Solving Problems Involving Linear Equations – Constant Rate

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1. Read, understand, and analyze the problem.

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According to science, the ambient temperature varies with height. The ground temperature is 33 °C and the ambient temperature in Tagaytay, situated at a height of 639 meters, is 29 °C. Assuming that the relationship between the temperature and height is linear, express the temperature T (in °C) in terms of the height h (in meters). Hint: ground temperature is at O meters elevation. What is the ambient temperature in La Trinidad, Benguet which is situated at 1318 meters above sea level?

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m = \frac{y}{x}
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Find: $T_L = \text{temperature in La Trinidad}$

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h_l = 1318 \text{ m. (height of La Trinidad)}
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$$y = mx + b$$

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$$y = mx + b$$
$$T = -\frac{4}{\sqrt{20}}$$

Given:
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$$y = mx + b$$
$$T = -\frac{4}{639}h$$

Given:
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 $b = 33$
 $h_L = 1318 \text{ m. (height of La Trinidad)}$

$$y = mx + b$$

 $T = -\frac{4}{639}h + 33$ Substitution Property

Given:
$$y = \text{temperature } T \text{ (in °C)}$$

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 $m = \frac{y}{x} = \frac{T}{h} = \frac{29 - 33}{639} = \frac{-4}{639}$
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 $h_L = 1318 \text{ m. (height of La Trinidad)}$

$$y = mx + b$$

 $T = -\frac{4}{639}h + 33$ Substitution Property

$$\therefore$$
 the working equation is $T = -\frac{4}{639}h + 33$



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Given: $h_L = 1318 \,\text{m.}$ (height of La Trinidad)

Find: T_L = temperature in La Trinidad

$$T = -\frac{4}{639}h + 33$$

$$T = -\frac{4}{639}h + 33$$
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 Substitution Property

$$T=-rac{4}{639}h+33$$

$$T_L=-rac{4}{639}(1318)+33 \quad ext{Substitution Property}$$

$$T_L=-8.25+33$$

$$T = -\frac{4}{639}h + 33$$

$$T_L = -\frac{4}{639}(1318) + 33$$
 Substitution Property
$$T_L = -8.25 + 33$$
 Simplification

$$T=-rac{4}{639}h+33$$
 $T_L=-rac{4}{639}(1318)+33$ Substitution Property $T_L=-8.25+33$ Simplification $T_L=24.75$

Given: $h_L = 1318$ m. (height of La Trinidad) Find: $T_L = \text{temperature in La Trinidad}$

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 $T_L=-rac{4}{639}(1318)+33$ Substitution Property $T_L=-8.25+33$ Simplification $T_L=24.75$ Simplification

∴ the temperature in La Trinidad is 24.75 °C.



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A small company buys computer equipment for 200,000 pesos. After 2 years the value of the computer equipment is expected to be 120,000 pesos. What linear equation can be used to assess the value V of the equipment given a time t in years after it is bought? What will be the value of the computer equipment 4 years after it was bought?

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Given: y = value V of equipment

x = time t in years

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x = \text{time } t \text{ in years}

m = \frac{y}{x}
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x = \text{time } t \text{ in years}

m = \frac{y}{x} = \frac{V}{t} =
```

Given:
$$y = \text{value } V \text{ of equipment}$$

 $x = \text{time } t \text{ in years}$
 $m = \frac{y}{x} = \frac{V}{t} = \frac{120,000 - 200,000}{2}$

Given:
$$y$$
 = value V of equipment x = time t in years m = $\frac{y}{x} = \frac{V}{t} = \frac{120,000 - 200,000}{2} = -40,000$

Given:
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 $x = \text{time } t \text{ in years}$
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$$t_4 = \text{time after 4 years}$$

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Given: y = value V of equipment x = time t in years m = \frac{y}{x} = \frac{V}{t} = \frac{120,000-200,000}{2} = -40,000 b = 200,000 t_4 = time after 4 years Find: V_4 = value after 4 years
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Given: y = \text{value } V \text{ of equipment}
          x = time t in years
          m = \frac{y}{x} = \frac{V}{t} = \frac{120,000 - 200,000}{2} = -40,000
          b = 200,000
          t_{A} = time after 4 years
Find:
          V_{A} = value after 4 years
y = mx + b
```

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          x = time t in years
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Find:
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```

```
Given: V = \text{value } V \text{ of equipment}
         x = time t in years
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          b = 200,000
          t_{A} = time after 4 years
Find:
         V_{A} = value after 4 years
y = mx + b
V = -40,000
```

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Given: V = \text{value } V \text{ of equipment}
         x = time t in years
          m = \frac{y}{x} = \frac{V}{t} = \frac{120,000 - 200,000}{2} = -40,000
          b = 200,000
          t_{A} = time after 4 years
Find:
         V_{A} = value after 4 years
y = mx + b
V = -40,000t
```

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Given: V = \text{value } V \text{ of equipment}
         x = time t in years
         m = \frac{y}{x} = \frac{V}{t} = \frac{120,000 - 200,000}{2} = -40,000
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          t_{A} = time after 4 years
Find:
         V_{A} = value after 4 years
v = mx + b
V = -40,000t + 200,000
```

```
Given: V = \text{value } V \text{ of equipment}
         x = time t in years
         m = \frac{y}{x} = \frac{V}{t} = \frac{120,000 - 200,000}{2} = -40,000
         b = 200,000
         t_{A} = time after 4 years
Find:
         V_{A} = value after 4 years
v = mx + b
V = -40,000t + 200,000 Substitution Property
```

Given:
$$y$$
 = value V of equipment x = time t in years
$$m = \frac{y}{x} = \frac{V}{t} = \frac{120,000 - 200,000}{2} = -40,000$$

$$b = 200,000$$

$$t_4 = \text{time after 4 years}$$
 Find: V_4 = value after 4 years

$$y = mx + b$$

$$V = -40,000t + 200,000$$
 Substitution Property

 \therefore the working equation is V = -40,000t + 200,000

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Given: t_4 = time after 4 years
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$$V = -40,000t + 200,000$$

```
Given: t_4 = time after 4 years
Find: V_4 = value after 4 years
V = -40,000t + 200,000
V_4 = -40,000(4) + 200,000
```

```
Given: t_4 = time after 4 years
Find: V_4 = value after 4 years
V = -40,000t + 200,000
V_4 = -40,000(4) + 200,000 Substitution
```

```
Given: t_4 = time after 4 years
Find: V_4 = value after 4 years
V = -40,000t + 200,000
V_4 = -40,000(4) + 200,000 Substitution
V_4 = -160,000 + 200,000
```

```
Given: t_{\Delta} = time after 4 years
Find: V_A = value after 4 years
V = -40,000t + 200,000
V_4 = -40,000(4) + 200,000
                              Substitution
V_{\rm A} = -160,000 + 200,000
```

Simplification

```
Given: t_{\Delta} = time after 4 years
Find: V_A = value after 4 years
V = -40,000t + 200,000
V_4 = -40,000(4) + 200,000
                              Substitution
V_{1} = -160,000 + 200,000
                             Simplification
V_4 = 40,000
```

Given:
$$t_4$$
 = time after 4 years
Find: V_4 = value after 4 years
 $V = -40,000t + 200,000$
 $V_4 = -40,000(4) + 200,000$ Substitution
 $V_4 = -160,000 + 200,000$ Simplification
 $V_4 = 40,000$ Simplification

... the value of the equipment after 4 years is \$\frac{1}{2}40,000.



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Thank you for watching.