# Probability of an Event

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## What is the Probability of an Event?

If an event E has n(E) equally likely outcomes and its sample space S has n(S) likely outcomes, then the probability of the event E is:

$$P(E) = \frac{\text{number of elements in } E}{\text{number of elements in } S} = \frac{n(E)}{n(S)}$$

$$S = \{HH, HT, TH, TT\}$$

$$S = \{HH, HT, TH, TT\}$$
  
 $E = \{HH\}$ 

$$S = \{HH, HT, TH, TT\}$$
  $n(S) = 4$   
 $E = \{HH\}$ 

$$S = \{HH, HT, TH, TT\}$$
  $n(S) = 4$   
 $E = \{HH\}$   $n(E) = 1$ 

Two coins are tossed. What is the probability of getting two heads?

$$S = \{HH, HT, TH, TT\}$$
  $n(S) = 4$   
 $E = \{HH\}$   $n(E) = 1$ 

P(E)

$$S = \{HH, HT, TH, TT\}$$
  $n(S) = 4$   
 $E = \{HH\}$   $n(E) = 1$   

$$P(E) = \frac{n(E)}{n(S)}$$

$$S = \{HH, HT, TH, TT\}$$
  $n(S) = 4$   
 $E = \{HH\}$   $n(E) = 1$   

$$P(E) = \frac{n(E)}{n(S)}$$

$$P(E)$$

$$S = \{HH, HT, TH, TT\}$$

$$E = \{HH\}$$

$$n(S) = 4$$

$$n(E) = 1$$

$$P(E) = \frac{n(E)}{n(S)}$$

$$P(E) = \frac{1}{4}$$

$$S = \{HH, HT, TH, TT\}$$
  $n(S) = 4$   
 $E = \{HH\}$   $n(E) = 1$   

$$P(E) = \frac{n(E)}{n(S)}$$
  

$$P(E) = \frac{1}{4} \text{ or } 25\%$$

$$S = \{1, 2, 3, 4, 5, 6\}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
 $E = \{2, 3, 5\}$ 

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{2, 3, 5\}$ 

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{2, 3, 5\}$   $n(E) = 3$ 

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{2, 3, 5\}$   $n(E) = 3$   
 $P(E)$ 

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{2, 3, 5\}$   $n(E) = 3$   
 $P(E) = \frac{n(E)}{n(S)}$ 

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{2, 3, 5\}$   $n(E) = 3$   
 $P(E) = \frac{n(E)}{n(S)}$   
 $P(E)$ 

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{2, 3, 5\}$   $n(E) = 3$   
 $P(E) = \frac{n(E)}{n(S)}$   
 $P(E) = \frac{3}{6}$ 

P(E)

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{2, 3, 5\}$   $n(E) = 3$   
 $P(E) = \frac{n(E)}{n(S)}$   
 $P(E) = \frac{3}{6}$ 

A die is rolled. What is the probability of getting a prime number?

n(S) = 6n(E) = 3

$$S = \{1, 2, 3, 4, 5, 6\}$$

$$E = \{2, 3, 5\}$$

$$P(E) = \frac{n(E)}{n(S)}$$

$$P(E) = \frac{3}{6}$$

$$P(E) = \frac{1}{2}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{2, 3, 5\}$   $n(E) = 3$   
 $P(E) = \frac{n(E)}{n(S)}$   
 $P(E) = \frac{3}{6}$   
 $P(E) = \frac{1}{2}$  or 50%

$$S = \{A\heartsuit, \ldots, K\heartsuit, \}$$

$$\mathcal{S} = \{A\heartsuit, \dots, K\heartsuit, A\diamondsuit, \dots, K\diamondsuit, A\clubsuit, \dots, K\clubsuit, \dots$$

$$\mathcal{S} = \{A\heartsuit, \dots, K\heartsuit, A\diamondsuit, \dots, K\diamondsuit, A\clubsuit, \dots, K\clubsuit, A\spadesuit, \dots, K\spadesuit\}$$

$$S = \{A\heartsuit, \dots, K\heartsuit, A\diamondsuit, \dots, K\diamondsuit, A\clubsuit, \dots, K\clubsuit, A\spadesuit, \dots, K\spadesuit\}$$
 $E = \{A\clubsuit, A\spadesuit\}$ 

$$S = \{A\heartsuit, \dots, K\heartsuit, \qquad n(S) = 52$$
  
 $A\diamondsuit, \dots, K\diamondsuit, \qquad A\clubsuit, \dots, K\clubsuit, \qquad A\spadesuit, \dots, K\spadesuit\}$   
 $E = \{A\clubsuit, A\spadesuit\}$ 

