Graphing Systems of Linear Equations in Two Variables

Jonathan R. Bacolod

Sauyo High School

1. Identify the x-intercept and y-intercept of each equation in the system.

- 1. Identify the x-intercept and y-intercept of each equation in the system.
- 2. Plot the intercepts of both equations on the same Cartesian plane.

- 1. Identify the x-intercept and y-intercept of each equation in the system.
- 2. Plot the intercepts of both equations on the same Cartesian plane.
- Connect the x-intercept and y-intercept.

Graph Solution Kind of System

Graph	Solution	Kind of System
Parallel	None	Inconsistent

Graph	Solution	Kind of System
Parallel	None	Inconsistent
Coinciding	Infinitely many	Consistent-Dependent

Graph	Solution	Kind of System
Parallel	None	Inconsistent
Coinciding	Infinitely many	Consistent-Dependent
Intersecting	One	Consistent-Independent

Example 1

Graph, identify the kind of system, and describe the graph of the following system of linear equations:

$$\begin{cases} x + y = -2 \\ 2x + 2y = -4 \end{cases}$$

$$x + y = -2$$

$$\mathbf{x} + \mathbf{y} = -\mathbf{2}$$

$$x + y = -2$$

Let
$$y = 0$$

$$x + y = -2$$

Let
$$y = 0$$

$$x + 0 = -2$$

$$x + y = -2$$

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$x + y = -2$$

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

$$x + y = -2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

$$x + y = -2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

Let
$$x = 0$$

$$x + y = -2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$X = -2$$

$$(-2,0)$$

Let
$$x = 0$$

$$0 + y = -2$$

$$x + y = -2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$X = -2$$

$$(-2,0)$$

Let
$$x = 0$$

$$0 + y = -2$$

$$y = -2$$

$$x + y = -2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$X = -2$$

$$(-2,0)$$

Let
$$x = 0$$

$$0 + y = -2$$

$$y = -2$$

$$(0, -2)$$

Second equation
$$2x + 2y = -4$$

$$2x + 2y = -4$$

$$2x + 2y = -4$$

Let
$$y = 0$$

$$2x + 2y = -4$$

Let
$$y = 0$$

$$2x + 2(0) = -4$$

$$2x + 2y = -4$$

Let
$$y = 0$$

$$2x + 2(0) = -4$$

$$2x + 0 = -4$$

$$2x + 2y = -4$$

Let
$$y = 0$$

$$2x + 2(0) = -4$$

$$2x + 0 = -4$$

$$\frac{2x}{2} = \frac{-4}{2}$$

$$2x + 2y = -4$$

Let
$$y = 0$$

$$2x + 2(0) = -4$$

$$2x + 0 = -4$$

$$\frac{2x}{2} = \frac{-4}{2}$$

$$x = -2$$

$$2x + 2y = -4$$

Let
$$y = 0$$

$$2x + 2(0) = -4$$

$$2x + 0 = -4$$

$$\frac{2x}{2} = \frac{-4}{2}$$

$$x = -2$$

$$(-2,0)$$

Second equation
$$2x + 2y = -4$$

$$2x + 2y = -4$$

Second equation
$$2x + 2y = -4$$

$$2x + 2y = -4$$

Let
$$x = 0$$

$$2x + 2y = -4$$

Let
$$x = 0$$

$$2(0) + 2y = -4$$

$$2x + 2y = -4$$

Let
$$x = 0$$

$$2(0) + 2y = -4$$

$$0 + 2y = -4$$

$$2x + 2y = -4$$

Let
$$x = 0$$

$$2(0) + 2y = -4$$

$$0 + 2y = -4$$

Use Division Property
$$\frac{2y}{2} = \frac{-4}{2}$$

$$\frac{2y}{2} = \frac{-2}{2}$$

Second equation

$$2x + 2y = -4$$

Let
$$x = 0$$

$$2(0) + 2y = -4$$

$$0+2y=-4$$

$$\frac{2y}{2} = \frac{-4}{2}$$

$$y = -2$$

Second equation

$$2x + 2y = -4$$

Let
$$x = 0$$

$$2(0) + 2y = -4$$

$$0 + 2y = -4$$

$$\frac{2y}{2} = \frac{-4}{2}$$

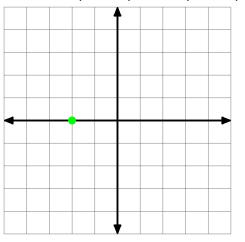
$$y = -2$$

$$(0, -2)$$

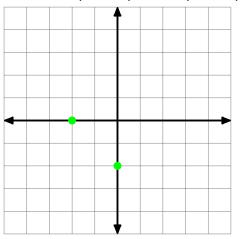
$$ightharpoonup$$
 (-2,0) and (0,-2) for $x+y=-2$

