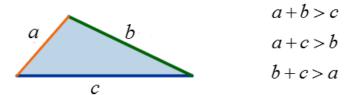
#### Triangle Inequality Theorem

Jonathan R. Bacolod

Sauyo High School

# What is the Triangle Inequality Theorem?

The sum of the lengths of any two sides of a triangle is greater than the length of the third side.



Write *Yes* if the given measures can form a triangle or *No* if not.

1. 8, 14, 9

$$8 + 14 > 9$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$8 + 14 > 9$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$8 + 14 > 9$$

$$14 + 9 > 8$$

$$8 + 14 > 9$$

$$14 + 9 > 8$$

$$8 + 14 > 9$$
  
 $14 + 9 > 8$   
 $8 + 9 > 14$ 

$$8 + 14 > 9$$
 True  $14 + 9 > 8$  True  $8 + 9 > 14$  True

Write *Yes* if the given measures can form a triangle or *No* if not.

$$8 + 14 > 9$$
 True  $14 + 9 > 8$  True  $8 + 9 > 14$  True

Yes

Write *Yes* if the given measures can form a triangle or *No* if not.

2. 3, 6, 2

$$3 + 6 > 2$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$3 + 6 > 2$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$3 + 6 > 2$$

$$6 + 2 > 3$$

$$3+6>2$$
 True  $6+2>3$  True

Write *Yes* if the given measures can form a triangle or *No* if not.

$$3 + 6 > 2$$

$$6 + 2 > 3$$

$$3 + 2 > 6$$

True

3 + 6 > 2	True
6 + 2 > 3	True
3 + 2 > 6	False

Write *Yes* if the given measures can form a triangle or *No* if not.

$$3+6>2$$
 True  $6+2>3$  True  $3+2>6$  False

No

Write *Yes* if the given measures can form a triangle or *No* if not.

3. 8, 2, 8

$$8 + 2 > 8$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$8 + 2 > 8$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$8 + 2 > 8$$

$$2 + 8 > 8$$

$$\begin{array}{ll} 8+2>8 & \text{True} \\ 2+8>8 & \text{True} \end{array}$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$8 + 2 > 8$$

$$2 + 8 > 8$$

$$8 + 8 > 2$$

True

$$8+2>8$$
 True  $2+8>8$  True  $8+8>2$  True

Write *Yes* if the given measures can form a triangle or *No* if not.

3. 8, 2, 8

$$8+2>8$$
 True  $2+8>8$  True  $8+8>2$  True

Yes

Write *Yes* if the given measures can form a triangle or *No* if not.

4. 6, 5, 9

$$6 + 5 > 9$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6 + 5 > 9$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6 + 5 > 9$$

$$5 + 9 > 6$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6 + 5 > 9$$

$$5 + 9 > 6$$

True

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6 + 5 > 9$$

$$5 + 9 > 6$$

$$6 + 9 > 5$$

True

$$6+5>9$$
 True  $5+9>6$  True  $6+9>5$  True

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6+5>9$$
 True  $5+9>6$  True  $6+9>5$  True

Yes

Write *Yes* if the given measures can form a triangle or *No* if not.

5. 1, 13, 13

Write *Yes* if the given measures can form a triangle or *No* if not.

5. 1, 13, 13

$$1 + 13 > 13$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$1 + 13 > 13$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$1 + 13 > 13$$
  
 $13 + 13 > 1$ 

$$1 + 13 > 13$$
  
 $13 + 13 > 1$ 

Write *Yes* if the given measures can form a triangle or *No* if not.

$$1 + 13 > 13$$
  
 $13 + 13 > 1$   
 $1 + 13 > 13$ 

True True

$$1 + 13 > 13$$
 True  $13 + 13 > 1$  True  $1 + 13 > 13$  True

Write *Yes* if the given measures can form a triangle or *No* if not.

$$1 + 13 > 13$$
 True  $13 + 13 > 1$  True  $1 + 13 > 13$  True

Yes

Write *Yes* if the given measures can form a triangle or *No* if not.

