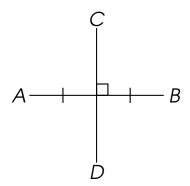
Applying Triangle Congruence in Constructing Perpendicular Lines

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What is a Perpendicular Bisector?

The line drawn perpendicular through the midpoint of a given line segment.



What You Need

1. Compass



What You Need

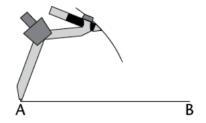
- 1. Compass
- 2. Ruler



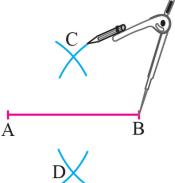
1. Draw the line segment AB.



2. Place the compass on one endpoint of the line segment (point A). Draw an arc above and below the line.

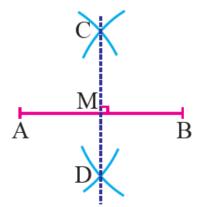


3. Without changing the compass width, place the compass on point B. Draw an arc above and below the line so that the arcs cross the first two.



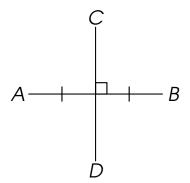


4. Use a ruler to join the points where the arcs intersect. This line segment (*CD*) is the bisector of *AB*.



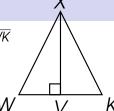
What is the Perpendicular Bisector Theorem?

If a point is on the perpendicular bisector of a segment, then it is equidistant from the segment's endpoints.



Given: $\overline{\textit{XV}}$ is a perpendicular bisector of $\overline{\textit{WK}}$

Prove: $\overline{\mathit{WX}} \cong \overline{\mathit{KX}}$



Given: $\overline{\textit{XV}}$ is a perpendicular bisector of $\overline{\textit{WK}}$

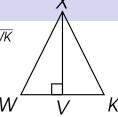
Prove: $\overline{WX} \cong \overline{KX}$

Proof:

Statements Reasons

Given: $\overline{\mathit{XV}}$ is a perpendicular bisector of $\overline{\mathit{WK}}$

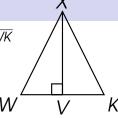
Prove: $\overline{WX} \cong \overline{KX}$



Statements	Reasons
1. \overline{XV} is a perpendicular bisector of \overline{WK}	1. Given

Given: $\overline{\mathit{XV}}$ is a perpendicular bisector of $\overline{\mathit{WK}}$

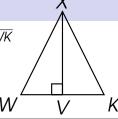
Prove: $\overline{WX} \cong \overline{KX}$



Statements	Reasons
1. XV is a perpendicular bisector of WK	1. Given
2. $\angle XVW$, $\angle XVK$ are right angles, $\overline{WV} \cong \overline{KV}$	2. Def. of perpendicular bisector

Given: $\overline{\textit{XV}}$ is a perpendicular bisector of $\overline{\textit{WK}}$

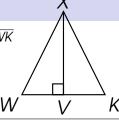
Prove: $\overline{WX} \cong \overline{KX}$



Statements	Reasons
1. \overline{XV} is a perpendicular bisector of \overline{WK}	1. Given
2. $\angle XVW$, $\angle XVK$ are right angles, $\overline{WV} \cong \overline{KV}$	2. Def. of perpendicular bisector
3. $m \angle XVW = 90^{\circ}, m \angle XVK = 90^{\circ}$	3. Def. of Right $\angle s$

Given: $\overline{\mathit{XV}}$ is a perpendicular bisector of $\overline{\mathit{WK}}$

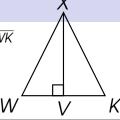
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1. \overline{XV} is a perpendicular bisector of \overline{WK}	1. Given
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3. $m \angle XVW = 90^{\circ}, m \angle XVK = 90^{\circ}$	3. Def. of Right ∠s
$4. \ \angle XVW \cong \angle XVK$	4. Def. of Cong. ∠s

Given: $\overline{\mathit{XV}}$ is a perpendicular bisector of $\overline{\mathit{WK}}$

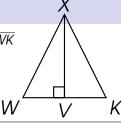
Prove: $\overline{WX} \cong \overline{KX}$



Statements	Reasons
1. \overline{XV} is a perpendicular bisector of \overline{WK}	1. Given
2. $\angle XVW$, $\angle XVK$ are right angles, $\overline{WV} \cong \overline{KV}$	2. Def. of perpendicular bisector
3. <i>m∠XVW</i> = 90°, <i>m∠XVK</i> = 90°	3. Def. of Right $\angle s$
4. ∠XVW ≅ ∠XVK	4. Def. of Cong. ∠s
$5. \ \overline{XV} \cong \overline{XV}$	5. Reflexive Prop.

