

$$\prod_j p(x^{(j)} | y) p(y)$$

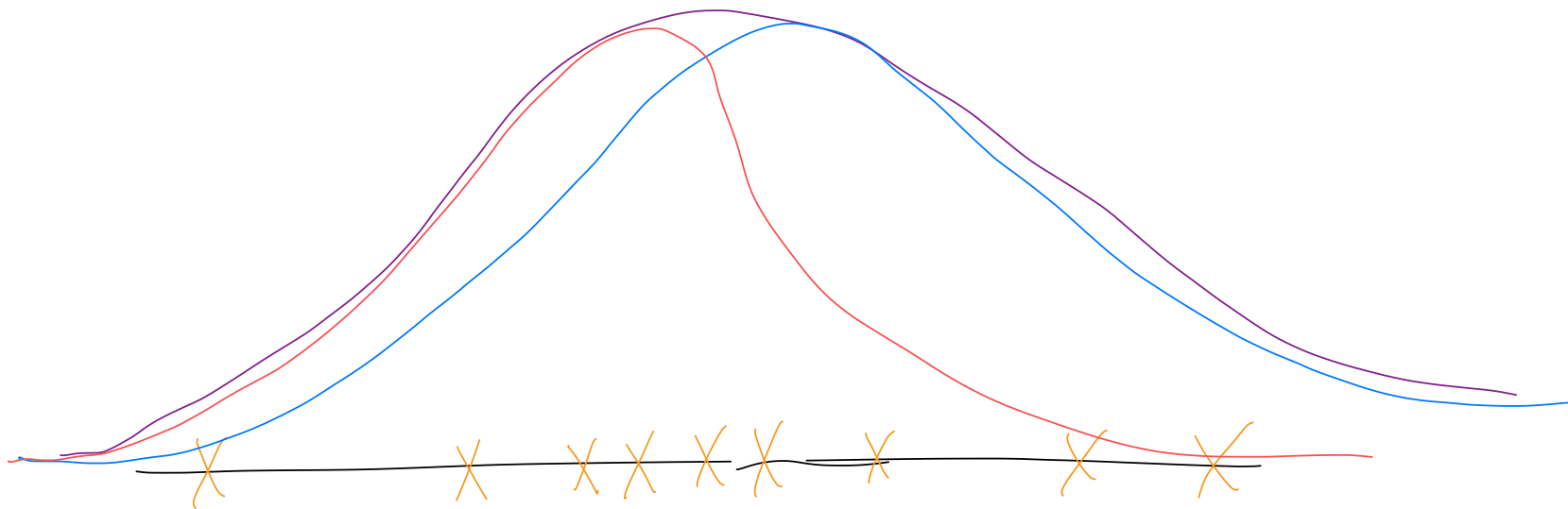
$$\log(p(y)) + \sum_j \log(p(x^{(j)} | y))$$

$$\frac{\text{\# of times } j^{\text{th}} \text{ attribute was } t \text{ and } y \text{ was } c}{\text{\# of samples with class } c} + \frac{1}{\text{\# of choices for feature } j}$$

