Illustrating Linear Functions

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What is a Linear Function?

A linear function is defined by f(x) = mx + b, where m is the slope and b is the y-intercept, $m, b \in \mathbb{R}$ and $m \neq 0$. The degree of the function is one and its graph is a line.

Is the function f defined by f(x) = 2x - 3 a linear function? If yes, determine the slope m and the y-intercept b.

$$f(x) = 2x - 3$$

$$f(x) = 2x - 3$$

in the form f(x) = mx + b

$$f(x) = 2x - 3$$

in the form f(x) = mx + b degree = 1

$$f(x) = 2x - 3$$

in the form f(x) = mx + bdegree = 1 \therefore yes, it is a linear function

$$f(x) = 2x - 3$$

in the form f(x) = mx + bdegree = 1 ... yes, it is a linear function m = 2

$$f(x) = 2x - 3$$

in the form f(x) = mx + bdegree = 1 \therefore yes, it is a linear function m = 2b = -3

Is the function g defined by g(x) = -x a linear function? If yes, determine the slope m and the y-intercept b.

$$g(x) = -x$$

$$g(x) = -x$$

in the form f(x) = mx + b

$$g(x) = -x$$

in the form f(x) = mx + b degree = 1

$$g(x) = -x$$

in the form f(x) = mx + bdegree = 1 \therefore yes, it is a linear function

$$g(x) = -x$$

in the form f(x) = mx + bdegree = 1 ... yes, it is a linear function m = -1

$$g(x) = -x$$

```
in the form f(x) = mx + b
degree = 1
\therefore yes, it is a linear function m = -1
b = 0
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Is the function h defined by $h(x) = x^2 - 2$ a linear function? If yes, determine the slope m and the y-intercept b.

$$h(x)=x^2-2$$

$$h(x) = x^2 - 2$$

not in the form f(x) = mx + b

$$h(x) = x^2 - 2$$

not in the form f(x) = mx + b degree = 2

$$h(x) = x^2 - 2$$

not in the form f(x) = mx + bdegree = 2 \therefore no, it is not a linear function

$$h(x) = -2$$

$$h(x) = -2$$

not in the form f(x) = mx + b

$$h(x) = -2$$

not in the form f(x) = mx + bdegree = 0

$$h(x) = -2$$

not in the form f(x) = mx + bdegree = 0 \therefore no, it is not a linear function

$$f(x) = -3x$$

$$f(x) = -3x$$
 Yes,

$$f(x) = -3x$$
 Yes, $m = -3$,

$$f(x) = -3x$$
 Yes, $m = -3, b = 0$

$$f(x) = -3x$$
 Yes, $m = -3, b = 0$
 $g(x) = -3$

$$f(x) = -3x$$
 Yes, $m = -3, b = 0$
 $g(x) = -3$ No

$$f(x) = -3x$$
 Yes, $m = -3, b = 0$
 $g(x) = -3$ No
 $h(x) = x^2$

$$f(x) = -3x$$
 Yes, $m = -3$, $b = 0$
 $g(x) = -3$ No
 $h(x) = x^2$ No

$$f(x) = -3x$$
