



Reasoning and Querying with Knowledge Graphs

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Lecturer in Artificial Intelligence

Before we start...

GitHub Repository

https://github.com/city-knowledge-graphs/phd-course-uji



Agenda

Four sessions split into two days

– Morning sessions:

- Theory: 9:30-11:00

- Break 30 min

Hands-on: 11:30-13:00

Lunch break (1hour)

– Afternoon sessions:

- Theory: 14:00-15:30

- Break 30 min

- Hands-on: 16:00-17:30

Course Organization

- ✓ Introduction to Knowledge Graphs
 - ✓ Lab: Creation of a small knowledge graph and ontology.
- 2. Reasoning and Querying with Knowledge Graphs
 - Lab: First steps with the SPARQL query language.
- 3. Matching: KG-to-KG and CSV-to-KG
 - Lab: Creation of a (simple) matching system.
- 4. Knowledge Graphs and Language Models
 - Lab: Ontology Embeddings with OWL2Vec*.

PART I: SPARQL Query Language for RDF-based KGs

SPARQL by Example

SPARQL

- SPARQL Protocol And RDF Query Language
- Standard language to query graph data represented as RDF triples
- W3C Recommendations
 - SPARQL 1.0: W3C Recommendation 15 January 2008
 - SPARQL 1.1: W3C Recommendation 21 March 2013

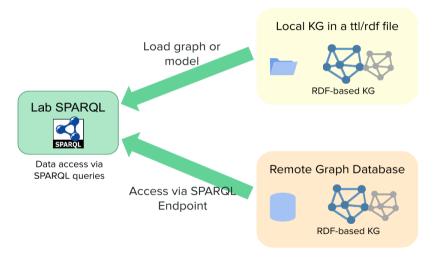
SPARQL

- SPARQL Protocol And RDF Query Language
- Standard language to query graph data represented as RDF triples
- W3C Recommendations
 - SPARQL 1.0: W3C Recommendation 15 January 2008
 - SPARQL 1.1: W3C Recommendation 21 March 2013
- Documentation:
 - Syntax and semantics of the SPARQL query language for RDF:

```
http://www.w3.org/TR/rdf-sparql-query/
https://www.w3.org/TR/sparql11-overview/
```

- Examples: https://www.w3.org/2008/09/sparql-by-example/

SPARQL: local and remote KG access



SPARQL Examples (i)

- Based on DBpedia: RDF version of Wikipedia with information about actors, movies, etc.: https://dbpedia.org/
- Web interface for SPARQL writing: http://dbpedia.org/sparql

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People called "Johnny Depp"

```
PREFIX foaf: <a href="http://xmlns.com/foaf/0.1/">http://xmlns.com/foaf/0.1/>
SELECT DISTINCT ?jd WHERE {
     ?jd foaf:name "Johnny Depp"@en .
}
```

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SELECT DISTINCT ?jd WHERE {
     ?jd foaf:name "Johnny Depp"@en .
```

Answer:

```
?id
<a href="http://dbpedia.org/resource/Johnny_Depp">http://dbpedia.org/resource/Johnny_Depp></a>
```

SPARQL Examples (ii)

Films starring "Johnny Depp"

```
PREFIX foaf: <http://xmlns.com/foaf/0.1/>
PREFIX dbo: <http://dbpedia.org/ontology/>
SELECT ?m WHERE {
    ?jd foaf:name "Johnny Depp"@en .
    ?m dbo:starring ?jd .
}
```

(*) dbo:starring comes from the https://dbpedia.org/ontology/

SPARQL Examples (ii)

Films starring "Johnny Depp"

Answer:

```
?m
<http://dbpedia.org/resource/Dead_Man>
<http://dbpedia.org/resource/Edward_Scissorhands>
<http://dbpedia.org/resource/Arizona_Dream>...
```

(*) dbo:starring comes from the https://dbpedia.org/ontology/

SPARQL Examples (iii)

Names of people who co-starred with "Johnny Depp"

```
SELECT DISTINCT ?costar WHERE {
    ?jd foaf:name "Johnny Depp"@en .
    ?m dbo:starring ?jd .
    ?m dbo:starring ?other .
    ?other foaf:name ?costar .
}
```

SPARQL Examples (iii)

Names of people who co-starred with "Johnny Depp"

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SELECT DISTINCT ?costar WHERE {
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    ?m dbo:starring ?other .
    ?other foaf:name ?costar .
}
```

Answer:

```
?costar

"Al Pacino"@en

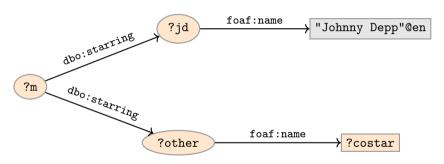
"Antonio Banderas"@en

"Johnny Depp"@en

"Marlon Brando"@en
```

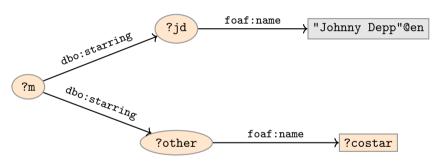
Graph Patterns

The previous SPARQL query as a graph:



Graph Patterns

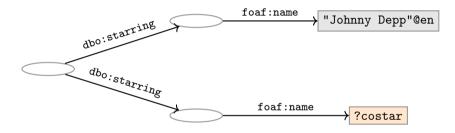
The previous SPARQL query as a graph:



Pattern matching: assign values to variables to make this a sub-graph of the RDF graph!

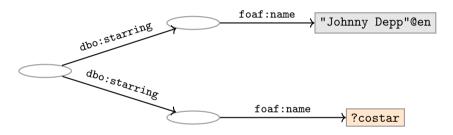
Graph with blank nodes

Variables not SELECTED can equivalently be blank:



Graph with blank nodes

Variables not SELECTED can equivalently be blank:



Pattern matching: a function that assigns values (*i.e.*, resource, a blank node, or a literal) to variables and blank nodes to make this a sub-graph of the RDF graph!

