Solving Systems of Linear Equations in Two Variables by Substitution Method

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1. Solve one equation for one variable in terms of the other variable.

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- 2. Substitute the expression obtained in STEP 1 into the other equation.

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- 3. Solve the resulting equation in one variable.

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- 2. Substitute the expression obtained in STEP 1 into the other equation.
- 3. Solve the resulting equation in one variable.
- 4. Find the value of the other variable by substituting the solution found in STEP 3 into any equation containing both variables.

- 1. Solve one equation for one variable in terms of the other variable.
- 2. Substitute the expression obtained in STEP 1 into the other equation.
- 3. Solve the resulting equation in one variable.
- 4. Find the value of the other variable by substituting the solution found in STEP 3 into any equation containing both variables.
- 5. Check the solution in the original equations.



Solve the following system using the substitution method:

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Step 1: Solve one equation for one variable in terms of the other variable.

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

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$$x + y = 4$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

$$x + y = 4$$

Use Subtraction Property

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

$$x + y = 4$$

Use Subtraction Property

$$x + y - y = -y + 4$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

$$x + y = 4$$

Use Subtraction Property
Simplify

$$x + y - y = -y + 4$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Use Subtraction Property

Simplify

$$x + y = 4$$

$$x + y - y = -y + 4$$

$$x = -y + 4$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Use Subtraction Property

Simplify

Equation 3

$$\mathbf{x} + \mathbf{y} = \mathbf{4}$$

$$x + y - y = -y + 4$$

$$x = -y + 4$$

Step 1: Solve one equation for one variable in terms of the other variable.

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

First equation

Use Subtraction Property

Simplify

Equation 3

$$\mathbf{x} + \mathbf{y} = \mathbf{4}$$

$$x + y - y = -y + 4$$

$$x = -y + 4$$

$$x = -y + 4$$

Step 2: Substitute the expression obtained in step 1 into the other equation.

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Step 2: Substitute the expression obtained in step 1 into the other equation.

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Second equation

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

$$x-y=2$$

Step 2: Substitute the expression obtained in step 1 into the other equation.

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Second equation

$$x-y=2$$

Substitute Eq. 3: x = -y + 4

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Second equation

$$x-y=2$$

Substitute Eq. 3:
$$x = -y + 4$$
 $-y + 4 - y = 2$

$$-y+4-y=2$$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Second equation

$$x-y=2$$

Substitute Eq. 3:
$$x = -y + 4$$

$$-y + 4 - y = 2$$

Simplify

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Second equation

$$x-y=2$$

Substitute Eq. 3:
$$x = -y + 4$$

$$-y+4-y=2$$

$$-2y + 4 = 2$$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Second equation

$$x-y=2$$

Substitute Eq. 3:
$$x = -y + 4$$

$$-y+4-y=2$$

$$-2y + 4 = 2$$

Use Subtraction Property

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Second equation

$$x-y=2$$

Substitute Eq. 3:
$$x = -y + 4$$

$$-y+4-y=2$$

$$-2y + 4 = 2$$

$$-2y + 4 - 4 = 2 - 4$$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Second equation

$$x-y=2$$

Substitute Eq. 3:
$$x = -y + 4$$

$$-y+4-y=2$$

$$-2y + 4 = 2$$

$$-2y + 4 - 4 = 2 - 4$$

Simplify

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Second equation

$$x-y=2$$

Substitute Eq. 3:
$$x = -y + 4$$

$$-y+4-y=2$$

$$-2y + 4 = 2$$

$$-2y + 4 - 4 = 2 - 4$$

$$-2y = -2$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

$$x-y=2$$

Substitute Eq. 3:
$$x = -y + 4$$

$$-y+4-y=2$$

$$-2y + 4 = 2$$

$$-2y + 4 - 4 = 2 - 4$$

$$-2y = -2$$

Use Division Property

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Substitute Eq. 3:
$$x = -y + 4$$