 Yes, $m = -3$, $b = 0$
 $g(x) = -3$ No
 $h(x) = x^2$ No
 $f(x) = 2x - 3$

$$f(x) = -3x$$
 Yes, $m = -3, b = 0$
 $g(x) = -3$ No
 $h(x) = x^2$ No
 $f(x) = 2x - 3$ Yes,

$$f(x) = -3x$$
 Yes, $m = -3, b = 0$
 $g(x) = -3$ No
 $h(x) = x^2$ No
 $f(x) = 2x - 3$ Yes, $m = 2$.

$$f(x) = -3x$$
 Yes, $m = -3, b = 0$
 $g(x) = -3$ No
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 $f(x) = 2x - 3$ Yes, $m = 2, b = -3$

$$f(x) = -3x$$
 Yes, $m = -3$, $b = 0$
 $g(x) = -3$ No
 $h(x) = x^2$ No
 $f(x) = 2x - 3$ Yes, $m = 2$, $b = -3$
 $g(x) = -3 + x$

$$f(x) = -3x$$
 Yes, $m = -3, b = 0$
 $g(x) = -3$ No
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 $f(x) = 2x - 3$ Yes, $m = 2, b = -3$
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$$f(x) = -3x$$
 Yes, $m = -3$, $b = 0$
 $g(x) = -3$ No
 $h(x) = x^2$ No
 $f(x) = 2x - 3$ Yes, $m = 2$, $b = -3$
 $g(x) = -3 + x$ Yes, $m = 1$, $b = -3$
 $h(x) = \frac{4}{3}x$

$$f(x) = -3x$$
 Yes, $m = -3, b = 0$
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$$f(x) = -3x$$
 Yes, $m = -3$, $b = 0$
 $g(x) = -3$ No
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 $h(x) = \frac{4}{3}x$ Yes, $m = \frac{4}{3}$

$$f(x) = -3x$$
 Yes, $m = -3, b = 0$
 $g(x) = -3$ No
 $h(x) = x^2$ No
 $f(x) = 2x - 3$ Yes, $m = 2, b = -3$
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$$f(x) = -3x$$
 Yes, $m = -3, b = 0$
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$$f(x) = -3x$$
 Yes, $m = -3$, $b = 0$
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 $h(x) = \frac{4}{3}x$ Yes, $m = \frac{4}{3}$, $b = 0$
 $h(x) = \frac{1}{2}$ No

1. Determine the values of the function at the given values of x. Then determine the coordinates to be plotted.

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- Construct a table of values from the coordinates.

- 1. Determine the values of the function at the given values of x. Then determine the coordinates to be plotted.
- Construct a table of values from the coordinates.
- 3. Plot the coordinates and connect them.

Determine the values of the function f if f(x) = 2x - 1 at x = -3, 0, 2. Interpret the results, determine the ordered pairs, and graph the function f.

Step 1: Determine the values of the function at the given values of x. Then determine the coordinates to be plotted.

$$f(x) = 2x - 1$$
 at $x = -3$

$$f(x) = 2x - 1$$
 at $x = -3$
Linear function $f(x) = 2x - 1$