$$S = \{A\heartsuit, \dots, K\heartsuit, \qquad n(S) = 52$$
  
 $A\diamondsuit, \dots, K\diamondsuit, \qquad n(E) = 2$   
 $A\clubsuit, \dots, K\clubsuit, \qquad A\spadesuit, \dots, K\spadesuit\}$   
 $E = \{A\clubsuit, A\spadesuit\}$ 

$$S = \{A\heartsuit, \dots, K\heartsuit, \qquad n(S) = 52$$
  
 $A\diamondsuit, \dots, K\diamondsuit, \qquad n(E) = 2$   
 $A\clubsuit, \dots, K\clubsuit, \qquad A\spadesuit, \dots, K\spadesuit\}$   
 $E = \{A\clubsuit, A\spadesuit\}$   
 $P(E)$ 

$$S = \{A\heartsuit, \dots, K\heartsuit, \qquad n(S) = 52$$
  
 $A\diamondsuit, \dots, K\diamondsuit, \qquad n(E) = 2$   
 $A\clubsuit, \dots, K\clubsuit, \qquad A\spadesuit, \dots, K\spadesuit\}$   
 $E = \{A\clubsuit, A\spadesuit\}$   
 $P(E) = \frac{n(E)}{n(S)}$ 

$$S = \{A\heartsuit, \dots, K\heartsuit, \qquad n(S) = 52$$
  
 $A\diamondsuit, \dots, K\diamondsuit, \qquad n(E) = 2$   
 $A\clubsuit, \dots, K\clubsuit, \qquad A\spadesuit, \dots, K\spadesuit\}$   
 $E = \{A\clubsuit, A\spadesuit\}$   
 $P(E) = \frac{n(E)}{n(S)} = \frac{2}{52}$ 

$$S = \{A\heartsuit, \dots, K\heartsuit, \qquad n(S) = 52$$
  
 $A\diamondsuit, \dots, K\diamondsuit, \qquad n(E) = 2$   
 $A\clubsuit, \dots, K\clubsuit, \qquad n(E) = 2$   
 $E = \{A\clubsuit, A\spadesuit\}$   
 $E = \{n(E) = \frac{n(E)}{n(S)} = \frac{2}{52}$   
 $E = \{n(E) = \frac{n(E)}{n(S)} = \frac{2}{52}$ 

A card is drawn from a standard deck of cards. What is the probability of getting a black ace?

$$S = \{A\heartsuit, \dots, K\heartsuit, \qquad n(S \land A\diamondsuit, \dots, K\diamondsuit, \land n(E \land A\clubsuit, \dots, K\clubsuit, \land A\spadesuit, \dots, K\clubsuit\}$$

$$E = \{A\clubsuit, A\spadesuit\}$$

$$P(E) = \frac{n(E)}{n(S)} = \frac{2}{52}$$

$$P(E) = \frac{1}{2}$$

$$n(S) = 52$$
  
 $n(E) = 2$ 

#### What are the Properties of Probability?

1. The probability of an event, P(E), is a number from 0 to 1 which tells how likely the event is to happen.

$$0 \le P(E) \le 1$$

#### What are the Properties of Probability?

Impossible	Unlikely	Even Chance	Likely	Certain
•	•	•	•	•
0	1 4	1/2	3 4	1
0	0.25	0.5	0.75	1
0%	25%	50%	75%	100%

The closer the probability of an event to 1, the more likely the event is to happen and the closer the probability of an event to zero, the less likely it is to happen.

$$S = \{1, 2, 3, 4, 5, 6\}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
 $E = \{2\}$ 

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{2\}$ 

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{2\}$   $n(E) = 1$ 

A die is rolled. What is the probability of getting an even prime number?

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{2\}$   $n(E) = 1$ 

P(E)

$$S = \{1, 2, 3, 4, 5, 6\}$$
 
$$E = \{2\}$$

$$n(S) = 6$$
$$n(E) = 1$$

$$P(E) = \frac{n(E)}{n(S)}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
$$E = \{2\}$$

$$n(S) = 6$$
  
 $n(E) = 1$ 

$$P(E) = \frac{n(E)}{n(S)}$$

$$S = \{1, 2, 3, 4, 5, 6\} \\ E = \{2\}$$

$$n(S) = 6$$
  
 $n(E) = 1$ 

$$P(E) = \frac{n(E)}{n(S)}$$

$$P(E)=\frac{1}{6}$$

A die is rolled. What is the probability of getting an even prime number?

n(S) = 6n(E) = 1

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
 $E = \{2\}$   
 $P(E) = \frac{n(E)}{n(S)}$ 

$$P(E) = \frac{1}{6}$$
 or 0.167

$$S = \{1, 2, 3, 4, 5, 6\}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
 $E = \{1, 2, 3, 4, 5\}$ 

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{1, 2, 3, 4, 5\}$ 

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{1, 2, 3, 4, 5\}$   $n(E) = 5$ 

A die is rolled. What is the probability of getting a number less than 6?