SPARQL Systematically

```
PREFIX foaf: <a href="http://xmlns.com/foaf/0.1/">http://xmlns.com/foaf/0.1/>
PREFIX dbo: <a href="http://dbpedia.org/ontology/">http://dbpedia.org/ontology/>
SELECT DISTINCT ?costar
WHERE {
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     ?m dbo:starring ?jd .
     ?m dbo:starring ?other .
     ?other foaf:name ?costar .
    FILTER (STR(?costar)!="Johnny Depp")
ORDER BY ?costar
I.TMTT 10
```

Prologue: prefix definitions

```
PREFIX foaf: <a href="http://xmlns.com/foaf/0.1/">http://xmlns.com/foaf/0.1/>
PREFIX dbo: <a href="http://dbpedia.org/ontology/">http://dbpedia.org/ontology/>
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    ?other foaf:name ?costar .
    FILTER (STR(?costar)!="Johnny Depp")
ORDER BY ?costar
LIMIT 10
```

Results: (1) query type (SELECT, ASK, CONSTRUCT, DESCRIBE), (2) remove duplicates (DISTINCT, REDUCED), (3) variable list.

```
PREFIX foaf: <a href="http://xmlns.com/foaf/0.1/">http://xmlns.com/foaf/0.1/>
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     ?other foaf:name ?costar .
    FILTER (STR(?costar)!="Johnny Depp")
ORDER BY ?costar
```

Query pattern: graph pattern to be matched

```
PREFIX foaf: <a href="http://xmlns.com/foaf/0.1/">http://xmlns.com/foaf/0.1/>
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LIMIT 10
```

Solution modifiers: ORDER BY, LIMIT, OFFSET

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    FILTER (STR(?costar)!="Johnny Depp")
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LIMIT 10
```

Types of Queries (i)

SELECT Compute table of bindings for variables

```
SELECT DISTINCT ?a ?b WHERE {
   [ dbo:starring ?a ;
     dbo:starring ?b ]
}
```

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```
SELECT DISTINCT ?a ?b WHERE {
   [ dbo:starring ?a ;
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}
```

CONSTRUCT Use bindings to construct a new RDF graph

```
CONSTRUCT {
    ?a foaf:knows ?b .
} WHERE {
    [ dbo:starring ?a ;
     dbo:starring ?b ]
}
```

Types of Queries (ii)

ASK Answer (yes/no) whether there is ≥ 1 match ASK WHERE { ?jd foaf:name "Johnny Depp"@en . }

Types of Queries (ii)

SPARQL Systematically: Solution Modifiers

Solution Sequences and Modifiers

- Permitted to SELECT queries only
- SELECT treats solutions as a sequence (solution sequence)
- Query patterns generate an unordered collection of solutions
- Sequence modifiers can modify the solution sequence (not the solution itself). Applied in this order:
 - Order
 - Projection
 - Distinct
 - Reduced
 - Offset
 - Limit

ORDER BY

- Used to sort the solution sequence in a given way:
- SELECT ... WHERE ... ORDER BY ...
- ASC for ascending order (default) and DESC for descending order

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- E.a.

```
SELECT ?city ?pop WHERE {
  ?city dbo:country ?country ;
        dbo:populationUrban ?pop .
} ORDER BY ?country DESC(?pop)
```

ORDER BY

- Used to sort the solution sequence in a given way:
- SELECT ... WHERE ... ORDER BY ...
- ASC for ascending order (default) and DESC for descending order
- E.g.

```
SELECT ?city ?pop WHERE {
    ?city dbo:country ?country ;
        dbo:populationUrban ?pop .
} ORDER BY ?country DESC(?pop)
```

- Standard defines sorting conventions for literals, URIs, etc.
- Not all "sorting" variables are required to appear in the SELECTION.

ORDER BY (Example)

```
SELECT DISTINCT ?costar
WHERE {
    ?jd foaf:name "Johnny Depp"@en .
    ?m dbo:starring ?jd .
    ?m dbo:starring ?other .
    ?other foaf:name ?costar .
    FILTER (STR(?costar)!="Johnny Depp")
}
ORDER BY ?costar
```

Projection, DISTINCT, REDUCED

- Projection (i.e., SELECTED variables) means that only some variables are part of the solution
 - Done with SELECT ?x ?y WHERE {?x dbo:starring ?y . }

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 - Done with SELECT DISTINCT ?x ?y WHERE {?x dbo:starring ?y. }
 - A solution is a duplicate if it assigns the same RDF terms to all variables as another solution.
- REDUCED allows to remove some or all duplicate solutions
 - Done with SELECT REDUCED ?x ?y WHERE {?x dbo:starring ?y . }
 - Motivation: Can be expensive to find and remove all duplicates
 - Behaviour left to the SPARQL engine.

OFFSET and LIMIT

- LIMIT: limits the number of results
- OFFSET: position/index of the first returned result
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- For example, solutions number 51 to 60:
 SELECT ?x ?y WHERE {?x dbo:starring ?y .} ORDER BY ?x
 LIMIT 10 OFFSET 50

OFFSET and LIMIT

- LIMIT: limits the number of results
- OFFSET: position/index of the first returned result
- Useful for paging through a large set of solutions
- For example, solutions number 51 to 60: SELECT ?x ?y WHERE {?x dbo:starring ?y .} ORDER BY ?x LIMIT 10 OFFSET 50
- LIMIT and OFFSET can be used separately
- OFFSET not meaningful without ORDER BY.

OFFSET and LIMIT (Example)

```
SELECT DISTINCT ?costar
WHERE {
    ?jd foaf:name "Johnny Depp"@en .
    ?m dbo:starring ?jd .
    ?m dbo:starring ?other .
    ?other foaf:name ?costar ...
    FILTER (STR(?costar)!="Johnny Depp")
ORDER BY ?costar
LIMIT 10 OFFSET 50
```

SPARQL Systematically: Query Graph Patterns

Query patterns

- Types of graph patterns for the query pattern (WHERE clause):
 - ✓ Basic Graph Patterns (BGP)
 - Filters or Constraints (FILTER)
 - Optional Graph Patterns (OPTIONAL)
 - Union Graph Patterns (UNION, Matching Alternatives)
 - Graph Graph Patterns (RDF Datasets)

Filters (i)

- A set of triple patterns may include constraints or filters
- Reduces matches of surrounding group where filter applies
- Example:

```
SELECT ?x
WHERE {
    ?x a dbo:Place ;
       dbo:populationUrban ?pop .
    FILTER (?pop > 1000000)
}
```

Filters (ii)

– Example:

```
SELECT DISTINCT ?costar
FROM <a href="http://dbpedia_dataset">http://dbpedia_dataset</a>
WHERE {
    ?jd foaf:name "Johnny Depp"@en .
    ?m dbo:starring ?jd .
    ?m dbo:starring ?other .
    ?other foaf:name ?costar .
    FILTER (STR(?costar)!="Johnny Depp")
ORDER BY ?costar
LIMIT 10 OFFSET 50
```

Filters: Functions and Operators

- Usual binary operators: | |, &&, =, !=, <, >, <=, >=, +, -, *, /.
- Usual unary operators: !, +, -.
- Unary tests: bound(?var), isURI(?var), isBlank(?var), isLiteral(?var).
- Accessors: str(?var), lang(?var), datatype(?var), year(?date), xsd:integer(?value)
- regex is used to match a variable with a regular expression. Always use with str(?var). E.g.: regex(str(?costar), "Alpacino").