6. 4, 6, 10

$$4 + 6 > 10$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$4 + 6 > 10$$

**False** 

Write *Yes* if the given measures can form a triangle or *No* if not.

$$4 + 6 > 10$$

$$6 + 10 > 4$$

**False** 

Write *Yes* if the given measures can form a triangle or *No* if not.

$$4 + 6 > 10$$

$$6 + 10 > 4$$

False

Write *Yes* if the given measures can form a triangle or *No* if not.

$$4 + 6 > 10$$

$$6 + 10 > 4$$

$$4 + 10 > 6$$

False

$$4+6>10$$
 False  $6+10>4$  True  $4+10>6$  True

Write *Yes* if the given measures can form a triangle or *No* if not.

$$4+6>10$$
 False  $6+10>4$  True  $4+10>6$  True

No

Write *Yes* if the given measures can form a triangle or *No* if not.

7. 6, 7, 9

$$6 + 7 > 9$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6 + 7 > 9$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6 + 7 > 9$$

$$7 + 9 > 6$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6 + 7 > 9$$

$$7 + 9 > 6$$

True

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6 + 7 > 9$$

$$7 + 9 > 6$$

$$6 + 9 > 7$$

True

$$6+7>9$$
 True  $7+9>6$  True  $6+9>7$  True

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6+7>9$$
 True  $7+9>6$  True  $6+9>7$  True

Yes

Write *Yes* if the given measures can form a triangle or *No* if not.

8. 4, 7, 12

$$4 + 7 > 12$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$4 + 7 > 12$$

**False** 

Write *Yes* if the given measures can form a triangle or *No* if not.

$$4 + 7 > 12$$

$$7 + 12 > 4$$

**False** 

Write *Yes* if the given measures can form a triangle or *No* if not.

$$4+7 > 12$$
  
 $7+12 > 4$ 

False True

Write *Yes* if the given measures can form a triangle or *No* if not.

$$4+7 > 12$$

$$7 + 12 > 4$$

$$4 + 12 > 7$$

False

$$4+7 > 12$$
 False  $7+12 > 4$  True  $4+12 > 7$  True

Write *Yes* if the given measures can form a triangle or *No* if not.

$$4+7 > 12$$
 False  $7+12 > 4$  True  $4+12 > 7$ 

No

Write *Yes* if the given measures can form a triangle or *No* if not.

9. 6, 15, 9

Write *Yes* if the given measures can form a triangle or *No* if not.

9. 6, 15, 9

$$6 + 15 > 9$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6 + 15 > 9$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6 + 15 > 9$$

$$15 + 9 > 6$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6 + 15 > 9$$

$$15 + 9 > 6$$

True

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6 + 15 > 9$$
  
 $15 + 9 > 6$ 

$$6 + 9 > 15$$

True

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6+15>9$$
 True  $15+9>6$  True  $6+9>15$  False

Write *Yes* if the given measures can form a triangle or *No* if not.

$$6+15>9$$
 True  $15+9>6$  True  $6+9>15$  False

No

Write *Yes* if the given measures can form a triangle or *No* if not.

10. 12, 11, 9

Write *Yes* if the given measures can form a triangle or *No* if not.

$$12 + 11 > 9$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$12 + 11 > 9$$

Write *Yes* if the given measures can form a triangle or *No* if not.

$$12 + 11 > 9$$
  
 $11 + 9 > 12$ 

Write *Yes* if the given measures can form a triangle or *No* if not.

$$12 + 11 > 9$$
  
 $11 + 9 > 12$ 

Write *Yes* if the given measures can form a triangle or *No* if not.

$$12 + 11 > 9$$
  
 $11 + 9 > 12$ 

$$12 + 9 > 11$$

True

Write *Yes* if the given measures can form a triangle or *No* if not.