Use Subtraction Property

Use Division Property

$$x - y = 2$$

$$-y + 4 - y = 2$$

$$-2y + 4 = 2$$

$$-2y+4-4=2-4$$

$$-2y = -2$$

$$\frac{-2y}{-2} = \frac{-2}{-2}$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

$$x-y=2$$

Substitute Eq. 3:
$$x = -y + 4$$

$$-y+4-y=2$$

$$-2y + 4 = 2$$

$$-2y + 4 - 4 = 2 - 4$$

$$-2y = -2$$

$$\frac{-2y}{-2} = \frac{-2}{-2}$$

Simplify

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Substitute Eq. 3:
$$x = -y + 4$$

$$x - y = 2$$

$$-y+4-y=2$$

$$-2y + 4 = 2$$

$$-2y + 4 - 4 = 2 - 4$$

$$-2y = -2$$

$$\frac{-2y}{-2} = \frac{-2}{-2}$$

$$y = 1$$

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

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$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

$$x + y = 4$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

$$x + y = 4$$

Substitute
$$y = 1$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Substitute
$$y = 1$$

$$x + y = 4$$
$$x + 1 = 4$$

$$x + 1 = 4$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

$$\mathbf{x} + \mathbf{y} = \mathbf{4}$$

Substitute
$$y = 1$$

$$x + y = 4$$
$$x + 1 = 4$$

Use Subtraction Property

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Substitute
$$y = 1$$

Use Subtraction Property

$$x + y = 4$$

$$x + 1 = 4$$

$$x + 1 - 1 = 4 - 1$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Substitute y = 1

Use Subtraction Property

Simplify

$$x + y = 4$$

$$x + 1 = 4$$

$$x + 1 - 1 = 4 - 1$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Substitute y = 1

Use Subtraction Property

Simplify

$$x + y = 4$$

$$x + 1 = 4$$

$$x + 1 - 1 = 4 - 1$$

$$x = 3$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Check: x = 3, y = 1

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Check:
$$x = 3, y = 1$$

$$x + y = 4$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Check:
$$x = 3, y = 1$$

$$x + y = 4$$

3 + 1 = 4

$$3 + 1 = 4$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Check:
$$x = 3, y = 1$$

$$x + y = 4$$

$$3 + 1 = 4$$

$$4 = 4$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Check:
$$x = 3, y = 1$$

$$x + y = 4$$

$$3 + 1 = 4$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

x - y = 2

Check:
$$x = 3, y = 1$$

$$x + y = 4$$

$$y = 4$$

$$3 + 1 = 4$$

$$4 = 4$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Check:
$$x = 3, y = 1$$

$$x + y = 4$$

$$3 + 1 = 4$$

$$x - v = 2$$

$$3 - 1 = 2$$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Check:
$$x = 3, y = 1$$

$$x + y = 4$$
 $x - y = 2$
 $3 + 1 = 4$ $3 - 1 = 2$
 $4 = 4$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Check:
$$x = 3, y = 1$$

$$x + y = 4$$
 $x - y = 2$
 $3 + 1 = 4$ $3 - 1 = 2$
 $4 = 4$

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Check: x = 3, y = 1

$$x + y = 4$$
 $x - y = 2$
 $3 + 1 = 4$ $3 - 1 = 2$
 $4 = 4$

 \therefore the solution set is (3, 1).

Solve the following system using the substitution method:

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Step 1: Solve one equation for one variable in terms of the other variable.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

$$4x + y = -2$$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

$$4x + y = -2$$

Use Subtraction Property

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

$$4x + y = -2$$

Use Subtraction Property 4x - 4x + y = -4x - 2

$$4x - 4x + y = -4x - 2$$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

$$4x + y = -2$$

Use Subtraction Property 4x - 4x + v = -4x - 2

$$4x - 4x + y = -4x - 2$$

Simplify

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

$$4x + y = -2$$

Use Subtraction Property

$$4x - 4x + y = -4x - 2$$

$$y = -4x - 2$$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

$$4x + y = -2$$

Use Subtraction Property

$$4x - 4x + y = -4x - 2$$

Simplify

$$y = -4x - 2$$

Equation 3

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

$$4x + y = -2$$

Use Subtraction Property

$$4x - 4x + y = -4x - 2$$

Simplify

$$y = -4x - 2$$

Equation 3

$$y = -4x - 2$$

Step 2: Substitute the expression obtained in step 1 into the other equation.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Step 2: Substitute the expression obtained in step 1 into the other equation.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

