Graphs of Linear Inequalities

Jonathan R. Bacolod

Sauyo High School

 Replace the inequality symbol with an equal sign. The resulting equation becomes the plane divider.

- Replace the inequality symbol with an equal sign. The resulting equation becomes the plane divider.
- Graph the corresponding equation. Use broken line if the inequality contains < or > symbol or a solid line if inequality contains < or > symbol.

- Replace the inequality symbol with an equal sign. The resulting equation becomes the plane divider.
- Graph the corresponding equation. Use broken line if the inequality contains < or > symbol or a solid line if inequality contains ≤ or > symbol.
- Choose a point on the plane not on the line and check if its coordinates satisfy the inequality.

- Replace the inequality symbol with an equal sign. The resulting equation becomes the plane divider.
- Graph the corresponding equation. Use broken line if the inequality contains < or > symbol or a solid line if inequality contains ≤ or > symbol.
- Choose a point on the plane not on the line and check if its coordinates satisfy the inequality.
- 4. If the inequality is satisfied, shade the region containing that point. If not, shade the other region.



Example 1

Graph the inequality $y \le 2x + 1$.

Example 1

Original inequality

Original inequality
$$y \le 2x + 1$$

Plane divider
$$y = 2x + 1$$

Example 1

Step 2: Graph the corresponding equation. Use broken line if the inequality contains < or > symbol or a solid line if inequality contains \le or \ge symbol.

