

 <b>GRADES 1 to 12 DAILY LESSON LOG</b>	<b>School</b>	Sauyo High School	<b>Grade Level</b>	Grade 10
	<b>Teacher</b>	Mr. Jonathan R. Bacolod, LPT	<b>Learning Area</b>	Mathematics
	<b>Teaching Dates and Time</b>	Week 1, January 3 – 7, 2019	<b>Quarter</b>	1st

I. OBJECTIVES	DAY 1	DAY 2	DAY 3	DAY 4
<b>A. Content Standards:</b>	The learner demonstrates understanding of key concepts of sequences, polynomials and polynomial equations.			
<b>B. Performance Standards:</b>	The learner is able to formulate and solve problems involving sequences, polynomials and polynomial equations in different disciplines through appropriate and accurate representations			
<b>C. Learning Competencies/ Objectives: (Write the LC code for each.)</b>	1. Evaluate the rules of given sequences; 2. Calculate the next terms of a given sequences; and, 3. Exhibit interest and perseverance in solving problems.	1. Execute the steps in finding the rule of a given arithmetic sequence; 2. Find the next terms of a given arithmetic sequence; and, 3. Project interest and enjoyment in solving problems.	1. State the steps in finding the arithmetic mean; 2. Generate the arithmetic mean given two terms of a sequence; and, 3. Display interest and willingness in solving problems.	1. Derive the formula in computing arithmetic series; 2. Compute the number of terms of a given arithmetic series; and, 3. Display enjoyment and independence in solving problems.
<b>II. CONTENT</b>	<b>PATTERNS AND ALGEBRA</b>			
	<b>Sequences</b>	<b>Arithmetic Sequences</b>	<b>Arithmetic Means</b>	<b>Arithmetic Series</b>
<b>III. LEARNING RESOURCES</b>				
<b>A. References</b>				
<b>1. Teacher’s Guide Pages</b>	pp. 1–10	pp. 11–21	pp. 22–30	pp. 31–41
<b>2. Learner’s Materials Pages</b>	pp. 1–6	pp. 7–13	pp. 14–18	pp. 19–25
<b>3. Textbook Pages</b>	pp. 1–8	pp. 9–18	pp. 19–25	pp. 26–35
<b>4. Additional Materials from Learning Resources Portal</b>				
<b>B. Other Learning Resources</b>	Flashcards	Flashcards	Flashcards	Flashcards
<b>IV. PROCEDURES</b>				

<p><b>A. Reviewing Previous Lesson or Presenting New Lesson</b></p>	<p style="text-align: center;"><b>Sequences</b></p> <p><b>Sequence:</b> a function whose domain is the finite set <math>\{1, 2, 3, \dots, n\}</math> or the infinite set <math>\{1, 2, 3, \dots\}</math>  <b>Finite Sequence:</b> a sequence of numbers that is a fixed length long  <b>Infinite Sequence:</b> an endless progression of numbers</p> <p style="text-align: center;"><b>Rules for Sequences</b></p> <p><b>Linear Sequence:</b> a sequence with constant first differences (<math>d_1</math>)</p> <ul style="list-style-type: none"> <li>• <math>a_n = an + b</math></li> <li>• <math>a + b = a_1</math></li> <li>• <math>a = d_1</math></li> </ul> <p><b>Quadratic Sequence:</b> a sequence with constant second differences (<math>d_2</math>)</p> <ul style="list-style-type: none"> <li>• <math>a_n = an^2 + bn + c</math></li> <li>• <math>a + b + c = a_1</math></li> <li>• <math>3a + b = d_1</math></li> <li>• <math>2a = d_2</math></li> </ul>	<p style="text-align: center;"><b>Arithmetic Sequences</b></p> <p><b>Arithmetic Sequence:</b> a sequence where every term after the first is obtained by adding a constant called the common difference</p> <p><b>Common difference:</b> the constant difference <math>d</math> between any two consecutive terms</p> <p>To find any term in an arithmetic sequence, use</p> $a_n = a_1 + (n - 1)d$	<p style="text-align: center;"><b>Arithmetic Means</b></p> <p><b>Arithmetic Extremes:</b> the first and last terms of a finite arithmetic sequence</p> <p><b>Arithmetic Means:</b> the terms between the arithmetic extremes</p> <p><b>Average:</b> the arithmetic mean between two numbers</p> <p>To insert more than one arithmetic mean, use the difference formula <math>d</math>.</p> $d = \frac{a_n - a_k}{n - k}$	<p style="text-align: center;"><b>Arithmetic Series</b></p> <p><b>Arithmetic Series:</b> the indicated sum of the terms of an arithmetic sequence</p> <p>If the first term and the <math>n^{th}</math> term are given, then</p> $S_n = \frac{n}{2}(a_1 + a_n)$ <p>If the <math>n^{th}</math> term is not given, then</p> $S_n = \frac{n}{2}[2a_1 + (n - 1)d]$
<p><b>B. Establishing a Purpose for the Lesson</b></p>	<p>The purpose of this lesson is to enable the students to solve real life problems involving sequences.</p>	<p>The purpose of this lesson is to enable the students to solve real life problems involving arithmetic sequences.</p>	<p>The purpose of this lesson is to enable the students to solve real life problems involving arithmetic means.</p>	<p>The purpose of this lesson is to enable the students to solve real life problems involving arithmetic series.</p>

