

Basic Concepts of Probability

Probability: a measure that is associated with how certain we are of outcomes of a particular experiment or activity

Experiment: a planned operation carried out under controlled conditions

Chance Experiment: an experiment whose result is not predetermined

Outcome: a result of an experiment

Sample Space: the list of all the possible outcomes of an experiment

Ways to Represent a Sample Space:

- 1. List the possible outcomes
- 2. Create a tree diagram
- 3. Create a Venn diagram

Event: any combination of outcomes

Equally likely: each outcome of an experiment occurs with equal probability

Practice Exercises

A. Write the sample space for each experiment.

- 1. A toss of a coin and a die.
- 2. A coin tossed three times.
- 3. A toss of two coins once.
- 4. A vowel of the English alphabet picked at random from a box.
- 5. A roll of a die and tossing a coin.

B. Do as directed in each of the following.

- 1. Let a coin and a die be tossed. Give the elements of the following events.
 - a. $A = \{\text{head or tail and an odd number}\}$
 - b. $B = \{\text{an outcome with a number less than 4}\}$
 - c. $C = \{\text{tails and an even number}\}$
 - d. $D = \{\text{heads and a number less than 5}\}$
 - e. $E = \{\text{an outcome with a number at most 4}\}$
- 2. A pair of dice is rolled. Write the elements of each event.
 - a. $G = \{\text{the largest of one of the two numbers is 3}\}$
 - b. $H = \{\text{the two numbers whose sum is at most 5}\}$
 - c. $I = \{\text{the pair of numbers have an even sum}\}$
 - d. $J = \{\text{the pair of numbers whose sum is 6 but none of the two is even}\}$

Problem Set

A. Write the sample space for each experiment.

- 1. A toss of a die and a coin.
- 2. A coin tossed two times.
- 3. A toss of three coins once.
- 4. A day of the week picked at random from a box.

B. Do as directed in each of the following.

- 1. Let a die and a coin be tossed. Give the elements of the following events.
 - a. $A = \{\text{an even number and a head or tail}\}$
 - b. $B = \{\text{an outcome with a number greater than 4}\}$
 - c. $C = \{\text{an odd number and tails}\}$
 - d. $D = \{\text{a number less than 3 and heads}\}$
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