More details in specification: http://www.w3.org/TR/rdf-sparql-query/

OPTIONAL Patterns

 Allows a match to leave some variables unbound (e.g. no data is available). e.g.,:

```
WHERE {
    ?x a dbo:Person ;
      foaf:name ?name .
    OPTIONAL {
      ?x dbo:birthDate ?date .
    }
}
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- ?x and ?name bound in every match, ?date is bound if available.

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WHERE {
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    OPTIONAL {
      ?x dbo:birthDate ?date .
    }
}
```

- ?x and ?name bound in every match, ?date is **bound if available**.
- Groups can contain several optional parts, evaluated separately

OPTIONAL Patterns: with FILTER

```
- Example:
    WHERE {
      ?x a dbo:Person :
         foaf:name ?name ...
      OPTIONAL {
        ?x dbo:birthDate ?date .
        FILTER (?date > "1980-01-01T00:00:00"^^xsd:dateTime)
```

 - ?x and ?name bound in every match, ?date is bound if available and from 1980 onwards.

Session 2. June, 2024

Matching Alternatives (UNION)

- A UNION pattern matches if any of some alternatives matches
- E.g.

```
SELECT DISTINCT ?writer
WHERE
  ?s rdf:type dbo:Book .
    ?s dbo:author ?writer .
  UNION
    ?s dbo:writer ?writer .
```

'Graph' Graph Patterns (RDF datasets)

- SPARQL queries are executed against an RDF dataset
- An RDF dataset comprises
 - One default graph (unnamed) graph. Target for this course.
 - Zero or more named graphs identified by an URI

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- SPARQL queries are executed against an RDF dataset
- An RDF dataset comprises
 - One default graph (unnamed) graph. Target for this course.
 - Zero or more named graphs identified by an URI
- FROM and FROM NAMED keywords allows to select an RDF dataset
- Keyword GRAPH makes the named graphs the active graph for pattern matching

SPARQL 1.1

SPARQL 1.1: new features

- The new features in SPARQL 1.1 QUERY language:
 - Assignments and Expressions
 - Aggregates
 - Subqueries
 - Negation (new syntax)
 - Property paths

SPARQL 1.1: new features

- The new features in SPARQL 1.1 QUERY language:
 - Assignments and Expressions
 - Aggregates
 - Subqueries
 - Negation (new syntax)
 - Property paths
- Specification for:
 - SPARQL 1.1 UPDATE Language
 - SPARQL 1.1 Federated Queries
 - SPARQL 1.1 Entailment Regimes

Assignment and Expressions

- The value of an expression can be assigned/bound to a new variable
- Can be used in SELECT, BIND or GROUP BY clauses: (expression AS ?var)

Expressions in SELECT clause

```
SELECT ?city (xsd:integer(?pop)/xsd:float(?area) AS ?density)
{
    ?city dbo:populationTotal ?pop .
    ?city dbo:PopulatedPlace/areaTotal ?area .
    ?city dbo:country dbr:United_Kingdom .
    FILTER (xsd:float(?area)>0.0)
}
```

Aggregates: Grouping and Filtering

- Solutions can optionally be grouped according to one or more expressions.
- To specify the group, use GROUP BY.
- If GROUP BY is not used, then only one (implicit) group

Aggregates: Grouping and Filtering

- Solutions can optionally be grouped according to one or more expressions.
- To specify the group, use GROUP BY.
- If GROUP BY is not used, then only one (implicit) group
- To filter solutions resulting from grouping, use HAVING.
- HAVING operates over grouped solution sets, in the same way that FILTER operates over un-grouped ones.

Aggregates: Example

Actors with more than 15 movies

Aggregates: Example

Actors with more than 15 movies

† Only expressions consisting of aggregates and constants may be projected, together with variables in GROUP, BY

Aggregates: common functions

- Count counts the number of times a variable has been bound.
- Sum sums numerical values of bound variables.
- Avg finds the average of numerical values of bound variables.
- Min finds the minimum of the numerical values of bound variables.
- Max finds the maximum of the numerical values of bound variables.

† Aggregates assume CWA and UNA

Subqueries

- A way to embed SPARQL queries within other queries
- Subqueries are evaluated first and the results are projected to the outer query.

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```
SELECT ?country ?pop (round(?pop/?worldpop*1000)/10 AS ?percentage) WHERE {
  ?country rdf:type dbo:Country .
  ?country dbo:populationTotal ?pop .
   SELECT (sum(?p) AS ?worldpop) WHERE {
      ?c rdf:type dbo:Country .
      ?c dbo:populationTotal ?p .}
   ORDER BY desc(?pop)
```

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- Subqueries are evaluated first and the results are projected to the outer query.

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   SELECT (sum(?p) AS ?worldpop) WHERE {
      ?c rdf:type dbo:Country .
      ?c dbo:populationTotal ?p .}
   ORDER BY desc(?pop)
```

† Note that the *Sum()* aggregation is done over all the elements (single default group).

Negation in SPARQL 1.1: MINUS and FILTER NOT EXISTS

Two ways to do negation. *e.g.*, retrieve people without a name:

```
SELECT DISTINCT * WHERE {
    ?person a foaf:Person .
    MINUS { ?person foaf:name ?name }
}

SELECT DISTINCT * WHERE {
    ?person a foaf:Person .
    FILTER NOT EXISTS { ?person foaf:name ?name }
}
```

Property paths: basic motivation

- Some queries get needlessly large.
- SPARQL 1.1 define a small language to defined paths.
- Examples:
 - city:ernesto foaf:knows+ ?friend to extract all friends of friends.
 - foaf:maker dc:creator instead of UNION.
 - Friend's names, { _:me foaf:knows/foaf:name ?friendsname }.
 - Sum several items:

```
SELECT (sum(?cost) AS ?total) { :order :hasItem/:price ?cost }
```

Property paths: example

```
PREFIX foaf: <http://xmlns.com/foaf/0.1/>
PREFIX dbo: <http://dbpedia.org/ontology/>
SELECT DISTINCT ?costar
WHERE {
    ?m dbo:starring/foaf:name "Johnny Depp"@en .
    ?m dbo:starring/foaf:name ?costar .
    FILTER (STR(?costar)!="Johnny Depp")
}
ORDER BY ?costar
```

†Similar to blank node syntax.