<b>C. Presenting Examples/ Instances of the Lesson</b>	<p>Some examples of sequences are the following:</p> <ol style="list-style-type: none"> <li>1. -2, 4, -8, 16,...</li> <li>2. 4, 1, -2, -5,...</li> <li>3. 1, 8, 27, 64,...</li> </ol>	<p>Some examples of arithmetic sequences are the following:</p> <ol style="list-style-type: none"> <li>1. <math>14, 6, -2, \dots a_{28}</math></li> <li>2. <math>3, 5, 7, \dots a_{21}</math></li> <li>3. <math>1.4, 4.5, 7.6, \dots a_{51}</math></li> </ol>	<p>Some examples of arithmetic means are the following:</p> <ol style="list-style-type: none"> <li>1. The arithmetic mean of 7 and 11 is 9.</li> <li>2. The arithmetic mean of 21 and 35 is 28.</li> <li>3. The two arithmetic means between 7 and 13 are 9 and 11.</li> </ol>	<p>Some examples of arithmetic series are the following:</p> <ol style="list-style-type: none"> <li>1. The sum of even integers from 5 to 11 is 24.</li> <li>2. <math>1 + 3 + 5 + 7 = 16</math></li> </ol>
<b>D. Discussing New Concepts and Practicing New Skills #1</b>	<p><b>Practice Exercises</b></p> <p>A. Find the first 5 terms of the sequence given the <math>n_{th}</math> term.</p> <ol style="list-style-type: none"> <li>1. <math>a_n = n + 4</math></li> <li>2. <math>a_n = 2n - 1</math></li> <li>3. <math>a_n = 12 - 3n</math></li> <li>4. <math>a_n = 3^n</math></li> <li>5. <math>a_n = -2^n</math></li> </ol>	<p><b>Practice Exercises</b></p> <p>A. Find the specified term of each arithmetic sequence.</p> <ol style="list-style-type: none"> <li>1. <math>2, 5, 8, \dots a_8</math></li> <li>2. <math>-11, -7, -3, \dots a_{23}</math></li> <li>3. <math>10, -2, -14, \dots a_{17}</math></li> <li>4. <math>y, x, 2x - y, \dots a_{10}</math></li> <li>5. <math>3, 3.25, 3.5, \dots a_{16}</math></li> </ol>	<p><b>Practice Exercises</b></p> <p>Insert the indicated number of arithmetic means between the given arithmetic extremes.</p> <ol style="list-style-type: none"> <li>1. 2 and 32 [1]</li> <li>2. -12 and 6 [3]</li> <li>3. 68 and 3 [4]</li> <li>4. <math>15x</math> and <math>23x</math> [1]</li> <li>5. <math>9\sqrt{3}</math> and <math>11\sqrt{3}</math> [1]</li> <li>6. <math>2\sqrt{5}</math> and <math>14\sqrt{5}</math> [2]</li> <li>7. <math>\frac{3}{7}</math> and <math>\frac{11}{7}</math> [1]</li> </ol>	<p><b>Practice Exercises</b></p> <p>A. Find the sum of each arithmetic sequence.</p> <ol style="list-style-type: none"> <li>1. 2, 5, 8, ... to 8 terms</li> <li>2. -11, -7, -3, ... to 23 terms</li> <li>3. Sum of odd integers from 1 to 100</li> <li>4. Sum of the integers between 50 and 200 which are divisible by 5</li> </ol>