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First equation

$$3x + 2y = 1$$

Step 2: Substitute the expression obtained in step 1 into the other equation.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

$$3x + 2y = 1$$

Substitute Eq. 3: y = -4x - 2

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

$$3x + 2y = 1$$

Substitute Eq. 3:
$$y = -4x - 2$$

$$3x + 2(-4x - 2) = 1$$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

$$3x + 2y = 1$$

Substitute Eq. 3:
$$y = -4x - 2$$

$$3x + 2(-4x - 2) = 1$$

Use Distributive Property

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

$$3x + 2y = 1$$

Substitute Eq. 3:
$$y = -4x - 2$$

$$3x + 2(-4x - 2) = 1$$

$$3x - 8x - 4 = 1$$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

$$3x + 2y = 1$$

Substitute Eq. 3:
$$y = -4x - 2$$

$$3x + 2(-4x - 2) = 1$$

$$3x - 8x - 4 = 1$$

Simplify

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

Substitute Eq. 3:
$$y = -4x - 2$$

$$3x + 2y = 1$$

$$3x + 2(-4x - 2) = 1$$

$$3x - 8x - 4 = 1$$

$$-5x - 4 = 1$$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

Substitute Eq. 3:
$$y = -4x - 2$$

Use Distributive Property

Simplify

Use Addition Property

$$3x + 2y = 1$$

$$3x + 2(-4x - 2) = 1$$

$$3x - 8x - 4 = 1$$

$$-5x - 4 = 1$$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

Substitute Eq. 3:
$$y = -4x - 2$$

$$3x + 2y = 1$$

$$3x + 2(-4x - 2) = 1$$

$$3x - 8x - 4 = 1$$

$$-5x - 4 = 1$$

$$-5x - 4 + 4 = 1 + 4$$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

Substitute Eq. 3:
$$y = -4x - 2$$

Use Distributive Property

Simplify

Use Addition Property

Simplify

$$3x + 2y = 1$$

$$3x + 2(-4x - 2) = 1$$

$$3x - 8x - 4 = 1$$

$$-5x - 4 = 1$$

$$-5x - 4 + 4 = 1 + 4$$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

Substitute Eq. 3:
$$y = -4x - 2$$

Use Distributive Property

Use Addition Property

Simplify

$$3x + 2y = 1$$

$$3x + 2(-4x - 2) = 1$$

$$3x - 8x - 4 = 1$$

$$-5x - 4 = 1$$

$$-5x - 4 + 4 = 1 + 4$$

$$-5x = 5$$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

Substitute Eq. 3:
$$y = -4x - 2$$

Use Distributive Property

Simplify

Use Addition Property

Simplify

Use Division Property

$$3x + 2y = 1$$

$$3x + 2(-4x - 2) = 1$$

$$3x - 8x - 4 = 1$$

$$-5x - 4 = 1$$

$$-5x - 4 + 4 = 1 + 4$$

$$-5x = 5$$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Substitute Eq. 3:
$$y = -4x - 2$$

$$3x + 2y = 1$$

$$3x + 2(-4x - 2) = 1$$

$$3x - 8x - 4 = 1$$

$$-5x - 4 = 1$$

$$-5x - 4 + 4 = 1 + 4$$

$$-5x = 5$$

$$\frac{-5x}{-5} = \frac{5}{-5}$$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Substitute Eq. 3:
$$y = -4x - 2$$