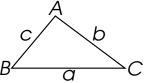
$$12 + 11 > 9$$
 True  $11 + 9 > 12$  True  $12 + 9 > 11$  True

Write *Yes* if the given measures can form a triangle or *No* if not.

$$12 + 11 > 9$$
 True  $11 + 9 > 12$  True  $12 + 9 > 11$  True

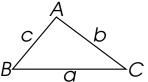
Yes

1. 
$$a = 5, b = 9$$



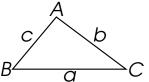
1. 
$$a = 5, b = 9$$

$$a+b>c$$



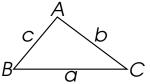
1. 
$$a = 5, b = 9$$

$$a+b>c$$
  
 $5+9>c$ 



1. 
$$a = 5, b = 9$$

$$a + b > c$$
  
 $5 + 9 > c$   
 $14 > c$ 



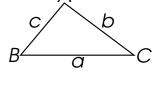
1. 
$$a = 5, b = 9$$

$$a+b>c$$
  $b+c>a$   
 $5+9>c$   
 $14>c$ 



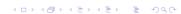
1. 
$$a = 5, b = 9$$

$$a+b>c$$
  $b+c>a$   
 $5+9>c$   $9+c>5$   
 $14>c$ 



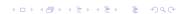
1. 
$$a = 5, b = 9$$

$$a+b>c$$
  $b+c>a$   
 $5+9>c$   $9+c>5$   
 $14>c$   $9-9+c>5-9$ 



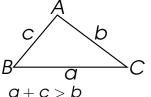
1. 
$$a = 5, b = 9$$

$$a+b>c$$
  $b+c>a$   
 $5+9>c$   $9+c>5$   
 $14>c$   $9-9+c>5-9$   
 $c>-4$ 



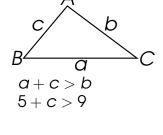
1. 
$$a = 5, b = 9$$

$$a+b>c$$
  $b+c>a$   
 $5+9>c$   $9+c>5$   
 $14>c$   $9-9+c>5-9$   
 $c>-4$ 



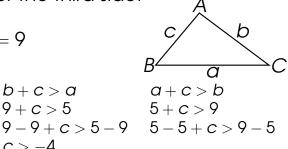
1. 
$$a = 5, b = 9$$

$$a+b>c$$
  $b+c>a$   
 $5+9>c$   $9+c>5$   
 $14>c$   $9-9+c>5-9$   
 $c>-4$ 



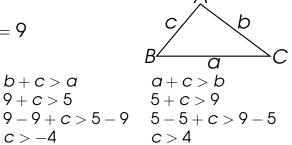
1. 
$$a = 5, b = 9$$

$$a+b>c$$
  $b+c>a$   
 $5+9>c$   $9+c>5$   
 $14>c$   $9-9+c>5-9$   
 $c>-4$ 



1. 
$$a = 5, b = 9$$

$$a+b>c$$
  $b+c>a$   
 $5+9>c$   $9+c>5$   
 $14>c$   $9-9+c>5-9$   
 $c>-4$ 



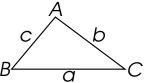
1. 
$$a = 5, b = 9$$

$$a+b>c$$
  $b+c>a$   
 $5+9>c$   $9+c>5$   
 $14>c$   $9-9+c>5-9$   
 $c>-4$ 

$$\therefore 4 < c < 14$$

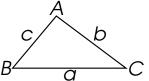


2. 
$$a = 6, c = 10$$



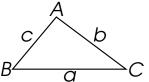
2. 
$$a = 6, c = 10$$

$$a+b>c$$



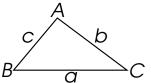
2. 
$$a = 6, c = 10$$

$$a + b > c$$
  
 $6 + b > 10$ 



2. 