<b>E. Discussing New Concepts and Practicing New Skills #2</b>	B. Determine the rule that governs each sequence. <div>             1. 5, 9, 13, 17,...             2. 2, 5, 8, 11,...             3. -11, -7, -1, 7,...             4. 1, 4, 10, 19,...             5. 1, -3, 9, -27,...             6. 1, 8, 27, 64,...             7. <math>\frac{1}{2}, \frac{1}{4}, \frac{1}{6}, \frac{1}{8}, \dots</math> </div>	B. Find the specified term. <div>             1. 18<sup>th</sup> term of the arithmetic sequence if <math>a_1 = 25</math> and <math>d = -2</math>.             2. 11<sup>th</sup> term of the arithmetic sequence if <math>a_1 = -15</math> and <math>d = 6</math>.             3. In the sequence 2, 6, 10,..., what term has a value of 106?             4. In the sequence 7, 4, 1,..., what term has a value of -296?           </div>		B. In each arithmetic series, find the specified unknown. <div>             1. <math>S_n = 90, a_1=10, a_n=26, n=?</math>             2. <math>S_n = 1,800, a_n=185, n=18, a_1=?</math>             3. <math>S_n = 119, a_1=5, d=4, n=?</math>             4. <math>a_{10} = 27.5, d=3, a_1=?, S_n=?</math>             5. Sum of odd integers from 1 to 100           </div>
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<p><b>F. Developing Mastery</b></p>	<p><b>Problem Set</b></p> <p>Find the first 5 terms of the sequence given the <math>n_{th}</math> term.</p> <ol style="list-style-type: none"> <li><math>a_n = n + 3</math></li> <li><math>a_n = 3n - 1</math></li> <li><math>a_n = 10 - 3n</math></li> <li><math>a_n = 2^n</math></li> <li><math>a_n = -3^n</math></li> </ol> <p>Determine the rule that governs each sequence.</p> <ol style="list-style-type: none"> <li>5, 10, 15, 20,...</li> <li>-1, -7, -11, -13,...</li> <li>-2, 4, -8, 16,...</li> <li>4, 1, -2, -5,...</li> <li>1, 8, 27, 64,...</li> <li><math>\frac{1}{3}, \frac{1}{7}, \frac{1}{11}, \frac{1}{15}, \dots</math></li> </ol>	<p><b>Problem Set</b></p> <p>A. Find the specified term of each arithmetic sequence.</p> <ol style="list-style-type: none"> <li>3, 5, 7, ... <math>a_{21}</math></li> <li>1.4, 4.5, 7.6, ... <math>a_{51}</math></li> <li><math>x - 2, 4x, 7x + 2, \dots a_{12}</math></li> <li>14, 6, -2, ... <math>a_{28}</math></li> <li>5, -1, -7, ... <math>a_{18}</math></li> </ol> <p>B. Find the specified term.</p> <ol style="list-style-type: none"> <li>17<sup>th</sup> term of the sequence if <math>a_8 = 5</math> and <math>a_{21} = -60</math>.</li> <li>5<sup>th</sup> term of the sequence if <math>a_{15} = 29</math> and <math>a_{27} = 47</math>.</li> <li>If <math>a_{24} = 85</math> and <math>a_{28} = 100</math>, <math>a_1 = ?</math></li> <li>If <math>a_1 = -4</math> and <math>a_{25} = -100</math>, <math>a_{101} = ?</math></li> </ol>	<p><b>Problem Set</b></p> <p>Insert the indicated number of arithmetic means between the given arithmetic extremes.</p> <ol style="list-style-type: none"> <li>-5 and 1 [2]</li> <li>24 and -12 [4]</li> <li>8 and 23 [4]</li> <li>4x and -16x [5]</li> <li><math>6\sqrt{5}</math> and <math>12\sqrt{5}</math> [1]</li> <li><math>-3\sqrt{3}</math> and <math>15\sqrt{3}</math> [5]</li> <li><math>\frac{1}{2}</math> and 2 [2]</li> </ol>	<p><b>Problem Set</b></p> <p>A. Find the sum of each arithmetic sequence.</p> <ol style="list-style-type: none"> <li>3, 5, 7, ... to 31 terms</li> <li>10, -2, -14, ... to 17 terms</li> <li>Sum of even integers from 10 to 90</li> <li>Sum of the integers between 2 and 100 which are divisible by 3</li> </ol> <p>B. In each arithmetic series, find the specified unknown.</p> <ol style="list-style-type: none"> <li><math>S_n = 50, a_1 = 4, a_n = 16, n = ?</math></li> <li><math>S_n = 195, a_n = 33, d = 3, a_1 = ?</math></li> <li><math>S_n = -15, a_1 = 12, d = -3, n = ?</math></li> <li>Sum of odd integers from 1 to 100</li> </ol>
<p><b>G. Finding Practical Application of Concepts and Skills in Daily Living</b></p>	<p>Let the students answer the following questions:</p> <ol style="list-style-type: none"> <li>In what real life situations or problems can we observe some examples of sequences?</li> <li>How can you apply your knowledge of sequences in solving these real life problems?</li> </ol>	<p>Let the students answer the following questions:</p> <ol style="list-style-type: none"> <li>In what real life situations or problems can we observe some examples of arithmetic sequences?</li> <li>How can you apply your knowledge of arithmetic sequences in solving these real life problems?</li> </ol>	<p>Let the students answer the following questions:</p> <ol style="list-style-type: none"> <li>In what real life situations or problems can we observe some examples of arithmetic means?</li> <li>How can you apply your knowledge of arithmetic means in solving these real life problems?</li> </ol>	<p>Let the students answer the following questions:</p> <ol style="list-style-type: none"> <li>In what real life situations or problems can we observe some examples of arithmetic series?</li> <li>How can you apply your knowledge of arithmetic series in solving these real life problems?</li> </ol>

