10. Introduction to mCRL2

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Requirements and Model-driven Engineering

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https://cister-labs.github.io/ramde2122

http://mcrl2.org

- Formal specification language with an associated toolset
- Used for modelling, validating and verifying concurrent systems and protocols
- Tool suggestion: use mcrl2ide (not mcrl2-gui)

Recall CCS semantics

$$\begin{array}{c} \text{(act)} & \begin{array}{c} \text{(sum-1)} \\ P_1 \stackrel{\alpha}{\rightarrow} P_1' \\ \hline \alpha.P \stackrel{\alpha}{\rightarrow} P \end{array} & \begin{array}{c} \text{(sum-2)} \\ P_2 \stackrel{\alpha}{\rightarrow} P_2' \\ \hline P_1 + P_2 \stackrel{\alpha}{\rightarrow} P_1' \\ \hline P_1 + P_2 \stackrel{\alpha}{\rightarrow} P_1' \\ \hline P_1 + P_2 \stackrel{\alpha}{\rightarrow} P_2' \\ \hline P_1 + P_2 \stackrel{\alpha}{\rightarrow} P_2' \\ \hline P_1 + P_2 \stackrel{\alpha}{\rightarrow} P_2' \\ \hline P_2 \stackrel{\alpha}{\rightarrow} P_2' \\ \hline P_2 \stackrel{\alpha}{\rightarrow} P_2' \\ \hline P_3 \stackrel{\alpha}{\rightarrow} P_2' \\ \hline P_4 \stackrel{\alpha}{\rightarrow} P_2' \\ \hline P_5 \stackrel{\alpha}{\rightarrow} P_2' \\ \hline P_5 \stackrel{\alpha}{\rightarrow} P_2' \\ \hline P_7 \stackrel{\alpha}{\rightarrow}$$

Processes in mCRL2

CCS in mCRL2

Syntax (by example)

$$\begin{array}{c} \textbf{a.0} \rightarrow \textbf{a} \\ \textbf{a.P} \rightarrow \textbf{a.P} \\ P_1 + P_2 \rightarrow \textbf{P1 + P2} \\ P \backslash L \rightarrow \textbf{block}(\textbf{L,P}) \\ P[f] \rightarrow \textbf{rename}(\textbf{f,P}) \\ \textbf{a.P} | \overline{\textbf{a}}.Q \rightarrow \textbf{comm}(\{\textbf{a1}|\textbf{a2}\rightarrow\textbf{a}\},\textbf{a1.P} \parallel \textbf{a2.Q}) \\ \textbf{a.P} | \overline{\textbf{a}}.Q \backslash \{\textbf{a}\} \rightarrow \textbf{block}(\{\textbf{a1},\textbf{a2}\},\textbf{comm}(\{\textbf{a1}|\textbf{a2}\rightarrow\textbf{a}\},\textbf{a1.P} \parallel \textbf{a2.Q})) \end{array}$$

CCS in mCRL2 hiding communication

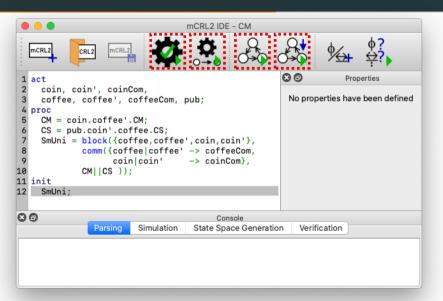
Syntax (by example)

```
a.0 \rightarrow a
                a.P \rightarrow a.P
        P_1 + P_2 \to P1 + P2
               P \setminus L \rightarrow block(L,P)
              P[f] \rightarrow rename(f,P)
        a.P|\overline{a}.Q \rightarrow \mathsf{hide}(\{a\}, comm(\{a1|a2\rightarrow a\}, a1.P \parallel a2.Q))
a.P|\overline{a}.Q\setminus\{a\} \rightarrow \mathsf{hide}(\{a\}, block(\{a1,a2\}, comm(\{a1|a2\rightarrow a\}, a2), a2)\}
                             a1.P | a2.Q)))
```

```
CM = \text{coin.}\overline{\text{coffee}}.CM
CS = \text{pub.}\overline{\text{coin.}}\text{coffee}.CS
SmUni = (CM|CS) \setminus \{\text{coin, coffee}\}
```

```
act
  coin, coin', coinCom,
  coffee, coffee', coffeeCom, pub;
proc
  CM = coin.coffee'.CM:
  CS = pub.coin'.coffee.CS;
  SmUni = block({coffee,coffee',coin,coin'},
          comm({coffee|coffee' → coffeeCom,
                coin|coin' → coinCom},
          CM | CS ));
init
  SmUni:
```

