Solving Systems of Linear Equations in Two Variables by Graphing

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1. Identify the intercepts or slopes of each equation in the system.

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- 2. Draw the graphs of both equations on the same Cartesian plane.

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- 2. Draw the graphs of both equations on the same Cartesian plane.
- 3. Interpret the graphs.

Graph

Solution

| Graph | Solution |
|----------|----------|
| Parallel | None |

| Graph | Solution |
|------------|-----------------|
| Parallel | None |
| Coinciding | Infinitely many |

| Graph | Solution |
|--------------|-----------------|
| Parallel | None |
| Coinciding | Infinitely many |
| Intersecting | One |

Example 1

Draw the graph of the following system of linear equations and tell whether it has one solution, no solution, or infinitely many solutions. If it has one solution, name its ordered pair.

$$\begin{cases} y = -x - 2 \\ 2x + 2y = -4 \end{cases}$$

$$y = -x - 2$$

$$y = -x - 2$$

Find the slope:

$$y=-x-2$$

$$m = -1$$

$$y=-x-2$$

Find the slope:

$$m = -1$$

$$y=-x-2$$

Find the slope:

$$m = -1$$

$$b = -2$$

Second equation
$$2x + 2y = -4$$

$$2x + 2y = -4$$

$$2x + 2y = -4$$

Let
$$y = 0$$

$$2x + 2y = -4$$

Let
$$y = 0$$

$$2x + 2(0) = -4$$

$$2x + 2y = -4$$

Let
$$y = 0$$

$$2x + 2(0) = -4$$

$$2x + 0 = -4$$

$$2x + 2y = -4$$

Let
$$y = 0$$

$$2x + 2(0) = -4$$

$$2x + 0 = -4$$

$$\frac{2x}{2} = \frac{-4}{2}$$

$$2x + 2y = -4$$

Let
$$y = 0$$

$$2x + 2(0) = -4$$

$$2x + 0 = -4$$

$$\frac{2x}{2} = \frac{-4}{2}$$

$$x = -2$$

$$2x + 2y = -4$$

Let
$$y = 0$$

$$2x + 2(0) = -4$$

$$2x + 0 = -4$$

$$\frac{2x}{2} = \frac{-4}{2}$$

$$x = -2$$

$$(-2,0)$$

Second equation
$$2x + 2y = -4$$

$$2x + 2y = -4$$

Second equation 2x + 2y = -4

$$2x + 2y = -4$$

Let
$$x = 0$$

$$2x + 2y = -4$$

Let
$$x = 0$$

$$2(0) + 2y = -4$$

$$2x + 2y = -4$$

Let
$$x = 0$$

$$2(0) + 2y = -4$$

$$0 + 2y = -4$$

$$2x + 2y = -4$$

Let
$$x = 0$$

$$2(0) + 2y = -4$$

$$0 + 2y = -4$$

Use Division Property
$$\frac{2y}{2} = \frac{-4}{2}$$

$$\frac{2y}{2} = \frac{-2}{2}$$

$$2x + 2y = -4$$

Let
$$x = 0$$

$$2(0) + 2y = -4$$

$$0 + 2y = -4$$

$$\frac{2y}{2} = \frac{-4}{2}$$

$$y = -2$$

$$2x + 2y = -4$$

Let
$$x = 0$$

$$2(0) + 2y = -4$$

$$0 + 2y = -4$$

$$\frac{2y}{2} = \frac{-4}{2}$$

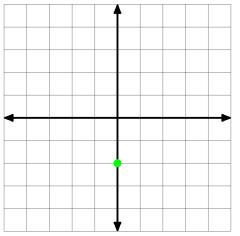
$$y = -2$$

$$(0, -2)$$

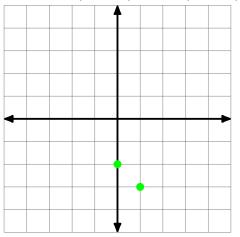
►
$$m = -1 = \frac{\text{rise}}{\text{run}}$$
 and $b = -2$ for $y = -x - 2$

- ► $m = -1 = \frac{\text{rise}}{\text{run}}$ and b = -2 for y = -x 2► (-2,0) and (0,-2) for 2x + 2y = -4