- (-2,0) and (0,-2) for x+y=-2
- (-2,0) and (0,-2) for 2x+2y=-4

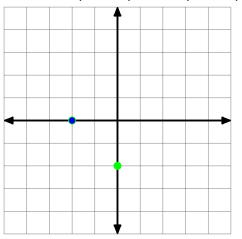
- (-2,0) and (0,-2) for x+y=-2
- (-2,0) and (0,-2) for 2x + 2y = -4



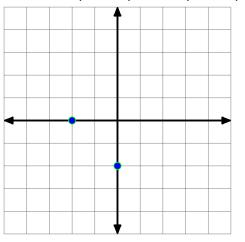
- (-2,0) and (0,-2) for x+y=-2
- (-2,0) and (0,-2) for 2x + 2y = -4



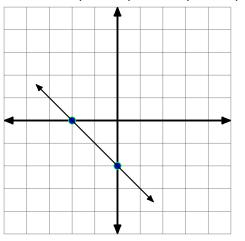
- (-2,0) and (0,-2) for x+y=-2
- (-2,0) and (0,-2) for 2x + 2y = -4



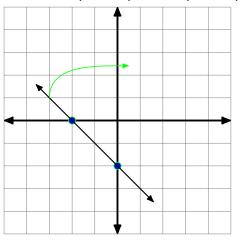
- (-2,0) and (0,-2) for x+y=-2
- (-2,0) and (0,-2) for 2x + 2y = -4



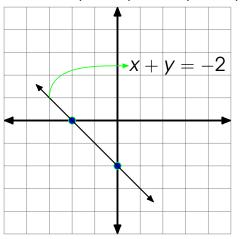
- (-2,0) and (0,-2) for x+y=-2
- (-2,0) and (0,-2) for 2x + 2y = -4



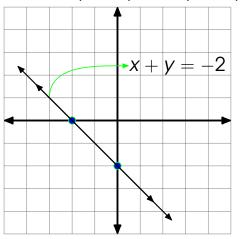
- (-2,0) and (0,-2) for x+y=-2
- (-2,0) and (0,-2) for 2x + 2y = -4



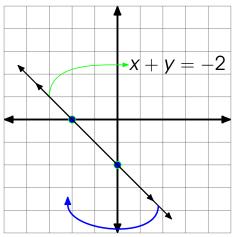
- (-2,0) and (0,-2) for x+y=-2
- (-2,0) and (0,-2) for 2x + 2y = -4



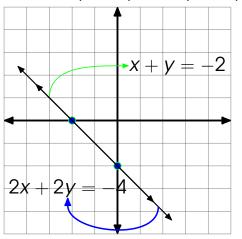
- ightharpoonup (-2,0) and (0,-2) for x+y=-2
- (-2,0) and (0,-2) for 2x + 2y = -4



- ightharpoonup (-2,0) and (0,-2) for x+y=-2
- (-2,0) and (0,-2) for 2x + 2y = -4

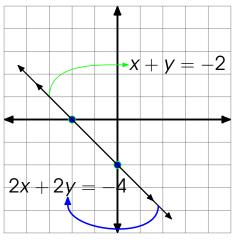


- (-2,0) and (0,-2) for x+y=-2
- (-2,0) and (0,-2) for 2x + 2y = -4



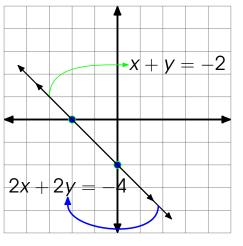
Plot:

- (-2,0) and (0,-2) for x+y=-2
- (-2,0) and (0,-2) for 2x + 2y = -4



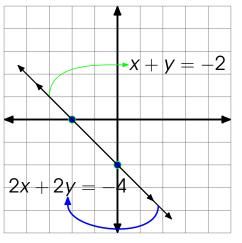
Graph: coinciding

- (-2,0) and (0,-2) for x+y=-2
- (-2,0) and (0,-2) for 2x + 2y = -4



- Graph: coinciding
- Solutions: infinitely many

- (-2,0) and (0,-2) for x+y=-2
- (-2,0) and (0,-2) for 2x + 2y = -4



- Graph: coinciding
- Solutions: infinitely many
- Kind: Consistentdependent

Graph, identify the kind of system, and describe the graph of the following system of linear equations:

$$\begin{cases} x + y = -2 \\ x + y = 3 \end{cases}$$

Step 1: Identify the x-intercept and y-intercept of each equation in the system.