Property paths: syntax

Syntax Form	Matches
iri	An (property) IRI. A path of length one.
^elt	Inverse path (object to subject).
elt1 / elt2	A sequence path of elt1 followed by elt2.
elt1 elt2	A alternative path of elt1 or elt2 (all possibilities are tried).
elt*	Seq. of zero or more matches of elt.
elt+	Seq. of one or more matches of elt.
elt?	Zero or one matches of elt.
!iri or !(iri1 irin)	Negated property set.
!^iri or !(^iri _i ^iri _n)	Negation of inverse path.
!(iri ₁ iri _j ^iri _{j+1} ^iri _n)	Negated combination of forward and inverese properties.
(elt)	A group path elt, brackets control precedence.

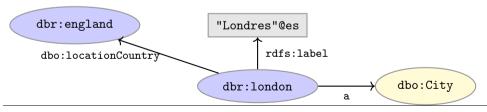
^{*} elt is a path element, which may itself be composed of path constructs (see Syntax form).

SPARQL Summary

SPARQL Summary (i)

Return all Cities:

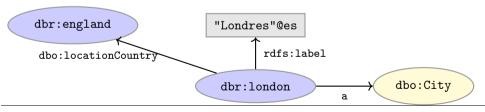
```
PREFIX dbo: <http://dbpedia.org/ontology/>
PREFIX rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>
SELECT DISTINCT ?city WHERE {
     ?city rdf:type dbo:City .
}
```



SPARQL Summary (i)

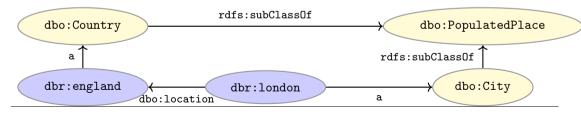
Return all Cities: Query Result= {dbr:london}

```
PREFIX dbo: <http://dbpedia.org/ontology/>
PREFIX rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>
SELECT DISTINCT ?city WHERE {
     ?city rdf:type dbo:City .
}
```



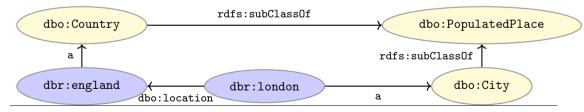
SPARQL Summary (ii)

Return all Populated Places:



SPARQL Summary (ii)

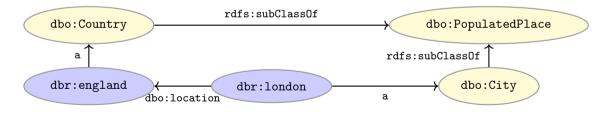
Return all Populated Places: Query Result= {}



PART II: Reasoning with Knowledge Graphs

Implicit Knowledge in KGs: Entailment

- Given a set of triples \mathcal{G} (i.e., a Graph), can we entail a triple t ($\mathcal{G} \models t$)?
- Can we entail the triple: dbr:london rdf:type dbo:PopulatedPlace and add it to the graph below? (Graph expansion via reasoning).
- Similarly for dbr:england



- Interpretations might be conceived as potential "realities" or "worlds".
- Interpretations assign values to elements.
 - (The **intuitions** behind set-theory are **formally represented**.)

- Interpretations might be conceived as potential "realities" or "worlds".
- Interpretations assign values to elements.
 - (The intuitions behind set-theory are formally represented.)
- Given an interpretation $\mathcal I$ and a set of triples $\mathcal G$
- $-\mathcal{G}$ is valid in \mathcal{I} (written $\mathcal{I} \models \mathcal{G}$), iff $\mathcal{I} \models t$ for all $t \in \mathcal{G}$.
- Then \mathcal{I} is also called a **model** of \mathcal{G} .

- The following interpretation \mathcal{I} is a model of our example \mathcal{G} :
 - $dbo:Citv^{\mathcal{I}} = \{dbr:london\}$
 - $dbo: Country^{\mathcal{I}} = \{dbr: england\}$
 - $dbo:PopulatedPlace^{\mathcal{I}} = \{dbr:london, dbr:england\}$
 - dbo:location^{\mathcal{I}} = { $\langle dbr:london, dbr:england \rangle$ }

- The following interpretation \mathcal{I} is a model of our example \mathcal{G} :
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 - $dbo: Country^{\mathcal{I}} = \{dbr: england\}$
 - $dbo:PopulatedPlace^{\mathcal{I}} = \{dbr:london, dbr:england\}$
 - dbo:location^{\mathcal{I}} = { $\langle dbr:london, dbr:england \rangle$ }
- $-\mathcal{I} \models \mathcal{G}$ (is a model of \mathcal{G}) as the following holds:
 - dbo:City $^{\mathcal{I}} \subseteq$ dbo:PopulatedPlace $^{\mathcal{I}}$
 - dbo:Country $^{\mathcal{I}} \subset dbo:PopulatedPlace^{\mathcal{I}}$
 - dbr:london $^{\mathcal{I}} \in dbo:City^{\mathcal{I}}$

- -t = dbr:london rdf:type dbo:PopulatedPlace
- Does $\mathcal{I} \models t$?

- -t = dbr:london rdf:type dbo:PopulatedPlace
- Does $\mathcal{I} \models t$?
 - Yes: $dbo:PopulatedPlace^{\mathcal{I}} = \{dbr:london, dbr:england\}$

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- Does \mathcal{G} $\models t$?

- -t = dbr:london rdf:type dbo:PopulatedPlace
- Does $\mathcal{I} \models t$?
 - Yes: $dbo:PopulatedPlace^{\mathcal{I}} = \{dbr:london, dbr:england\}$
- Does \mathcal{G} $\models t$?
 - if and only if
 - For any interpretation \mathcal{I} with $\mathcal{I} \models \mathcal{G}$
 - $-\mathcal{I} \models t$.
 - (Yes, in this case too.)

