

# Linear Equations in Two Variables

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# What is a Linear Equation?

Linear Equation: an equation in two variables which can be written in the form  $Ax + By = C$ , where  $A, B \neq 0$ , and  $A, B, C \in \mathbb{R}$ .

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# What is a Solution of a Linear Equation?

The solution of a linear equation in two variables is an ordered pair that makes the equation true.



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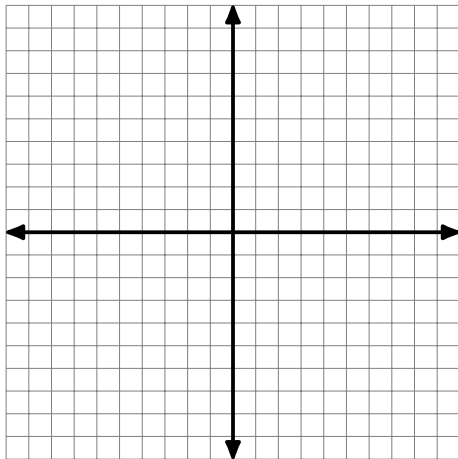
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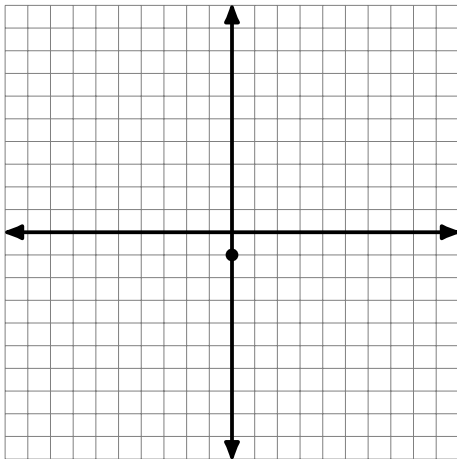
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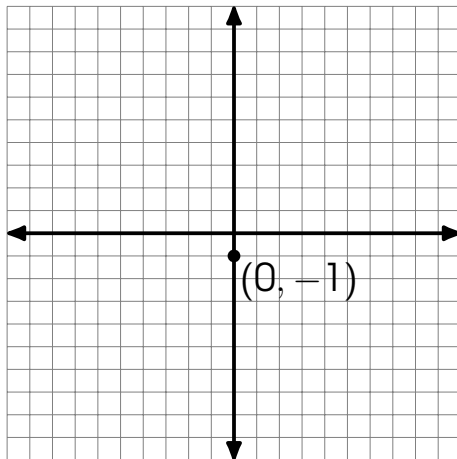
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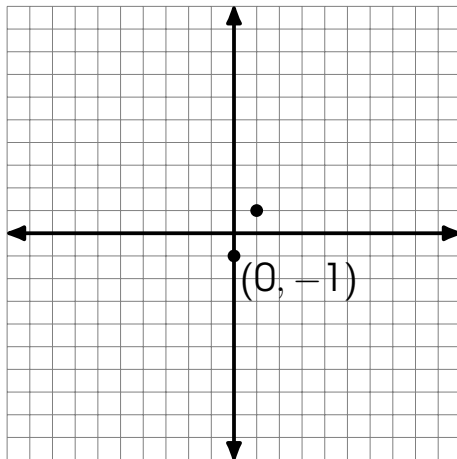
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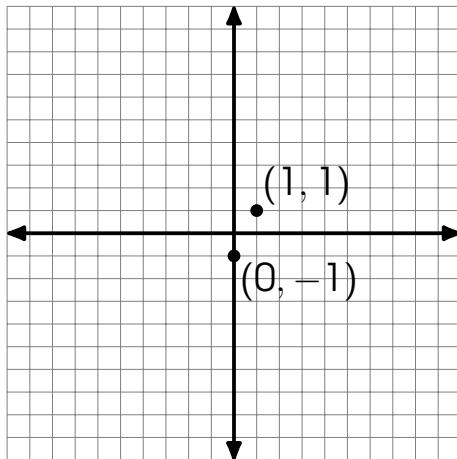
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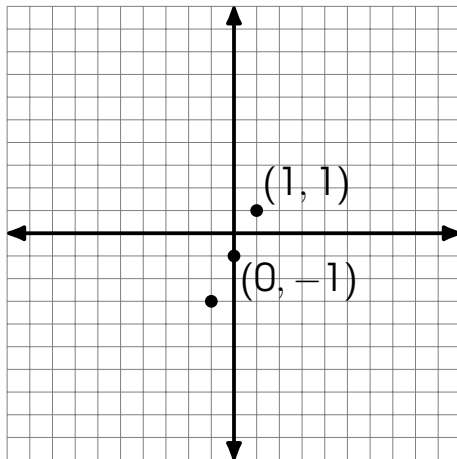
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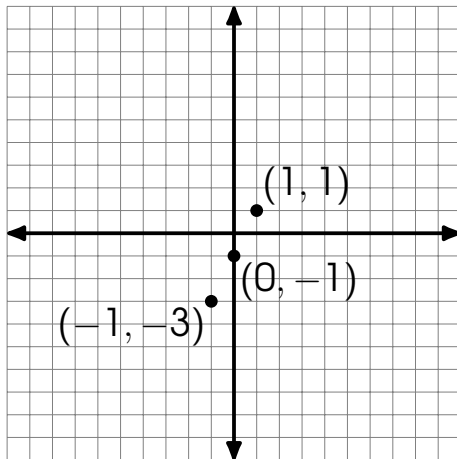
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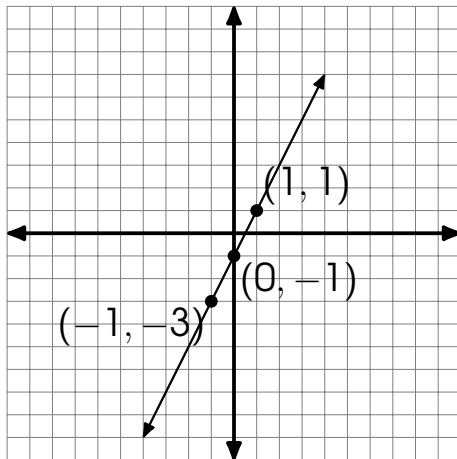
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$\therefore$  if  $x = -2$ , then  $y = 4$ .

**Thank you for watching.**