$$a = 6, c = 10$$

$$a+b>c$$
  
 $6+b>10$   
 $6-6+b>10-6$ 



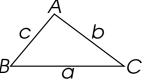
2. 
$$a = 6, c = 10$$

$$a+b>c$$
  
 $6+b>10$   
 $6-6+b>10-6$   
 $b>4$ 



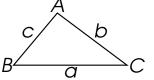
2. 
$$a = 6, c = 10$$

$$a+b>c$$
  
 $6+b>10$   
 $6-6+b>10-6$   
 $b>4$ 



2. 
$$a = 6, c = 10$$

$$a+b>c$$
  $b+c>a$   
 $6+b>10$   $b+10>6$   
 $6-6+b>10-6$   
 $b>4$ 



2. 
$$a = 6, c = 10$$

$$a+b>c$$
  $b+c>a$   
 $6+b>10$   $b+10>6$   
 $6-6+b>10-6$   $b+10-10>6-10$   
 $b>4$ 

2. 
$$a = 6, c = 10$$

$$a+b>c$$
  $b+c>a$   
 $6+b>10$   $b+10>6$   
 $6-6+b>10-6$   $b+10-10>6-10$   
 $b>4$   $b>-4$ 

2. 
$$a = 6, c = 10$$

$$a+b>c$$
  $b+c>a$   $a+c>b$   
 $6+b>10$   $b+10>6$   
 $6-6+b>10-6$   $b+10-10>6-10$   
 $b>4$   $b>-4$ 

2. 
$$a = 6, c = 10$$

$$a+b>c$$
  $b+c>a$   $a+c>b$   
 $b+b>10$   $b+10>b$   $b+10>b$   
 $b>4$   $b>-4$   $a+c>b$   
 $b+10>b$ 

2. 
$$a = 6, c = 10$$

$$a+b>c$$
  $b+c>a$   $a+c>b$   
 $b+b>10$   $b+10>b$   $b+10>b$   
 $b-6+b>10-6$   $b+10-10>b-10$   $b>b$   
 $b>4$   $b>-4$ 

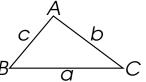
2. 
$$a = 6, c = 10$$

$$a+b>c$$
  $b+c>a$   $a+c>b$   
 $b+b>10$   $b+10>b$   $b+10>b$   
 $b-b>4$   $b>-4$   $a+c>b$ 

$$\therefore 4 < b < 16$$

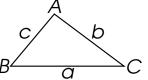


3. 
$$b = 11, c = 8$$



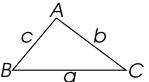
3. 
$$b = 11, c = 8$$

$$a+b>c$$



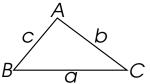
3. 
$$b = 11, c = 8$$

$$a + b > c$$
  
 $a + 11 > 8$ 



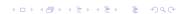
3. 
$$b = 11, c = 8$$

$$a+b>c$$
  
 $a+11>8$   
 $a+11-11>8-11$ 



3. 
$$b = 11, c = 8$$

$$a+b>c$$
  
 $a+11>8$   
 $a+11-11>8-11$   
 $a>-3$ 



3. 
$$b = 11, c = 8$$

$$a + b > c$$
  
 $a + 11 > 8$   
 $a + 11 - 11 > 8 - 11$   
 $a > -3$ 

$$B \xrightarrow{C} B$$

$$b + c > a$$

3. 
$$b = 11, c = 8$$

$$a+b>c$$
  
 $a+11>8$   
 $a+11-11>8-11$   
 $a>-3$ 

$$b + c > a$$
  
11 + 8 >  $a$ 

3. 
$$b = 11, c = 8$$

$$a+b>c$$
  $b+c>a$   
 $a+11>8$   $11+8>a$   
 $a+11-11>8-11$   $19>a$   
 $a>-3$ 

