

I. OBJECTIVES	DAY 1	DAY 2	DAY 3	DAY 4	DAY 5
Learning Competencies/ Objectives:	 Define the factorial notation; Find the factorial notation to determine whether a binomial is a factor of a given polynomial; and, Demonstrate perseverance and willingness in solving problems. 	tal principle of counting; 2. Calculate the fundamental principle of counting to determine whether a bino-	 Illustrate the permutation; Compute the permutation to determine whether a binomial is a factor of a given polynomial; and, Exhibit enjoyment and self-reliance in solving problems. 	 Describe the distinguishable permutation; Compute the distinguishable permutation to determine whether a binomial is a factor of a given polynomial; and, Display enjoyment and interest in solving problems. 	mutations;
II. CONTENT	PATTERNS AND ALGEBRA				
	Factorial Notation	Fundamental Principle of Counting	Permutation	Distinguishable Permutation	Circular Permutations
III. LEARNING RESOURCES					
A. References					
1. Teacher's Guide Pages	pp. 290–296	pp. 297–304	pp. 305–310	pp. 311–318	pp. 319–324
2. Learner's Materials Pages	pp. 275–281	pp. 282–289	pp. 290–295	pp. 296–303	pp. 304–309
3. Textbook Pages	pp. 303–309	pp. 310–317	pp. 318–323	pp. 324–331	pp. 332–337
4. Additional Materials from Learning Resources Portal					
B. Other Learning Resources	Flashcards	Flashcards	Flashcards	Flashcards	Flashcards
IV. PROCEDURES				1	

A. Rev	iewi	ng Previous				
Lesson	\mathbf{or}	Presenting				
New Lesson						

Factorial Notation

n-Factorial: the product of the positive integer n and all the positive integers less than n. For any natural number n,

$$n! \ n(n-1)(n-2)\dots(3)\cdot(2)\cdot(1).$$

For the number 0,

0! 1.

The number of permutations of n objects taken r at a time

$$P(n,r) \ \frac{n!}{(n-r)!}, \ n \ge r.$$

If n r, then

$$P(n,r)$$
 $n!$

Fundamental Principle of Counting: If one thing can occur in m ways and a second thing can occur in n ways, and a third thing can occur in p ways, and so on, then the sequence of things can occur in $m \times n \times p \times \dots$ ways.

The Fundamental

Principle of Counting

Circular Permutations

Circular Permutations: a special case of permutation where the arrangement of things is in a circular pattern The number of circular permutations of n different things is:

$$(n-1)! (n-1)(n-2)\cdots(2)(1)$$

The number of permutations of n different things around a key ring and the like is:

$$\frac{(n-1)!}{2} \frac{(n-1)(n-2)\dots(2)(1)}{2}$$

Permutation

Permutations: the different possible arrangements of a set of objects.

Distinguishable Permutation

Distinguishable Permutations: the permutations of a set of objects where some of them are alike

The number of distinguishable permutations of n objects when p are alike, q are alike, s are alike, and so on, is given by

$$P \frac{n!}{p!q!r!}$$

B. Establishing a Pur-	The purpose of this lesson	The purpose of this lesson	The purpose of this lesson	The purpose of this lesson	The purpose of this lesson
pose for the Lesson	is to enable the students to	is to enable the students to	is to enable the students to	is to enable the students to	is to enable the students to
	solve real life problems in-	solve real life problems in-	solve real life problems in-	solve real life problems in-	solve real life problems in-
	volving the factorial nota-	volving the fundamental prin-	volving the permutation.	volving the distinguishable	volving the circular permu-
	tion.	ciple of counting.		permutation.	tations.

$\mathbf{C}.$	Discussing	\mathbf{New}
Conc	epts and Prac	cticing
New	Skills #1	

Practice Exercises

A. Evaluate.

- 1. 6! 3. 9! 5! 4!
- 2. 4! 5!4. 7! -5. $\frac{6!}{4!3!}$
- B. Simplify by factorization.

1.
$$\frac{7!-6?}{6}$$
 $\frac{6! \ 4!}{31}$ $\frac{7! \ 6!-5!}{5!}$

$$\frac{2!}{6!} \cdot \frac{7! - 6!}{6!} \cdot \frac{8! - 6}{55}$$

Practice Exercises

Find the number of possible outcomes for each scenario using the fundamental counting principle.