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{1, 2, 3, 4, 5\}$   $n(E) = 5$ 

P(E)

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
 $E = \{1, 2, 3, 4, 5\}$ 

$$n(S) = 6$$
$$n(E) = 5$$

$$P(E) = \frac{n(E)}{n(S)}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
 $E = \{1, 2, 3, 4, 5\}$ 

$$n(S) = 6$$
$$n(E) = 5$$

$$P(E) = \frac{n(E)}{n(S)}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
 $E = \{1, 2, 3, 4, 5\}$ 

$$n(S) = 6$$
$$n(E) = 5$$

$$P(E) = \frac{n(E)}{n(S)}$$

$$P(E)=\frac{5}{6}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$

$$E = \{1, 2, 3, 4, 5\}$$

$$P(E) = \frac{n(E)}{n(S)}$$

$$P(E) = \frac{5}{6} \text{ or } 0.83$$

$$n(S) = 6$$
  
 $n(E) = 5$ 

#### What are the Properties of Probability?

2. The probability of an event that cannot happen is 0.

$$P(\varnothing)=0$$

$$S = \{1, 2, 3, 4, 5, 6\}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
 $E = \{\}$ 

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{\}$ 

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{\}$   $n(E) = 0$ 

A die is rolled. What is the probability of getting a number greater than 6?

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{\}$   $n(E) = 0$ 

P(E)

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
 $E = \{\}$ 

$$n(S) = 6$$
$$n(E) = 0$$

$$P(E) = \frac{n(E)}{n(S)}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{\}$   $n(E) = 0$ 

$$P(E) = \frac{n(E)}{n(S)}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
$$E = \{\}$$

$$n(S) = 6$$
$$n(E) = 0$$

$$P(E) = \frac{n(E)}{n(S)}$$

$$P(E)=\frac{0}{6}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
 $E = \{\}$ 

$$n(S) = 6$$
$$n(E) = 0$$

$$P(E) = \frac{n(E)}{n(S)}$$

$$P(E) = \frac{0}{6} \text{ or } 0$$

#### What are the Properties of Probability?

3. If an event is sure to happen, then the probability is 1.

$$S = \{1, 2, 3, 4, 5, 6\}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
 $E = \{1, 2, 3, 4, 5, 6\}$ 

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
 $E = \{1, 2, 3, 4, 5, 6\}$ 

$$n(S) = 6$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{1, 2, 3, 4, 5, 6\}$   $n(E) = 6$ 

A die is rolled. What is the probability of getting a number greater than 0?

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{1, 2, 3, 4, 5, 6\}$   $n(E) = 6$ 

P(E)

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{1, 2, 3, 4, 5, 6\}$   $n(E) = 6$ 

$$P(E) = \frac{n(E)}{n(S)}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $E = \{1, 2, 3, 4, 5, 6\}$   $n(E) = 6$ 

$$P(E) = \frac{n(E)}{n(S)}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
  
$$E = \{1, 2, 3, 4, 5, 6\}$$

$$n(S) = 6$$
  
 $n(E) = 6$ 

$$P(E) = \frac{n(E)}{n(S)}$$

$$P(E)=\frac{6}{6}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
 
$$E = \{1, 2, 3, 4, 5, 6\}$$

$$n(S) = 6$$
  
 $n(E) = 6$ 

$$P(E) = \frac{n(E)}{n(S)}$$

$$P(E) = \frac{6}{6}$$
 or 1

#### What are the Properties of Probability?

4. The sum of the probabilities of all the outcomes in the sample space is 1.

$$P(H)=\frac{1}{2}$$

$$P(H) = \frac{1}{2}$$

$$P(T) = \frac{1}{2}$$

$$P(H) = \frac{1}{2}$$

$$P(T) = \frac{1}{2}$$

$$P(H) = \frac{1}{2}$$

$$P(T) = \frac{1}{2}$$

$$P(S) = P(H) + P(T)$$

$$P(H) = \frac{1}{2}$$

$$P(T) = \frac{1}{2}$$

$$P(S) = P(H) + P(T)$$

$$P(S)$$

$$P(H) = \frac{1}{2}$$
 $P(T) = \frac{1}{2}$ 
 $P(S) = P(H) + P(T)$ 
 $P(S) = \frac{1}{2} + \frac{1}{2}$ 

