



Message Authentication Code

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1

Message Authentication Codes (MACs)

PRINCIPLES OF MACS

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Hash functions

2

2

Message Authentication Code

- Synonyms
 - Cryptographic checksum
 - Keyed hash function
- Similarly to digital signatures, MACs provide message authentication and integrity
- Unlike digital signatures, MACs are symmetric schemes and do not provide nonrepudiation
- MACs are much faster than digital signatures

3

Communication model



MAC Generation $S: \{0,1\}^* \times \{0,1\}^k \rightarrow \{0,1\}^m \rightarrow$

MAC Verification $V: \{0,1\}^* \times \{0,1\}^k \times \{0,1\}^m \rightarrow \text{Boolean} \rightarrow$

MAC generation

$t = S(k, x)$

Alice and Bob want to be assured that any manipulations of a message m in transit are detected

$t \leftarrow S(k, x)$

$\{true, false\} \leftarrow V(x, k, t)$

MAC verification

$t' = \text{MAC}(k, x)$

return $(t == t')$

4

Message Authentication Code (MAC)

- A MAC is defined by (Gen, S, V)
 - Gen takes as input 1^n and outputs a key k
 - S takes as input a key k and a message $x \in \{0, 1\}^*$ and outputs a tag t , s.t. $t = S_k(x)$
 - V takes as input a key k , a message x and a tag t and returns true or false
- Consistency property
 - For all key k and message x , $V_k(x, S_k(x)) = \text{true}$

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5

5

Properties of MACs (\rightarrow)

- Cryptographic checksum
 - A MAC generates a cryptographically secure authentication tag for a given message.
- Symmetric
 - MACs are based on secret symmetric keys. The signing and verifying parties must share a secret key.
- Arbitrary message size
 - MACs accept messages of arbitrary length.
- Fixed output length
 - MACs generate fixed-size authentication tags.

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6

6

Properties of MACs

- Message integrity
 - MACs provide message integrity: Any manipulations of a message during transit will be detected by the receiver.
- Message authentication
 - The receiving party is assured of the origin of the message.
- No nonrepudiation
 - Since MACs are based on symmetric principles, they do not provide nonrepudiation

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7

7

Security

- Threat model
 - Adaptive chosen-message attack
 - Assume the attacker can induce the sender to authenticate messages of the attacker's choice
- Security goal
 - Existential unforgeability
 - Attacker should be unable to forge a valid tag on any message not authenticated by the sender

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8

8

Security

- Computation-resistance (chosen message attack)

- For each key k , given zero or more (x_i, t_i) pairs, where $t_i = S_k(x_i)$, it is computationally infeasible to compute (x, t) , s.t. $t = S_k(x)$, for any new input $x \neq x_i$ (including possible $t = t_i$ for some i)
- Adaptive chosen-message attack
- Existential forgery

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9

9

Replay

- Mac does not prevent replay
 - No stateless mechanism can
- Replay attack can be a significant real-world concern
- Need to protect against replay at a higher layer

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10

10

Types of forgery

- **Selective forgery** – Attacks whereby an adversary is able to produce a new text-MAC pair for a text of his choice (or perhaps partially under his control)
 - Note that here the selected value is the text for which a MAC is forged, whereas in a chosen-text attack the chosen value is the text of a text-MAC pair used for analytical purposes (e.g., to forge a MAC on a distinct text).
- **Existential forgery** – Attacks whereby an adversary is able to produce a new text-MAC pair, but with no control over the value of that text.

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11

11

Implications of a secure MAC

- **FACT 1** – Computation resistance → key non-recovery (but not vice versa)
 - It must be computationally infeasible to compute k from (x_i, t_i) s
 - However, it may be possible to forge a tag without knowing the key

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12

12

Implications of a secure MAC

- **FACT 2** - Attacker cannot produce a valid tag for any new message
 - Given (x, t) , attacker cannot even produce (x, t') – a collision – for $t' \neq t$

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13

Implications of a secure MAC

- **FACT 3** - For an adversary not knowing k
 - S must be 2nd-preimage and collision resistant;
 - S must be preimage resistant w.r.t. a chosen-text attack;
- **FACT 4** - Secure MAC definition says nothing about preimage and 2nd-preimage for parties knowing k
 - Mutual trust model

