

School	Sauyo High School	Grade Level	Grade 10
Teacher	Mr. Jonathan R. Bacolod, LPT	Learning Area	Mathematics
Teaching Dates and Time	Week 10, August 5 – 9, 2019	Quarter	1st

I. OBJECTIVES	DAY 1	DAY 2	DAY 3	DAY 4	DAY 5
Learning Competencies/ Objectives:	 Describe the steps in finding the next terms of a fibonacci sequence; Solve the next terms of a fibonacci sequence; and, Show willingness and interest in solving problems. 	 Describe a polynomial function; Determine the kind, the degree, the leading coefficient, and the constant term of a polynomial function; and, Exhibit patience and self-reliance in solving problems. 	synthetic division; and,	 Demonstrate the remainder theorem; Compute the remainder of a polynomial using the remainder theorem; and, Exhibit determination and self-reliance in solving problems. 	 Discuss the factor theorem; Use the factor theorem to determine whether a binomial is a factor of a given polynomial; and, Exhibit perseverance and interest in solving problems.
II. CONTENT	PATTERNS AND ALGEBRA				
	Fibonacci Sequence	Polynomial Function	Synthetic Division	Remainder Theorem	Factor Theorem
III. LEARNING RESOURCES					
A. References					
1. Teacher's Guide Pages	pp. 83–91	pp. 62–66	pp. 67–73	pp. 74–78	pp. 79–85
2. Learner's Materials Pages	pp. 50–54	pp. 52–55	pp. 56–61	pp. 62–65	pp. 66–71
3. Textbook Pages	pp. 70–76	pp. 62–66	pp. 67–73	pp. 74–78	pp. 79–85
4. Additional Materials from Learning Resources Portal B. Other Learning	Flashcards	Flashcards	Flashcards	Flashcards	Flashcards
Resources					

A. Reviewing Previous Lesson or Presenting New Lesson	Fibonacci Sequence	P
	Fibonacci Sequence: a sequence in which the terms are found by adding the two previous terms	Polyn of alg each varia stant
	In symbols, $F_n = F_{n-1} + F_{n-2}, \ n > 2$	whol An al a pol squa
		ative the d tion.
		Poly i
		p(x)
		wher
		Degr Func of x
		polyr
		Lead
		nonz polyr range
		Pol
		Zer
		Cor
		Line
		Cub
		Out

Polynomial Function

Polynomial: a special kind of algebraic expression where each term is a constant, a variable, or a product of constants and variables raised to whole number exponents

An algebraic expression is not a polynomial when there are square roots of variables, negative powers, and variables in the denominator of any fraction.

Polynomial Function: function defined by

$$p(x) = a_n x^n + a_{n-1} x^{n-1} + a_{n-2} x^{n-1}$$

where n is a positive integer

Degree of a Polynomial Function: the largest power of x that appears in the polynomial

Leading Coefficient: the first nonzero coefficient when a polynomial function is arranged in descending order

Synthetic Division

Division Algorithm: If P(x) and D(x) are polynomials and $D(x) \neq 0$, then there exists a unique polynomial Q(x) and R such that

$$P(x) = D(x) \cdot Q(x) + R$$

Dividend = Divisor · Quotient + Remainder

Steps for Synthetic Division

- 1. Set up the synthetic division.
- ⁻²+2..+**Bring**adown the leading coefficient to the bottom row.
 - 3. Multiply *c* by the value just written on the bottom row.
 - 4. Add the column created in step 3.
 - 5. Repeat until done.
 - 6. Write out the answer.

Polynomial FunctionDegreeZero FunctionNoneConstant Function0Linear Function1Quadratic Function2Cubic Function3Quartic Function4Quintic Function5 n^{th} degree Polynomial Functionn

Remainder Theorem

Remainder Theorem: If a polynomial P(x) is divided by x - c, then the remainder is P(c).

$$R = P(c)$$

Ways to Find the Remainder:

- 1. Use synthetic division.
- 2. Calculate P(c).