$$P(H) = \frac{1}{2}$$

$$P(T) = \frac{1}{2}$$

$$P(S) = P(H) + P(T)$$

$$P(S) = \frac{1}{2} + \frac{1}{2}$$

$$P(H) = \frac{1}{2}$$

$$P(T) = \frac{1}{2}$$

$$P(S) = P(H) + P(T)$$

$$P(S) = \frac{1}{2} + \frac{1}{2}$$

$$P(S) = \frac{2}{2}$$

$$P(H) = \frac{1}{2}$$

$$P(T) = \frac{1}{2}$$

$$P(S) = P(H) + P(T)$$

$$P(S) = \frac{1}{2} + \frac{1}{2}$$

$$P(S) = \frac{2}{2} = 1$$

$$P(1)=\frac{1}{6}$$

$$P(1) = \frac{1}{6}$$

$$P(2) = \frac{1}{6}$$

$$P(1) = \frac{1}{6}$$
  $P(3) = \frac{1}{6}$   $P(2) = \frac{1}{6}$ 

$$P(1) = \frac{1}{6}$$
  $P(3) = \frac{1}{6}$   $P(4) = \frac{1}{6}$ 

$$P(1) = \frac{1}{6}$$
  $P(3) = \frac{1}{6}$   $P(4) = \frac{1}{6}$ 

$$P(5)=\frac{1}{6}$$

$$P(1) = \frac{1}{6}$$

$$P(2) = \frac{1}{6}$$

$$P(3) = \frac{1}{6}$$
  
 $P(4) = \frac{1}{6}$ 

$$P(4) = \frac{1}{6}$$

$$P(5) = \frac{1}{6}$$
  
 $P(6) = \frac{1}{6}$ 

$$P(6) = \frac{1}{6}$$

$$P(1) = \frac{1}{6}$$
 $P(2) = \frac{1}{6}$ 

$$P(3) = \frac{1}{6}$$
 $P(4) = \frac{1}{6}$ 

$$P(5) = \frac{1}{6}$$
  
 $P(6) = \frac{1}{6}$ 

$$P(1) = \frac{1}{6}$$
  $P(3) = \frac{1}{6}$   $P(5) = \frac{1}{6}$   $P(6) = \frac{1}{6}$ 

$$P(S) = P(1) + P(2) + P(3) + P(4) + P(5) + P(6)$$

$$P(1) = \frac{1}{6} \qquad P(3) = \frac{1}{6} \qquad P(5) = \frac{1}{6}$$

$$P(2) = \frac{1}{6} \qquad P(4) = \frac{1}{6} \qquad P(6) = \frac{1}{6}$$

$$P(S) = P(1) + P(2) + P(3) + P(4) + P(5) + P(6)$$

$$P(S)$$

$$P(1) = \frac{1}{6} \qquad P(3) = \frac{1}{6} \qquad P(5) = \frac{1}{6}$$

$$P(2) = \frac{1}{6} \qquad P(4) = \frac{1}{6} \qquad P(6) = \frac{1}{6}$$

$$P(S) = P(1) + P(2) + P(3) + P(4) + P(5) + P(6)$$

$$P(S) = \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6}$$

$$P(1) = \frac{1}{6} \qquad P(3) = \frac{1}{6} \qquad P(5) = \frac{1}{6}$$

$$P(2) = \frac{1}{6} \qquad P(4) = \frac{1}{6} \qquad P(6) = \frac{1}{6}$$

$$P(S) = P(1) + P(2) + P(3) + P(4) + P(5) + P(6)$$

$$P(S) = \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6}$$

$$P(S)$$

$$P(1) = \frac{1}{6} \qquad P(3) = \frac{1}{6} \qquad P(5) = \frac{1}{6}$$

$$P(2) = \frac{1}{6} \qquad P(4) = \frac{1}{6} \qquad P(6) = \frac{1}{6}$$

$$P(S) = P(1) + P(2) + P(3) + P(4) + P(5) + P(6)$$

$$P(S) = \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6}$$

$$P(S) = \frac{6}{6}$$

$$P(1) = \frac{1}{6} \qquad P(3) = \frac{1}{6} \qquad P(5) = \frac{1}{6}$$

$$P(2) = \frac{1}{6} \qquad P(4) = \frac{1}{6} \qquad P(6) = \frac{1}{6}$$

$$P(S) = P(1) + P(2) + P(3) + P(4) + P(5) + P(6)$$

$$P(S) = \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6}$$

$$P(S) = \frac{6}{6} = 1$$

#### What are the Properties of Probability?

5. The probability of any two disjoint events  $E_1$  and  $E_2$  is the sum of the probabilities of each individual event.

$$P(E_1 \text{ or } E_2) = P(E_1) + P(E_2)$$

A die is rolled. What is the probability of getting 2 or an odd number?