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14

14

How to use MACs in practice

- In combination with encryption
 - x : plaintext; t : tag; y : ciphertext; z : transmitted message;
 ek : encryption key; ak : MAC key (authentication key)
 - Option 1 (SSL)
 - $t = S_{ak}(x)$; $y = E_{ek}(x || t)$, $z = c$
 - Option 2 (IpSec)
 - $y = E_{ek}(x)$; $t = S_{ak}(c)$; $z = y || t$
 - Option 3 (SSH)
 - $y = E_{ek}(x)$; $t = S_{ak}(x)$; $z = y || t$

15

Other uses

- One-time password
 - Based on time-synchronization
 - Based on challenge-response

16

Message Authentication Codes (MACs)

HOW TO BUILD A MAC

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17

17

How to build a MAC

- From Block Ciphers (more in general from PRF)
 - CBC-MAC
 - NMAC
 - PMAC
- From a hash functions
 - HMAC

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18

18

HMAC

How to build a MAC from a hash function

- Insecure constructions
 - Secret prefix scheme
 - $S(k, x) = H(k || x)$, H hash function
 - Secret suffix scheme
 - $S(k, x) = H(x || k)$, H hash function
 - Forgery is possible in both cases
 - HMAC construction is necessary

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19

19

Insecurity of prefix scheme

- Let $x = (x_1, x_2, x_3, \dots, x_n)$
- Let $t = S(k, x) = H(k || x_1, x_2, \dots, x_n)$
- Existential forgery attack
 - **Objective:** construct t' of $x' = x_1, x_2, \dots, x_n, x_{n+1}$ without knowing k (x_{n+1} : additional block)
 - **Assumption:** H follows the Merkle-Damgard scheme
 - **The attack:** $t' = h(x_{n+1}, t)$ with h compression function
 - Forging (x', t') only needs the previous hash output t (but not k)

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20

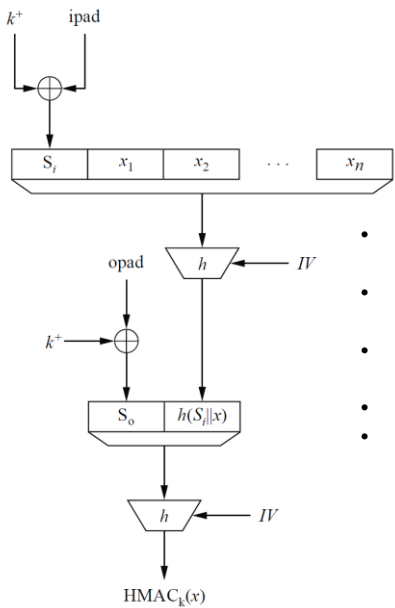
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Insecurity of the suffix scheme

- Let $t = S(k, x) = H(x || k)$
- Existential forgery attack
 - **Objective:** Construct t' of a x' without knowing the key k
 - **Assumption:** H follows the Merkle-Damgard scheme
 - **The attack**
 - Assume the adversary can find a collision $H(x) = H(x')$
 - Then, $t = h(H(x), k) = h(H(x'), k)$, thus $t' = t$, where h compression function

21

HMAC



- K^+ : padded key (key K padded with 0 up to b bit)
- $Ip\text{ad}$ = 0x36 repeated $b/8$ times
- $Op\text{ad}$ = 0x5C repeated $b/8$ times
- b block size
- h incorporated hash function