- 1. Boys and girls in a family with two children.
- 2. Choosing a cellphone that comes in black, white, or transparent that is 3G or 4G.
- 3. A choice of muffin or toast bread with coffee, milk, or juice.
- 4. Basketball uniform in white, red, blue, yellow, or green which comes in sizes small, medium, or large.
- 5. A die is rolled thrice.

Practice Exercises

Solve each permutation problem completely.

- 1. A teacher wants to assign 4 different tasks to her 4 students. In how many possible ways can she do it?
- 2. In a certain general assembly, three major prizes are at stake. In how many ways can the first, second, and third prizes be drawn from a box containing 120 names?
- 3. In how many different ways can 5 bicycles be parked if there are 7 available parking spaces?
- 4. There are 8 basketball teams competing for the top 4 standings in order to move up to the semi-finals. Find the number of possible rankings of the four top teams.
- 5. In how many different ways can 12 people occupy the 12 seats in a front row of a minitheater?

Practice Exercises

A. Find the number of distinguishable permutations for the following.

- 1. 3. 5. ALAPA**AHP**MPA**PBYWIIBX**NI
- 2. 4. MAGSABAKAYAN

Practice Exercises

Solve each problem completely.

- 1. In how many ways can 10 different colored toy horses be arranged in a merry-go-round?
- 2. In how many ways can 9 people be seated at a round table?
- 3. In how many ways can nine different colored beads be arranged on a bracelet?
- 4. In how many ways can eight keys be arranged on a key ring?
- 5. Snow white arranges the seven dwarfs around a maypole.
 - a. In how many ways can she arrange them?
 - b. In how many ways can she do it if Doc and Sleepy are to be together?
 - c. In how many ways can she do it if Grumpy and Dopey must not be together?

D. Discussing New Concepts and Practicing New Skills #2 C. Simplify the following.	B. Find the number of distinguishable permutations for each situation.
1. $\frac{n!}{n}$ 3. $\frac{(n\ 2)!}{n!}$ $\frac{(n\ 1)!}{(n-1)!}$ 2. $\frac{(n\ 1)!}{n!}$ 5. $\frac{(n\ 1)!}{(n-1)!}$	1. In how many ways can two blue marbles and four red marbles be arranged in a row?
	2. In how many different ways can five red balls, two white balls, and seven blue balls be arranged in a row?
	3. Faith bought four vanilla ice-cream cones, three chocolate cones, two strawberry cones, and five ube-langka cones for her 14 tutors.
	In how many ways can she distribute the cones among her tutors?

E. Developing I	Mastery
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Problem Set

A. Evaluate.

- $1. \quad 7! \quad 3. \quad 8! \quad \quad 3!$ 6!
- 2. 3! 5!4. 9! -5.
- B. Simplify by factorization.

1.
$$6! - 5! \cdot \frac{7! \ 5!}{5} \cdot \frac{7! \ 5!}{60} \cdot \frac{6! \ 5! - 4}{4!}$$

- C. Simplify the following.

1.
$$\frac{n!}{(n-1)!} \frac{3!}{(n-1)!} \frac{(n-1)!}{(n-1)!}$$

Problem Set

Find the number of possible outcomes for each scenario using the fundamental counting principle.

- 1. Clocks come in 2 styles: wall or desk. They come in 5 colors: white, black, red, blue, or orange.
- 2. Elias has a choice of a queen or king with a choice of hearts, diamonds, clubs, or spades.
- 3. A coin is tossed five times.
- 4. A coin is tossed and a $(n\ 1)! - n! (n-1)!$ die is rolled.
 - (n-1). Notebooks come in 4 colors: red, yellow, green, and blue. They come in 2 types: 5subject and 7-subject.

Problem Set

Solve each permutation problem completely.

- 1. How many 4-digit numbers can be formed from the digits 1, 3, 5, 6, 8, and 9 if no repetition is allowed?
- 2. If there are 10 people and only 6 chairs are available, in how many ways can they be seated?
- 3. In how many different ways can a president, vice president, a secretary, and a treasurer be chosen from a class of 15 students?
- 4. In how many different ways can a first, second, and third prizes be awarded in a game with eight contestants?
- 5. If four persons enter a bus on which there are ten vacant seats, how many ways can the four be seated?