Step 1: Identify the x-intercept and y-intercept of each equation in the system.

First equation

$$x + y = -2$$

$$x + y = -2$$

$$x + y = -2$$

Let
$$y = 0$$

$$x + y = -2$$

Let
$$y = 0$$

$$x + 0 = -2$$

$$x + y = -2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

Simplify

First	equation	1
1 11 31	equalion	•

$$x + y = -2$$

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$x+y=-2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

Coordinates

First equation	First	equation	
----------------	--------------	----------	--

$$x + y = -2$$

Let
$$y = 0$$
 $x + 0 = -2$

Simplify
$$x = -2$$

Coordinates
$$(-2,0)$$

$$x+y=-2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

$$x + y = -2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

Let
$$x = 0$$

$$x + y = -2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

Let
$$x = 0$$

$$0 + y = -2$$

$$x + y = -2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

Find the y-intercept:

Let
$$x = 0$$

$$0 + y = -2$$

Simplify

$$x + y = -2$$

x + 0 = -2

Find the x-intercept:

Let
$$y = 0$$

Simplify
$$x = -2$$

Coordinates
$$(-2,0)$$

Let
$$x = 0$$
 $0 + y = -2$

Simplify
$$y = -2$$

$$x + y = -2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

Find the y-intercept:

Let
$$x = 0$$

$$0 + v = -2$$

$$y = -2$$

Coordinates

$$x+y=-2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

Let
$$x = 0$$

$$0 + v = -2$$

$$y = -2$$

$$(0, -2)$$

Step 1: Identify the x-intercept and y-intercept of each equation in the system.

Step 1: Identify the x-intercept and y-intercept of each equation in the system.

Second equation

$$x + y = 3$$

$$x + y = 3$$

$$x + y = 3$$

Let
$$y = 0$$

$$x + y = 3$$

Let
$$y = 0$$

$$x + 0 = 3$$

$$x + y = 3$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 3$$

Simplify

$$x + y = 3$$

Let
$$y = 0$$

$$x + 0 = 3$$

$$x = 3$$

$$x + y = 3$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 3$$

$$x = 3$$

Coordinates

Second equation	$\mathbf{x} + \mathbf{y} = 3$
-----------------	-------------------------------

Let
$$y = 0$$
 $x + 0 = 3$

Simplify
$$x = 3$$

Coordinates
$$(3,0)$$

$$x + y = 3$$

x + 0 = 3

Let
$$y = 0$$

$$x = 3$$

$$x + y = 3$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 3$$

$$x = 3$$

Let
$$x = 0$$

$$x + y = 3$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 3$$

$$x = 3$$

Let
$$x = 0$$

$$0 + y = 3$$

$$x + y = 3$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 3$$

$$x = 3$$

Find the y-intercept:

Let
$$x = 0$$

$$0 + y = 3$$

Simplify

$$x + y = 3$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 3$$

$$x = 3$$

Let
$$x = 0$$

$$0 + y = 3$$

$$y = 3$$

$$x + y = 3$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 3$$

$$x = 3$$

Find the y-intercept:

Let
$$x = 0$$

$$0 + y = 3$$

$$y = 3$$

Coordinates

$$x + y = 3$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 3$$

$$x = 3$$

Let
$$x = 0$$

$$0 + y = 3$$

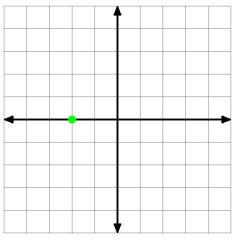
$$y = 3$$

$$(-2,0)$$
 and $(0,-2)$ for $x+y=-2$

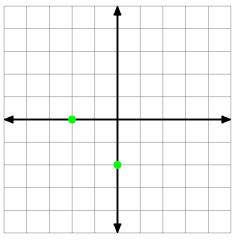
Step 2: Plot the intercepts of both equations on the same Cartesian plane.

