Worksheet 1.3.3: Multiplication and Division of Rational Algebraic Expressions

A. True or False

Write True if the statement is true or False if it is false. One point each.

- 1. The reciprocal of $\frac{x+y}{x^2+xy}$ is $\frac{x^2+xy}{x+y}$.
- 2. The reciprocal of $\frac{1}{3m^3}$ is $3m^3$.
- 3. The reciprocal of $a^2 4$ is (a+2)(a-2).
- 4. The reciprocal of 3x 6 is 3(x 2).
- 5. The reciprocal of $\frac{5m-2n}{2n-1}$ is $\frac{2n-1}{5m-2n}$.

B. Finding the Factored Form

Find the factored form of each polynomial. Choose the answer from the box. Write the letter only. One point each.

a.
$$(x+3)(x+2)$$

b. $(x+4)(2x+3)$
c. $(2x-5)(x+4)$
d. $3x(x+1)$

f.
$$(x+6)(x-7)$$

b.
$$(x+4)(2x+3)$$

g.
$$2x(x+5)$$

c.
$$(2x-5)(x+4)$$

h.
$$5(4x-3)$$

d.
$$3x(x+1)$$

i.
$$7(x-2)$$

e.
$$3(x+7)(x-1)$$

j.
$$(x-3)^2$$

6.
$$3x^2 + 18x - 21$$

11.
$$20x - 15$$

7.
$$2x^2 + 11x + 12$$

12.
$$3x^2 + 3x$$

8.
$$7x - 14$$

13.
$$x^2 + 5x + 6$$

9.
$$x^2 - x - 42$$

14.
$$x^2 - 6x + 9$$

10.
$$2x^2 + 3x - 20$$

15.
$$2x^2 + 10x$$

C. Multiplying and Dividing Rational Expressions

Perform the indicated operation. Choose the answer from the box. Write the letter only. One point each.

a.
$$\frac{4(x-8)}{x+2}$$

f.
$$\frac{x+3}{x-10}$$

b.
$$\frac{2}{3x(x-5)}$$

g.
$$2(x-1)$$

c.
$$\frac{3}{2x(x+4)}$$

h.
$$\frac{8x(x-2)}{x-9}$$

$$d. \ \frac{7}{x-7}$$

i.
$$\frac{10x^2}{x+2}$$

e.
$$\frac{5}{x+6}$$

j.
$$\frac{x+10}{3}$$

16.
$$\frac{x^2-1}{x} \cdot \frac{2x}{x+1}$$

17.
$$\frac{1}{x+5} \cdot \frac{7x+35}{x-7}$$

18.
$$\frac{x^2 - 17x + 72}{x + 2} \cdot \frac{4x + 4}{x^2 - 8x - 9}$$

19.
$$\frac{x-4}{7x-28} \cdot \frac{7x+70}{3}$$

20.
$$\frac{4x-20}{x^2-10x+25} \cdot \frac{x+7}{6x^2+42x}$$

21.
$$\frac{3}{2x} \div \frac{7x + 28}{7}$$

22.
$$\frac{12x+12}{x-9} \div \frac{12x+12}{8x^2-16x}$$

23.
$$\frac{5}{7x^2} \div \frac{x^2 + 12x + 36}{7x^3 + 42x^2}$$

24.
$$\frac{10x^3 + 100x^2}{6x^2 - 48x} \div \frac{x^2 + 12x + 20}{6x^2 - 48x}$$

25.
$$\frac{x+3}{x^2-x-90} \div \frac{x-1}{x^2+8x-9}$$