$$S = \{1, 2, 3, 4, 5, 6\}$$

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S = \{1, 2, 3, 4, 5, 6\}
{Getting 2} = {2}
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S = \{1, 2, 3, 4, 5, 6\}
{Getting 2} = {2}
{Getting odd} = {1, 3, 5}
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S = \{1, 2, 3, 4, 5, 6\} n(S) = 6 {Getting 2} = {2} {Getting odd} = {1, 3, 5}
```

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
{Getting 2} = {2}  $n(Getting 2) = 1$   
{Getting odd} = {1, 3, 5}

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $\{\text{Getting 2}\} = \{2\}$   $n(\text{Getting 2}) = 1$   
 $\{\text{Getting odd}\} = \{1, 3, 5\}$   $n(\text{Getting odd}) = 3$ 

A die is rolled. What is the probability of getting 2 or an odd number?

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
{Getting 2} = {2}  $n(Getting 2) = 1$   
{Getting odd} = {1, 3, 5}  $n(Getting 2) = 3$ 

P(Getting 2 or odd)

A die is rolled. What is the probability of getting 2 or an odd number?

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $\{\text{Getting 2}\} = \{2\}$   $n(\text{Getting 2}) = 1$   
 $\{\text{Getting odd}\} = \{1, 3, 5\}$   $n(\text{Getting odd}) = 3$ 

P(Getting 2 or odd) = P(Getting 2) + P(Getting odd)

```
S = \{1, 2, 3, 4, 5, 6\} n(S) = 6

\{Getting 2\} = \{2\} n(Getting 2) = 1

\{Getting odd\} = \{1, 3, 5\} n(Getting odd) = 3

P(Getting 2 \text{ or odd}) = P(Getting 2) + P(Getting odd)

P(Getting 2 \text{ or odd})
```

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $\{\text{Getting 2}\} = \{2\}$   $n(\text{Getting 2}) = 1$   
 $\{\text{Getting odd}\} = \{1, 3, 5\}$   $n(\text{Getting odd}) = 3$   
 $P(\text{Getting 2 or odd}) = P(\text{Getting 2}) + P(\text{Getting odd})$   
 $P(\text{Getting 2 or odd}) = \frac{1}{6} + \frac{3}{6}$ 

P(Getting 2 or odd)

A die is rolled. What is the probability of getting 2 or an odd number?

$$S = \{1, 2, 3, 4, 5, 6\}$$
  $n(S) = 6$   
 $\{\text{Getting 2}\} = \{2\}$   $n(\text{Getting 2}) = 1$   
 $\{\text{Getting odd}\} = \{1, 3, 5\}$   $n(\text{Getting odd}) = 3$   
 $P(\text{Getting 2 or odd}) = P(\text{Getting 2}) + P(\text{Getting odd})$   
 $P(\text{Getting 2 or odd}) = \frac{1}{6} + \frac{3}{6}$ 

$$S = \{1, 2, 3, 4, 5, 6\}$$
 
$$n(S) = 6$$
 
$$\{Getting 2\} = \{2\}$$
 
$$n(Getting 2) = 1$$
 
$$\{Getting odd\} = \{1, 3, 5\}$$
 
$$n(Getting odd) = 3$$
 
$$P(Getting 2 \text{ or odd}) = P(Getting 2) + P(Getting odd)$$
 
$$P(Getting 2 \text{ or odd}) = \frac{1}{6} + \frac{3}{6}$$
 
$$P(Getting 2 \text{ or odd}) = \frac{4}{6}$$

$$S = \{1, 2, 3, 4, 5, 6\}$$
 
$$n(S) = 6$$
 
$$\{Getting 2\} = \{2\}$$
 
$$n(Getting 2) = 1$$
 
$$\{Getting odd\} = \{1, 3, 5\}$$
 
$$n(Getting odd) = 3$$
 
$$P(Getting 2 \text{ or odd}) = P(Getting 2) + P(Getting odd)$$
 
$$P(Getting 2 \text{ or odd}) = \frac{1}{6} + \frac{3}{6}$$
 
$$P(Getting 2 \text{ or odd}) = \frac{4}{6} \text{ or } \frac{2}{3}$$

## What are the Properties of Probability?

6. The probability of any event which is not in *E* is the difference between 1 and the probability of event *E*.

$$P(E') = 1 - P(E)$$

E' signifies "not in E."

$$S = \{A\heartsuit, \ldots, K\heartsuit, \}$$

$$\mathcal{S} = \{A\heartsuit, \dots, K\heartsuit, A\diamondsuit, \dots, K\diamondsuit, A\clubsuit, \dots, K\clubsuit, \dots \}$$

$$S = \{A\heartsuit, \dots, K\heartsuit, A\diamondsuit, \dots, K\diamondsuit, A\clubsuit, \dots, K\clubsuit, A\spadesuit, \dots, K\spadesuit\}$$

$$S = \{A\heartsuit, \dots, K\heartsuit, A\diamondsuit, \dots, K\diamondsuit, A\clubsuit, \dots, K\clubsuit, A\spadesuit, \dots, K\spadesuit\}$$
 $F = \{J\heartsuit, \dots, K\heartsuit, \dots, K\diamondsuit, \dots,$ 

$$S = \{A\heartsuit, \dots, K\heartsuit, A\diamondsuit, \dots, K\diamondsuit, A\clubsuit, \dots, K\clubsuit, A\spadesuit, \dots, K\clubsuit\}$$

$$F = \{J\heartsuit, \dots, K\heartsuit, J\diamondsuit, \dots, K\diamondsuit, \dots, K\diamondsuit,$$