$$f(x) = 2x - 1$$
 at $x = -3$
Linear function $f(x) = 2x - 1$
Substitute $x = -3$

$$f(x) = 2x - 1$$
 at $x = -3$

$$f(x) = 2x - 1$$

Substitute
$$x = -3$$

$$f(-3) = 2(-3) - 1$$

$$f(x) = 2x - 1$$
 at $x = -3$

$$f(x) = 2x - 1$$

Substitute
$$x = -3$$

$$f(-3) = 2(-3) - 1$$

Simplify

$$f(x) = 2x - 1$$
 at $x = -3$
Linear function $f(x) = 2x - 1$
Substitute $x = -3$ $f(-3) = 2(-3) - 1$
Simplify $f(-3) = -6 - 1$

$$f(x) = 2x - 1$$
 at $x = -3$

$$f(x) = 2x - 1$$

Substitute x = -3

$$f(-3) = 2(-3) - 1$$

Simplify

$$f(-3) = -6 - 1$$

Simplify

$$f(x) = 2x - 1$$
 at $x = -3$

Linear function f(x) = 2x - 1

Substitute x = -3 f(-3) = 2(-3) - 1

Simplify f(-3) = -6 - 1

Simplify f(-3) = -7

$$f(x) = 2x - 1$$
 at $x = -3$

Linear function f(x) = 2x - 1

Substitute x = -3 f(-3) = 2(-3) - 1

Simplify f(-3) = -6 - 1

Simplify f(-3) = -7

 \therefore the value of f at x = -3 is -7 and the ordered pair is (-3, -7)

$$f(x) = 2x - 1$$
 at $x = 0$

$$f(x) = 2x - 1$$
 at $x = 0$
Linear function $f(x) = 2x - 1$

$$f(x) = 2x - 1$$
 at $x = 0$
Linear function $f(x) = 2x - 1$
Substitute $x = 0$

$$f(x) = 2x - 1$$
 at $x = 0$
Linear function $f(x) = 2x - 1$
Substitute $x = 0$ $f(0) = 2(0) - 1$

$$f(x) = 2x - 1$$
 at $x = 0$
Linear function $f(x) = 2x - 1$
Substitute $x = 0$ $f(0) = 2(0) - 1$
Simplify

$$f(x) = 2x - 1$$
 at $x = 0$
Linear function $f(x) = 2x - 1$
Substitute $x = 0$ $f(0) = 2(0) - 1$
Simplify $f(0) = 0 - 1$

$$f(x) = 2x - 1$$
 at $x = 0$

$$f(x) = 2x - 1$$

Substitute x = 0

$$f(0) = 2(0) - 1$$

Simplify

$$f(0) = 0 - 1$$

Simplify

Simplify

f(0) = 0 - 1

$$f(x) = 2x - 1$$
 at $x = 0$
Linear function $f(x) = 2x - 1$
Substitute $x = 0$ $f(0) = 2(0) - 1$

Simplify f(0) = -1

$$f(x) = 2x - 1$$
 at $x = 0$
Linear function $f(x) = 2x - 1$

Substitute
$$x = 0$$
 $f(0) = 2(0) - 1$

Simplify
$$f(0) = 0 - 1$$

Simplify
$$f(0) = -1$$

 \therefore the value of f at x = 0 is -1 and the ordered pair is (0, -1)

$$f(x) = 2x - 1$$
 at $x = 2$

$$f(x) = 2x - 1$$
 at $x = 2$
Linear function $f(x) = 2x - 1$

$$f(x) = 2x - 1$$
 at $x = 2$
Linear function $f(x) = 2x - 1$
Substitute $x = 2$

$$f(x) = 2x - 1$$
 at $x = 2$
Linear function $f(x) = 2x - 1$
Substitute $x = 2$ $f(2) = 2(2) - 1$

$$f(x) = 2x - 1$$
 at $x = 2$
Linear function $f(x) = 2x - 1$
Substitute $x = 2$ $f(2) = 2(2) - 1$
Simplify

$$f(x) = 2x - 1$$
 at $x = 2$