$$3x + 2y = 1$$

$$3x + 2(-4x - 2) = 1$$

$$3x - 8x - 4 = 1$$

$$-5x - 4 = 1$$

$$-5x - 4 + 4 = 1 + 4$$

$$-5x = 5$$

$$\frac{-5x}{-5} = \frac{5}{-5}$$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Substitute Eq. 3:
$$y = -4x - 2$$

$$3x + 2y = 1$$

$$3x + 2(-4x - 2) = 1$$

$$3x - 8x - 4 = 1$$

$$-5x - 4 = 1$$

$$-5x - 4 + 4 = 1 + 4$$

$$-5x = 5$$

$$\frac{-5x}{-5} = \frac{5}{-5}$$

$$x = -1$$

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

$$3x + 2y = 1$$

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

$$3x + 2y = 1$$

Substitute x = -1

First equation

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$
 First equation
$$3x + 2y = 1$$
 Substitute $x = -1$
$$3(-1) + 2y = 1$$

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$
$$3x + 2y = 1$$
$$4x - 1$$
$$3(-1) + 2y = 1$$

Substitute x = -1Simplify

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x+2y=1\\ 4x+y=-2 \end{cases}$$
 First equation
$$3x+2y=1$$
 Substitute $x=-1$
$$3(-1)+2y=1$$
 Simplify
$$-3+2y=1$$

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

$$3x + 2y = 1$$

Substitute
$$x = -1$$

$$3(-1)+2y=1$$

$$-3 + 2y = 1$$

Use Addition Property

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$
First equation
$$3x + 2y = 1$$
Substitute $x = -1$
$$3(-1) + 2y = 1$$
Simplify
$$-3 + 2y = 1$$

Simplify

First equation

Use Addition Property

$$-3 + 3 + 2y = 1 + 3$$

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

$$3x + 2y = 1$$

Substitute
$$x = -1$$

$$3(-1) + 2y = 1$$

$$-3 + 2y = 1$$

$$-3 + 3 + 2y = 1 + 3$$

Simplify

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

$$3x + 2y = 1$$

Substitute
$$x = -1$$

$$3(-1) + 2y = 1$$

$$-3 + 2y = 1$$

$$-3 + 3 + 2y = 1 + 3$$

$$2y = 4$$

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

$$3x + 2y = 1$$

Substitute
$$x = -1$$

$$3(-1) + 2y = 1$$

$$-3 + 2y = 1$$

Use Addition Property

$$-3 + 3 + 2y = 1 + 3$$

Simplify

$$2y = 4$$

Use Division Property

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

Substitute
$$x = -1$$

3x + 2y = 1

$$3(-1) + 2y = 1$$

$$-3 + 2y = 1$$

$$-3 + 3 + 2y = 1 + 3$$

$$2y = 4$$

$$\frac{2y}{2} = \frac{4}{2}$$

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

First equation

Substitute
$$x = -1$$

3x + 2y = 1

$$3(-1) + 2y = 1$$

$$-3 + 2y = 1$$

$$-3 + 3 + 2y = 1 + 3$$

$$2y = 4$$

$$\frac{2y}{2} = \frac{4}{2}$$

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Substitute
$$x = -1$$

$$3x + 2y = 1$$

$$3(-1) + 2y = 1$$

$$-3 + 2y = 1$$

$$-3 + 3 + 2y = 1 + 3$$

$$2y = 4$$

$$\frac{2y}{2} = \frac{4}{2}$$

$$y=2$$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Check: x = -1, y = 2

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Check:
$$x = -1, y = 2$$

$$3x + 2y = 1$$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Check:
$$x = -1, y = 2$$

$$3x + 2y = 1$$

 $3(-1) + 2(2) = 1$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Check:
$$x = -1, y = 2$$

$$3x + 2y = 1$$

 $3(-1) + 2(2) = 1$
 $-3 + 4 = 1$

-3 + 4 = 1

1 = 1

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$
Check: $x = -1, y = 2$

$$3x + 2y = 1$$

$$3(-1) + 2(2) = 1$$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Check:
$$x = -1, y = 2$$