3. 
$$b = 11, c = 8$$

$$a+b>c$$
  $b+c>$   $a+11>8$   $11+8$   $a+11-11>8-11 19>a$   $a>-3$ 

$$b+c>a a+c>b$$
  
 $11+8>a$   
 $19>a$ 

3. 
$$b = 11, c = 8$$

$$a+b>c$$
  $b+c>$   $11+8$   $a+11-11>8-11$   $19>a$   $a>-3$ 

$$b+c>a$$
  $a+c>b$   
 $11+8>a$   $a+8>11$   
 $19>a$ 

3. 
$$b = 11, c = 8$$

$$a+b>c$$
  $b+c>c$   $11+8>$   $a+11-11>8-11$   $19>a$   $a>-3$ 

3. 
$$b = 11, c = 8$$

$$a+b>c$$
  $b+c>$   $11+8>$   $11+8>$   $a+11-11>8-11$   $19>a$   $a>-3$ 

3. 
$$b = 11, c = 8$$

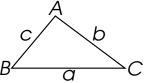
$$a+b>c$$
  $b+c>c$   $11+8>c$   $a+11-11>8-11$   $19>a$   $a>-3$ 

$$B \overline{\hspace{1cm}} C$$
 $b+c>a \quad a+c>b$ 
 $11+8>a \quad a+8>11$ 
 $19>a \quad a+8-8>11-8$ 
 $a>3$ 

$$\therefore 3 < a < 19$$

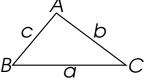


4. 
$$a = 3, b = 13$$



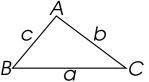
4. 
$$a = 3, b = 13$$

$$a+b>c$$



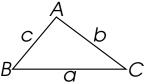
4. 
$$a = 3, b = 13$$

$$a + b > c$$
  
3 + 13 > c



4. 
$$a = 3, b = 13$$

$$a + b > c$$
  
3 + 13 > c  
16 > c



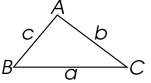
4. 
$$a = 3, b = 13$$

$$a+b>c$$
  $b+c>a$   
 $3+13>c$   
 $16>c$ 



4. 
$$a = 3, b = 13$$

$$a+b>c$$
  $b+c>a$   
 $3+13>c$   $13+c>3$   
 $16>c$ 



4. 
$$a = 3, b = 13$$

$$a+b>c$$
  $b+c>a$   
 $3+13>c$   $13+c>3$   
 $16>c$   $13-13+c>3-13$ 

4. 
$$a = 3, b = 13$$

$$a+b>c$$
  $b+c>a$   
 $3+13>c$   $13+c>3$   
 $16>c$   $13-13+c>3-13$   
 $c>-10$ 

Two sides of  $\triangle ABC$  have the following measures. Find the range of possible measures for the third side.

4. 
$$a = 3, b = 13$$

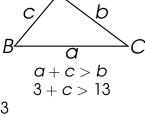
$$a+b>c$$
  $b+c>a$   
 $3+13>c$   $13+c>3$   
 $16>c$   $13-13+c>3-13$   
 $c>-10$ 



a+c>b

4. 
$$a = 3, b = 13$$

$$a+b>c$$
  $b+c>a$   
 $3+13>c$   $13+c>3$   
 $16>c$   $13-13+c>3-13$   
 $c>-10$ 



4. 
$$a = 3, b = 13$$

$$a+b>c$$
  $b+c>a$   $a+c>b$   
 $3+13>c$   $13+c>3$   $3+c>13$   
 $16>c$   $13-13+c>3-13$   $3-3+c>13-3$   
 $c>-10$ 

$$\begin{array}{c|c}
 & a \\
 & a + c > b \\
 & 3 + c > 13 \\
 & 3 - 3 + c > 13 - 3
\end{array}$$

4. 
$$a = 3, b = 13$$

$$a+b>c$$
  $b+c>a$   $a+c>b$   
 $3+13>c$   $13+c>3$   $3+c>13$   
 $16>c$   $13-13+c>3-13$   $3-3+c>13-3$   
 $c>-10$   $c>10$ 

4. 
$$a = 3, b = 13$$

$$a+b>c$$
  $b+c>a$   $a+c>b$   
 $3+13>c$   $13+c>3$   $3+c>13$   
 $16>c$   $13-13+c>3-13$   $3-3+c>13-3$   
 $c>-10$   $c>10$ 

$$\therefore 10 < c < 16$$



# Thank you for attending the virtual class.