Original inequality $y \le 2x + 1$

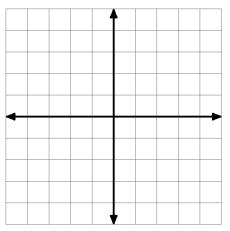
Plane divider y = 2x + 1

m=2 b=1

$$y = 2x + 1$$

$$m = 2$$

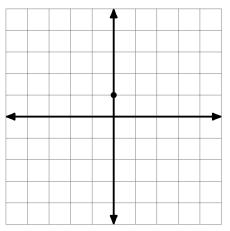
$$b = 1$$



$$y = 2x + 1$$

$$m = 2$$

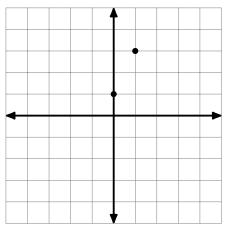
$$b = 1$$



$$y = 2x + 1$$

$$m = 2$$

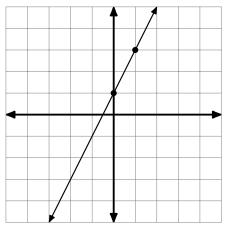
$$b = 1$$



$$y = 2x + 1$$

$$m = 2$$



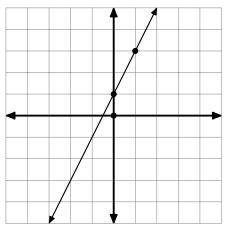


$$y \leq 2x + 1$$

$$y = 2x + 1$$

$$m=2$$

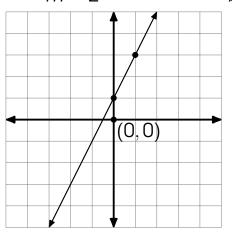




Plane divider

$$y = 2x + 1$$

$$m = 2$$

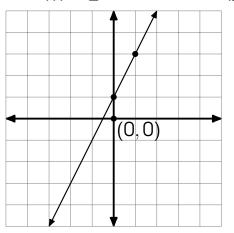


Let
$$x = 0, y = 0$$

Plane divider

$$y = 2x + 1$$

$$m = 2$$



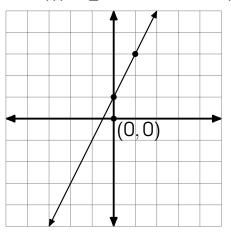
Let
$$x = 0, y = 0$$

 $y < 2x + 1$

Plane divider

$$y = 2x + 1$$

$$m = 2$$

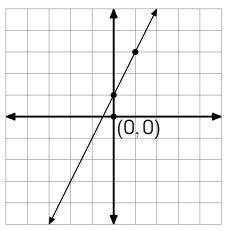


Let
$$x = 0, y = 0$$

 $y \le 2x + 1$
 $0 \le 2(0) + 1$

$$y = 2x + 1$$
$$b = 1$$

$$m = 2$$



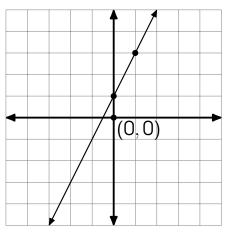
Let
$$x = 0, y = 0$$

 $y \le 2x + 1$
 $0 \le 2(0) + 1$
 $0 \le 0 + 1$

Plane divider

$$y = 2x + 1$$

$$m = 2$$



Let
$$x = 0, y = 0$$

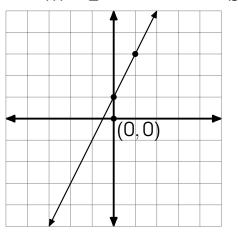
 $y \le 2x + 1$
 $0 \le 2(0) + 1$
 $0 \le 0 + 1$
 $0 < 1$

$$y \leq 2x + 1$$

$$y = 2x + 1$$

$$m=2$$





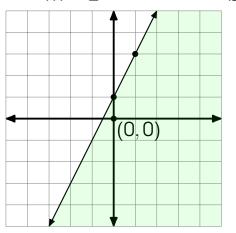
Let
$$x = 0, y = 0$$

 $y \le 2x + 1$
 $0 \le 2(0) + 1$
 $0 \le 0 + 1$
 $0 \le 1$

Plane divider

$$y = 2x + 1$$

$$m = 2$$



Let
$$x = 0, y = 0$$

 $y \le 2x + 1$
 $0 \le 2(0) + 1$
 $0 \le 0 + 1$
 $0 \le 1$

Example 2

Graph the inequality x - 2y > -2.

Original inequality x - 2y > -2

$$x - 2y > -2$$

Original inequality x - 2y > -2

$$x - 2y > -2$$

Example 2 Step 1: Replace the inequality symbol with an equal sign. The resulting equation becomes the plane divider.