$$3x + 2y = 1$$

 $3(-1) + 2(2) = 1$
 $-3 + 4 = 1$
 $1 = 1$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$
Check: $x = -1, y = 2$

$$3x + 2y = 1 \\ 3(-1) + 2(2) = 1$$

$$-3 + 4 = 1$$

$$1 = 1 \checkmark$$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$
Check: $x = -1, y = 2$

$$3x + 2y = 1 \qquad 4x + y = -2$$

$$3(-1) + 2(2) = 1 \qquad 4(-1) + 2 = -2$$

$$-3 + 4 = 1$$

$$1 = 1 \checkmark$$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Check:
$$x = -1, y = 2$$

$$3x + 2y = 1$$
 $4x + y = -2$
 $3(-1) + 2(2) = 1$ $4(-1) + 2 = -2$
 $-3 + 4 = 1$ $-4 + 2 = -2$
 $1 = 1$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Check: x = -1, y = 2

$$3x + 2y = 1$$
 $4x + y = -2$
 $3(-1) + 2(2) = 1$ $4(-1) + 2 = -2$
 $-3 + 4 = 1$ $-4 + 2 = -2$
 $-2 = -2$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Check: x = -1, y = 2

$$3x + 2y = 1$$
 $4x + y = -2$
 $3(-1) + 2(2) = 1$ $4(-1) + 2 = -2$
 $-3 + 4 = 1$ $-4 + 2 = -2$
 $1 = 1$

$$\begin{cases} 3x + 2y = 1 \\ 4x + y = -2 \end{cases}$$

Check: x = -1, y = 2

$$3x + 2y = 1$$
 $4x + y = -2$
 $3(-1) + 2(2) = 1$ $4(-1) + 2 = -2$
 $-3 + 4 = 1$ $-4 + 2 = -2$
 $1 = 1$

 \therefore the solution set is (-1,2).

Solve the following system using the substitution method:

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Step 1: Solve one equation for one variable in terms of the other variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation

Step 1: Solve one equation for one variable in terms of the other variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation

$$x + 2y = 5$$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation

$$x + 2y = 5$$

Use Subtraction Property

Step 1: Solve one equation for one variable in terms of the other variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation

$$x + 2y = 5$$

Use Subtraction Property

$$x + 2y - 2y = -2y + 5$$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation

$$x + 2y = 5$$

Use Subtraction Property

$$x + 2y - 2y = -2y + 5$$

Simplify

Step 1: Solve one equation for one variable in terms of the other variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation x + 2y = 5Use Subtraction Property x + 2y - 2y = -2y + 5

Simplify x = -2y + 5

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation

$$x + 2y = 5$$

Use Subtraction Property

$$x + 2y - 2y = -2y + 5$$

Simplify

$$x = -2y + 5$$

Equation 3

Step 1: Solve one equation for one variable in terms of the other variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation	$\mathbf{x} + \mathbf{2y} = 5$
Use Subtraction Property	x + 2y - 2y = -2y + 5
Simplify	x = -2y + 5
Equation 3	x = -2y + 5

Step 2: Substitute the expression obtained in step 1 into the other equation.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Step 2: Substitute the expression obtained in step 1 into the other equation.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Step 2: Substitute the expression obtained in step 1 into the other equation.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

$$2x - 3y = -11$$

Step 2: Substitute the expression obtained in step 1 into the other equation.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

First equation

$$2x - 3y = -11$$

Substitute Eq. 3: x = -2y + 5

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

$$2x - 3y = -11$$

Substitute Eq. 3:
$$x = -2y + 5$$
 $2(-2y + 5) - 3y = -11$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