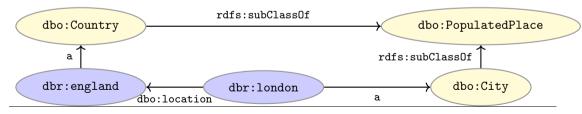
- -t = dbr:london rdf:type dbo:PopulatedPlace
- Does $\mathcal{I} \models t$?
 - Yes: $dbo:PopulatedPlace^{\mathcal{I}} = \{dbr:london, dbr:england\}$
- − Does $\mathcal{G} \models t$?
 - if and only if
 - For any interpretation \mathcal{I} with $\mathcal{I} \models \mathcal{G}$
 - $-\mathcal{I} \models t$.
 - (Yes, in this case too.)
- Does $\mathcal{G} \models t_2$ (t_2 =dbr:london rdf:type dbo:Country)?

- -t = dbr:london rdf:type dbo:PopulatedPlace
- Does $\mathcal{I} \models t$?
 - Yes: dbo:PopulatedPlace $^{\mathcal{I}} = \{dbr: london, dbr: england\}$
- Does $\mathcal{G} \models t$?
 - if and only if
 - For any interpretation \mathcal{I} with $\mathcal{I} \models \mathcal{G}$
 - $-\mathcal{I} \models t$.
 - (Yes. in this case too.)
- Does $\mathcal{G} \models t_2$ (t_2 =dbr:london rdf:type dbo:Country)?
 - No: Our \mathcal{I} is a counter example. $\mathcal{I} \models \mathcal{G}$ but $\mathcal{I} \not\models t_2$

SPARQL Example: with entailment

Return all Populated places:

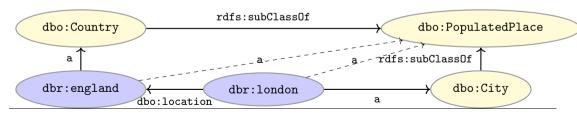
```
PREFIX dbo: <http://dbpedia.org/ontology/>
PREFIX rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>
SELECT DISTINCT ?place WHERE {
     ?place rdf:type dbo:PopulatedPlace .
}
```



SPARQL Example: with entailment

Return all Populated places: Query Result= {dbr:england, dbr:london}

```
PREFIX dbo: <http://dbpedia.org/ontology/>
PREFIX rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>
SELECT DISTINCT ?place WHERE {
     ?place rdf:type dbo:PopulatedPlace .
}
```



Model-Theoretic Semantics in practice

- Model-theoretic semantics yields an unambigous notion of entailment.
- In principle, all interpretations need to be considered.
- However there are infinitely many such interpretations,
- An algorithm should terminate in finite time.

Foundations of Semantic Web Technologies. Chapter 3.

Syntactic methods for Entailment

Syntactic Reasoning

- From the computation point of view, we need means to decide entailment syntactically.
- Syntactic methods operate
 - only on the form of a statement, that is on its concrete grammatical structure (i.e., triples),
 - without recurring to interpretations.
- Syntactic methods should justify that their so-called operational semantics are expected with respect to model-theoretic semantics.

OWL 2 Reasoning Algorithms (i)

- Reasoning in OWL 2 is typically based on (Hyper)Tableau Reasoning Algorithms (tableau = truth tree)
- Algorithm tries to construct an abstraction of a model.

OWL 2 Reasoning Algorithms (i)

- Reasoning in OWL 2 is typically based on (Hyper)Tableau Reasoning Algorithms (tableau = truth tree)
- Algorithm tries to construct an abstraction of a model.
- State-of-the-art algorithms:
 - − e.g., HermiT (default option in Protégé).

OWL 2 Reasoning Algorithms (ii)

- ✓ OWL 2 Reasoners are optimised for TBox tasks.
- Effective with many realistic ontologies.
- ABox reasoning tasks are untractable with relatively small KGs.
- Decidability is open when querying OWL-based KGs with SPARQL.
- There are some tricks to make it work, but complexity is still high.
- The main problem is that one cannot just expand the (knowledge) graph and then execute a SPARQL query
- Solution: OWL 2 Profiles

Computational properties: https://www.w3.org/TR/owl2-profiles/#Computational_Properties
Seminars by Prof. lan Horrocks: http://www.cs.ox.ac.uk/people/ian.horrocks/Seminars/seminars.html

OWL 1, OWL 2 (profiles) and RDFS

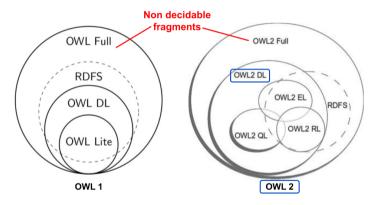
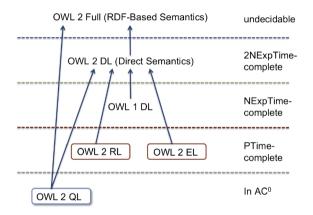


Image adapted from Olivier Cure and Guillaume Blin. RDF Database Systems (Chapter 3). 2015. Elsevier.

Data Complexity in OWL 2 and Profiles



https://www.w3.org/TR/owl2-profiles/

OWL 2 Profiles summary

- OWL 2 has various profiles that correspond to different DLs.
- These profiles have very interesting computational properties.

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- These profiles have very interesting computational properties.
 - OWL 2 QL:
 - Specifically designed for efficient database integration.
 - OWL 2 EL:
 - A lightweight language with polynomial time reasoning.
 - OWL 2 RL:
 - Designed for compatibility with rule-based inference tools.
 - Efficient reasoning with large datasets.

OWL QL Profile

- ✓ Required language so that queries can be rewritten using the TBox.
- Used in Ontology Based Data Access (OBDA) where SPARQL queries are translated to SQL

Not supported, simplified:

- disjunction
- universal quantification, cardinalities, and functional roles
- X = (SameIndividual)
- enumerations (closed classes)
- subproperties of chains, transitivity
- reduced list of datatypes

OWL EL Profile

- Standard reasoning tasks in P time
- Very good for large ontologies.
- ✓ Used in many biomedical ontologies (e.g., SNOMED CT).
- ✓ Reasoning can be performed via saturation (i.e., inference rules).