Problem Set

- A. Find the number of distinguishable permutations for the following.

 - 2. REPETITION
 - 3. PHILIBPINESSISSIPPI $_2$.
- B. Find the number of distinguishable permutations for each situation.
 - 1. In how many wavs can 4 green marbles and 6 blue marbles be arranged in a row?
 - 2. How many distinguishable permutations are possible with all the letters of the word ELLIPSES?
 - 3. Find the number of distinguishable permutations of the digits of the number 348,838.

Problem Set

Solve each problem completely.

five boys and three girls be arranged in a 1. PARAMLEGOOGOLPLEXcircle if the girls must always stand together?

1. In how many ways can

- Mother, father, and four children stand in a circle. In how many ways can they arrange themselves if mother and father stand opposite each other?
- 3. In how my ways can ten kevs be arranged on a key ring?
- 4. If a spinner is divided in 7 equal parts, how many ways can you arrange 7 colors in it?
- 5. King Arthur arranges his 13 knights around a circular table.
 - a. In how many ways can he arrange them?
 - b. In how many ways can he do if Galahad it Parcivale and are to be seated together?
 - c. In how many ways can he do it

F. Finding Practical Application of Concepts and Skills in Daily Living	Let the students answer the following questions: 1. In what real life situations or problems can we observe some examples of factorial notation? 2. How can you apply your knowledge of factorial notation in solving these real life problems?	Let the students answer the following questions: 1. In what real life situations or problems can we observe some examples of fundamental principle of counting? 2. How can you apply your knowledge of fundamental principle of counting in solving these real life problems?	Let the students answer the following questions: 1. In what real life situations or problems can we observe some examples of permutation? 2. How can you apply your knowledge of permutation in solving these real life problems?	Let the students answer the following questions: 1. In what real life situations or problems can we observe some examples of distinguishable permutation? 2. How can you apply your knowledge of distinguishable permutation in solving these real life problems?	Let the students answer the following questions: 1. In what real life situations or problems can we observe some examples of circular permutations? 2. How can you apply your knowledge of circular permutations in solving these real life problems?
G. Making Generalization and Abstractions about the Lesson	Let the students answer the following questions: 1. In your own words, what is the factorial notation? 2. How do we solve problems involving factorial notation?	Let the students answer the following questions: 1. In your own words, what is the fundamental principle of counting? 2. How do we solve problems involving fundamental principle of counting?	Let the students answer the following questions: 1. In your own words, what is the permutation? 2. How do we solve problems involving permutation?	Let the students answer the following questions: 1. In your own words, what is the distinguishable permutation? 2. How do we solve problems involving distinguishable permutation?	Let the students answer the following questions: 1. In your own words, what is the circular permutations? 2. How do we solve problems involving circular permutations?
H. Evaluating Learning I. Additional Activities for Application or Reme-					
diation VI. REMARKS	Objectives have been attained: Objectives were not attained due to:	Objectives have been attained: Objectives were not attained due to:	Objectives have been attained: Objectives were not attained due to:	Objectives have been attained: Objectives were not attained due to:	tained: Objectives were not

VII. REFLECTION					
A. No. of learners who	10–Bohr:out of				
earned 80% in the evalu-	10-Avogadro:out of				
ation					
B. No. of learners who	10–Bohr:out of				
require additional activi-	10-Avogadro:out of				
ties for remediation who					
scored below 80%					
C. Did the remedial	10–Bohr:	10–Bohr:	10–Bohr:	10–Bohr:	10–Bohr:
lessons work? No.	10–Avogadro:	10-Avogadro:	10-Avogadro:	10-Avogadro:	10–Avogadro:
of learners who have					
caught up with the					
lesson					
D. No. of learners who	10–Bohr:	10–Bohr:	10–Bohr:	10–Bohr:	10–Bohr:
continue to require reme-	10–Avogadro:	10-Avogadro:	10-Avogadro:	10-Avogadro:	10–Avogadro:
diation					
E. Which of my teach-					
ing strategies worked					
well? Why did these					
work?					
F. What difficulties did					
I encounter which my					
principal or supervisor					
can help me solve?					
G. What innovation or					
localized materials did					
I use/discover which I					
wish to share with other					
teachers?					