First equation

$$2x - 3y = -11$$

Substitute Eq. 3: x = -2y + 5 2(-2y + 5) - 3y = -11Use Distributive Property

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

First equation

$$2x - 3y = -11$$

Substitute Eq. 3:
$$x = -2y + 5$$
 $2(-2y + 5) - 3y = -11$

Use Distributive Property -4y + 10 - 3y = -11

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

$$2x - 3y = -11$$

Substitute Eq. 3:
$$x = -2y + 5$$
 $2(-2y + 5) - 3y = -11$
Use Distributive Property $-4y + 10 - 3y = -11$
Simplify

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

$$2x - 3y = -11$$

Substitute Eq. 3:
$$x = -2y + 5$$
 $2(-2y + 5) - 3y = -11$
Use Distributive Property $-4y + 10 - 3y = -11$
Simplify $-7y + 10 = -11$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

First equation

$$2x - 3y = -11$$

Substitute Eq. 3:
$$x = -2y + 5$$
 $2(-2y + 5) - 3y = -11$

Use Distributive Property

$$-4y + 10 - 3y = -11$$

$$-7y + 10 = -11$$

Use Subtraction Property

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

$$2x - 3y = -11$$

Substitute Eq. 3:
$$x = -2y + 5$$
 $2(-2y + 5) - 3y = -11$

Use Distributive Property
$$-4y + 10 - 3y = -11$$

Simplify
$$-7y + 10 = -11$$

Use Subtraction Property
$$-7y + 10 - 10 = -11 - 10$$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

First equation

$$2x - 3y = -11$$

Substitute Eq. 3:
$$x = -2y + 5$$
 $2(-2y + 5) - 3y = -11$

Use Distributive Property
$$-4y + 10 - 3y = -11$$

Simplify
$$-7y + 10 = -11$$

Use Subtraction Property
$$-7y + 10 - 10 = -11 - 10$$

Simplify

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

$$2x - 3y = -11$$

Substitute Eq. 3:
$$x = -2y + 5$$
 $2(-2y + 5) - 3y = -11$

Use Distributive Property
$$-4y + 10 - 3y = -11$$

Simplify
$$-7y + 10 = -11$$

Use Subtraction Property
$$-7y + 10 - 10 = -11 - 10$$

Simplify
$$-7y = -21$$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

First equation

$$2x - 3y = -11$$

Substitute Eq. 3:
$$x = -2y + 5$$
 $2(-2y + 5) - 3y = -11$

Use Distributive Property -4y + 10 - 3y = -11

Simplify -7y + 10 = -11

Use Subtraction Property -7y + 10 - 10 = -11 - 10

Simplify -7y = -21

Use Division Property

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

$$2x - 3y = -11$$

Substitute Eq. 3:
$$x = -2y + 5$$
 $2(-2y + 5) - 3y = -11$

Use Distributive Property
$$-4y + 10 - 3y = -11$$

Simplify
$$-7y + 10 = -11$$

Use Subtraction Property
$$-7y + 10 - 10 = -11 - 10$$

Simplify
$$-7y = -21$$
$$-7y = -2$$

Use Division Property
$$\frac{-7y}{-7} = \frac{-21}{-7}$$

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

First equation

$$2x - 3y = -11$$

Substitute Eq. 3:
$$x = -2y + 5$$
 $2(-2y + 5) - 3y = -11$

Use Distributive Property
$$-4y + 10 - 3y = -11$$

Simplify
$$-7y + 10 = -11$$

Use Subtraction Property
$$-7y + 10 - 10 = -11 - 10$$

Simplify
$$-7y = -21$$
$$-7y - 2$$

Use Division Property
$$\frac{-7y}{-7} = \frac{-21}{-7}$$

Simplify

Step 3: Solve the resulting equation in one variable.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

First equation

$$2x - 3y = -11$$

Substitute Eq. 3:
$$x = -2y + 5$$
 $2(-2y + 5) - 3y = -11$

Use Distributive Property -4y + 10 - 3y = -11

Simplify -7y + 10 = -11

Use Subtraction Property -7y + 10 - 10 = -11 - 10

Simplify -7y = -21

Use Division Property $\frac{-7y}{-7} = \frac{-21}{-7}$

Simplify y = 3

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation

$$x + 2y = 5$$

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation

$$x + 2y = 5$$

Substitute y = 3

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation

$$x + 2y = 5$$

Substitute
$$y = 3$$

$$x + 2(3) = 5$$

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation

$$x+2y=5$$

Substitute
$$y = 3$$

$$x + 2(3) = 5$$

Simplify

Step 4: Find the value of the other variable by substituting the solution found in step 3 into any equation containing both variables.