- (-2,0) and (0,-2) for x+y=-2
- \blacktriangleright (3,0) and (0,3) for x + y = 3

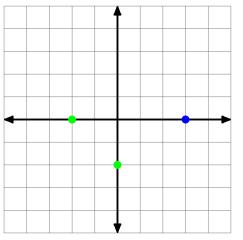
- (-2,0) and (0,-2) for x+y=-2
- \blacktriangleright (3,0) and (0,3) for x + y = 3



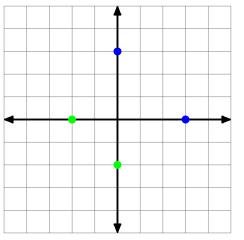
- (-2,0) and (0,-2) for x+y=-2
- \blacktriangleright (3,0) and (0,3) for x + y = 3



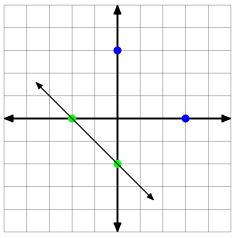
- (-2,0) and (0,-2) for x+y=-2
- \blacktriangleright (3,0) and (0,3) for x + y = 3



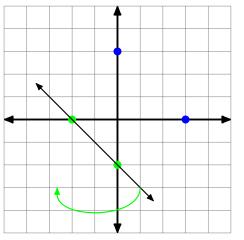
- (-2,0) and (0,-2) for x+y=-2
- \blacktriangleright (3,0) and (0,3) for x + y = 3



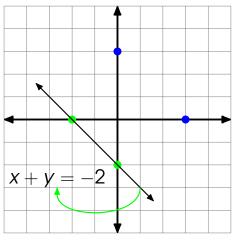
- (-2,0) and (0,-2) for x+y=-2
- ▶ (3,0) and (0,3) for x + y = 3



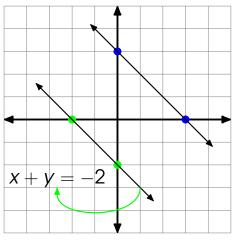
- (-2,0) and (0,-2) for x+y=-2
- \blacktriangleright (3,0) and (0,3) for x + y = 3



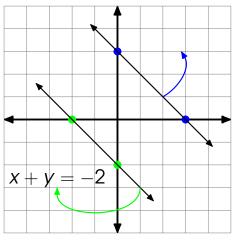
- (-2,0) and (0,-2) for x+y=-2
- \blacktriangleright (3,0) and (0,3) for x+y=3



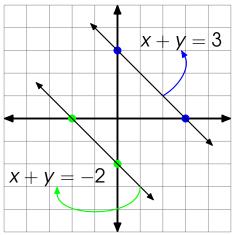
- (-2,0) and (0,-2) for x+y=-2
- \blacktriangleright (3,0) and (0,3) for x+y=3



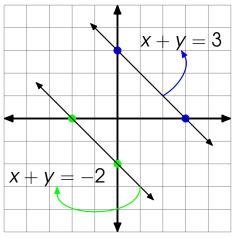
- (-2,0) and (0,-2) for x+y=-2
- \blacktriangleright (3,0) and (0,3) for x+y=3



- (-2,0) and (0,-2) for x+y=-2
- ightharpoonup (3,0) and (0,3) for x + y = 3

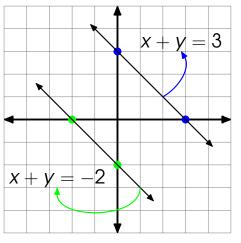


- (-2,0) and (0,-2) for x+y=-2
- ightharpoonup (3,0) and (0,3) for x + y = 3



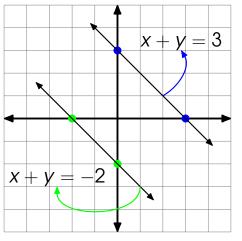
Graph: parallel

- (-2,0) and (0,-2) for x+y=-2
- \blacktriangleright (3,0) and (0,3) for x+y=3



- Graph: parallel
- ► Solutions: none

- (-2,0) and (0,-2) for x+y=-2
- ightharpoonup (3,0) and (0,3) for x + y = 3



- Graph: parallel
- Solutions: none
- Kind: Inconsistent

Graph, identify the kind of system, and describe the graph of the following system of linear equations:

$$\begin{cases} x + y = 4 \\ x - y = 2 \end{cases}$$

Step 1: Identify the x-intercept and y-intercept of each equation in the system.

Step 1: Identify the x-intercept and y-intercept of each equation in the system.