mCRL2 IDE



Parse

Simulate

Visualize

Minimize & Visualize

Specifications *.mcrl2

```
act
  action1, action2, ...:
  action3, action4 : Type;
proc
  P1 = ...;
  P2(x: Bool) = \dots
      % Process expression
init
  SmUni:
```

```
sort list = struct
        empty | cons(A,List);
map sum2: Int # Int \rightarrow Int;
var x, y: Int;
egn
  sum2(x,y) = (x+y) * (x+y);
  % Data patterns & expressions
```

https://mcrl2.org/web/user_manual/language_reference/index.html

Process Expressions

$$P = PE$$
;

```
a Action
        alb Multi-action
          P Process
      delta Deadlock
a(DataExpr) Parameterized Act.
P(DataExpr) Parameterized Proc.
       a.PE Sequencing
   PE1+PE2 Choice
  PE1 || PE2 | Parallel
```

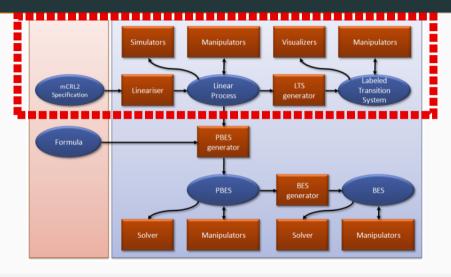
```
block({a,b},PE) Block
allow({a,b},PE) Allow
rename({a→b},PE) Rename
comm({a|b→c},PE) Communicate
sum m: Nat . PE Gen. Choice
```

Data Expressions

P(exp)

```
true Boolean
                                                         exp + exp Sum
                42 Pos. Nat. Int. Real
                                                     max(exp, exp) And
              !exp Not
                                                       exp mod exp Remainder of div.
        exp && exp And
                                                   [exp.exp...] List
         exp \parallel exp \mid Or
                                                  \{exp, exp, \ldots\} Set
        exp => exp Implies
                                              \{exp:2.exp:1,\ldots\} Bag
forall n:Nat . exp For all
                                               lambda n:Nat .exp Function
exists n:Nat . exp Exists
```

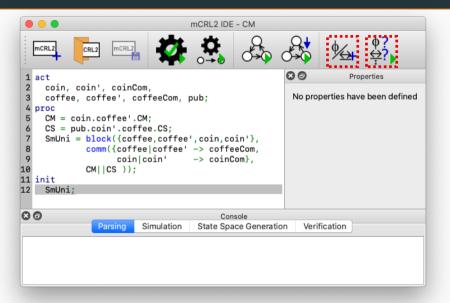
mCRL2 toolset overview



Assignment 1: https://cister-labs.github.io/ramde2122/assignments/al-modelling.pdf

Logic and Verification

mCRL2 IDE



Add properties

Verify properties

mCRL2 - modal logic

Syntax (simplified)

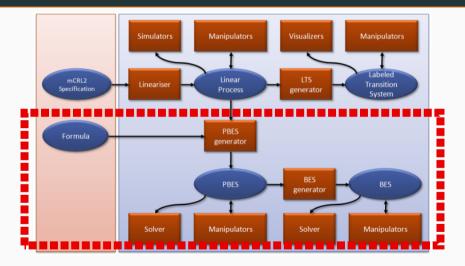
```
\phi = \text{true} \mid \text{false} \mid \text{forall x:T.} \phi \mid \text{ exists x.:T} \phi \mid \phi \ OP \ \phi \mid !\phi \mid [mod] \phi \mid < mod > \phi \mid \dots mod = \alpha \mid \text{nil} \mid mod + mod \mid mod \cdot mod \mid mod * \mid mod + \alpha = \text{a(d)} \mid \text{a|b|c} \mid \text{true} \mid \text{false} \mid \alpha \ OP \ \alpha \mid !\alpha \mid \text{forall x:T.} \alpha \mid \text{ exists x:T.} \alpha \mid \dots
```

where
$$T = \{Bool, Nat, Int, \ldots\}$$
 and $OP = \{=>, \&\&, \parallel\}$

Example

"[true*.a]true" means: whenever an 'a' appears after any number of steps, it must be immediately followed by 'b'.

mCRL2 toolset overview



 $Assignment\ 2: \quad \texttt{https://cister-labs.github.io/ramde2122/assignments/a2-verification.pdf}$