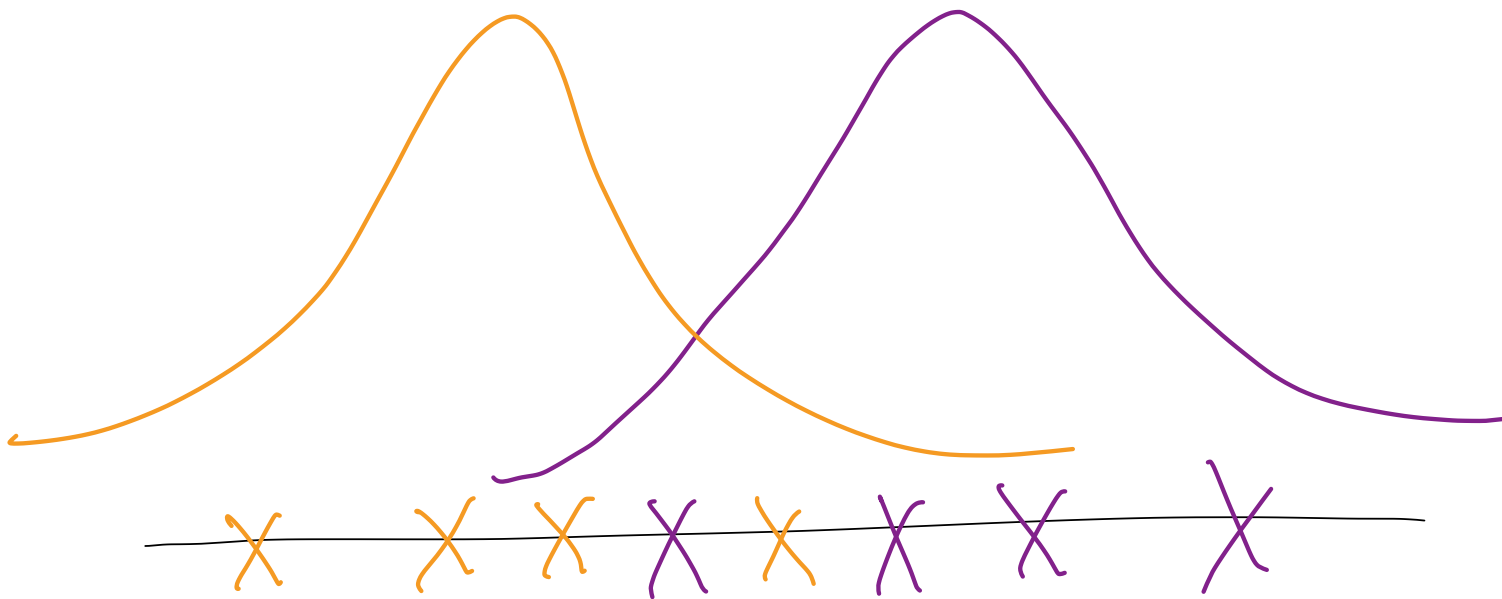
$P(\text{sunny} | \text{golf})$

$P(\text{cloudy} | \text{golf})$

$P(\text{rainy} | \text{golf})$



$$N(\mu, \sigma^2)$$



$$\overbrace{p(D | \theta_1, \dots, \theta_m)}^{\text{likelihood}}$$

MLE: maximum likelihood estimation

$$p(z | \mu, \sigma) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(z-\mu)^2}{2\sigma^2}}$$

$$p(D | \mu, \sigma) = \left(\frac{1}{\sqrt{2\pi\sigma^2}} \right)^N \prod_{i=1}^N e^{-\frac{(x_i - \mu)^2}{2\sigma^2}}$$

$$3x^2 + 4y + 6xy + 10$$

$$\frac{\partial}{\partial x} = 6x + 0 + 6y$$

$$\mathcal{L}(\mu) = p(D|\mu, \sigma) = \left(\frac{1}{\sqrt{2\pi}\sigma^d} \right)^N \prod_{i=1}^N e^{-\frac{(x_i - \mu)^2}{2\sigma^d}}$$

$$\ln \mathcal{L}(\mu) = \ln \left(\frac{1}{\sqrt{2\pi}\sigma^d} \right)^N + \sum_{i=1}^N \ln \left(e^{-\frac{(x_i - \mu)^2}{2\sigma^d}} \right)$$

$$\ln \left(\frac{1}{\sqrt{2\pi}\sigma^d} \right)^N + \sum_{i=1}^N -\frac{(x_i - \mu)^2}{2\sigma^d}$$

$$\frac{\partial}{\partial \mu} \ln \mathcal{L}(\mu) = 0 + \sum_{i=1}^N -\frac{2(x_i - \mu)(-1)}{2\sigma^d}$$

$$0 = \sum_{i=1}^N \frac{-2(x_i - \mu)(-1)}{2\sigma^2}$$

$$0 = \frac{2}{2\sigma^2} \sum (x_i - \mu)$$

$$0 = \frac{1}{\sigma^2} \sum_i (x_i - \mu)$$

$$0 = \sum_i^N (x_i - \mu)$$

$$= -N\mu + \sum_{i=1}^N x_i$$

$$N\mu = \sum_{i=1}^N x_i \quad \Rightarrow \quad \mu = \frac{\sum_{i=1}^N x_i}{N}$$

$$\log L(\sigma) = \log \left(\frac{1}{\sigma \sqrt{2\pi}} \right)^N + \sum_{i=1}^N \frac{-(x_i - \mu)^2}{2\sigma^2}$$

$$= N \log \left(\frac{1}{\sigma} \cdot \frac{1}{\sqrt{2\pi}} \right) + \quad "$$

$$= -N \log(\sigma) - N(\log(\sqrt{2\pi})) + \quad "$$

$$= -N \log(\sigma) - N(\log(\sqrt{2\pi})) + \sum_{i=1}^N -(x_i - \mu)^2 \left(\frac{1}{2} \right) (\sigma^{-2})$$

$$= -N \frac{1}{\sigma} + \frac{1}{2} \sum_{i=1}^N -(x_i - \mu)^2 (-2\sigma^{-3})$$

$$0 = -N \frac{1}{\sigma} - \frac{1}{\sigma^3} \sum_{i=1}^N -(x_i - \mu)^2$$

$$\frac{N}{\sigma} = \frac{1}{\sigma^3} \sum_{i=1}^N (x_i - \mu)^2$$

$$N \sigma^2 = \sum_{i=1}^N (x_i - \mu)^2$$

$$\sigma^2 = \frac{\sum_{i=1}^N (x_i - \mu)^2}{N}$$

the dog ran
cat dog

dog cat cat
the

[cant word a , cant word b , cant word c , ...
...]

$$P(x | y=c)$$

of ^{freq} this word occurred
in documents of class

of total word count
for that class