Area of Sectors and Segments of a Circle

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September 21, 2019



Sector of a Circle

Sector: a region in the circle bounded by two radii and the minor arc they determine

The area of a sector is represented by $A = \frac{n}{360}\pi r^2$, where n is the number of degrees in the central angle of a sector.



Example

To solve for the area of the shaded region:

$$n = 90^{\circ}$$

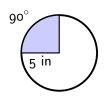
$$r = 5 \text{ in.}$$

$$A = \frac{n}{360}\pi r^{2}$$

$$A = \frac{90}{360}(\pi)(5^{2})$$

$$A = \frac{1}{4}(\pi)(25)$$

$$A = \frac{25}{4}\pi \text{ in}^{2}$$



Segment of a Circle

Segment: a region bounded by an arc and the chord of the arc The **area of a segment** of a circle is found by subtracting the area of a triangle from the area of a sector.

$$A_{segment} = A_{sector} - A_{triangle}$$



Example

To solve for the area of the shaded region: $n = 90^{\circ}$, r = 5 in.

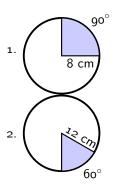
$$\begin{split} A_{sector} &= \frac{n}{360} \pi r^2 & A_{triangle} &= \frac{1}{2} bh \\ A_{sector} &= \frac{90}{360} (\pi) (5^2) & A_{triangle} &= \frac{1}{2} (5) (5) \\ A_{sector} &= \frac{1}{4} (\pi) (25) & A_{triangle} &= \frac{25}{2} \text{ in}^2 \\ A_{sector} &= \frac{25}{4} \pi \text{ in}^2 \end{split}$$

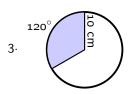


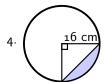
$$\begin{aligned} A_{segment} &= A_{sector} - A_{triangle} \\ A_{segment} &= \frac{25}{4} \pi - \frac{25}{2} \\ A_{segment} &= -\frac{25}{2} + \frac{25}{4} \pi \text{ in}^2 \end{aligned}$$

Practice Exercises

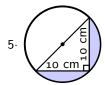
Find the area of each shaded region/s in each figure. Express your answer in terms of π .

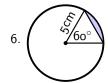


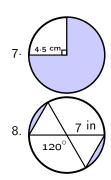




Practice Exercises

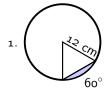


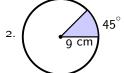


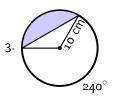


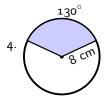
Problem Set

Find the area of each shaded region/s in each figure. Express your answer in terms of π .









Problem Set