x - 2y > -2Original inequality

x - 2y = -2Change > to =

Original inequality x - 2y > -2

$$x - 2y > -2$$

$$x - 2y = -2$$

Subtraction Property

Original inequality
$$x - 2y > -2$$

Change
$$>$$
 to $=$ $x - 2y = -2$

Subtraction Property
$$x - x - 2y = -x - 2$$

Original inequality
$$x - 2y > -2$$

Change
$$>$$
 to $=$ $x - 2y = -2$

Subtraction Property
$$x - x - 2y = -x - 2$$

Simplification

$$x - 2y > -2$$

$$x-2y=-2$$

Subtraction Property
$$x - x - 2y = -x - 2$$

$$x - x - 2y = -x - 2$$

$$-2y = -x - 2$$

$$x - 2y > -2$$

$$x-2y=-2$$

Subtraction Property x - x - 2y = -x - 2

$$x - x - 2y = -x - 2$$

Simplification

$$-2y=-x-2$$

Division Property

$$x - 2y > -2$$

$$x-2y=-2$$

Subtraction Property x - x - 2y = -x - 2

$$x - x - 2y = -x - 2$$

$$-2y = -x - 2$$

$$\frac{-2y}{-2} = \frac{-x}{-2} - \frac{2}{-2}$$

$$x - 2y > -2$$

$$x-2y=-2$$

Subtraction Property

$$x - x - 2y = -x - 2$$

Simplification

$$-2y = -x - 2$$

$$\frac{-2y}{-2} = \frac{-x}{-2} - \frac{2}{-2}$$

Simplification

$$x - 2y > -2$$

$$x-2y=-2$$

$$x - x - 2y = -x - 2$$

$$-2y = -x - 2$$

$$\frac{-2y}{-2} = \frac{-x}{-2} - \frac{2}{-2}$$

$$y=\frac{1}{2}x+1$$

$$x - 2y > -2$$

$$x - 2y = -2$$

Subtraction Property

$$x - x - 2y = -x - 2$$

Simplification

$$-2y = -x - 2$$

Division Property

$$\frac{-2y}{-2} = \frac{-x}{-2} - \frac{2}{-2}$$

Simplification

$$y=\frac{1}{2}x+1$$

$$m=\frac{1}{2}$$

$$b = 1$$

Example 2

Step 2: Graph the corresponding equation. Use broken line if the inequality contains < or > symbol or a solid line if inequality contains \leq or \geq symbol.

Original inequality x - 2y > -2

$$y = \frac{1}{2}x + 1$$

$$m=\frac{1}{2}$$

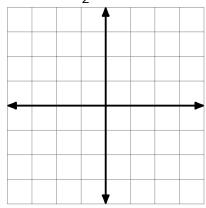
$$b = 1$$

$$x - 2y > -2$$

$$y = \frac{1}{2}x + 1$$

$$m = \frac{1}{2}$$

$$b = 1$$

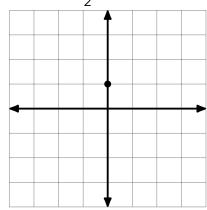


$$x - 2y > -2$$

$$y = \frac{1}{2}x + 1$$

$$m=\frac{1}{2}$$



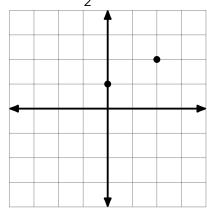


$$x - 2y > -2$$

$$y = \frac{1}{2}x + 1$$

$$m=\frac{1}{2}$$

$$b = 1$$

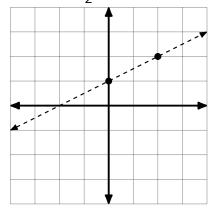


$$x - 2y > -2$$

$$y = \frac{1}{2}x + 1$$

$$m=\frac{1}{2}$$

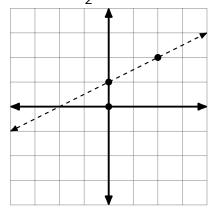
$$b = 1$$



$$y = \frac{1}{2}x + 1$$

$$m=\frac{1}{2}$$

$$b = 1$$

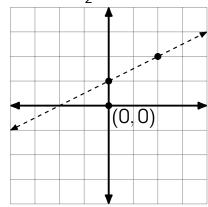


$$x - 2y > -2$$

$$y = \frac{1}{2}x + 1$$

$$m=\frac{1}{2}$$

$$b = 1$$

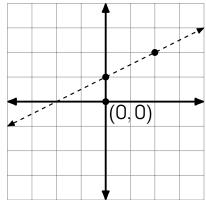


$$x - 2y > -2$$

$$y = \frac{1}{2}x + 1$$

$$m=\frac{1}{2}$$

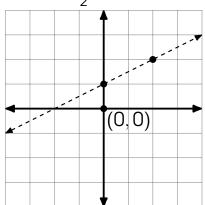
$$b = 1$$



Let
$$x = 0, y = 0$$

$$y = \frac{1}{2}x + 1$$

$$m=\frac{1}{2}$$



$$b = 1$$

Let
$$x = 0, y = 0$$

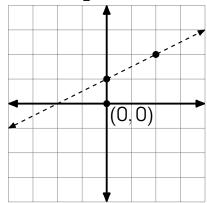
 $x - 2y > -2$

$$x - 2y > -2$$

$$y = \frac{1}{2}x + 1$$

$$m = \frac{1}{2}$$

$$b = 1$$



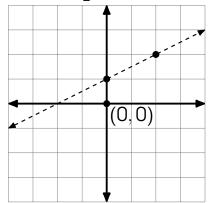
Let
$$x = 0$$
, $y = 0$
 $x - 2y > -2$
 $0 - 2(0) > -2$