Not supported features, simplified:

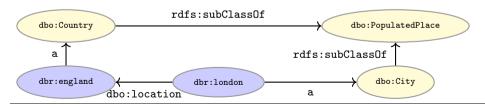
- ightharpoonup negation (but $C \sqcap D \sqsubseteq \bot$ possible)
- disjunction
- universal quantification and cardinalities
- inverse roles and some role characteristics
- reduced list of datatypes

OWL 2 RL Profile

- Y Puts syntactic constraints in the way in which constructs are used (i.e., syntactic subset of OWL 2).
- Imposes a reduced list of allowed datatypes.
- ✓ OWL 2 RL axioms can be directly translated into datalog rules.
- Enables desirable computational properties using rule-based reasoning engines.

Reasoning in the OWL QL Profile

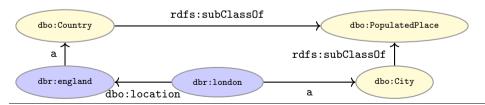
- Reasoning is performed via backward chaining (e.g., rewriting of a given query Q into Q' via the ontology axioms, instead of expanding the graph). For example:



Reasoning in the OWL QL Profile

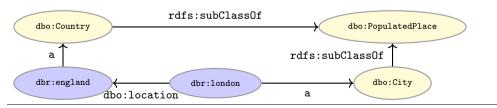
- Reasoning is performed via backward chaining (e.g., rewriting of a given query Q into Q' via the ontology axioms, instead of expanding the graph). For example:

```
Q: SELECT DISTINCT ?place WHERE {?place rdf:type dbo:PopulatedPlace . }
```



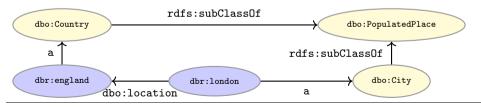
Reasoning in the OWL QL Profile

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Reasoning in the OWL QL Profile

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Inference rules

Inference rules (i)

- Inference rules (also known as deduction rules or derivation rules) is an option to describe syntactic solutions.
- The general form of an inference rule is:

$$\frac{P_1,\ldots,P_n}{P}$$

- the P_i are **premises** (body)
- and P is the **conclusion** (head).
- An inference rule may have,
 - any number of premises (typically one or two),
 - but only one conclusion.

Inference rules (ii)

- Recall that syllogisms (i.e., inference) can be traced back to Aristotle
- Example:

All human are mortal
Socrates is a human
Therefore. Socrates is mortal

Inference rules (iii)

- The whole set of inference rules given for a logic is called **deduction** calculus.
- ⊢ is the inference relation, while ⊨ was the entailment relation using model theoretic semantics.
 - − We write $\Gamma \vdash P$ if we can deduce P from the premises Γ .

Inference rules (iii)

- The whole set of inference rules given for a logic is called **deduction** calculus.
- ⊢ is the inference relation, while ⊨ was the entailment relation using model theoretic semantics.
 - − We write $\Gamma \vdash P$ if we can deduce P from the premises Γ .
- In our example:
 - the **premises** Γ are a **set of triples** (*i.e.*, a (sub)graph \mathcal{G}),
 - the conclusion P is a new triple t
 - After applying the rules to \mathcal{G} we will get an **expanded graph** \mathcal{G}'

RDFS Inference Rules

RDFS supports several rules. Organized into three groups:

1. Type propagation:

- "London is a City, all Cities are populated places, so. . . "

2. Property propagation:

- "London is the capital of England, anything that is capital of a country is also located in that country, so..."

3. Domain and range propagation:

- "Everything that has a capital is a country, so England is a..."
- "Everything that is a capital is a city, so London is a..."

Type propagation

- Members of superclasses:

(*) rdfs9, rdfs10, rdfs11 are the names of the inference rules in the W3C standard. A, B are classes; x is an instance.

Type propagation

– Members of superclasses:

– Reflexivity of sub-class relation:

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Type propagation

Members of superclasses:

Reflexivity of sub-class relation:

Transitivity of sub-class relation:

(*) rdfs9. rdfs10. rdfs11 are the names of the inference rules in the W3C standard. A. B are classes: x is an instance.

Type propagation: Examples

– Members of superclasses:

```
:City rdfs:subClassOf :PopulatedPlace . :london rdf:type :City . :london rdf:type :PopulatedPlace . rdfs9
```

Reflexivity of sub-class relation:

```
:City rdf:type rdfs:Class .
:City rdfs:subClassOf :City .
```

Transitivity of sub-class relation:

```
:City rdfs:subClassOf :PopulatedPlace . :PopulatedPlace rdfs:subClassOf :Place . rdfs11
```

Property Propagation

- Transitivity:

```
P rdfs:subPropertyOf Q . Q rdfs:subPropertyOf R .

P rdfs:subPropertyOf R . rdfs5
```

(*) P, Q are properties; u, v are instances.

Property Propagation

- Transitivity:

- Reflexivity:

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Property Propagation

- Transitivity:

- Reflexivity:

– Property transfer:

(*) P, Q are properties; u, v are instances.

Property Propagation: Examples

- Transitivity:

```
:has_writer rdfs:subPropertyOf :has_author . :has_author rdfs:subPropertyOf :has_creator . rdfs:subPropertyOf :has_creator .
```

- Reflexivity:

```
:has_writer rdf:type rdf:Property .
:has_writer rdfs:subPropertyOf :has_writer .
```

Property transfer:

```
:has_author rdfs:subPropertyOf :has_creator . :Hamlet :has_author :Shakespeare . rdfs
```

Domain and range propagation

Typing triggered by the use of properties.

- Domain propagation:

(*) P, Q are properties; x, y are instances.

Domain and range propagation

Typing triggered by the use of properties.

- Domain propagation:

- Range propagation:

(*) P, Q are properties; x, y are instances.

Domain and Range Propagation: Examples

– Domain propagation:

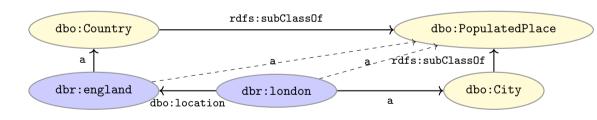
```
:capitalOf rdfs:domain :City . :london :capitalOf :england . :clondon rdf:type :City . rdfs2
```

– Range propagation:

RDFS inference rules in our example

```
dbo:City rdfs:subClassOf dbo:PopulatedPlace . dbr:london rdf:type dbo:City . dbr:london rdf:type dbo:PopulatedPace . rdfs9
```

```
dbo:Country rdfs:subClassOf dbo:PopulatedPlace . dbr:england rdf:type dbo:Country . dbr:england rdf:type dbo:PopulatedPlace .
```



Inference rules in the OWL EL Profile

- Reasoning can be performed via saturation[†] (i.e., inference rules).
- For example:

† Using a saturation-based approach over an OWL 2 ontology is not possible.