```
S = \{A\heartsuit, \ldots, K\heartsuit, \}
           A\diamondsuit,\ldots,K\diamondsuit,
            A.....K.
           A \spadesuit, \ldots, K \spadesuit \}
F = \{J\heartsuit, \ldots, K\heartsuit,
            J\diamondsuit,\ldots,K\diamondsuit,
            J♣, . . . , K♣,
            J \spadesuit, \ldots, K \spadesuit \}
```

$$S = \{A\heartsuit, \dots, K\heartsuit, \quad n(S) = 52$$

$$A\diamondsuit, \dots, K\diamondsuit,$$

$$A\clubsuit, \dots, K\clubsuit,$$

$$A\spadesuit, \dots, K\diamondsuit,$$

$$J\diamondsuit, \dots, K\diamondsuit,$$

$$J\diamondsuit, \dots, K\diamondsuit,$$

$$J\diamondsuit, \dots, K\diamondsuit,$$

$$J\clubsuit, \dots, K\clubsuit,$$

$$S = \{A\heartsuit, \dots, K\heartsuit, \quad n(S) = 52$$

$$A\diamondsuit, \dots, K\diamondsuit, \quad n(F) = 12$$

$$A\clubsuit, \dots, K\clubsuit,$$

$$A\spadesuit, \dots, K\diamondsuit,$$

$$J\diamondsuit, \dots, K\diamondsuit,$$

$$J\diamondsuit, \dots, K\diamondsuit,$$

$$J\diamondsuit, \dots, K\diamondsuit,$$

$$J\clubsuit, \dots, K\clubsuit,$$

