

# Practice Exercises

Cube each binomial.

1.  $(x + 5)^3$

2.  $(a - 3b)^3$

3.  $(4h^2 + 2k)^3$

4.  $(-3x - 2y)^3$

5.  $(5m + 2n^2)^3$

B. Fill in the blanks.

1.  $(x - 3y)^3 = x^3 - \underline{\hspace{2cm}} + 27xy^2 - \underline{\hspace{2cm}}$

2.  $(2x + z^2)^3 = 8x^3 + \underline{\hspace{2cm}} + \underline{\hspace{2cm}} + z^6$

3.  $(-3t^2 - 2y^3)^3 = -27t^6 - \underline{\hspace{2cm}} - 36t^2y^6 - \underline{\hspace{2cm}}$

4.  $(-xy^2 + 3z^2)^3 = \underline{\hspace{2cm}} + 9x^2y^4z^2 - \underline{\hspace{2cm}} + 27z^6$

5.  $(x^2y^3 - 2z^3)^3 = x^6y^9 - \underline{\hspace{2cm}} + \underline{\hspace{2cm}} - 8z^9$

# Problem Set

## A. Cube each binomial.

1.  $(2m + 3r)^3$

2.  $(-4a - c)^3$

3.  $(3h^2 - 2i)^3$

4.  $(5x + 3y)^3$

5.  $(2m - 4n^3)^3$

## B. Fill in the blanks.

1.  $(2x - y)^3 = 8x^3 - \underline{\hspace{2cm}} + \underline{\hspace{2cm}} - y^3$

2.  $(3x + z^3)^3 = \underline{\hspace{2cm}} + \underline{\hspace{2cm}} + 9xz^6 + z^9$

3.  $(-2t^2 - y^3)^3 = -8t^6 - \underline{\hspace{2cm}} - \underline{\hspace{2cm}} - y^9$

4.  $(-3xy^2 + z^2)^3 = -27x^3y^6 + \underline{\hspace{2cm}} - \underline{\hspace{2cm}} + z^6$

5.  $(3x^3y^2 - 2z^2)^3 = \underline{\hspace{2cm}} - \underline{\hspace{2cm}} + 36x^3y^2z^4 - 8z^6$

# Problem Set

A.

$$\begin{aligned} 1. \quad & (2m + 3r)^3 \\ &= (2m)^3 + 3(2m)^2(3r) + 3(2m)(3r)^2 + (3r)^3 \\ &= 8m^3 + 9r(4m^2) + 6m(9r^2) + 27r^3 \\ &= 8m^3 + 36rm^2 + 54mr^2 + 27r^3 \end{aligned}$$

$$\begin{aligned} 2. \quad & (-4a - c)^3 \\ &= (-4a)^3 + 3(-4a)^2(-c) + 3(-4a)(-c)^2 + (-c)^3 \\ &= -64a^3 - 3c(16a^2) - 12a(c^2) - c^3 \\ &= -64a^3 - 48a^2c - 12ac^2 - c^3 \end{aligned}$$

$$\begin{aligned} 3. \quad & (3h^2 - 2i)^3 \\ &= (3h^2)^3 + 3(3h^2)^2(-2i) + 3(3h^2)(-2i)^2 + (-2i)^3 \\ &= 27h^6 - 6i(9h^4) + 9h^2(4i^2) - 8i^3 \\ &= 27h^6 - 54ih^4 + 36h^2i^2 - 8i^3 \end{aligned}$$

$$\begin{aligned}
4. \quad & (5x + 3y)^3 \\
&= (5x)^3 + 3(5x)^2(3y) + 3(5x)(3y)^2 + (3y)^3 \\
&= 125x^3 + 9y(25x^2) + 15x(9y^2) + 27y^3 \\
&= 125x^3 + 225x^2y + 135xy^2 + 27y^3
\end{aligned}$$

$$\begin{aligned}
5. \quad & (2m - 4n^3)^3 \\
&= (2m)^3 + 3(2m)^2(-4n^3) + 3(2m)(-4n^3)^2 + (-4n^3)^3 \\
&= 8m^3 - 12n^3(4m^2) + 6m(16n^6) - 64n^9 \\
&= 8m^3 - 48m^2n^3 + 96mn^6 - 64n^9
\end{aligned}$$

**B.**

$$\begin{aligned}
1. \quad &= (2x)^3 + 3(2x)^2(-y) + 3(2x)(-y)^2 + (-y)^3 \\
&= 8x^3 - 3y(4x^2) + 6x(y^2) - y^3 \\
&= 8x^3 - 12x^2y + 6xy^2 - y^3
\end{aligned}$$

**Missing terms =  $12x^2y$ ,  $6xy^2$**

$$\begin{aligned}
2. \quad &= (3x)^3 + 3(3x)^2(z^3) + 3(3x)(z^3)^2 + (z^3)^3 \\
&= 27x^3 + 3z^3(9x^2) + 9x(z^6) + z^9
\end{aligned}$$

$$= 27x^3 + 27x^2z^3 + 9xz^6 + z^9$$

$$\text{Missing terms} = 27x^3, 27x^2z^3$$

$$3. = (-2t^2)^3 + 3(-2t^2)^2(y^3) + 3(-2t^2)(y^3)^2 + (y^3)^3$$

$$= -8t^6 + 3y^3(4t^4) - 6t^2(y^6) + y^9$$

$$= -8t^6 - 12t^4y^3 - 6t^2y^6 - y^9$$

$$\text{Missing terms} = 12t^4y^3, 6t^2y^6$$

$$4. = (-3xy^2)^3 + 3(-3xy^2)^2(z^2) + 3(-3xy^2)(z^2)^2 + (z^2)^3$$

$$= -27x^3y^6 + 3z^2(9x^2y^4) - 9xy^2(z^4) + z^6$$

$$= -27x^3y^6 + 27x^2y^4z^2 - 9xy^2z^4 + z^6$$

$$\text{Missing terms} = 27x^2y^4z^2, 9xy^2z^4$$

$$5. = (3x^3y^2)^3 + 3(3x^3y^2)^2(-2z^2) + 3(3x^3y^2)(-2z^2)^2$$

$$+ (-2z^2)^3$$

$$= 27x^9y^6 - 6z^2(9x^6y^4) + 9x^3y^2(4z^4) - 8z^6$$

$$= 27x^9y^6 - 54x^6y^4z^2 + 36x^3y^2z^4 - 8z^6$$

$$\text{Missing terms} = 27x^9y^6, 54x^6y^4z^2$$