Factor Theorem

Factor Theorem: If P(x) is a polynomial and P(c) = 0, then x - c is a factor of P(x). Conversely, if x - c is a factor of P(x), then P(c) = 0.

B. Establishing a Purpose for the Lesson	The purpose of this lesson is to enable the students to solve real life problems involving fibonacci sequence.	The purpose of this lesson is to enable the students to solve real life problems involving polynomial functions.	The purpose of this lesson is to enable the students to solve real life problems involving synthetic division.	The purpose of this lesson is to enable the students to solve real life problems involving the remainder theorem.	The purpose of this lesson is to enable the students to solve real life problems involving the factor theorem.
C. Discussing New Concepts	Practice Exercises	Practice Exercises	Practice Exercises	Practice Exercises	Practice Exercises
and Practicing New Skills #1	Find the missing terms of each sequence. 1. 6, 6, 12,,, 2. 0.3, 0.3,,, 3. 5, 5, 10,,, 4. √2,√2,,, 5. 6,,, 18,	A. Determine which of the following are polynomial functions. 1. $f(x) = 2x - 1$ 2. $h(x) = 4^{x} - 7$ 3. $F(x) = 7 + 5x^{-2} + 4x^{5}$ 4. $f(x) = -x^{5} + 7x^{2} - 4 + x^{\frac{1}{2}}$ 5. $h(x) = \frac{5 + x^{3}}{7}$	A. Divide the polynomials using the long method. Express your answer as $P(x) = D(x) \cdot Q(x) + R$. 1. $(x^3 - 7x - 6) \div (x - 2)$ 2. $(4x^2 + 5x + 8) \div (x + 1)$ 3. $(10x^4 + 5x^3 + 4x^2 - 9) \div (x + 1)$ 4. $(2x^4 - 6x^3 + x^2 - 3x - 3) \div (x - 3)$ 5. $(4x^4 + 5x^3 + 2x^2 - 1) \div (x + 1)$	at $x = -3$ 3. $f(x) = x^4 + 3x^3 - 17x^2 + 2x - 7$ at $x = 3$	2. $(x + 1); P(x) = 2x^3 + 5x^2 + 4x + 1$
			(0. 2)	2 at x = 2	5. $(2x-1)$; $P(x) = 2x^3 - 7x^2 + x + 1$

D. Discussing New Concepts	B. Determine the kind of	B. Divide the polynomials us-	B. Use the remainder theo-	
and Practicing New Skills #2	function, the degree, the lead-	ing synthetic division. Ex-	rem to find the remainder	
	ing coefficient, and the con-	press your answer as $P(x) =$	of the following polynomial	
	stant term.	$D(x) \cdot Q(x) + R$.	functions.	
	Stafft term.	D(x) = Q(x) + H.	Turicuons.	
	$1 D(x) = 4x^3 15x 1$	1. $(5x^2 - 10x - 47) \div (x - 6)$	$f(x) = 4x^3 + 2x + 10 \text{ at}$	
	$6 + 7x^5$	4)	x = -3	
	$2. G(x) = 3x^4 - 5x^6 +$	2. $(x^3-x^2-x-2) \div (x-2)$	$2. f(x) = 2x^3 + 4x^2 - 5x +$	
	$8x^2 - 4x^3$		9 at $x = -3$	
	3. $f(x) = 9 - 3x^2 - 3x +$	3. $(x^4+9x^3+4x^2+50x+$	3. $f(x) = 3x^3 - 7x^2 + 5x -$	
	$6x^4$	$9) \div (x+8)$	2 at x = -2	
	O.A.	(x + 0)	$\sum \operatorname{dt} x = -2$	
	1 () (0 0)2	4 4 9 3 19 2 9		
	4. $h(x) = x(2x-3)^2$ 5. $F(x) = \frac{2x-5x^5+7x}{3}$	4. $(x^4 - 8x^3 + 10x^2 + 2x +$	3	
	5 _	$4) \div (x-2)$	x = -2	
	$5 F(x) = \frac{2x - 5x^3 + 7x}{1}$			
	3	5. $(x^5+6x^4-3x^2-22x-$	5. $f(x) = 6x^2 + 3x - 9$ at	
		$(29) \div (x+6)$	x = 1	
		20) . (3. 1 0)	N = 1	

