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1 Basic

1.1 .vimrc

```
syn on
se ai nu ru cul mouse=a
se cin et ts=2 sw=2 sts=2
so $VIMRUNTIME/mswin.vim
colo desert
se gfn=Monospace\ 14
noremap <buffer><F9> :! g++ -std=c++14 -O2 -Wall -
    Wshadow '%' -o '%<'<CR>
noremap <buffer><F5> :! './%<'<CR>
noremap <buffer><F6> :! './%<' < './%.in'<CR>
noremap <buffer><F7> :! './%<' < './%.in' > './%.out'
    <CR>
```

1.2 Increase Stack Size

```
//stack resize (linux)
#include <sys/resource.h>
void increase_stack_size() {
    const rlim_t ks = 64*1024*1024;
    struct rlimit rl;
    int res=getrlimit(RLIMIT_STACK, &rl);
    if(res==0){
        if(rl.rlim_cur<ks){
            rl.rlim_cur=ks;
            res=setrlimit(RLIMIT_STACK, &rl);
        }
    }
}
```

2 Math

2.1 Euclidean's Algorithm

```
// a must be greater than b
pair< int, int > gcd( int a, int b ) {
    if ( b == 0 ) return { 1, 0 };
    pair< int, int > q = gcd( b, b % a );
    return { q.second, q.first - q.second * ( a / b ) };
}
```

2.2 Big Integer

```
const int base = 1000000000;
const int base_digits = 9;

class Bigint {
public:
    vector< int > a;
    int sign;

    Bigint() : sign( 1 ) {}
    Bigint( long long v ) { *this = v; }
    Bigint( const string &s ) { read( s ); }
    void operator=( const Bigint &v ) {
        sign = v.sign;
        a = v.a;
    }
    void operator=( long long v ) {
        sign = 1;
        if ( v < 0 ) sign = -1, v = -v;
        for ( ; v > 0; v = v / base ) a.push_back( v % base );
    }
    Bigint operator+( const Bigint &v ) const {
        if ( sign == v.sign ) {
            Bigint res = v;
            for ( int i = 0, carry = 0; i < (int)max( a.size(), v.a.size() ) || carry; ++i ) {
                if ( i == (int)res.a.size() ) res.a.push_back( 0 );
                res.a[ i ] += carry + ( i < (int)a.size() ? a[ i ] : 0 );
                carry = res.a[ i ] >= base;
                if ( carry ) res.a[ i ] -= base;
            }
        }
    }
}
```

```

    }
    return res;
}
return *this - ( -v );
}
Bigint operator-( const Bigint &v ) const {
    if ( sign == v.sign ) {
        if ( abs() >= v.abs() ) {
            Bigint res = *this;
            for ( int i = 0, carry = 0; i < (int)v.a.size() || carry; ++i ) {
                res.a[ i ] -= carry + ( i < (int)v.a.size() ? v.a[ i ] : 0 );
                carry = res.a[ i ] < 0;
                if ( carry ) res.a[ i ] += base;
            }
            res.trim();
            return res;
        }
        return -( v - *this );
    }
    return *this + ( -v );
}
void operator*=( int v ) {
    if ( v < 0 ) sign = -sign, v = -v;
    for ( int i = 0, carry = 0; i < (int)a.size() || carry; ++i ) {
        if ( i == (int)a.size() ) a.push_back( 0 );
        long long cur = a[ i ] * (long long)v + carry;
        carry = (int)( cur / base );
        a[ i ] = (int)( cur % base );
    }
    trim();
}
Bigint operator*( int v ) const {
    Bigint res = *this;
    res *= v;
    return res;
}

friend pair< Bigint, Bigint > divmod( const Bigint &
    a1, const Bigint &b1 ) {
    int norm = base / ( b1.a.back() + 1 );
    Bigint a = a1.abs() * norm;
    Bigint b = b1.abs() * norm;
    Bigint q, r;
    q.a.resize( a.a.size() );

    for ( int i = a.a.size() - 1; i >= 0; i-- ) {
        r *= base;
        r += a.a[ i ];
        int s1 = r.a.size() <= b.a.size() ? 0 : r.a[ b.a.size() ];
        int s2 = r.a.size() <= b.a.size() - 1 ? 0 : r.a[ b.a.size() - 1 ];
        int d = ( (long long)base * s1 + s2 ) / b.a.back();
        r -= b * d;
        while ( r < 0 ) r += b, --d;
        q.a[ i ] = d;
    }

    q.sign = a1.sign * b1.sign;
    r.sign = a1.sign;
    q.trim();
    r.trim();
    return make_pair( q, r / norm );
}

Bigint operator/( const Bigint &v ) const { return
    divmod( *this, v ).first; }

Bigint operator%( const Bigint &v ) const { return
    divmod( *this, v ).second; }

void operator/=( int v ) {
    if ( v < 0 ) sign = -sign, v = -v;
    for ( int i = (int)a.size() - 1, rem = 0; i >= 0; --i ) {
        long long cur = a[ i ] + rem * (long long)base;
        a[ i ] = (int)( cur / v );
        rem = (int)( cur % v );
    }
}