Given: \overline{XV} is a perpendicular bisector of \overline{WK}

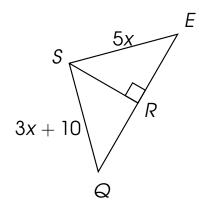
Prove: $\overline{WX} \cong \overline{KX}$



Statements	Reasons
1. \overline{XV} is a perpendicular bisector of \overline{WK}	1. Given
2. ∠XVW,∠XVK are right	2. Def. of
angles, $\overline{WV} \cong \overline{KV}$	perpendicular
	bisector
3. <i>m∠XVW</i> = 90°, <i>m∠XVK</i> = 90°	3. Def. of Right $\angle s$
4. ∠XVW ≅ ∠XVK	4. Def. of Cong. ∠s
$5. \ \overline{XV} \cong \overline{XV}$	5. Reflexive Prop.
6. $\triangle XVW \cong \triangle XVK$	6. SAS Postulate
	7. Corresponding
7. $\overline{WX} \cong \overline{KX}$	Parts of \cong Triangles
	are ≅ (CPCTC)

Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

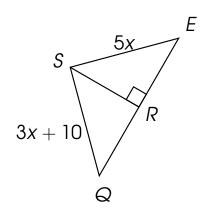
Find: mSQ



Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

Find: mSQ

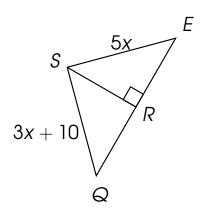
 $\overline{SQ}\cong$



Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

Find: mSQ

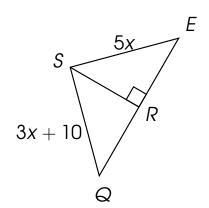
 $\overline{\mathit{SQ}}\cong \overline{\mathit{SE}}$



Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

Find: mSQ

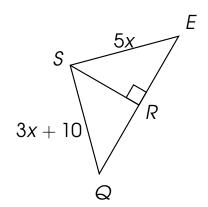
 $\overline{SQ} \cong \overline{SE}$ $m\overline{SQ} = m\overline{SE}$



Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

Find: mSQ

 $\overline{SQ} \cong \overline{SE}$ $m\overline{SQ} = m\overline{SE}$ 3x + 10 = 5x



Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

Find: mSQ

$$\overline{SQ} \cong \overline{SE}$$

$$m\overline{SQ} = m\overline{SE}$$

$$3x + 10 = 5x$$

$$3x - 5x + 10 - 10 = 5x - 5x - 10$$

$$3x + 10$$

Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

Find: mSQ

$$\overline{SQ} \cong \overline{SE} \\
m\overline{SQ} = m\overline{SE} \\
3x + 10 = 5x \\
3x - 5x + 10 - 10 = 5x - 5x - 10 \\
-2x = -10$$

$$3x + 10$$

Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

Find: $m\overline{SQ}$

$$\overline{SQ} \cong \overline{SE}$$

$$m\overline{SQ} = m\overline{SE}$$

$$3x + 10 = 5x$$

$$3x - 5x + 10 - 10 = 5x - 5x - 10$$

$$-2x = -10$$

$$\frac{-2x}{-2} = \frac{-10}{-2}$$

$$3x + 10$$

Given: \overline{SR} is a perpendicular bisector of \overline{EQ} Find: \overline{mSQ}

$$\overline{SQ} \cong \overline{SE}$$

$$m\overline{SQ} = m\overline{SE}$$

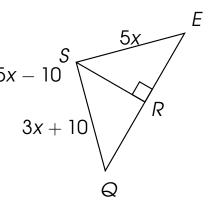
$$3x + 10 = 5x$$

$$3x - 5x + 10 - 10 = 5x - 5x - 10$$

$$-2x = -10$$

$$\frac{-2x}{-2} = \frac{-10}{-2}$$

$$x = 5$$



Given: \overline{SR} is a perpendicular bisector of \overline{EQ} Find: \overline{mSQ}

$$\overline{SQ} \cong \overline{SE}$$

$$m\overline{SQ} = m\overline{SE}$$

$$3x + 10 = 5x$$

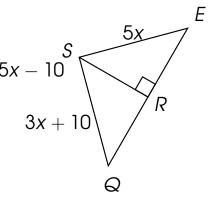
$$3x - 5x + 10 - 10 = 5x - 5x - 10$$

$$-2x = -10$$

$$\frac{-2x}{-2} = \frac{-10}{-2}$$

$$x = 5$$

$$m\overline{SQ} = 3x + 10$$



Given: \overline{SR} is a perpendicular bisector of \overline{EQ} Find: \overline{mSQ}