E. Developing Mastery	Problem Set
7 0 7	Find the missing terms of each sequence.
	1. 2, 2, 4,,
	2. 0.2, 0.2,,
	3. $\frac{1}{4}, \frac{1}{4}, \frac{1}{2}, \dots,$
	4. 5x,, 10x,
	5, $\frac{3}{2}$,, $\frac{9}{2}$, $\frac{15}{2}$
	6, 2, 3, 5,,
	7. 0.5,, 1,,
	8. $\frac{1}{16}$, $\frac{1}{16}$,,
	9. 3x, 7x,,
	10, $\frac{5}{3}$,, 5,

Problem Set

A. Determine which of the following are polynomial functions.

1.
$$f(x) = 3x^2 + 5$$

2.
$$h(x) = 5x^3 + x - 3$$

3.
$$F(x) = \frac{3x^2}{2x^3}$$

4.
$$f(x) = 6x(x^2 - 1)$$

5.
$$h(x) = \sqrt{x^7 + 3x^6 - 4x}$$

B. Determine the kind of function, the degree, the leading coefficient, and the constant term.

1.
$$P(x) = -11 + x^4 - 3x^2$$

2.
$$G(x) = \frac{1}{2}x^2 + 4x^3 + 5$$

3.
$$f(x) = 5\sqrt{3}x - 7 + 2x^2$$

4.
$$h(x) = 7.5x^{10} - 3x^4 + 11x^8$$

5.
$$F(x) = x(5x^3+7)$$

Problem Set

A. Divide the polynomials using the long method. Express your answer as $P(x) = D(x) \cdot Q(x) + R$.

1.
$$(x^3 - 14x + 8) \div (x + 4)$$

2.
$$(x^2+10) \div (x+4)$$

3.
$$(x^3 + 8x^2 - 3x + 16) \div (x+5)$$

4.
$$(x^4 - 6x^3 - 40x + 33) \div (x - 7)$$

5.
$$(-10x^5 + 3x - 7) \div (x-1)$$

B. Divide the polynomials using synthetic division. Express your answer as $P(x) = D(x) \cdot Q(x) + R$.

1.
$$(8x^2+30x-11) \div (x+4)$$

2.
$$(x^4 - 8x^3 - x^2 + 62x - 34) \div (x - 7)$$

3.
$$(x^4+6x^3+11x^2+29x-13) \div (x+5)$$

4.
$$(x^5-25x^3-7x^2-37x-18) \div (x+5)$$

5.
$$(x^4 + 10x^3 + 21x^2 + 6x - 8) \div (x+2)$$

Problem Set

A. Use synthetic division to find the remainder of the following polynomial functions.

1.
$$f(x) = x^3 + x^2 - 5x - 6$$
 at $x = 2$

2.
$$f(x) = x^3 + 5x^2 + 10x + 12$$
 at $x = -2$

3.
$$f(x) = x^5 - 47x^3 - 16x^2 + 8x + 52$$
 at $x = 7$

4.
$$f(x) = x^4 - 2x^3 +$$

 $x^2 - 4$ at $x = -1$

5.
$$f(x) = x^2 - 5x - 2$$

at $x = -2$

B. Use the remainder theorem to find the remainder of the following polynomial functions.

1.
$$f(x) = 2x^3 - 5x^2 + 3x - 7$$

at $x = 3$

2.
$$f(x) = 2x^3 - 9x^2 + 14x - 8$$

at $x = -2$

3.
$$f(x) = 4x^4 + 5x^3 + 8x^2$$

at $x = 4$

4.
$$f(x) = 5x^4 + 6x^3 + 10x^2$$
 at $x = 5$

Problem Set

Use the factor theorem to determine whether the binomial is a factor of the given polynomial.

