


# Generating PRNG by Hash/MAC

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## Introduction



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- As an MDC/MAC produces an *apparently* random output, then it can be used to build a PRNG
- ISO 18031 *Random Bit Generation*
  - PRNG based on hash
- NIST SP 800-90 *Recommendation for Random Number Generation Using Random Bit Generators*
  - PRNG based on hash
  - PRNG based on HMAC


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# PRNG based on hash function



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- **SP 800-90, ISO 1**
  - V = seed
  - seedlen: size in bits of the seed
  - n = number of output bit
  - Outlen: size in bits of the hash output

- $m = \lceil n/\text{outlen} \rceil$ ;
- W = **null**; // null string of bit
- data = V;
- **for** i = 0 **to** m
  - $w_i = H(\text{data})$
  - $W = || w_i$
  - $\text{data} = (\text{data} + 1) \bmod 2^{\text{seedlen}}$
- **return** msb(W, n)


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# PRNG based on HMAC



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- **NIST SP 800-90**
  - $m = \lceil n/\text{outlen} \rceil$
  - $w_0 = V$ ; W = **null**;
  - **for** i = 1 **to** m
    - $w_i = \text{HMAC}_k(w_{i-1})$
    - $W = || w_i$
  - **return** msb(W, n)

- **IEEE 802.11i**
  - $m = \lceil n/\text{outlen} \rceil$ ;
  - W = **null**;
  - **for** i = 1 **to** m
    - $w_i = \text{HMAC}_k(V || i)$
    - $W = || w_i$
  - **return** msb(W, n)

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## PRNG based on HMAC



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- **TLS/WTLS**

- $m = \lceil n/\text{outlen} \rceil$
- $A(0) = V$ ;  $W = \text{null}$ ;
- **for**  $i = 1$  **to**  $m$ 
  - $A(i) = \text{HMAC}_k(A(i-1))$ ;
  - $w_i = \text{HMAC}_k(A(i) \parallel V)$ ;
  - $W = \parallel w_i$ ;
- **return**  $\text{msb}(W, n)$

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