Linear function $f(x) = 2x - 1$
Substitute $x = 2$ $f(2) = 2(2) - 1$
Simplify $f(2) = 4 - 1$

$$f(x) = 2x - 1$$
 at $x = 2$

$$f(x) = 2x - 1$$

Substitute x = 2

$$f(2) = 2(2) - 1$$

Simplify

$$f(2) = 4 - 1$$

Simplify

Simplify

f(2) = 3

$$f(x) = 2x - 1$$
 at $x = 2$
Linear function $f(x) = 2x - 1$
Substitute $x = 2$ $f(2) = 2(2) - 1$
Simplify $f(2) = 4 - 1$

$$f(x) = 2x - 1$$
 at $x = 2$
Linear function $f(x) = 2x - 1$
Substitute $x = 2$ $f(2) = 2(2) - 1$
Simplify $f(2) = 4 - 1$
Simplify $f(2) = 3$

: the value of f at x = 2 is 3 and the ordered pair is (2,3)

Set of ordered pairs: $\{(-3, -7), (0, -1), (2, 3)\}$ Table of values:

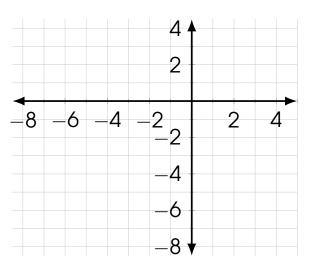
Set of ordered pairs:
$$\{(-3, -7), (0, -1), (2, 3)\}$$

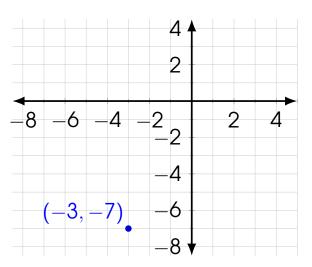
Table of values:

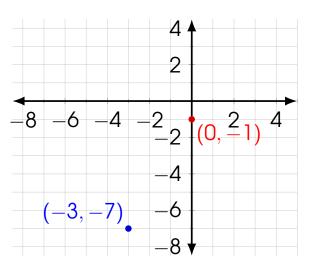
Set of ordered pairs:
$$\{(-3, -7), (0, -1), (2, 3)\}$$

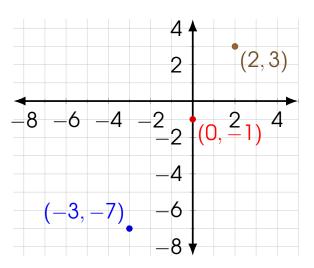
Table of values:

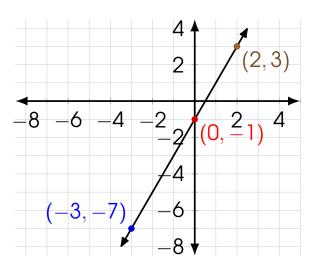
Χ	-3	0	2
f(x)	-7	-1	3











Determine the values of the function f if g(x) = -3x - 4 at x = -2, 0, 1. Interpret the results, determine the ordered pairs, and graph the function f.

$$g(x) = -3x - 4$$
 at $x = -2$

$$g(x) = -3x - 4$$
 at $x = -2$

$$g(x) = -3x - 4$$

$$g(x) = -3x - 4$$
 at $x = -2$

$$g(x) = -3x - 4$$

Substitute x = -2

$$g(x) = -3x - 4$$
 at $x = -2$

$$g(x) = -3x - 4$$

Substitute
$$x = -2$$

$$g(-2) = -3(-2) - 4$$

$$g(x) = -3x - 4$$
 at $x = -2$

Linear function g(x) = -3x - 4Substitute x = -2 g(-2) = -3(-2) - 4Simplify

$$g(x) = -3x - 4$$
 at $x = -2$

Linear function
$$g(x) = -3x - 4$$

Substitute $x = -2$ $g(-2) = -3(-2) - 4$
Simplify $g(-2) = 6 - 4$

$$g(x) = -3x - 4$$
 at $x = -2$

Substitute x = -2

Simplify

Simplify

$$g(x) = -3x - 4$$

$$g(-2) = -3(-2) - 4$$

$$g(-2) = 6 - 4$$

$$g(x) = -3x - 4$$
 at $x = -2$

Linear function
$$g(x) = -3x - 4$$

Substitute $x = -2$ $g(-2) = -3(-2) - 4$
Simplify $g(-2) = 6 - 4$
Simplify $g(-2) = 2$

$$g(x) = -3x - 4$$
 at $x = -2$

Linear function
$$g(x) = -3x - 4$$

Substitute $x = -2$ $g(-2) = -3(-2) - 4$
Simplify $g(-2) = 6 - 4$
Simplify $g(-2) = 2$

∴ the value of g at x = -2 is 2 and the ordered pair is (-2,2)

$$g(x) = -3x - 4$$
 at $x = 0$

$$g(x) = -3x - 4$$
 at $x = 0$
Linear function $g(x) = -3x - 4$

$$g(x) = -3x - 4$$
 at $x = 0$
Linear function $g(x) = -3x - 4$