ELK reasoner (also available as Protégé plugin): https://github.com/liveontologies/elk-reasoner/wiki

Inference rules in the OWL 2 RL Profile

Reasoning via full materialisation of the graph, similarly to RDFS inference rules. e.g.,:

 See W3C specification for further inference rules in OWL 2 RL in addition to the RDFS ones.

W3C: https://www.w3.org/TR/owl2-profiles/#Reasoning_in_OWL_2_RL_and_RDF_Graphs_using_Rules GraphDB: https://graphdb.ontotext.com/documentation/standard/reasoning.html

OWL 2 Important Practical Examples

Open World Assumptions

Closed World Assumption (CWA)

- Complete knowledge.
- Any statement that is not known to be true is false. (*)
- Typical semantics for database systems.

Open World Assumptions

Closed World Assumption (CWA)

- Complete knowledge.
- Any statement that is not known to be true is false. (*)
- Typical semantics for database systems.

Open World Assumption (**OWA**)

- Potential incomplete knowledge.
- (*) does not hold.
- Typical semantics for logic-based systems (including OWL).

Name Assumptions

Unique Name Assumption (UNA)

- Different names **always** denote different things.
 - E.g., $a^{\mathcal{I}} \neq b^{\mathcal{I}}$.
 - common in relational databases.

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Non-unique Name Assumption (NUNA)

- Different names need not denote different things. As in OWL.
 - dbpedia: $Person^{\mathcal{I}} = foaf: Person^{\mathcal{I}}$.
 - wikidata:ernesto $^{\mathcal{I}}$ = city:ernesto $^{\mathcal{I}}$

Name Assumptions

Unique Name Assumption (UNA)

- Different names always denote different things.
 - E.g., $a^{\mathcal{I}} \neq b^{\mathcal{I}}$.
 - common in relational databases.

Non-unique Name Assumption (NUNA)

- Different names need not denote different things. As in OWL.
 - dbpedia: $Person^{\mathcal{I}} = foaf: Person^{\mathcal{I}}$.
 - wikidata: ernesto $^{\mathcal{I}}$ = city: ernesto $^{\mathcal{I}}$

Equal names (e.g., URIs) always denote the same "thing".

- E.g., cannot have city:ernesto^{\mathcal{I}} \neq city:ernesto^{\mathcal{I}}.

Necessary conditions and primitive classes

Hawaiian pizza **implies** having pineapple as ingredient (among others); but not the other way round.



Sufficient conditions and defined classes

Meat pizza **implies** having meat as ingredient (and being pizza).

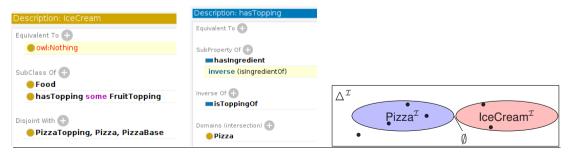
A pizza with meat as ingredient **implies** being a meat pizza.

Hawaiian pizzas have ham as ingredient and thus they are meat pizzas.



Detecting modelling errors

- Ice cream implies having fruit as topping
- Ice cream is disjoint with Pizza
- The domain of has topping is pizza, that is, having any topping implies being a pizza.
- Domain is a type of <u>sufficient condition</u>, global scope for the property.



Common mistakes: part-of VS subclass-of (i)

City subClassOf isLocatedIn some Country

isLocatedIn

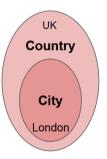
Castellon

City

Country

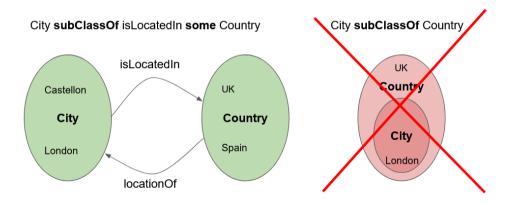
Spain

City subClassOf Country



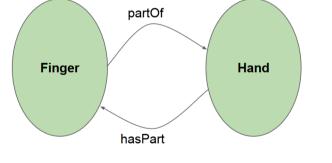
locationOf

Common mistakes: part-of VS subclass-of (i)

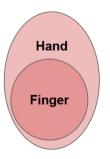


Common mistakes: part-of VS subclass-of (ii)

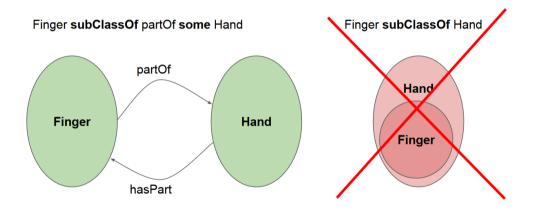
Finger subClassOf partOf some Hand



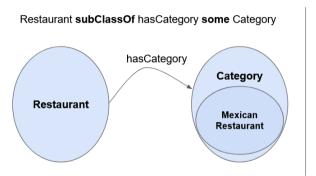
Finger subClassOf Hand



Common mistakes: part-of VS subclass-of (ii)



Common mistakes: part-of VS subclass-of (iii)

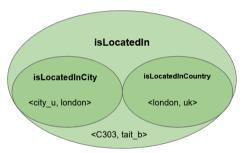


Mexican_Restaurant subClassOf
Restaurant

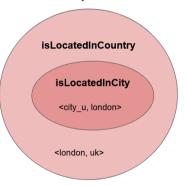


Common mistakes: property hierarchy

isLocatedInCity **subPropertyOf** isLocatedIn isLocatedInCountry **subPropertyOf** isLocatedIn

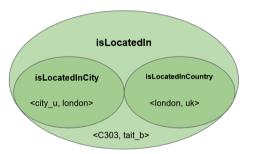


isLocatedInCity **subPropertyOf** isLocatedinCountry

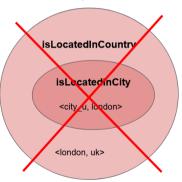


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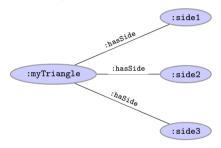


isLocatedInCity **subPropertyOf** isLocatedinCountry



OWL 2 and Open World Assumption

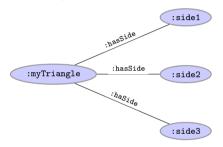
- :Triangle EquivalentTo :hasSide exactly 3 :Side



- is :myTriangle a :Triangle?