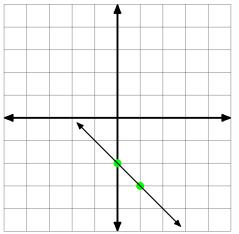
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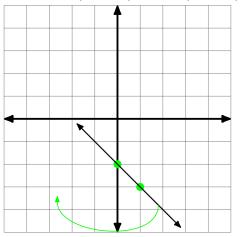
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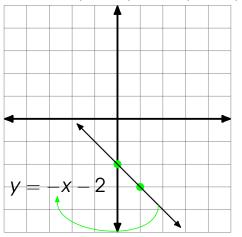
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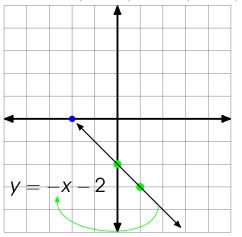
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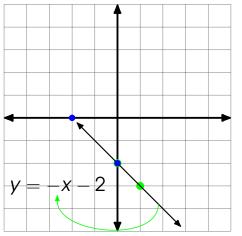
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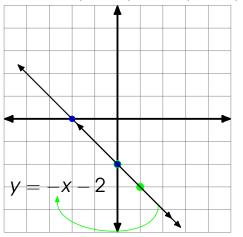
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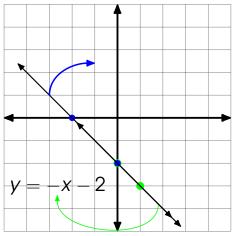
- ► $m = -1 = \frac{\text{rise}}{\text{run}}$ and b = -2 for y = -x 2► (-2,0) and (0,-2) for 2x + 2y = -4



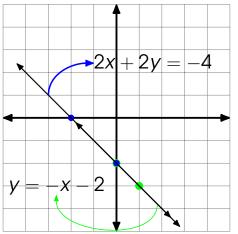
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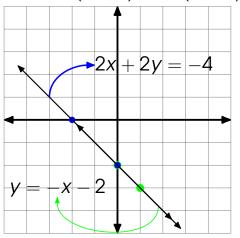


- ► $m = -1 = \frac{\text{rise}}{\text{run}}$ and b = -2 for y = -x 2► (-2,0) and (0,-2) for 2x + 2y = -4



►
$$m = -1 = \frac{\text{rise}}{\text{run}}$$
 and $b = -2$ for $y = -x - 2$
► $(-2,0)$ and $(0,-2)$ for $2x + 2y = -4$

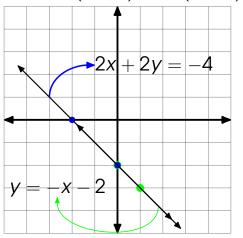
$$(-2,0)$$
 and $(0,-2)$ for $2x+2y=-2$



Graph: coinciding

►
$$m = -1 = \frac{\text{rise}}{\text{run}}$$
 and $b = -2$ for $y = -x - 2$
► $(-2,0)$ and $(0,-2)$ for $2x + 2y = -4$

$$(-2,0)$$
 and $(0,-2)$ for $2x+2y=-2$



- Graph: coinciding
- Solutions: infinitely many

Example 2

Draw the graph of the following system of linear equations and tell whether it has one solution, no solution, or infinitely many solutions. If it has one solution, name its ordered pair.

$$\begin{cases} x + y = -2 \\ y = -x + 3 \end{cases}$$

Example 2

Step 1: Identify the intercepts or slopes of each equation in the system.

$$x + y = -2$$

$$x + y = -2$$

$$x + y = -2$$

Let
$$y = 0$$

$$x + y = -2$$

Let
$$y = 0$$

$$x + 0 = -2$$

$$x + y = -2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

Simplify

$$x + y = -2$$

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$x+y=-2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

Coordinates

| Firet | equation | |
|---------|----------|--|
| 1 11 31 | equalion | |

$$x + y = -2$$

Let
$$y = 0$$
 $x + 0 = -2$

Simplify
$$x = -2$$

Coordinates
$$(-2,0)$$

$$x+y=-2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

$$x + y = -2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

Let
$$x = 0$$

$$x+y=-2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

Let
$$x = 0$$

$$0 + y = -2$$

$$x+y=-2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

Find the y-intercept:

Let
$$x = 0$$

$$0 + y = -2$$

Simplify

$$x+y=-2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

Let
$$x = 0$$

$$0 + v = -2$$

$$y = -2$$

$$x+y=-2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

Find the y-intercept:

Let
$$x = 0$$

$$0 + v = -2$$

$$y = -2$$

Coordinates

$$x+y=-2$$

Find the x-intercept:

Let
$$y = 0$$

$$x + 0 = -2$$

$$x = -2$$

$$(-2,0)$$

Let
$$x = 0$$

$$0 + v = -2$$

$$y = -2$$

$$(0, -2)$$

Example 2

Step 1: Identify the intercepts or slopes of each equation in the system.

Step 1: Identify the intercepts or slopes of each equation in the system.

Second equation

$$y = -x + 3$$

Second equation

$$y = -x + 3$$

Find the slope:

$$y=-x+3$$

$$m = -1$$

Second equation

$$y=-x+3$$

Find the slope:

$$m = -1$$

$$y=-x+3$$

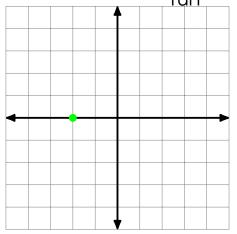
$$m = -1$$

$$b = 3$$

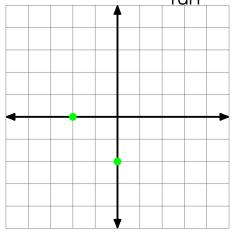
$$(-2,0)$$
 and $(0,-2)$ for $x+y=-2$

- (-2,0) and (0,-2) for x+y=-2
- $ightharpoonup m = -1 = \frac{\text{rise}}{\text{run}}$ and b = 3 for y = -x + 3

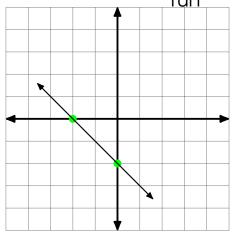
- (-2,0) and (0,-2) for x+y=-2



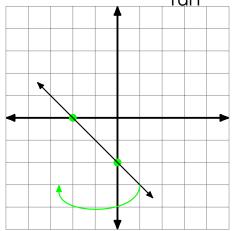
- (-2,0) and (0,-2) for x+y=-2



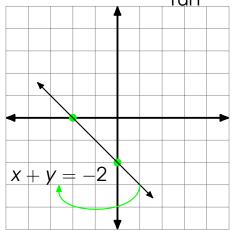
(-2,0) and (0,-2) for x+y=-2



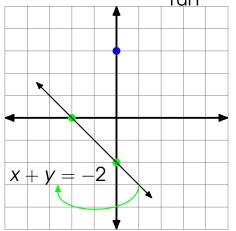
(-2,0) and (0,-2) for x+y=-2



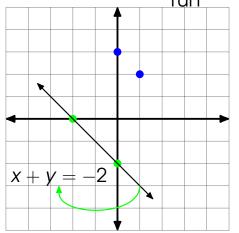
- (-2,0) and (0,-2) for x+y=-2



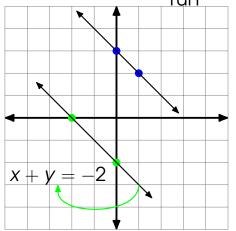
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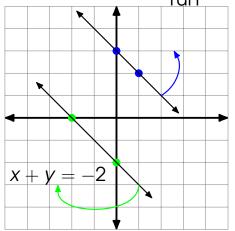
- (-2,0) and (0,-2) for x+y=-2



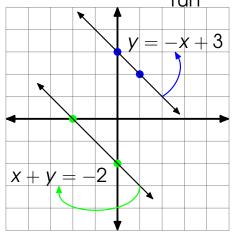
- (-2,0) and (0,-2) for x+y=-2



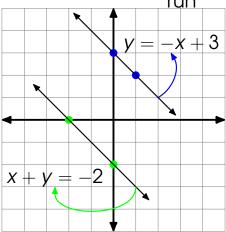
(-2,0) and (0,-2) for x+y=-2



- (-2,0) and (0,-2) for x+y=-2

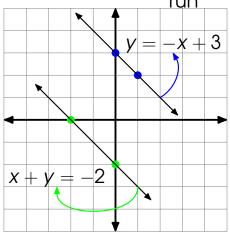


$$(-2,0)$$
 and $(0,-2)$ for $x+y=-2$



Graph: parallel

$$(-2,0)$$
 and $(0,-2)$ for $x+y=-2$



- Graph: parallel
- ► Solutions: none

Draw the graph of the following system of linear equations and tell whether it has one solution, no solution, or infinitely many solutions. If it has one solution, name its ordered pair.