$$x - 2y > -2$$

$$y = \frac{1}{2}x + 1$$

$$m=\frac{1}{2}$$

$$b = 1$$



Let
$$x = 0, y = 0$$

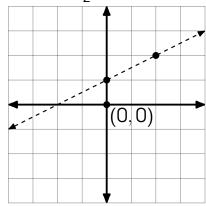
 $x - 2y > -2$
 $0 - 2(0) > -2$
 $0 - 0 > -2$

$$x - 2y > -2$$

$$y = \frac{1}{2}x + 1$$

$$m=\frac{1}{2}$$

$$b = 1$$



Let
$$x = 0, y = 0$$

 $x - 2y > -2$
 $0 - 2(0) > -2$
 $0 - 0 > -2$
 $0 > -2$

$$x - 2y > -2$$

$$y = \frac{1}{2}x + 1$$

$$m=\frac{1}{2}$$

$$b = 1$$

Let
$$x = 0, y = 0$$

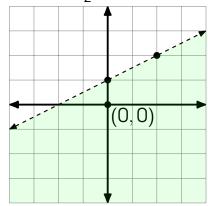
 $x - 2y > -2$
 $0 - 2(0) > -2$
 $0 - 0 > -2$
 $0 > -2$

$$x - 2y > -2$$

$$y = \frac{1}{2}x + 1$$

$$m = \frac{1}{2}$$

$$b = 1$$



Let
$$x = 0, y = 0$$

 $x - 2y > -2$
 $0 - 2(0) > -2$
 $0 - 0 > -2$
 $0 > -2$

Example 3

Graph the inequality $2x - 2y \ge -8$.

$$2x - 2y \ge -8$$

$$2x - 2y \ge -8$$

Change > to =

$$2x - 2y \ge -8$$

Change
$$\geq$$
 to $=$

$$2x - 2y = -8$$

$$2x - 2y \ge -8$$

Change
$$\geq$$
 to $=$

$$2x - 2y = -8$$

Subtraction Property

Change \geq to = 2x - 2y = -8

Subtraction Property 2x - 2x - 2y = -2x - 8

Change > to = 2x - 2y = -8

Subtraction Property 2x - 2x - 2y = -2x - 8

Simplification

Change \geq to = 2x - 2y = -8

Subtraction Property 2x - 2x - 2y = -2x - 8

Simplification -2y = -2x - 8

$$2x - 2y \ge -8$$

Change
$$\geq$$
 to $=$

$$2x - 2y = -8$$

Subtraction Property
$$2x - 2x - 2y = -2x - 8$$

$$-2y = -2x - 8$$

Division Property

$$2x - 2y \ge -8$$

Change
$$\geq$$
 to $=$

$$2x - 2y = -8$$

Subtraction Property
$$2x - 2x - 2y = -2x - 8$$

$$-2y = -2x - 8$$

$$\frac{-2y}{-2} = \frac{-2x}{-2} - \frac{8}{-2}$$

$$2x - 2y \ge -8$$

Change
$$\geq$$
 to $=$

$$2x - 2y = -8$$

Subtraction Property

$$2x - 2x - 2y = -2x - 8$$

$$-2y = -2x - 8$$

$$\frac{-2y}{-2} = \frac{-2x}{-2} - \frac{8}{-2}$$

Simplification

$$2x - 2y \ge -8$$

Change
$$\geq$$
 to $=$

$$2x - 2y = -8$$

Subtraction Property

$$2x - 2x - 2y = -2x - 8$$

$$-2y = -2x - 8$$

$$\frac{-2y}{-2} = \frac{-2x}{-2} - \frac{8}{-2}$$

$$y = x + 4$$

$$2x - 2y \ge -8$$

Change
$$\geq$$
 to $=$

$$2x - 2y = -8$$

Subtraction Property
$$2x - 2x - 2y = -2x - 8$$

$$-2y = -2x - 8$$

$$\frac{-2y}{-2} = \frac{-2x}{-2} - \frac{8}{-2}$$

$$y = x + 4$$

$$m = 1$$

$$b = 4$$

Example 3

Step 2: Graph the corresponding equation. Use broken line if the inequality contains < or > symbol or a solid line if inequality contains \le or \ge symbol.