```
S = \{A\heartsuit, \dots, K\heartsuit, \quad n(S) = 52\}
                                                                                    P(\text{not F})
          A\diamondsuit,\ldots,K\diamondsuit,\quad n(F)=12
           A♣....K♣.
           A \spadesuit, \ldots, K \spadesuit \}
F = \{J\heartsuit, \ldots, K\heartsuit,
           J\diamondsuit,\ldots,K\diamondsuit,
           J♣, . . . , K♣,
           J \spadesuit, \ldots, K \spadesuit \}
```

$$S = \{A\heartsuit, \dots, K\heartsuit, \quad n(S) = 52$$
  
 $A\diamondsuit, \dots, K\diamondsuit, \quad n(F) = 12$   
 $A\clubsuit, \dots, K\clubsuit,$   
 $A\spadesuit, \dots, K\diamondsuit,$   
 $A\diamondsuit, \dots, K\diamondsuit,$   
 $J\diamondsuit, \dots, K\diamondsuit,$ 

$$S = \{A\heartsuit, \dots, K\heartsuit, \quad n(S) = 52$$
  
 $A\diamondsuit, \dots, K\diamondsuit, \quad n(F) = 12$   
 $A\clubsuit, \dots, K\clubsuit,$   
 $A\spadesuit, \dots, K\diamondsuit,$   
 $A\diamondsuit, \dots, K\diamondsuit,$ 

$$S = \{A\heartsuit, \dots, K\heartsuit, \quad n(S) = 52$$
  
 $A\diamondsuit, \dots, K\diamondsuit, \quad n(F) = 12$   
 $A\clubsuit, \dots, K\clubsuit,$   
 $A\spadesuit, \dots, K\diamondsuit,$   
 $J\diamondsuit, \dots, K\diamondsuit,$   
 $J\diamondsuit, \dots, K\diamondsuit,$   
 $J\diamondsuit, \dots, K\diamondsuit,$   
 $J\spadesuit, \dots, K\diamondsuit,$   
 $J\diamondsuit, \dots, K\diamondsuit,$   
 $J\diamondsuit, \dots, K\diamondsuit,$ 

$$S = \{A\heartsuit, \dots, K\heartsuit, \quad n(S) = 52$$
  
 $A\diamondsuit, \dots, K\diamondsuit, \quad n(F) = 12$   
 $A\clubsuit, \dots, K\clubsuit,$   
 $A\spadesuit, \dots, K\diamondsuit,$   
 $A\diamondsuit, \dots, K\diamondsuit,$ 

$$S = \{A\heartsuit, \dots, K\heartsuit, \quad n(S) = 52$$
  
 $A\diamondsuit, \dots, K\diamondsuit, \quad n(F) = 12$   
 $A\clubsuit, \dots, K\clubsuit,$   
 $A\spadesuit, \dots, K\diamondsuit,$   
 $F = \{J\heartsuit, \dots, K\diamondsuit,$   
 $J\diamondsuit, \dots, K\diamondsuit,$ 

$$S = \{A\heartsuit, \dots, K\heartsuit, \quad n(S) = 52$$
  
 $A\diamondsuit, \dots, K\diamondsuit, \quad n(F) = 12$   
 $A\clubsuit, \dots, K\clubsuit,$   
 $A\spadesuit, \dots, K\diamondsuit,$   
 $A\diamondsuit, \dots, K\diamondsuit,$   

$$S = \{A\heartsuit, \dots, K\heartsuit, \quad n(S) = 52$$
  
 $A\diamondsuit, \dots, K\diamondsuit, \quad n(F) = 12$   
 $A\clubsuit, \dots, K\clubsuit,$   
 $A\spadesuit, \dots, K\diamondsuit,$   
 $A\diamondsuit, \dots, K\diamondsuit,$ 

#### Practice

1. What is the probability of getting a HEART from a deck of cards?

#### Practice

1. What is the probability of getting a HEART from a deck of cards?

$$n(S) = 52$$

#### Practice

1. What is the probability of getting a HEART from a deck of cards?

$$n(S) = 52$$
$$n(\heartsuit) = 13$$

$$n(S) = 52$$
  
 $n(\heartsuit) = 13$   
 $P(\heartsuit)$ 

$$n(S) = 52$$
  
 $n(\heartsuit) = 13$   
 $P(\heartsuit) = \frac{n(\heartsuit)}{n(S)}$ 

$$n(S) = 52$$
  
 $n(\heartsuit) = 13$   
 $P(\heartsuit) = \frac{n(\heartsuit)}{n(S)}$   
 $P(\heartsuit)$ 

$$n(S) = 52$$

$$n(\heartsuit) = 13$$

$$P(\heartsuit) = \frac{n(\heartsuit)}{n(S)}$$

$$P(\heartsuit) = \frac{13}{52}$$

$$n(S) = 52$$

$$n(\heartsuit) = 13$$

$$P(\heartsuit) = \frac{n(\heartsuit)}{n(S)}$$

$$P(\heartsuit) = \frac{13}{52}$$

$$P(\heartsuit)$$

$$n(S) = 52$$

$$n(\heartsuit) = 13$$

$$P(\heartsuit) = \frac{n(\heartsuit)}{n(S)}$$

$$P(\heartsuit) = \frac{13}{52}$$

$$P(\heartsuit) = \frac{1}{13}$$

$$n(S) = 20$$

$$n(S) = 20$$
  
 $n(blue marble) = 5$ 