$$\begin{cases} y = -x + 4 \\ x - y = 2 \end{cases}$$

Step 1: Identify the intercepts or slopes of each equation in the system.

$$y = -x + 4$$

$$y = -x + 4$$

Find the slope:

| First | equo | ıtion |
|--------------|------|-------|
| | 1 | |

$$y=-x+4$$

$$m = -1$$

$$y=-x+4$$

Find the slope:

$$m = -1$$

| First equation | y = |
|----------------|------------|
|----------------|------------|

Find the slope: m = -1

Find the y-intercept: b = 4

-x + 4

Step 1: Identify the intercepts or slopes of each equation in the system.

$$x-y=2$$

$$x-y=2$$

$$x-y=2$$

Let
$$y = 0$$

Step 1: Identify the intercepts or slopes of each equation in the system.

Second equation

$$x-y=2$$

Let
$$y = 0$$

$$x - 0 = 2$$

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

Simplify

Step 1: Identify the intercepts or slopes of each equation in the system.

 $\mathbf{x} - \mathbf{y} = \mathbf{2}$

Let
$$y = 0$$
 $x - 0 = 2$

Simplify
$$x = 2$$

$$\mathbf{x} - \mathbf{y} = \mathbf{2}$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Coordinates

Step 1: Identify the intercepts or slopes of each equation in the system.

| Second equation | $\mathbf{x} - \mathbf{y} = 2$ |
|-----------------|-------------------------------|
|-----------------|-------------------------------|

Let
$$y = 0$$
 $x - 0 = 2$

Simplify
$$x = 2$$

Coordinates
$$(2,0)$$

Step 1: Identify the intercepts or slopes of each equation in the system.

Second equation

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Let
$$x = 0$$

$$x - y = 2$$

Find the x-intercept:

Let
$$y = 0$$
 $x - 0 = 2$

Simplify
$$x = 2$$

Coordinates
$$(2,0)$$

Let
$$x = 0$$
 $0 - y = 2$

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Find the y-intercept:

Let
$$x = 0$$

$$0 - y = 2$$

Simplify

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Find the y-intercept:

Let
$$x = 0$$

$$0 - y = 2$$

$$-y = 2$$

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Find the y-intercept:

Let
$$x = 0$$

$$0 - v = 2$$

$$-y = 2$$

Use MPE

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$
 $x - 0 = 2$

Simplify
$$x = 2$$

Coordinates
$$(2,0)$$

Find the y-intercept:

Let
$$x = 0$$
 $0 - y = 2$

Simplify
$$-y = 2$$

Use MPE
$$-1(-y) = -1(2)$$

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

$$x - 0 = 2$$

$$x = 2$$

Find the y-intercept:

Let
$$x = 0$$

$$0 - v = 2$$

$$-v = 2$$

$$-1(-y) = -1(2)$$

Simplify

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$
 $x - 0 = 2$

Simplify
$$x = 2$$

Coordinates
$$(2,0)$$

Find the y-intercept:

Let
$$x = 0$$
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Simplify
$$-y=2$$

Use MPE
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Find the x-intercept:

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$$x = 0$$

$$0 - y = 2$$

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$$-1(-y) = -1(2)$$

$$y = -2$$

Coordinates

$$x-y=2$$

Find the x-intercept:

Let
$$y = 0$$

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$$x = 2$$

Find the y-intercept:

Let
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$$-v = 2$$

$$-1(-y) = -1(2)$$

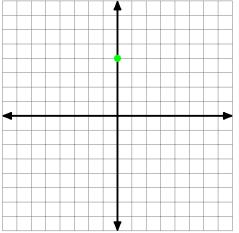
$$y = -2$$

$$(0, -2)$$

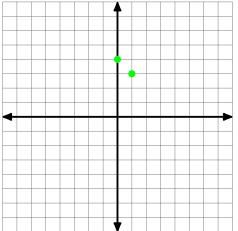
$$ightharpoonup m=-1=rac{\mathrm{rise}}{\mathrm{run}}$$
 and $b=4$ for $y=-x+4$

- ► $m = -1 = \frac{\text{rise}}{\text{run}}$ and b = 4 for y = -x + 4► (2,0) and (0,-2) for x y = 2

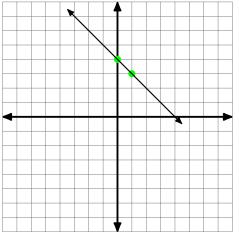
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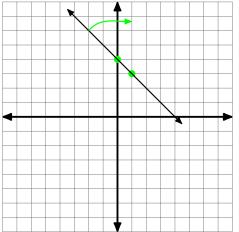
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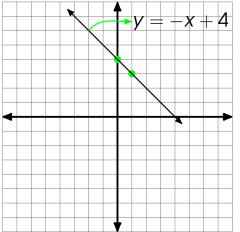
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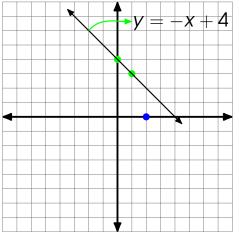
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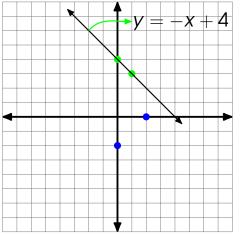
- m = -1 = rise/run and b = 4 for y = -x + 4
 (2,0) and (0, -2) for x y = 2



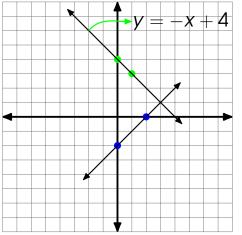
- m = -1 = rise/run and b = 4 for y = -x + 4
 (2,0) and (0, -2) for x y = 2



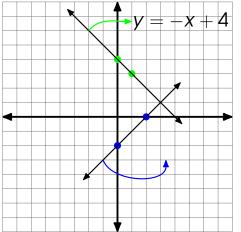
- m = -1 = rise/run and b = 4 for y = -x + 4
 (2,0) and (0, -2) for x y = 2



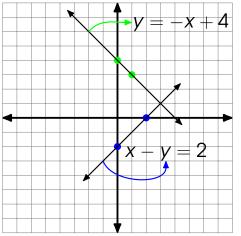
- m = -1 = rise/run and b = 4 for y = -x + 4
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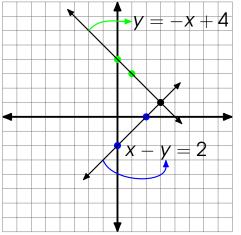
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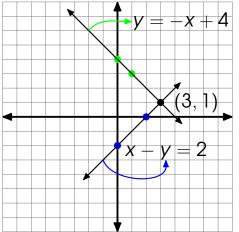
- m = -1 = rise/run and b = 4 for y = -x + 4
 (2,0) and (0, -2) for x y = 2



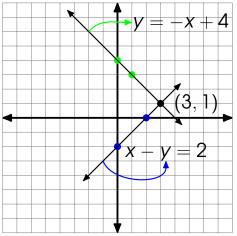
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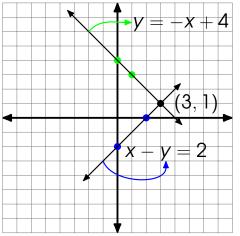


•
$$(2,0)$$
 and $(0,-2)$ for $x-y=2$

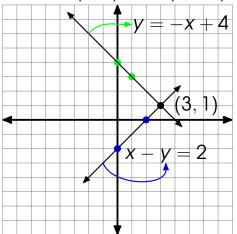


Graph: intersecting

•
$$(2,0)$$
 and $(0,-2)$ for $x-y=2$



- Graph: intersecting
- Solution: one



- Graph: intersecting
- Solution: one
- Solution set: (3, 1)

Thank you for watching.