$$\overline{SQ} \cong \overline{SE}$$

$$m\overline{SQ} = m\overline{SE}$$

$$3x + 10 = 5x$$

$$3x - 5x + 10 - 10 = 5x - 5x - 10$$

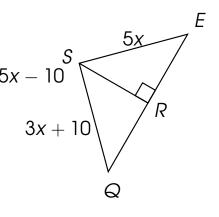
$$-2x = -10$$

$$\frac{-2x}{-2} = \frac{-10}{-2}$$

$$3x + 3x + 3x - 5x - 10$$

$$m\overline{SQ} = 3x + 10$$
$$m\overline{SQ} = 3(5) + 10$$

x = 5



 $mS\overline{Q} = 25$ units

Given: SR is a perpendicular bisector of EQ Find: mSQ

$$\overline{SQ} \cong \overline{SE}$$

$$m\overline{SQ} = m\overline{SE}$$

$$3x + 10 = 5x$$

$$3x - 5x + 10 - 10 = 5x - 5x - 10$$

$$-2x = -10$$

$$-2x = -10$$

$$-2 = -10$$

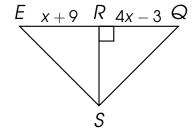
$$x = 5$$

$$m\overline{SQ} = 3x + 10$$

$$m\overline{SQ} = 3(5) + 10$$

Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

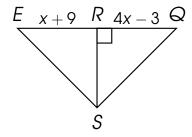
Find: $m\overline{ER}$



Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

Find: $m\overline{ER}$

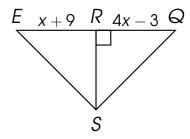
 $\overline{\mathit{ER}}\cong$



Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

Find: mER

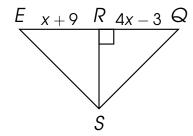
 $\overline{\it ER}\cong \overline{\it QR}$



Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

Find: $m\overline{ER}$

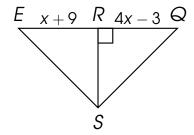
 $\overline{ER} \cong \overline{QR}$ $\overline{mER} = \overline{mQR}$



Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

Find: mER

$$\overline{ER} \cong \overline{QR}$$
 $m\overline{ER} = m\overline{QR}$
 $x + 9 = 4x - 3$

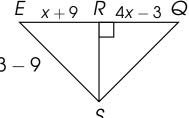


Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

Find: mER

$$\overline{ER} \cong \overline{QR}$$
 $m\overline{ER} = m\overline{QR}$
 $x + 9 = 4x - 3$

$$x - 4x + 9 - 9 = 4x - 4x - 3 - 9$$



Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

Find: $m\overline{ER}$

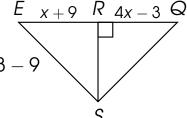
$$\overline{ER} \cong \overline{QR}$$

$$m\overline{ER} = m\overline{QR}$$

$$x + 9 = 4x - 3$$

$$x - 4x + 9 - 9 = 4x - 4x - 3 - 9$$

$$-3x = -12$$



Given: \overline{SR} is a perpendicular bisector of \overline{EQ}

Find: $m\overline{ER}$

$$\overline{ER} \cong \overline{QR}$$

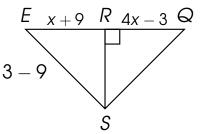
$$m\overline{ER} = m\overline{QR}$$

$$x + 9 = 4x - 3$$

$$x - 4x + 9 - 9 = 4x - 4x - 3 - 9$$

$$-3x = -12$$

$$\frac{-3x}{-3} = \frac{-12}{-3}$$



Given: \overline{SR} is a perpendicular bisector of \overline{EQ} Find: \overline{mFR}

$$\overline{\it ER}\cong \overline{\it QR}$$

$$mER = mQR$$

$$x+9=4x-3$$

$$x - 4x + 9 - 9 = 4x - 4x - 3 - 9$$

$$-3x = -12$$

$$\frac{-3x}{2} = \frac{-12}{2}$$

$$-3 -3$$
 $x = 4$

Given: \overline{SR} is a perpendicular bisector of \overline{EQ} Find: \overline{mFR}

$$\overline{ER} \cong \overline{QR}$$

$$m\overline{ER} = m\overline{QR}$$

$$x + 9 = 4x - 3$$

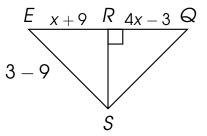
$$x - 4x + 9 - 9 = 4x - 4x - 3 - 9$$

$$-3x = -12$$

$$\frac{-3x}{-3} = \frac{-12}{-3}$$

$$x = 4$$

$$m\overline{ER} = x + 9$$



Given: \overline{SR} is a perpendicular bisector of \overline{EQ} Find: \overline{mFR}

$$\overline{ER} \cong \overline{QR}$$

$$m\overline{ER} = m\overline{QR}$$

$$x + 9 = 4x - 3$$

$$x - 4x + 9 - 9 = 4x - 4x - 3 - 9$$

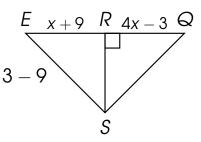
$$-3x = -12$$

$$\frac{-3x}{2} = \frac{-12}{2}$$

$$x = 4$$

$$m\overline{ER} = x + 9$$

 $m\overline{ER} = 4 + 9$



Given: \overline{SR} is a perpendicular bisector of \overline{EQ} Find: \overline{mFR}

$$\overline{ER} \cong \overline{QR}$$

$$m\overline{ER} = m\overline{QR}$$

$$x + 9 = 4x - 3$$

$$x - 4x + 9 - 9 = 4x - 4x - 3 - 9$$

$$-3x = -12$$

$$-3x = -12$$

$$m\overline{ER} = x + 9$$

 $m\overline{ER} = 4 + 9$
 $m\overline{FR} = 13$ units

x=4



Thank you for watching.