

Distinguishable Permutation

Total points = 68

Problem Set

A.

1. $n = 8$
 $p = 2$
 $q = 3$
 $P = \frac{n!}{p!q!}$
 $P = \frac{2!3!}{8!}$
 $= \frac{(8)(7)(6)(5)(4)(3!)}{(2)(1)(3!)}$
 $= 3,360$ distinguishable permutations

2. $n = 10$
 $p = 2$
 $q = 2$
 $r = 2$
 $P = \frac{n!}{p!q!r!}$
 $P = \frac{10!}{2!2!2!}$
 $= \frac{(10)(9)(8)(7)(6)(5)(4)(3)(2)!}{(2!)(2)(1)(2)(1)}$
 $= 453,600$ distinguishable permutations

3. $n = 11$
 $p = 3$
 $q = 3$
 $P = \frac{n!}{p!q!}$
 $P = \frac{11!}{3!3!}$
 $=$

$\frac{(11)(10)(9)(8)(7)(6)(5)(4)(3!)}{(3!)(3)(2)(1)}$
 $= 1,108,800$ distinguishable permutations

4. $n = 10$
 $p = 2$
 $q = 3$
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 $= 151,200$ distinguishable permutations

$n = 11$
 $p = 4$
 $q = 4$
 $r = 2$
 $P = \frac{n!}{p!q!r!}$
 $P = \frac{11!}{4!4!2!}$
 $= \frac{(11)(10)(9)(8)(7)(6)(5)(4!)}{(4!)(4)(3)(2)(1)(2)(1)}$
 $= 34,650$ distinguishable permutations

B.

1. $n = 10$
 $p = 4$
 $q = 6$
 $P = \frac{n!}{p!q!}$
 $P = \frac{10!}{4!6!}$
 $= \frac{(10)(9)(8)(7)(6!)}{(4)(3)(2)(1)(6!)}$
 $= 210$ ways
2. $n = 8$
 $p = 2$
 $q = 2$
 $r = 2$
 $P = \frac{n!}{p!q!r!}$
 $P = \frac{8!}{2!2!2!}$
 $= \frac{(8)(7)(6)(5)(4)(3)(2!)}{(2!)(2)(1)(2)(1)}$
 $= 5,040$ distinguishable permutations
3. $n = 6$
 $p = 2$
 $q = 3$
 $P = \frac{n!}{p!q!}$
 $P = \frac{6!}{2!3!}$
 $= \frac{(6)(5)(4)(3!)}{(2)(1)(3!)}$
 $= 60$ distinguishable permutations

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