```

```

    }
    trim();
}
Bigint operator/( int v ) const {
    Bigint res = *this;
    res /= v;
    return res;
}
int operator%( int v ) const {
    if ( v < 0 ) v = -v;
    int m = 0;
    for ( int i = a.size() - 1; i >= 0; --i ) m = ( a[ i ] + m * (long long)base ) % v;
    return m * sign;
}

void operator+=( const Bigint &v ) { *this = *this + v; }
void operator-=( const Bigint &v ) { *this = *this - v; }
void operator*=( const Bigint &v ) { *this = *this * v; }
void operator/=( const Bigint &v ) { *this = *this / v; }

bool operator<( const Bigint &v ) const {
    if ( sign != v.sign ) return sign < v.sign;
    if ( a.size() != v.a.size() ) return a.size() * sign < v.a.size() * v.sign;
    for ( int i = a.size() - 1; i >= 0; i-- )
        if ( a[ i ] != v.a[ i ] ) return a[ i ] * sign < v.a[ i ] * sign;
    return false;
}

bool operator>( const Bigint &v ) const { return v < *this; }
bool operator<=( const Bigint &v ) const { return !( v < *this ); }
bool operator>=( const Bigint &v ) const { return !( *this < v ); }
bool operator==( const Bigint &v ) const { return !( *this < v ) && !( v < *this ); }
bool operator!=( const Bigint &v ) const { return *this < v || v < *this; }

void trim() {
    while ( !a.empty() && !a.back() ) a.pop_back();
    if ( a.empty() ) sign = 1;
}
bool isZero() const { return a.empty() || ( a.size() == 1 && !a[ 0 ] ); }
Bigint operator-() const {
    Bigint res = *this;
    res.sign = -sign;
    return res;
}
Bigint abs() const {
    Bigint res = *this;
    res.sign = res.sign;
    return res;
}
long long longValue() const {
    long long res = 0;
    for ( int i = a.size() - 1; i >= 0; i-- ) res = res * base + a[ i ];
    return res * sign;
}

friend Bigint gcd( const Bigint &a, const Bigint &b ) {
    return b.isZero() ? a : gcd( b, a % b );
}
friend Bigint lcm( const Bigint &a, const Bigint &b ) {
    return a / gcd( a, b ) * b;
}
void read( const string &s ) {
    sign = 1;
    a.clear();
    int pos = 0;
    while ( pos < (int)s.size() && ( s[ pos ] == '-' || s[ pos ] == '+' ) ) {
        if ( s[ pos ] == '-' ) sign = -sign;
        ++pos;
    }
}

