

Activity 1.4.1: Multiplication and Division of Rational Algebraic Expressions

Total points = 33

A. Solutions

1.  $\frac{12mn^2}{6xy^2} \cdot \frac{9x^2y^2}{4m^2n^2}$  ✓  
 $= \frac{9x}{2m}$  ✓

2.  $\frac{x^2-y^2}{2xy} \cdot \frac{y^2}{x+y}$  ✓  
 $= \frac{(x-y)(x+y)}{2xy} \cdot \frac{y^2}{x+y}$  ✓  
 $= \frac{2xy}{y(x-y)}$  ✓  
 $= \frac{2x}{x^2-2x}$  ✓

3.  $\frac{x^2-4x-5}{x^2-3x-10} \cdot \frac{x^2-4x-5}{x^2-4}$  ✓  
 $= \frac{(x-5)(x+2)}{(x-5)(x+2)} \cdot \frac{(x-5)(x+1)}{(x-2)(x+2)}$  ✓  
 $= \frac{x(x+1)}{(x+2)^2}$  ✓

4.  $\frac{x^2+4x+4}{x^2+3x+2} \cdot \frac{x^2-1}{x^2-4}$  ✓  
 $= \frac{(x+2)(x+2)}{(x+1)(x+2)} \cdot \frac{(x-1)(x+1)}{(x-2)(x+2)}$  ✓  
 $= \frac{x-1}{x-2}$  ✓

5.  $\frac{a^2+2ab+b^2}{a^2-b^2} \cdot \frac{a-b}{a+b}$  ✓  
 $= \frac{(a+b)(a+b)}{(a-b)(a+b)} \cdot \frac{a-b}{a+b}$  ✓  
 $= 1$  ✓

B. Solutions

1.  $\frac{14x^2}{20y^2} \div \frac{56x^2}{y}$  ✓  
 $= \frac{14x^2}{20y^2} \cdot \frac{y}{56x^2}$  ✓  
 $= \frac{1}{80y}$  ✓

2.  $\frac{4a-4b}{30a^2} \div \frac{a-b}{9a}$  ✓  
 $= \frac{4a-4b}{30a^2} \cdot \frac{9a}{a-b}$  ✓  
 $= \frac{4(a-b)}{30a^2} \cdot \frac{9a}{a-b}$  ✓  
 $= \frac{6}{5a}$  ✓

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 $= \frac{9x}{2m}$  ✓

2.  $\frac{x^2-y^2}{2xy} \cdot \frac{y^2}{x+y}$  ✓  
 $= \frac{(x-y)(x+y)}{2xy} \cdot \frac{y^2}{x+y}$  ✓  
 $= \frac{y(x-y)}{2x}$  ✓

3.  $\frac{x^2-2x}{x^2-3x-10} \cdot \frac{x^2-4x-5}{x^2-4}$  ✓  
 $= \frac{(x-5)(x+2)}{(x-5)(x+2)} \cdot \frac{(x-5)(x+1)}{(x-2)(x+2)}$  ✓  
 $= \frac{x(x+1)}{(x+2)^2}$  ✓

4.  $\frac{x^2+4x+4}{x^2+3x+2} \cdot \frac{x^2-1}{x^2-4}$  ✓  
 $= \frac{(x+2)(x+2)}{(x+1)(x+2)} \cdot \frac{(x-1)(x+1)}{(x-2)(x+2)}$  ✓  
 $= \frac{x-1}{x-2}$  ✓

5.  $\frac{a^2+2ab+b^2}{a^2-b^2} \cdot \frac{a-b}{a+b}$  ✓  
 $= \frac{(a+b)(a+b)}{(a-b)(a+b)} \cdot \frac{a-b}{a+b}$  ✓  
 $= 1$  ✓

B. Solutions

1.  $\frac{14x^2}{20y^2} \div \frac{56x^2}{y}$  ✓  
 $= \frac{14x^2}{20y^2} \cdot \frac{y}{56x^2}$  ✓  
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2.  $\frac{4a-4b}{30a^2} \div \frac{a-b}{9a}$  ✓  
 $= \frac{4a-4b}{30a^2} \cdot \frac{9a}{a-b}$  ✓  
 $= \frac{4(a-b)}{30a^2} \cdot \frac{9a}{a-b}$  ✓  
 $= \frac{6}{5a}$  ✓

3.  $\frac{x^2-4}{x^2+4x+4} \div \frac{x^2-x-2}{x^2+3x+2}$  ✓  
 $= \frac{x^2-4}{x^2-4} \cdot \frac{x^2+3x+2}{x^2+3x+2}$  ✓  
 $= \frac{(x-2)(x+2)}{(x+2)(x+2)} \cdot \frac{(x+1)(x+2)}{(x-2)(x+1)}$  ✓  
 $= 1$  ✓

4.  $\frac{x^2-2x-3}{x^2-3x} \div \frac{x^2-4}{x^2+2x}$  ✓  
 $= \frac{x^2-2x-3}{x^2-2x-3} \cdot \frac{x^2+2x}{x^2+2x}$  ✓  
 $= \frac{(x-3)(x+1)}{x(x-3)} \cdot \frac{x(x+2)}{(x-2)(x+2)}$  ✓  
 $= \frac{x+1}{x-2}$  ✓

5.  $\frac{x^2-4}{x^2+2x} \div \frac{x^2+x-6}{2x+4}$  ✓  
 $= \frac{x^2-4}{x^2-4} \cdot \frac{2x+4}{2x+4}$  ✓  
 $= \frac{x^2+2x}{(x-2)(x+2)} \cdot \frac{x^2+x-6}{2(x+2)}$  ✓  
 $= \frac{x(x+2)}{x(x+2)} \cdot \frac{2(x+2)}{(x-2)(x+3)}$  ✓  
 $= \frac{2(x+2)}{x(x+3)}$  ✓