Original inequality $2x - 2y \ge -8$

Plane divider y = x + 4

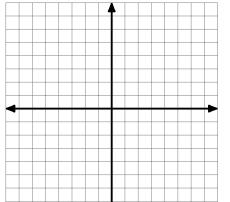
m=1 b=4

$$2x - 2y \ge -8$$

Plane divider

$$y = x + 4$$

$$m = 1$$

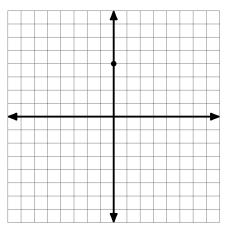


$$2x - 2y \ge -8$$

Plane divider

$$y = x + 4$$

$$m = 1$$

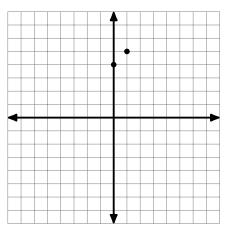


$$2x - 2y \ge -8$$

Plane divider

$$y = x + 4$$

$$m = 1$$

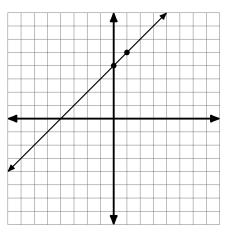


$$2x - 2y \ge -8$$

Plane divider

$$y = x + 4$$

$$m = 1$$

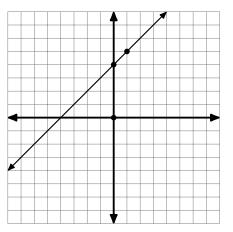


$$2x - 2y \ge -8$$

Plane divider

$$y = x + 4$$

$$m = 1$$

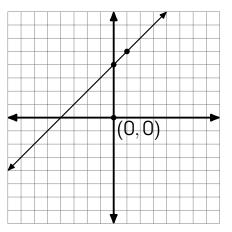


$$2x - 2y \ge -8$$

Plane divider

$$y = x + 4$$

$$m = 1$$

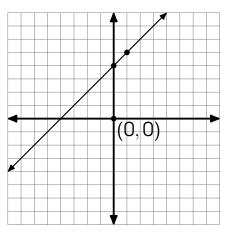


$$2x - 2y \ge -8$$

$$y = x + 4$$

$$m = 1$$

$$b = 4$$

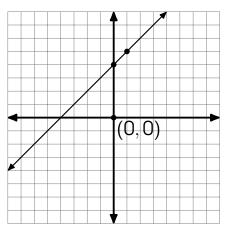


Let
$$x = 0, y = 0$$

$$b=4$$

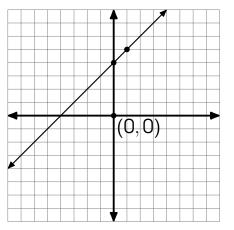
y = x + 4

$$m = 1$$



Let
$$x = 0$$
, $y = 0$
 $2x - 2y > -8$

$$m = 1$$



$$2x - 2y \ge -8$$

$$y = x + 4$$

$$b = 4$$

Let
$$x = 0, y = 0$$

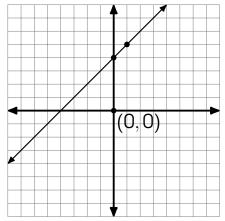
 $2x - 2y \ge -8$
 $2(0) - 2(0) \ge -8$

$$2x - 2y \ge -8$$

$$y = x + 4$$

$$m = 1$$





Let
$$x = 0, y = 0$$

 $2x - 2y \ge -8$
 $2(0) - 2(0) \ge -8$
 $0 - 0 > -8$

$$y = x + 4$$

$$m = 1$$



Let
$$x = 0, y = 0$$

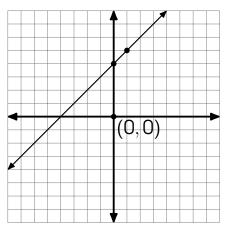
 $2x - 2y \ge -8$