22

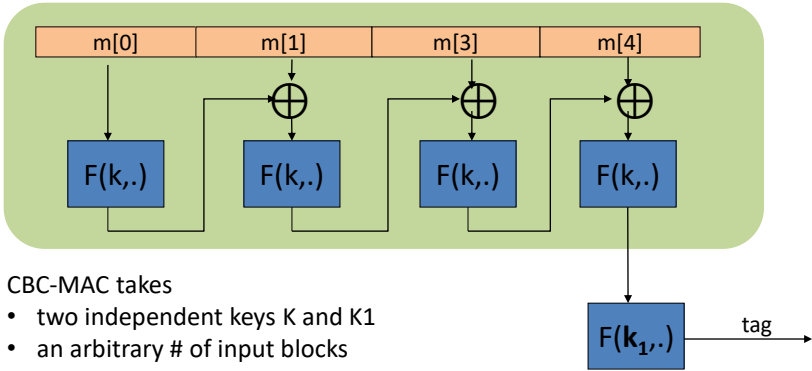
HMAC

- Computational efficiency
 - The message is hashed in the inner hash
 - The outer hash only hashes two blocks
- Security
 - There exists a proof of security in HMAC
 - THM - If an attacker can break HMAC then (s)he can break H

23

CBC-MAC: construction

raw CBC



- CBC-MAC takes
- two independent keys K and K_1
 - an arbitrary # of input blocks
 - PRF F is a cipher
 - $F = \text{DES} \rightarrow \text{Data Auth. Data (DAA, FIPS PUB 113, ANSI X9.17)}$
- Without the last encryption, rawCBC would be insecure

24

CBC-MAC: security

- Normally CBC-MAC does not use the last encryption
➔ rawCBC
- rawCBC is insecure
 - Proof (An existential forgery attack)
 1. The adversary chooses a one-block message x
 2. The adversary requests $t = \text{rawCBC}(k, x)$ where $t = E(k, x)$
 3. The adversary outputs $t' = t$ as MAC forgery of the two-block message $x' = x, (t \oplus x)$

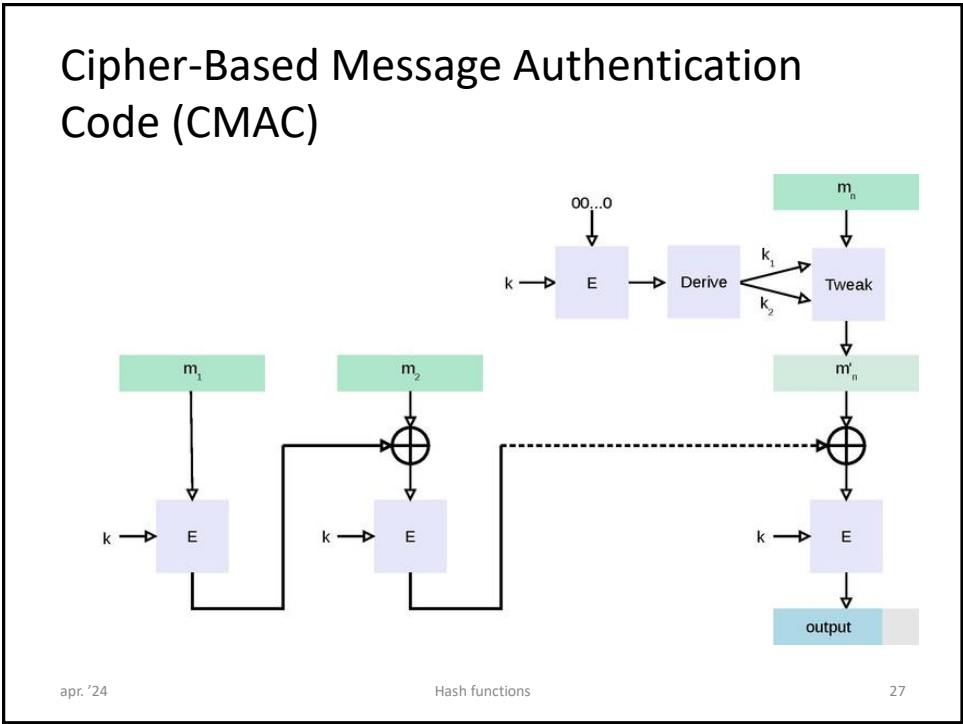
25

CBC-MAC: security

- Proof (for brevity rawCBC = H)
 - Let $t' = H(k, x') = H(k, (x, (t \oplus x))) =$
 $E(k, (E(k, x) \oplus (t \oplus x))) =$
 $E(k, t \oplus (t \oplus x)) =$
 $E(k, x) = t$, where E is the cipher