```

```

    for ( int i = s.size() - 1; i >= pos; i -=
        base_digits ) {
        int x = 0;
        for ( int j = max( pos, i - base_digits + 1 ); j
            <= i; j++ ) x = x * 10 + s[ j ] - '0';
        a.push_back( x );
    }
    trim();
}
friend istream &operator>>( istream &stream, Bigint &
    v ) {
    string s;
    stream >> s;
    v.read( s );
    return stream;
}
friend ostream &operator<<( ostream &stream, const
    Bigint &v ) {
    if ( v.sign == -1 ) stream << '-';
    stream << ( v.a.empty() ? 0 : v.a.back() );
    for ( int i = (int)v.a.size() - 2; i >= 0; --i )
        stream << setw( base_digits ) << setfill( '0' )
            << v.a[ i ];
    return stream;
}
static vector< int > convert_base( const vector< int
    > &a, int old_digits, int new_digits ) {
    vector< long long > p( max( old_digits, new_digits
        ) + 1 );
    p[ 0 ] = 1;
    for ( int i = 1; i < (int)p.size(); i++ ) p[ i ] =
        p[ i - 1 ] * 10;
    vector< int > res;
    long long cur = 0;
    int cur_digits = 0;
    for ( int i = 0; i < (int)a.size(); i++ ) {
        cur += a[ i ] * p[ cur_digits ];
        cur_digits += old_digits;
        while ( cur_digits >= new_digits ) {
            res.push_back( int( cur % p[ new_digits ] ) );
            cur /= p[ new_digits ];
            cur_digits -= new_digits;
        }
    }
    res.push_back( (int)cur );
    while ( !res.empty() && !res.back() ) res.pop_back
        ();
    return res;
}
typedef vector< long long > vll;
static vll karatsubaMultiply( const vll &a, const vll
    &b ) {
    int n = a.size();
    vll res( n + n );
    if ( n <= 32 ) {
        for ( int i = 0; i < n; i++ )
            for ( int j = 0; j < n; j++ ) res[ i + j ] += a
                [ i ] * b[ j ];
        return res;
    }
    int k = n >> 1;
    vll a1( a.begin(), a.begin() + k );
    vll a2( a.begin() + k, a.end() );
    vll b1( b.begin(), b.begin() + k );
    vll b2( b.begin() + k, b.end() );

    vll a1b1 = karatsubaMultiply( a1, b1 );
    vll a2b2 = karatsubaMultiply( a2, b2 );

    for ( int i = 0; i < k; i++ ) a2[ i ] += a1[ i ];
    for ( int i = 0; i < k; i++ ) b2[ i ] += b1[ i ];

    vll r = karatsubaMultiply( a2, b2 );
    for ( int i = 0; i < (int)a1b1.size(); i++ ) r[ i ]
        -= a1b1[ i ];
    for ( int i = 0; i < (int)a2b2.size(); i++ ) r[ i ]
        -= a2b2[ i ];

    for ( int i = 0; i < (int)r.size(); i++ ) res[ i +
        k ] += r[ i ];
    for ( int i = 0; i < (int)a1b1.size(); i++ ) res[ i
        ] += a1b1[ i ];
}

```

```

    for ( int i = 0; i < (int)a2b2.size(); i++ ) res[ i
        + n ] += a2b2[ i ];
    return res;
}
Bigint operator*( const Bigint &v ) const {
    vector< int > a6 = convert_base( this->a,
        base_digits, 6 );
    vector< int > b6 = convert_base( v.a, base_digits,
        6 );
    vll a( a6.begin(), a6.end() );
    vll b( b6.begin(), b6.end() );
    while ( a.size() < b.size() ) a.push_back( 0 );
    while ( b.size() < a.size() ) b.push_back( 0 );
    while ( a.size() & ( a.size() - 1 ) ) a.push_back(
        0 ), b.push_back( 0 );
    vll c = karatsubaMultiply( a, b );
    Bigint res;
    res.sign = sign * v.sign;
    for ( int i = 0, carry = 0; i < (int)c.size(); i++
        ) {
        long long cur = c[ i ] + carry;
        res.a.push_back( (int)( cur % 1000000 ) );
        carry = (int)( cur / 1000000 );
    }
    res.a = convert_base( res.a, 6, base_digits );
    res.trim();
    return res;
}
};