1.
$$(x-2)$$
; $P(x) = x^{20} - 4x^{18} + 3x - 6$

2.
$$(x-4)$$
; $P(x) = 3x^3 - 15x^2 + 10x + 8$

3.
$$(x+2)$$
; $P(x) = x^4 - 3x^3 + 5x - 2$

4.
$$(x-2)$$
; $P(x) = 3x^4 - 6x^3 + 5x + 10$

5.
$$(x+5)$$
; $P(x) = x^3 + x^2 - 25x + 25$

F. Finding Practical Application of Concepts and Skills in	Let the students answer the following questions:	Let the students answer the following questions:	Let the students answer the following questions:	Let the students answer the following questions:	Let the students answer the following questions:
Daily Living	 In what real life situations or problems can we observe some examples of fibonacci sequence? How can you apply your knowledge of fibonacci sequence in solving these real life problems? 	 In what real life situations or problems can we observe some examples of polynomial functions? How can you apply your knowledge of polynomial functions in solving these real life problems? 	 In what real life situations or problems can we observe some examples of synthetic division? How can you apply your knowledge of synthetic division in solving these real life problems? 	 In what real life situations or problems can we observe some examples of the remainder theorem? How can you apply your knowledge of remainder theorem in solving these real life problems? 	 In what real life situations or problems can we observe some examples of factor theorem? How can you apply your knowledge of factor theorem in solving these real life problems?
G. Making Generalization and Abstractions about the Lesson	Let the students answer the following questions: 1. In your own words, what is a fibonacci sequence? 2. How do we solve problems involving fibonacci sequence?	Let the students answer the following questions: 1. In your own words, what is a polynomial function? 2. How do we solve problems involving polynomial functions?	Let the students answer the following questions: 1. In your own words, what is synthetic division? 2. How do we solve problems involving synthetic division?	Let the students answer the following questions: 1. In your own words, what is the remainder theorem? 2. How do we solve problems involving remainder theorem?	Let the students answer the following questions: 1. In your own words, what is the factor theorem? 2. How do we solve problems involving factor theorem?
H. Evaluating Learning					
I. Additional Activities for Application or Remediation					
VI. REMARKS	Objectives have been attained: Objectives were not attained due to:	Objectives have been attained: Objectives were not attained due to:	Objectives have been attained: Objectives were not attained due to:	Objectives have been attained: Objectives were not attained due to:	Objectives have been attained: Objectives were not attained due to:
VII. REFLECTION					

A. No. of learners who	10–Bohr:out of				
earned 80% in the evaluation	10–Avogadro:out of				
B. No. of learners who re-	10–Bohr:out of				
quire additional activities for	10–Avogadro:out of				
remediation who scored below 80%					
C. Did the remedial lessons	10–Bohr:	10–Bohr:	10–Bohr:	10–Bohr:	10–Bohr:
work? No. of learners who	10–Avogadro:	10–Avogadro:	10–Avogadro:	10–Avogadro:	10–Avogadro:
have caught up with the les-					
son					
D. No. of learners who con-	10–Bohr:	10–Bohr:	10–Bohr:	10–Bohr:	10–Bohr:
tinue to require remediation	10–Avogadro:	10–Avogadro:	10–Avogadro:	10–Avogadro:	10–Avogadro:
E. Which of my teaching					
strategies worked well? Why					
did these work?					
F. What difficulties did I en-					
counter which my principal					
or supervisor can help me					
solve?					
G. What innovation or					
localized materials did I					
use/discover which I wish to					
share with other teachers?					