Substitute $x = 0$

$$g(x) = -3x - 4$$
 at $x = 0$

$$g(x) = -3x - 4$$

Substitute
$$x = 0$$

$$g(0) = -3(0) - 4$$

$$g(x) = -3x - 4$$
 at $x = 0$

$$g(x) = -3x - 4$$

Substitute x = 0

$$g(0) = -3(0) - 4$$

Simplify

$$g(x) = -3x - 4$$
 at $x = 0$

Linear function g(x) = -3x - 4

Substitute x = 0 g(0) = -3(0) - 4

Simplify g(0) = 0 - 4

$$g(x) = -3x - 4$$
 at $x = 0$

$$g(x) = -3x - 4$$

Substitute x = 0

$$g(0) = -3(0) - 4$$

Simplify

$$g(0) = 0 - 4$$

Simplify

$$g(x) = -3x - 4$$
 at $x = 0$

Linear function g(x) = -3x - 4

Substitute x = 0 g(0) = -3(0) - 4

Simplify g(0) = 0 - 4

Simplify g(0) = -4

$$g(x) = -3x - 4$$
 at $x = 0$

Linear function g(x) = -3x - 4

Substitute x = 0 g(0) = -3(0) - 4

Simplify g(0) = 0 - 4

Simplify g(0) = -4

... the value of g at x = 0 is -4 and the ordered pair is (0, -4)

$$g(x) = -3x - 4$$
 at $x = 1$

$$g(x) = -3x - 4$$
 at $x = 1$
Linear function $g(x) = -3x - 4$

$$g(x) = -3x - 4$$
 at $x = 1$
Linear function $g(x) = -3x - 4$
Substitute $x = 1$

$$g(x) = -3x - 4$$
 at $x = 1$
Linear function $g(x) = -3x - 4$
Substitute $x = 1$ $g(1) = -3(1) - 4$

Simplify

$$g(x) = -3x - 4$$
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Linear function $g(x) = -3x - 4$
Substitute $x = 1$ $g(1) = -3(1) - 4$

$$g(x) = -3x - 4$$
 at $x = 1$
Linear function $g(x) = -3x - 4$
Substitute $x = 1$ $g(1) = -3(1) - 4$
Simplify $g(1) = -3 - 4$

$$g(x) = -3x - 4$$
 at $x = 1$

Linear function

$$g(x) = -3x - 4$$

Substitute x = 1

$$g(1) = -3(1) - 4$$

Simplify

$$g(1) = -3 - 4$$

Simplify

$$g(x) = -3x - 4$$
 at $x = 1$

Linear function g(x) = -3x - 4

Substitute x = 1 g(1) = -3(1) - 4

Simplify g(1) = -3 - 4

Simplify g(1) = -7

$$g(x) = -3x - 4$$
 at $x = 1$

Linear function g(x) = -3x - 4

Substitute x = 1 g(1) = -3(1) - 4

Simplify g(1) = -3 - 4

Simplify g(1) = -7

... the value of g at x = 1 is -7 and the ordered pair is (1, -7)

Set of ordered pairs: $\{(-2,2),(0,-4),(1,-7)\}$ Table of values:

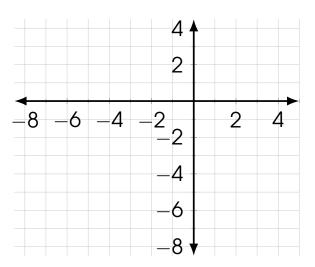
Set of ordered pairs: $\{(-2,2),(0,-4),(1,-7)\}$

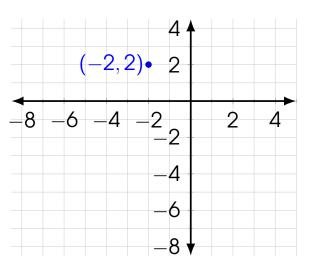
Table of values:

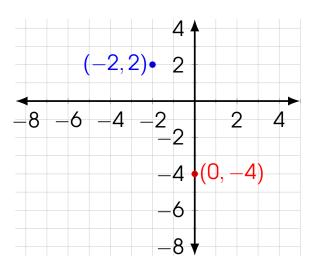
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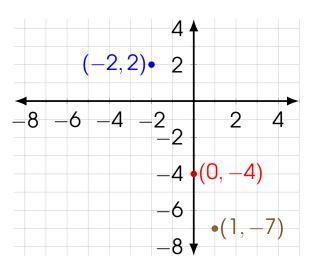
Table of values:

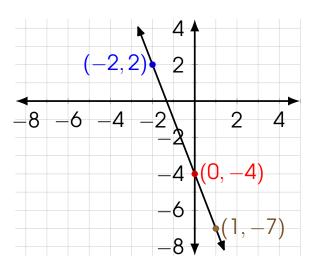
Χ	-2	0	1
f(x)	2	-4	-7











Thank you for watching.