```

2.3 FFT

```

// const int MAXN = 262144;
// (must be 2^k)
// before any usage, run pre_fft() first
//
// To implement poly. multiply:
//
// fft( n , a );
// fft( n , b );
// for( int i = 0 ; i < n ; i++ )
//     c[ i ] = a[ i ] * b[ i ];
// fft( n , c , 1 );
//
// then you have the result in c :: [cplx]
typedef long double ld;
typedef complex<ld> cplx;
const ld PI = acos(-1);
const cplx I(0, 1);
cplx omega[MAXN+1];
void pre_fft(){
    for(int i=0; i<=MAXN; i++)
        omega[i] = exp(i * 2 * PI / MAXN * I);
}
// n must be 2^k
void fft(int n, cplx a[], bool inv=false){
    int basic = MAXN / n;
    int theta = basic;
    for (int m = n; m >= 2; m >= 1) {
        int mh = m >> 1;
        for (int i = 0; i < mh; i++) {
            cplx w = omega[inv ? MAXN-(i*theta%MAXN)
                : i*theta%MAXN];
            for (int j = i; j < n; j += m) {
                int k = j + mh;
                cplx x = a[j] - a[k];
                a[j] += a[k];
                a[k] = w * x;
            }
        }
        theta = (theta * 2) % MAXN;
    }
    int i = 0;
    for (int j = 1; j < n - 1; j++) {
        for (int k = n >> 1; k > (i ^ k); k >= 1);
        if (j < i) swap(a[i], a[j]);
    }
    if (inv)
        for (i = 0; i < n; i++)
            a[i] /= n;
}

```

```

}

```

2.4 NTT

```

typedef long long LL;
// Remember coefficient are mod P
/* p=a*2^n+1
n    2^n    p    a    root
5    32     97    3    5
6    64    193    3    5
7    128   257    2    3
8    256   257    1    3
9    512  7681   15   17
10   1024 12289   12   11
11   2048 12289    6   11
12   4096 12289    3   11
13   8192 40961    5    3
14  16384 65537    4    3
15  32768 65537    2    3
16  65536 65537    1    3
17 131072 786433    6   10
18 262144 786433    3   10 (605028353,
    2308, 3)
19 524288 5767169   11    3
20 1048576 7340033    7    3
21 2097152 23068673   11    3
22 4194304 104857601  25    3
23 8388608 167772161  20    3
24 16777216 167772161 10    3
25 33554432 167772161 5     3 (1107296257, 33,
    10)
26 67108864 469762049 7     3
27 134217728 2013265921 15  31 */
// (must be 2^k)
// To implement poly. multiply:
// NTT<P, root, MAXN> ntt;
// ntt( n , a ); // or ntt.tran( n , a );
// ntt( n , b );
// for( int i = 0 ; i < n ; i++ )
//   c[ i ] = a[ i ] * b[ i ];
// ntt( n , c , 1 );
//
// then you have the result in c :: [LL]
template<LL P, LL root, int MAXN>
struct NTT{
    static LL bigmod(LL a, LL b) {
        LL res = 1;
        for (LL bs = a; b; b >>= 1, bs = (bs * bs) % P) {
            if(b&1) res=(res*bs)%P;
        }
        return res;
    }
    static LL inv(LL a, LL b) {
        if(a==1)return 1;
        return (((LL)(a-inv(b%a,a))*b+1)/a)%b;
    }
    LL omega[MAXN+1];
    NTT() {
        omega[0] = 1;
        LL r = bigmod(root, (P-1)/MAXN);
        for (int i=1; i<=MAXN; i++)
            omega[i] = (omega[i-1]*r)%P;
    }
    // n must be 2^k
    void tran(int n, LL a[], bool inv_ntt=false){
        int basic = MAXN / n;
        int theta = basic;
        for (int m = n; m >= 2; m >>= 1) {
            int mh = m >> 1;
            for (int i = 0; i < mh; i++) {
                LL w = omega[i*theta%MAXN];
                for (int j = i; j < n; j += m) {
                    int k = j + mh;
                    LL x = a[j] - a[k];
                    if (x < 0) x += P;
                    a[j] += a[k];
                    if (a[j] > P) a[j] -= P;
                    a[k] = (w * x) % P;
                }
            }
        }
    }
}

```

```

        theta = (theta * 2) % MAXN;
    }
    int i = 0;
    for (int j = 1; j < n - 1; j++) {
        for (int k = n >> 1; k > (i ^= k); k >>= 1);
        if (j < i) swap(a[i], a[j]);
    }
    if (inv_ntt) {
        LL ni = inv(n,P);
        reverse( a+1 , a+n );
        for (i = 0; i < n; i++)
            a[i] = (a[i] * ni) % P;
    }
}
void operator()(int n, LL a[], bool inv_ntt=false) {
    tran(n, a, inv_ntt);
}
};
const LL P=2013265921,root=31;
const int MAXN=4194304;
NTT<P, root, MAXN> ntt;

