

Practice Exercises

Sketch the graph of each polynomial function.

1. $f(x) = (x - 2)(x + 1)$

2. $f(x) = (x - 2)(x + 1)(x + 3)$

3. $f(x) = (x - 2)^2(x + 2)^2$

4. $f(x) = x^4 - 2x^3 - 3x^2 + 4x + 4$

5. $f(x) = -x^3 - 9x^2 - 27x - 27$

Problem Set

Sketch the graph of each polynomial function.

1. $f(x) = (x - 2)(x - 1)(x - 3)$

2. $f(x) = x(x + 1)^2$

3. $f(x) = x(x - 2)(x + 1)(x + 3)$

4. $f(x) = (x + 2)(x - 1)(x - 3)^2$

Problem Set

1. $a_n : +, n = 3(\text{odd}), \text{Case 1}$

$$0 = (x - 2)(x - 1)(x - 3)$$

$$x - 2 = 0$$

$$x = 2$$

$$x - 1 = 0$$

$$x = 1$$

$$x - 3 = 0$$

$$x = 3$$

$$\text{Roots} = \{1, 2, 3\}$$

2. $a_n : +, n = 3(\text{odd}), \text{Case 1}$

$$0 = x(x + 1)^2$$

$$x = 0$$

$$(x + 1)^2 = 0$$

$$\sqrt{(x + 1)^2} = \sqrt{0}$$

$$x + 1 = 0$$

$$x = -1 \text{ of mult. 2}$$

$$\text{Roots} = \{0, -1 \text{ of mult. 2}\}$$

3. $a_n = +, n = 4(\text{even}), \text{Case 3}$

$$0 = x(x - 2)(x + 1)(x + 3)$$

$$x = 0$$

$$x - 2 = 0$$

$$x = 2$$

$$x + 1 = 0$$

$$x = -1$$

$$x + 3 = 0$$

$$x = -3$$

$$\text{Roots} = \{-3, -1, 0, 2\}$$

If $x = -2$:

$$f(-2) = -2(-2 - 2)(-2 + 1)(-2 + 3)$$

$$f(-2) = -2(-4)(-1)(1)$$

$$f(-2) = -8$$

$$\therefore (-2, -8)$$

If $x = 1$:

$$f(1) = 1(1-2)(1+1)(1+3)$$

$$f(1) = 1(-1)(2)(4)$$

$$f(1) = -8$$

$$\therefore (1, -8)$$

$$0 = (x+2)(x-1)(x-3)^2$$

$$x+2=0$$

$$x=-2$$

$$x-1=0$$

$$x=1$$

$$(x-3)^2=0$$

$$\sqrt{(x-3)^2} = \sqrt{0}$$

$$x-3=0$$

$$x=3 \text{ of mult. } 2$$

4. $a_n = +$, $n = 4(\text{even})$, Case 3 Roots = $\{-2, 1, 3 \text{ of mult. } 2\}$