```
n(S) = 20

n(blue marble) = 5

P(blue marble)
```

$$n(S) = 20$$
  
 $n(\text{blue marble}) = 5$   
 $P(\text{blue marble}) = \frac{n(\text{blue marble})}{n(S)}$ 

$$n(S) = 20$$
  
 $n(\text{blue marble}) = 5$   
 $P(\text{blue marble}) = \frac{n(\text{blue marble})}{n(S)}$   
 $P(\text{blue marble})$ 

$$n(S) = 20$$
  
 $n(\text{blue marble}) = 5$   
 $P(\text{blue marble}) = \frac{n(\text{blue marble})}{n(S)}$   
 $P(\text{blue marble}) = \frac{5}{20}$ 

2. There are 20 marbles in a container: 4 are red, 5 are blue, and 11 are yellow. What is the probability that a blue marble will be picked?

$$n(S) = 20$$
  
 $n(\text{blue marble}) = 5$   
 $P(\text{blue marble}) = \frac{n(\text{blue marble})}{n(S)}$   
 $P(\text{blue marble}) = \frac{5}{20}$ 

P(blue marble)



$$n(S) = 20$$
  
 $n(\text{blue marble}) = 5$   
 $P(\text{blue marble}) = \frac{n(\text{blue marble})}{n(S)}$   
 $P(\text{blue marble}) = \frac{5}{20}$   
 $P(\text{blue marble}) = \frac{1}{4}$ 

$$n(S) = 12$$

$$n(S) = 12$$
  
 $n(E) = 4$ 

$$n(S) = 12$$
  
 $n(E) = 4$   
 $P(E')$ 

$$n(S) = 12$$
  
 $n(E) = 4$   
 $P(E') = 1 - P(E)$ 

$$n(S) = 12$$
  
 $n(E) = 4$   
 $P(E') = 1 - P(E)$   
 $P(E')$ 

$$n(S) = 12$$
  
 $n(E) = 4$   
 $P(E') = 1 - P(E)$   
 $P(E') = 1 - \frac{4}{12}$ 

P(E')

$$n(S) = 12$$
  
 $n(E) = 4$   
 $P(E') = 1 - P(E)$   
 $P(E') = 1 - \frac{4}{12}$ 

$$n(S) = 12$$
  
 $n(E) = 4$   
 $P(E') = 1 - P(E)$   
 $P(E') = 1 - \frac{4}{12}$   
 $P(E') = \frac{8}{12}$ 

$$n(S) = 12$$
  
 $n(E) = 4$   
 $P(E') = 1 - P(E)$   
 $P(E') = 1 - \frac{4}{12}$   
 $P(E') = \frac{8}{12}$  or  $\frac{2}{3}$ 

$$n(S) = 45$$

$$n(S) = 45$$
  
 $n(boy) = 25$ 

$$n(S) = 45$$
  
 $n(boy) = 25$   
 $P(girl)$ 

$$n(S) = 45$$
  
 $n(boy) = 25$   
 $P(girl) = 1 - P(boy)$ 

```
n(S) = 45

n(boy) = 25

P(girl) = 1 - P(boy)

P(girl)
```

$$n(S) = 45$$
  
 $n(boy) = 25$   
 $P(girl) = 1 - P(boy)$   
 $P(girl) = 1 - \frac{25}{45}$ 

$$n(S) = 45$$
  
 $n(boy) = 25$   
 $P(girl) = 1 - P(boy)$   
 $P(girl) = 1 - \frac{25}{45}$ 

$$n(S) = 45$$
  
 $n(boy) = 25$   
 $P(girl) = 1 - P(boy)$   
 $P(girl) = 1 - \frac{25}{45}$   
 $P(girl) = \frac{20}{45}$ 

$$n(S) = 45$$
  
 $n(boy) = 25$   
 $P(girl) = 1 - P(boy)$   
 $P(girl) = 1 - \frac{25}{45}$   
 $P(girl) = \frac{20}{45}$  or  $\frac{4}{9}$ 

$$n(S) = 4$$

$$n(S) = 4$$
$$n(TT) = 1$$

$$n(S) = 4$$
  
 $n(TT) = 1$   
 $n(HH) = 1$ 

```
n(S) = 4

n(TT) = 1

n(HH) = 1

P(TT \text{ or } HH)
```

```
n(S) = 4

n(TT) = 1

n(HH) = 1

P(TT \text{ or } HH) = P(TT) + P(HH)
```

```
n(S) = 4

n(TT) = 1

n(HH) = 1

P(TT \text{ or } HH) = P(TT) + P(HH)

P(TT \text{ or } HH)
```

$$n(S) = 4$$
  
 $n(TT) = 1$   
 $n(HH) = 1$   
 $P(TT \text{ or } HH) = P(TT) + P(HH)$   
 $P(TT \text{ or } HH) = \frac{1}{4} + \frac{1}{4}$ 

P(TT or HH)

$$n(S) = 4$$
  
 $n(TT) = 1$   
 $n(HH) = 1$   
 $P(TT \text{ or } HH) = P(TT) + P(HH)$   
 $P(TT \text{ or } HH) = \frac{1}{4} + \frac{1}{4}$ 

$$n(S) = 4$$
  
 $n(TT) = 1$   
 $n(HH) = 1$   
 $P(TT \text{ or } HH) = P(TT) + P(HH)$   
 $P(TT \text{ or } HH) = \frac{1}{4} + \frac{1}{4}$   
 $P(TT \text{ or } HH) = \frac{2}{4}$ 

$$n(S) = 4$$
  
 $n(TT) = 1$   
 $n(HH) = 1$   
 $P(TT \text{ or HH}) = P(TT) + P(HH)$   
 $P(TT \text{ or HH}) = \frac{1}{4} + \frac{1}{4}$   
 $P(TT \text{ or HH}) = \frac{2}{4} \text{ or } \frac{1}{2}$ 

# Thank you for attending the virtual class.