Array Based

- Store stack using an array (in python store using list)
- How can we represent to be as efficient as possible?
 - Can **push** be $O(1)$?
 - Can **pop** be $O(1)$?
 - Possible to implement so they are both $O(1)$?

Array Based

- Just keep filling elements
 - Keep track of index representing `top`
 - Setting value of element is $O(1)$
- In Python don't need to worry about resizing (lists do this automatically)
- Conceptually though -- resizing is expensive
 - Don't resize everytime we add
 - Grab a chunk more (typically 2x) when we need to resize
 - $O(n)$, but happens rarely