Q.E.D

26



27

CMAC

- CMAC overcomes the problems of CBC-MAC
- CMAC uses three keys K, K_1, K_2
 - K is k bit, K_1 and K_2 are n bit
 - K_1 and K_2 can be derived from K (NIST 800-38B)
 - $L = E_K(0^n)$
 - $K_1 = L \cdot x$ (if $\text{len}(x)$ is an integer multiple of n)
 - $K_2 = L \cdot x^2$ (if $\text{len}(x)$ is not an integer multiple of n)
 - Polynomials $x, x^2 \in GF(2^n)$, multiplication \cdot in $GF(2^n)$
- $E = \text{AES}, 3\text{DES}$

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28

CBC-MAC & CMAC drawbacks

- CBC-MAC and CMAC are not suitable for high-speed implementations because they are neither pipelineable nor parallelizable

29

Message Authentication Code (MAC)

PADDING

30

MAC Padding

- Pad by zeroes \Rightarrow insecure
 - $\text{pad}(m)$ and $\text{pad}(m \parallel 0)$ have the same MAC
- Padding must be an invertible function
 - $m_0 \neq m_1 \Rightarrow \text{pad}(m_0) \neq \text{pad}(m_1)$
- Standard padding (ISO)
 - Append “100...00” as needed
 - Scan right to left
 - “1” determines the beginning of the pad
 - Add a dummy block if necessary
 - When the message is a multiple of the block
 - The dummy block is necessary or existential forgery arises

31

Padding by 0es is a bad idea

- Proof
 - Let $x = x_1, x_2, x_3$ where x_3 is shorter than a block
 - Let's pad x_3 as follows $x_3^* \leftarrow x_3 \parallel 000$ (for example)
 - Let t be the tag outputted.
 - Consider now a message $x' = x \parallel 0$.
 - x' would be composed of three blocks $x'_1 = x_1, x'_2 = x_2$, and $x'_3 = x_3 \parallel 0$.
 - x'_3 needs padding and becomes $x_3'^* = x_3 \parallel 0 \parallel 00 = x_3 \parallel 000$.
 - So, x and x' after padding are equal and thus have the same tag.
- QED

32

On dummy block

- Without dummy block, existential forgery arises
- Proof
 - Let $x = x_1, x_2$ which needs padding
 - Build $x^* = x_1, x_2 || 100$, where x^* is the padded message
 - Consider now $x' = x_1, x_2 || 100$
 - Since x' is a multiple of the block we don't pad it
 - It follows that $x' = x^*$ and thus x and x' have the same tag

QED

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33

33

TIMING ATTACK

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34

34

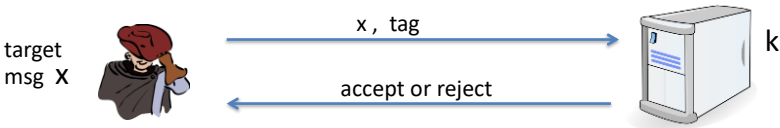
Timing Attack

- Example: Keyczar crypto library (Python) [simplified]

```
def Verify(key, msg, tag):  
    return HMAC(key, msg) == tag
```
- The problem: operator '==' is implemented as a byte-by-byte comparison
 - It returns false when first inequality found

35

Timing attack



- Timing attack: to compute tag for target message do:
- Step 1: Query server with random tag
 - Step 2: Loop over all possible first bytes of tag and query server.
Stop when verification takes a little longer than in step 1
 - Step 3: Repeat for all tag bytes until valid tag found

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36

Defense – solution #1 🤔

- Make string comparator always take same time
- Solution 1:

```
return false if tag has wrong length
result = 0
for x, y in zip( HMAC(key,msg) , tag):
    result |= ord(x) ^ ord(y)
return result == 0
```
- Can be difficult to ensure due to optimizing compiler

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37

37

Defense – solution #2 😊

- Make string comparator always take same time
- Solution 2

```
def Verify(key, msg, tag):
    mac = HMAC(key, msg)
    return HMAC(key, mac) == HMAC(key, tag)
```
- Attacker doesn't know values being compared

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38

38