First equation

$$x + y = 4$$

$$x + y = 4$$

$$x + y = 4$$

Let
$$y = 0$$

$$x + y = 4$$

Let
$$y = 0$$

$$x + 0 = 4$$

$$x + y = 4$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 4$$

Simplify

$$x + y = 4$$

Let
$$y = 0$$

$$x + 0 = 4$$

$$x = 4$$

$$x + y = 4$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 4$$

$$x = 4$$

Coordinates

First equation	$\mathbf{x} + \mathbf{y} = 4$
----------------	-------------------------------

Let
$$y = 0$$
 $x + 0 = 4$

Simplify
$$x = 4$$

Coordinates
$$(4,0)$$

First equation	
----------------	--

$$x + y = 4$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 4$$

$$x = 4$$

$$x + y = 4$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 4$$

$$x = 4$$

Let
$$x = 0$$

$$x + y = 4$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 4$$

$$x = 4$$

Let
$$x = 0$$

$$0 + y = 4$$

$$x + y = 4$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 4$$

$$x = 4$$

Find the y-intercept:

Let
$$x = 0$$

$$0 + y = 4$$

Simplify

$$x + y = 4$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 4$$

$$x = 4$$

Let
$$x = 0$$

$$0 + y = 4$$

$$y = 4$$

$$x + y = 4$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 4$$

$$x = 4$$

Find the y-intercept:

Let
$$x = 0$$

$$0 + y = 4$$

$$y = 4$$

Coordinates

$$x + y = 4$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = 4$$

$$x = 4$$

Let
$$x = 0$$

$$0 + y = 4$$

$$y = 4$$

Example 3

Step 1: Identify the x-intercept and y-intercept of each equation in the system.

Step 1: Identify the x-intercept and y-intercept of each equation in the system.

Second equation

$$x-y=2$$

$$x-y=2$$

$$\mathbf{x} - \mathbf{y} = \mathbf{2}$$

Let
$$y = 0$$

$$\mathbf{x} - \mathbf{y} = \mathbf{2}$$

Let
$$y = 0$$

$$x - 0 = 2$$

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

Simplify

Example 3

Step 1: Identify the x-intercept and y-intercept of each equation in the system.

Second equation

$$\mathbf{x} - \mathbf{y} = \mathbf{2}$$

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Coordinates

Example 3

Step 1: Identify the x-intercept and y-intercept of each equation in the system.

Second equation

$$x-y=2$$

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

x-y=2

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

$$x - y = 2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Let
$$x = 0$$

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

Let
$$x = 0$$

$$0 - y = 2$$

$$x - y = 2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Find the y-intercept:

Let
$$x = 0$$

$$0 - y = 2$$

Simplify

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Let
$$x = 0$$

$$0 - v = 2$$

$$-y=2$$

$$x - y = 2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Find the y-intercept:

Let
$$x = 0$$

$$0 - v = 2$$

$$-y = 2$$

Use MPE

$$\mathbf{x} - \mathbf{y} = \mathbf{2}$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Let
$$x = 0$$

$$0 - v = 2$$

$$-y = 2$$

$$-1(-y) = -1(2)$$

$$\mathbf{x} - \mathbf{y} = \mathbf{2}$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Find the y-intercept:

Let
$$x = 0$$

$$0 - v = 2$$

$$-v = 2$$

$$-1(-y) = -1(2)$$

Use Distributive Property

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Let
$$x = 0$$

$$0 - y = 2$$

$$-y = 2$$

$$-1(-y)=-1(2)$$

$$y = -2$$

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Find the y-intercept:

Let
$$x = 0$$

$$0 - y = 2$$

$$-y = 2$$

$$-1(-y) = -1(2)$$

$$y = -2$$

Coordinates

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

Coordinates

$$x = 2$$

Let
$$x = 0$$

$$0 - y = 2$$

$$-y = 2$$

$$-1(-y) = -1(2)$$

$$y = -2$$

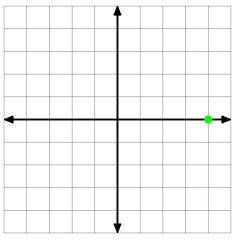
$$(0, -2)$$

• (4,0) and (0,4) for x + y = 4

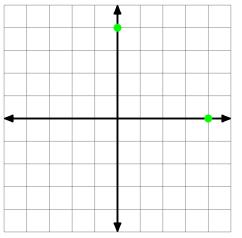
Step 2: Plot the intercepts of both equations on the same Cartesian plane.

