

Lesson 4.3.1: Applying Theorems on Triangle Inequality

Practice Exercises 4.3.1

A. Tell whether a triangle can be constructed with segments having these lengths. Write *Yes* or *No*.

- 1. 6, 8, 10
- 2. 4, 4, 7
- 3. 4, 5, 10
- 4. 4, 11, 12
- 5. 6, 8, 17

B. The measures of two sides of a triangle are given. Between what two numbers must the length of the third side fall?

- 1. 8 and 11
- 2. 20 and 30
- 3. 4 and 70
- 4. 7.5 and 2.5
- 5. 5 and 9

C. Given the lengths of the sides, identify the largest and smallest angle in each triangle.

- 1. $\triangle ABC$: $AB = 15, BC = 8$, and $AC = 12$
- 2. $\triangle DEF$: $DE = 5, EF = 8$, and $DF = 12$
- 3. $\triangle GHI$: $GH = 4, HI = 6$, and $GI = 3$
- 4. $\triangle JKL$: $JK = 4.9, KL = 4.5$, and $JL = 5.2$
- 5. $\triangle MNP$: $MN = 3\frac{2}{3}, NP = 6\frac{1}{2}$ and $MP = 5\frac{1}{4}$

D. Given the measures of two angles, identify the longest and shortest side in each triangle.

- 1. $\triangle ABC$: $m\angle A = 20^\circ$ and $m\angle B = 103^\circ$
- 2. $\triangle DEF$: $m\angle D = 17^\circ$ and $m\angle F = 53^\circ$
- 3. $\triangle GHI$: $m\angle H = 30^\circ$ and $m\angle I = 100^\circ$
- 4. $\triangle JKL$: $m\angle J = 26^\circ$ and $m\angle K = 95^\circ$
- 5. $\triangle MNP$: $m\angle N = 112^\circ$ and $m\angle P = 30^\circ$

E. List the sides of each triangle in order from shortest to longest if the angles have the indicated measures.

- 1. $\triangle ABC$: $m\angle A = 7x + 25, m\angle B = 96 - 5x$ and $m\angle C = 12x + 3$
- 2. $\triangle DEF$: $m\angle D = 5x + 20, m\angle E = 4x + 18$ and $m\angle F = 7x + 12$
- 3. $\triangle GHI$: $m\angle G = 8x + 6, m\angle H = 4x - 2$ and $m\angle I = 9x + 8$
- 4. $\triangle JKL$: $m\angle J = 16x + 3, m\angle K = 4x - 3$ and $m\angle L = 7x - 9$
- 5. $\triangle MNP$: $m\angle M = 16x - 1, m\angle N = 7x + 3$ and $m\angle P = 8x - 8$

Activity 4.3.1

A. Tell whether a triangle can be constructed with segments having these lengths. Write *Yes* or *No*.

- 1. 5, 7, 13
- 2. 5, 5, 8
- 3. 5, 6, 11
- 4. 5, 10, 11
- 5. 7, 9, 16

B. The measures of two sides of a triangle are given. Between what two numbers must the length of the third side fall?

- 1. 9 and 10
- 2. 10 and 20
- 3. 5 and 60
- 4. 6.5 and 3.5
- 5. 6 and 10

C. Given the lengths of the sides, identify the largest and smallest angle in each triangle.

- 1. $\triangle ABC$: $AB = 16, BC = 9$, and $AC = 11$
- 2. $\triangle DEF$: $DE = 4, EF = 9$, and $DF = 11$
- 3. $\triangle GHI$: $GH = 5, HI = 7$, and $GI = 4$
- 4. $\triangle JKL$: $JK = 5.9, KL = 4.5$, and $JL = 6.2$
- 5. $\triangle MNP$: $MN = 4\frac{1}{3}, NP = 5\frac{1}{2}$ and $MP = 7\frac{3}{4}$

D. Given the measures of two angles, identify the longest and shortest side in each triangle.

- 1. $\triangle ABC$: $m\angle A = 25^\circ$ and $m\angle B = 113^\circ$
- 2. $\triangle DEF$: $m\angle D = 18^\circ$ and $m\angle F = 57^\circ$
- 3. $\triangle GHI$: $m\angle H = 35^\circ$ and $m\angle I = 110^\circ$
- 4. $\triangle JKL$: $m\angle J = 23^\circ$ and $m\angle K = 94^\circ$
- 5. $\triangle MNP$: $m\angle N = 117^\circ$ and $m\angle P = 20^\circ$

E. List the sides of each triangle in order from shortest to longest if the angles have the indicated measures.

- 1. $\triangle ABC$: $m\angle A = 7x - 2, m\angle B = 20x - 10$ and $m\angle C = 6x - 6$
- 2. $\triangle DEF$: $m\angle D = 7x - 4, m\angle E = 17x - 4$ and $m\angle F = 2x + 6$
- 3. $\triangle GHI$: $m\angle G = 10x + 5, m\angle H = 9x - 7$ and $m\angle I = 4x - 2$
- 4. $\triangle JKL$: $m\angle J = 8x + 3, m\angle K = 6x + 1$ and $m\angle L = 5x + 5$
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