 $2(0) - 2(0) \ge -8$
 $0 - 0 \ge -8$
 $0 > -8$

$$2x - 2y \ge -8$$

$$y = x + 4$$

$$m = 1$$

$$b = 4$$



Let
$$x = 0, y = 0$$

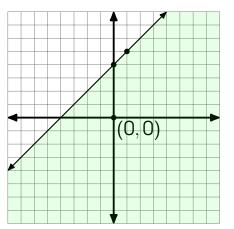
 $2x - 2y \ge -8$
 $2(0) - 2(0) \ge -8$
 $0 - 0 \ge -8$
 $0 > -8$

$$2x - 2y \ge -8$$

$$y = x + 4$$

$$m = 1$$

$$b = 4$$



Let
$$x = 0, y = 0$$

 $2x - 2y \ge -8$
 $2(0) - 2(0) \ge -8$
 $0 - 0 \ge -8$
 $0 > -8$

Example 4

Graph the inequality -3x + y < -2.

Original inequality
$$-3x + y < -2$$

Original inequality
$$-3x + y < -2$$

Change
$$<$$
 to $=$ $-3x + y = -2$

Original inequality
$$-3x + y < -2$$

Change
$$<$$
 to $=$ $-3x + y = -2$

Addition Property

Original inequality
$$-3x + y < -2$$

Change
$$<$$
 to $=$ $-3x + y = -2$

Addition Property
$$-3x + 3x + y = 3x - 2$$

Original inequality
$$-3x + y < -2$$

Change
$$<$$
 to $=$ $-3x + y = -2$

Addition Property
$$-3x + 3x + y = 3x - 2$$

Simplification

Original inequality
$$-3x + y < -2$$

Change
$$<$$
 to $=$ $-3x + y = -2$

Addition Property
$$-3x + 3x + y = 3x - 2$$

Simplification
$$y = 3x - 2$$

Original inequality
$$-3x + y < -2$$

Change
$$<$$
 to $=$ $-3x + y = -2$

Addition Property
$$-3x + 3x + y = 3x - 2$$

Simplification
$$y = 3x - 2$$

$$m = 3$$
 $b = -2$

Example 4

Step 2: Graph the corresponding equation. Use broken line if the inequality contains < or > symbol or a solid line if inequality contains \le or \ge symbol.