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation

$$x+2y=5$$

Substitute
$$y = 3$$

$$x + 2(3) = 5$$

$$x + 6 = 5$$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation

$$x + 2y = 5$$

Substitute
$$y = 3$$

$$x + 2(3) = 5$$

$$x + 6 = 5$$

Use Subtraction Property

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second	equation	

Substitute
$$y = 3$$

Use Subtraction Property

$$x + 2y = 5$$

$$x + 2(3) = 5$$

$$x + 6 = 5$$

$$x + 6 - 6 = 5 - 6$$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation

$$x+2y=5$$

Substitute
$$y = 3$$

$$x + 2(3) = 5$$

$$x + 6 = 5$$

$$x + 6 - 6 = 5 - 6$$

Simplify

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Second equation	x+2y=5
Substitute $y = 3$	x + 2(3) = 5
Simplify	x + 6 = 5
Use Subtraction Property	x + 6 - 6 = 5 - 6
Simplify	x = -1

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Check: x = -1, y = 3

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Check:
$$x = -1, y = 3$$

$$2x - 3y = -11$$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Check:
$$x = -1, y = 3$$

$$2x - 3y = -11$$

 $2(-1) - 3(3) = -11$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Check:
$$x = -1, y = 3$$

$$2x - 3y = -11$$

 $2(-1) - 3(3) = -11$
 $-2 - 9 = -11$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Check:
$$x = -1, y = 3$$

$$2x - 3y = -11$$

 $2(-1) - 3(3) = -11$
 $-2 - 9 = -11$
 $-11 = -11$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Check:
$$x = -1, y = 3$$

$$2x - 3y = -11$$

 $2(-1) - 3(3) = -11$
 $-2 - 9 = -11$
 $-11 = -11$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Check:
$$x = -1, y = 3$$

$$2x - 3y = -11$$
 $x + 2y = 5$
 $2(-1) - 3(3) = -11$
 $-2 - 9 = -11$
 $-11 = -11$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Check:
$$x = -1, y = 3$$

$$2x - 3y = -11$$
 $x + 2y = 5$
 $2(-1) - 3(3) = -11$ $-11 = -11$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Check:
$$x = -1, y = 3$$

$$2x - 3y = -11$$
 $x + 2y = 5$
 $2(-1) - 3(3) = -11$ $-1 + 2(3) = 5$
 $-2 - 9 = -11$ $-1 + 6 = 5$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Check:
$$x = -1, y = 3$$

$$2x - 3y = -11$$
 $x + 2y = 5$
 $2(-1) - 3(3) = -11$ $-1 + 2(3) = 5$
 $-2 - 9 = -11$ $-1 + 6 = 5$
 $-11 = -11$ \checkmark $5 = 5$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Check:
$$x = -1, y = 3$$

$$2x - 3y = -11$$
 $x + 2y = 5$
 $2(-1) - 3(3) = -11$ $-1 + 2(3) = 5$
 $-2 - 9 = -11$ $-1 + 6 = 5$
 $-11 = -11$ $5 = 5$

$$\begin{cases} 2x - 3y = -11 \\ x + 2y = 5 \end{cases}$$

Check: x = -1, y = 3

$$2x - 3y = -11$$
 $x + 2y = 5$
 $2(-1) - 3(3) = -11$ $-1 + 2(3) = 5$
 $-2 - 9 = -11$ $-1 + 6 = 5$
 $-11 = -11$ \checkmark $5 = 5$

 \therefore the solution set is (-1,3).

Thank you for watching.