<b>H. Making Generalization and Abstractions about the Lesson</b>	Let the students answer the following questions:  1. In your own words, what are sequences?  2. How do we solve problems involving sequences?	Let the students answer the following questions:  1. In your own words, what are arithmetic sequences?  2. How do we solve problems involving arithmetic sequences?	Let the students answer the following questions:  1. In your own words, what are arithmetic means?  2. How do we solve problems involving arithmetic means?	Let the students answer the following questions:  1. In your own words, what are arithmetic series?  2. How do we solve problems involving arithmetic series?
<b>I. Evaluating Learning</b>		<b>Quiz #1</b>  Find the specified term.  1. The $101^{th}$ term of the arithmetic sequence if $a_1=-5$ and $d=-4$ .  2. The $39^{th}$ term of the arithmetic sequence if $a_1 = 40$ and $d = \frac{1}{2}$ .  3. In the sequence 6, 10, 14,..., what term has a value of 286?  4. In the sequence $3, \frac{7}{3}, \frac{5}{3}, \dots$ , what term has a value of -27?  5. The $1^{st}$ term of the sequence if $a_5 = 26$ and $a_{12} = 47$ .  6. The $61^{th}$ term of the sequence if $a_4 = 8$ and $a_{21} = 26$ .  7. If $a_3=8$ and $a_{16}=47$ , $a_{71}=?$  8. If $a_{21}=64$ and $a_{100}=301$ , $a_{11}=?$		
<b>J. Additional Activities for Application or Remediation</b>				

VI. REMARKS	Objectives have been attained: _____ Objectives were not attained due to: _____	Objectives have been attained: _____ Objectives were not attained due to: _____	Objectives have been attained: _____ Objectives were not attained due to: _____	Objectives have been attained: _____ Objectives were not attained due to: _____
VII. REFLECTION				
A. No. of learners who earned 80% in the evaluation	10–Bohr: _____ out of _____ 10–Avogadro: _____ out of _____	10–Bohr: _____ out of _____ 10–Avogadro: _____ out of _____	10–Bohr: _____ out of _____ 10–Avogadro: _____ out of _____	10–Bohr: _____ out of _____ 10–Avogadro: _____ out of _____
B. No. of learners who require additional activities for remediation who scored below 80%	10–Bohr: _____ out of _____ 10–Avogadro: _____ out of _____	10–Bohr: _____ out of _____ 10–Avogadro: _____ out of _____	10–Bohr: _____ out of _____ 10–Avogadro: _____ out of _____	10–Bohr: _____ out of _____ 10–Avogadro: _____ out of _____
C. Did the remedial lessons work? No. of learners who have caught up with the lesson	10–Bohr: _____ 10–Avogadro: _____	10–Bohr: _____ 10–Avogadro: _____	10–Bohr: _____ 10–Avogadro: _____	10–Bohr: _____ 10–Avogadro: _____
D. No. of learners who continue to require remediation	10–Bohr: _____ 10–Avogadro: _____	10–Bohr: _____ 10–Avogadro: _____	10–Bohr: _____ 10–Avogadro: _____	10–Bohr: _____ 10–Avogadro: _____
E. Which of my teaching strategies worked well? Why did these work?				
F. What difficulties did I encounter which my principal or supervisor can help me solve?				
G. What innovation or localized materials did I use/discover which I wish to share with other teachers?				

Checked by:

DR. LORETO G. DOMINGO  
Head, Mathematics Department