OWL 2 and Open World Assumption

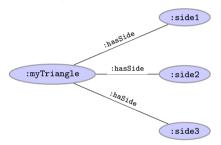
- :Triangle EquivalentTo :hasSide exactly 3 :Side



- is :myTriangle a :Triangle? I don't know because of OWA and NUNA.

OWL 2 and Open World Assumption

- :Triangle EquivalentTo :hasSide exactly 3 :Side



- is :myTriangle a :Triangle? I don't know because of OWA and NUNA.
- Solution: deductive reasoning complemented with SPARQL queries (in this case with aggregates) → SPARQL assumes a CWA.

Graph Database Solutions

How to store Graph models?

- Relational model
 - Single table with 3 columns (source, edge, target)
 - Property tables (one table per type of entity, e.g., Person, Module)
 - Binary tables (one table per relationship, e.g., source, target)

M. Wylot and others. RDF Data Storage and Query Processing Schemes. ACM Computing Surveys 2018

How to store Graph models?

Relational model

Session 2. June, 2024

- Single table with 3 columns (source, edge, target)
- Property tables (one table per type of entity, e.g., Person, Module)
- Binary tables (one table per relationship, e.g., source, target)
- Graph-based databases (NoSQL)

M. Wylot and others. RDF Data Storage and Query Processing Schemes. ACM Computing Surveys 2018

Graph database solutions

- Scale to large Knowledge Graphs.
- Sophisticated indexing structures.
- Optimised reasoning.
- Fast query performance.
- Server solution in production.

State-of-the-art solutions

Dimensions:

- Free version.
- Compliance with Semantic Web standards.
- Reasoning capabilities.
- In-memory or In-disk.
- Documentation and installation requirements.
- Additional features.

A Survey of RDF Stores & SPARQL Engines for Querying Knowledge Graphs. arXiv:2102.13027 2021 (Appendix A)

Semantic Web standards

- The World Wide Web Consortium (W3C) is an international community that develops open standards to ensure the long-term growth of the Web: https://www.w3.org/
- On the Web and beyond.

– Why standards?

- broader industry (and academic) agreement,
- interoperability across organizations and applications,
- avoids vendor lock-in of a particular (exchange or query) format.

Apache Jena TDB

- Free solution.
- Provides a native (in-disk) RDF store.
- In combination with Jena Fuseki to provide SPARQL Endpoint support.
- Supports reasoning as in Jena, but not direct support for OWL 2 nor the OWL 2 profiles.

https://jena.apache.org/documentation/tdb/

OpenLink Virtuoso

- Provides the SPARQL endpoint for DBpedia.
- Open source and commercial versions.
- Object-oriented database model.
- ✓ Native graph model storage provider for Jena and RDF4J.
- Custom inference rules. Partial support for OWL 2.

https://virtuoso.openlinksw.com/

http://vos.openlinksw.com/owiki/wiki/VOS

Blazegraph

- ✓ Provides the SPARQL Endpoint for Wikidata.
- Free and open source.
- Both in-memory and disk-oriented storage.
- Only supports OWL 1 Lite reasoning.
- Blazegraph team now working for Amazon.

https://blazegraph.com/

AllegroGraph

- Free and commercial licenses.
- Support for OWL 2 RL materialization.
- Client interface in several languages.
- Can be used to query both documents and graph data (via SPARQL).

https://allegrograph.com/

Neo4j

- Open source graph database.
- Based on the Property Graph Model.
- Cypher as graph query language (no native SPARQL support).
- Support via a plugin for RDF, RDFS and OWL vocabularies.
- Basic inferencing support.
- Support for Analytics.
- Interfaces in many languages.

https://neo4i.com/

GraphDB (formerly OWLIM)

- Free and commercial versions.
- Very easy to install and use.
- ✓ Powerful reasoning features: including OWL 2 QL and RL profiles.
- Supports SHACL validation.
- Includes text indexing via lucene.
- Powered the early Linked Data services at the BBC.

https://www.ontotext.com/products/graphdb/

RDFox

- Commercial system. Free academic license on request.
- Support for materialization-based datalog reasoning (including OWL 2 RL and SWRL rules).
- Supports SHACL validation.
- In-memory RDF engine.
- ✓ Access via Java API or remotely via REST API or SPARQL Endpoint.
- Limitation on the size of the memory.

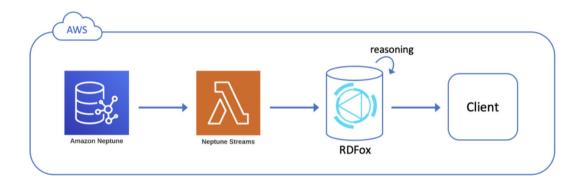
https://www.oxfordsemantic.tech/product

Amazon Neptune

- Cloud-based only solution.
- Blazegraph is now part of Amazon Neptune.
- On-Demand pricing.
- Native inferencing is not yet supported.
- Keep an eye on future development!

https://aws.amazon.com/neptune/

Amazon Neptune + RDFox



Amazon Neptune and RDFox: https://aws.amazon.com/blogs/database/use-semantic-reasoning-to-infer-new-facts-from-your-rdf-graph-by-integrating-rdfox-with-amazon-neptune/

Graph database/Triplestore benchmarking

Oracle Database 12c: 1.08 Trillion triples

AnzoGraph DB: 1.06 Trillion triples

AllegroGraph: 1.0 Trillion triples

Virtuoso: 94.2 Billion Triples

Stardog: 50 Billion triples

- **RDFox**: 19.47 Billion triples

– GraphDB: 17 Billion triples

Apache Jena TBD: 16.7 billion triples.

Numbers may not be up-to-date: https://www.w3.org/wiki/LargeTripleStores https://medium.com/wallscope/comparison-of-linked-data-triplestores-a-new-contender-c62ae04901d3 https://medium.com/wallscope/comparing-linked-data-triplestores-ebfac8c3ad4f

Laboratory: Hands-on SPARQL

SPARQL: local and remote KG access

