

Lesson 4.6.1: Basic Concepts of Probability

**Probability:** a measure that is associated with how certain we are of outcomes of a particular experiment or activity  
**Chance Experiment:** an activity which can be repeated over and over again and which have well-defined results  
**Outcome:** a result of an experiment  
**Sample Space:** the list of all the possible outcomes of an experiment. Each individual outcome is a sample point.  
**Ways to Represent a Sample Space:**

- List the possible outcomes
- Create a tree diagram
- Create a Venn diagram

**Event:** any combination of outcomes  
**Equally likely:** each outcome of an experiment occurs with equal probability

Practice Exercises 4.6.1

- A. Write the sample space for each experiment.
- A toss of a coin and a die.
  - A coin tossed three times.
  - A toss of two coins once.
  - A vowel of the English alphabet picked at random from a box.
  - A roll of a die and tossing a coin.
- B. Do as directed in each of the following.
- Let a coin and a die be tossed. Give the elements of the following events.
    - $A = \{\text{head or tail and an odd number}\}$
    - $B = \{\text{an outcome with a number less than 4}\}$
    - $C = \{\text{tails and an even number}\}$
    - $D = \{\text{heads and a number less than 5}\}$
    - $E = \{\text{an outcome with a number at most 4}\}$
  - A pair of dice is rolled. Write the elements of each event.
    - $G = \{\text{the largest of one of the two numbers is 3}\}$
    - $H = \{\text{the two numbers whose sum is at most 5}\}$
    - $I = \{\text{the pair of numbers have an even sum}\}$
    - $J = \{\text{the pair of numbers whose sum is 6 but none of the two is even}\}$

Activity 4.6.1

- A. Write the sample space for each experiment.
- A toss of a die and a coin.
  - A coin tossed two times.
  - A toss of three coins once.
  - A day of the week picked at random from a box.
- B. Do as directed in each of the following.
- Let a die and a coin be tossed. Give the elements of the following events.
    - $A = \{\text{an even number and a head or tail}\}$
    - $B = \{\text{an outcome with a number greater than 4}\}$
    - $C = \{\text{an odd number and tails}\}$
    - $D = \{\text{a number less than 3 and heads}\}$
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