- \blacktriangleright (4,0) and (0,4) for x+y=4
- (2,0) and (0,-2) for x-y=2

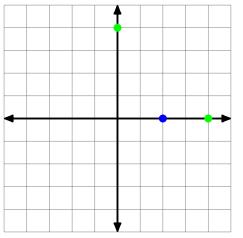
- \blacktriangleright (4,0) and (0,4) for x+y=4
- \triangleright (2,0) and (0,-2) for x-y=2



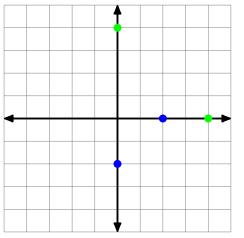
- \blacktriangleright (4,0) and (0,4) for x+y=4
- (2,0) and (0,-2) for x-y=2



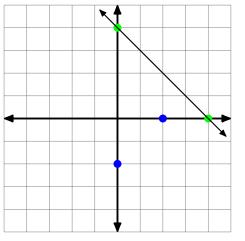
- \blacktriangleright (4,0) and (0,4) for x+y=4
- ightharpoonup (2,0) and (0,-2) for x-y=2



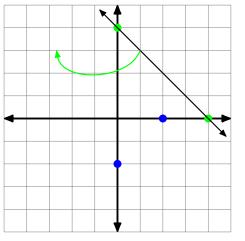
- \blacktriangleright (4,0) and (0,4) for x+y=4
- (2,0) and (0,-2) for x-y=2



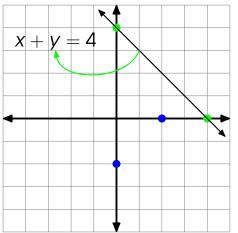
- \blacktriangleright (4,0) and (0,4) for x + y = 4
- ightharpoonup (2,0) and (0,-2) for x-y=2



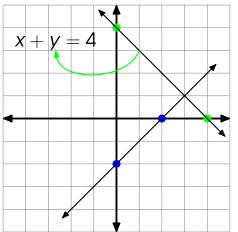
- \blacktriangleright (4,0) and (0,4) for x + y = 4
- ightharpoonup (2,0) and (0,-2) for x-y=2



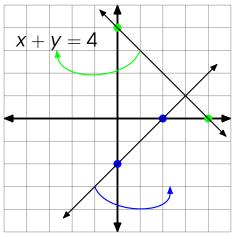
- \blacktriangleright (4,0) and (0,4) for x + y = 4
- (2,0) and (0,-2) for x-y=2



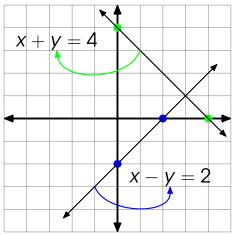
- \blacktriangleright (4,0) and (0,4) for x + y = 4
- (2,0) and (0,-2) for x-y=2



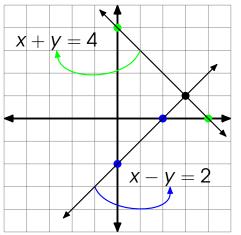
- \blacktriangleright (4,0) and (0,4) for x + y = 4
- (2,0) and (0,-2) for x-y=2



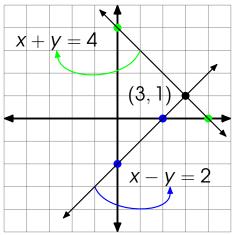
- \blacktriangleright (4,0) and (0,4) for x + y = 4
- (2,0) and (0,-2) for x-y=2



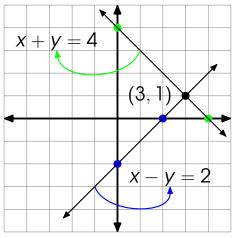
- \blacktriangleright (4,0) and (0,4) for x + y = 4
- (2,0) and (0,-2) for x-y=2



- \blacktriangleright (4,0) and (0,4) for x+y=4
- (2,0) and (0,-2) for x-y=2

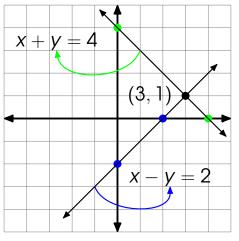


- \blacktriangleright (4,0) and (0,4) for x + y = 4
- (2,0) and (0,-2) for x-y=2



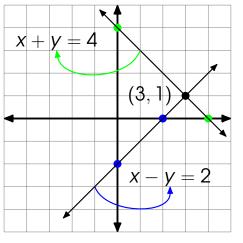
Graph: intersecting

- \blacktriangleright (4,0) and (0,4) for x + y = 4
- (2,0) and (0,-2) for x-y=2



- Graph: intersecting
- Solution: one

- ightharpoonup (4,0) and (0,4) for x + y = 4
- ▶ (2,0) and (0,-2) for x-y=2



- Graph: intersecting
- Solution: one
- Kind: Consistentindependent

Thank you for watching.