Original inequality
$$-3x + y < -2$$

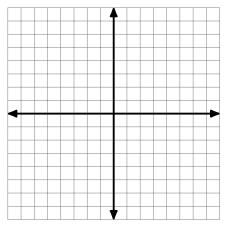
Plane divider
$$y = 3x - 2$$

$$m = 3$$
 $b = -2$

$$y = 3x - 2$$

$$m = 3$$

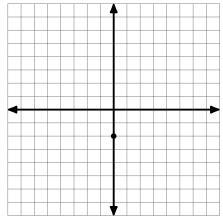




$$y = 3x - 2$$

$$m = 3$$

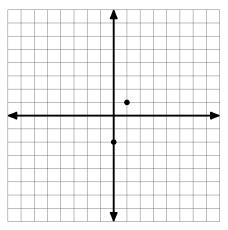




$$y = 3x - 2$$

$$m = 3$$

$$b = -2$$



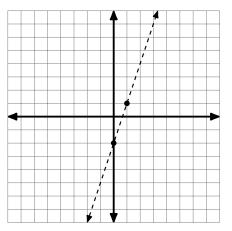
$$-3x + y < -2$$

Plane divider

$$y = 3x - 2$$

b = -2

$$m = 3$$



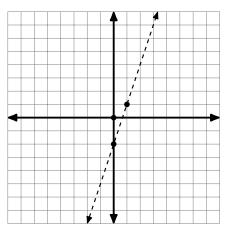
$$-3x + y < -2$$

Plane divider

$$y = 3x - 2$$

b = -2

$$m = 3$$



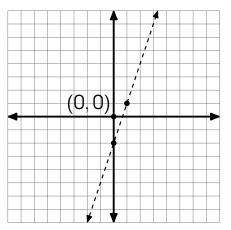
$$-3x + y < -2$$

Plane divider

$$y = 3x - 2$$

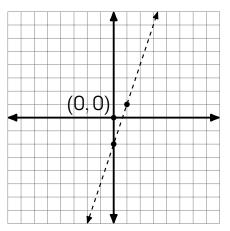
b = -2

$$m = 3$$



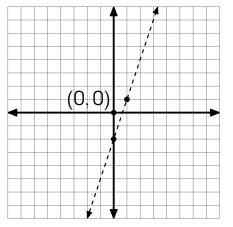
$$y = 3x - 2$$
$$b = -2$$

$$m = 3$$



Let
$$x = 0, y = 0$$

$$m = 3$$



$$-3x + y < -2$$

$$y = 3x - 2$$

$$b = -2$$

Let
$$x = 0, y = 0$$

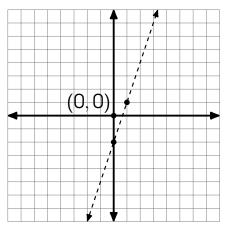
 $-3x + y < -2$

$$-3x + y < -2$$

$$y = 3x - 2$$

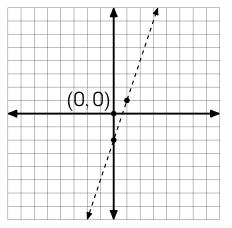
$$m = 3$$

$$b = -2$$



Let
$$x = 0$$
, $y = 0$
 $-3x + y < -2$
 $-3(0) + 0 < -2$

$$m = 3$$



$$-3x + y < -2$$

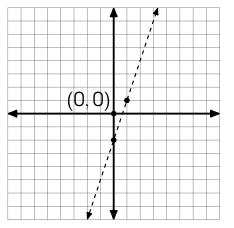
$$y = 3x - 2$$

$$b = -2$$

Let
$$x = 0, y = 0$$

 $-3x + y < -2$
 $-3(0) + 0 < -2$
 $0 + 0 < -2$

$$m = 3$$

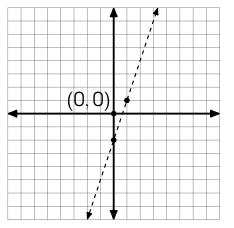


$$-3x + y < -2$$

$$y = 3x - 2$$
$$b = -2$$

Let
$$x = 0$$
, $y = 0$
 $-3x + y < -2$
 $-3(0) + 0 < -2$
 $0 + 0 < -2$
 $0 < -2$

$$m = 3$$



$$-3x + y < -2$$

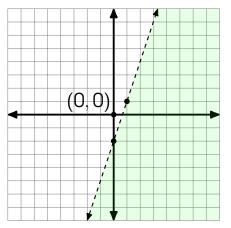
$$y = 3x - 2$$

$$b = -2$$

Let
$$x = 0, y = 0$$

 $-3x + y < -2$
 $-3(0) + 0 < -2$
 $0 + 0 < -2$
 $0 < -2$

$$m = 3$$



$$-3x + y < -2$$

$$y = 3x - 2$$

$$b = -2$$

Let
$$x = 0$$
, $y = 0$
 $-3x + y < -2$
 $-3(0) + 0 < -2$
 $0 + 0 < -2$
 $0 < -2$

Thank you for watching.