```

2.5 Miller Rabin

```

// n < 4,759,123,141    3 : 2, 7, 61
// n < 1,122,004,669,633 4 : 2, 13, 23, 1662803
// n < 3,474,749,660,383    6 : pirmses <= 13
// n < 2^64              7 :
// 2, 325, 9375, 28178, 450775, 9780504, 1795265022
// Make sure testing integer is in range [2, n-2] if
// you want to use magic.
bool witness(LL a,LL n,LL u,int t){
    LL x=mypow(a,u,n);
    for(int i=0;i<t;i++){
        LL nx=mul(x,x,n);
        if(nx==1&&x!=1&&x!=n-1) return 1;
        x=nx;
    }
    return x!=1;
}
bool miller_rabin(LL n,int s=100) {
    // iterate s times of witness on n
    // return 1 if prime, 0 otherwise
    if(n<2) return 0;
    if(!(n&1)) return n == 2;
    LL u=n-1; int t=0;
    // n-1 = u*2^t
    while(!(u&1)) u>>=1, t++;
    while(s--){
        LL a=randll()%(n-1)+1;
        if(witness(a,n,u,t)) return 0;
    }
    return 1;
}

```

2.6 Chinese Remainder

```

int pfn;
// number of distinct prime factors
int pf[MAXN]; // prime factor powers
int rem[MAXN]; // corresponding remainder
int pm[MAXN];
inline void generate_primes() {
    int i,j;
    pnum=1;
    prime[0]=2;
    for(i=3;i<MAXVAL;i+=2) {
        if(nprime[i]) continue;
        prime[pnum++]=i;
        for(j=i*i;j<MAXVAL;j+=i) nprime[j]=1;
    }
}
inline int inverse(int x,int p) {
    int q,tmp,a=x,b=p;
    int a0=1,a1=0,b0=0,b1=1;
    while(b) {
        q=a/b; tmp=b; b=a-b*q; a=tmp;
        tmp=b0; b0=a0-b0*q; a0=tmp;
    }
}

```

```

    tmp=b1; b1=a1-b1*q; a1=tmp;
}
return a0;
}
inline void decompose_mod() {
    int i,p,t=mod;
    pfn=0;
    for(i=0;i<pnum&&prime[i]<=t;i++) {
        p=prime[i];
        if(t%p==0) {
            pf[pfn]=1;
            while(t%p==0) {
                t/=p;
                pf[pfn]*=p;
            }
            pfn++;
        }
    }
    if(t>1) pf[pfn++]=t;
}
inline int chinese_remainder() {
    int i,m,s=0;
    for(i=0;i<pfn;i++) {
        m=mod/pf[i];
        pm[i]=(LL)m*inverse(m,pf[i])%mod;
        s=(s+(LL)pm[i]*rem[i])%mod;
    }
    return s;
}

```

2.7 Pollard's rho

```

// does not work when n is prime
LL f(LL x, LL mod){
    return add(mul(x,x,mod),1,mod);
}
LL pollard_rho(LL n) {
    if(!(n&1)) return 2;
    while(true){
        LL y=2, x=rand()%(n-1)+1, res=1;
        for(int sz=2; res==1; sz*=2) {
            for(int i=0; i<sz && res<=1; i++) {
                x = f(x, n);
                res = __gcd(abs(x-y), n);
            }
            y = x;
        }
        if (res!=0 && res!=n) return res;
    }
}

```

2.8 Roots of Polynomial

```

const double eps = 1e-12;
const double inf = 1e+12;
double a[ 10 ], x[ 10 ];
int n;
int sign( double x ){
    return (x < -eps)?(-1):(x>eps);
}
double f(double a[], int n, double x){
    double tmp=1,sum=0;
    for(int i=0;i<=n;i++){
        sum=sum+a[i]*tmp;
        tmp=tmp*x;
    }
    return sum;
}
double binary(double l,double r,double a[],int n){
    int sl=sign(f(a,n,l)),sr=sign(f(a,n,r));
    if(sl==0) return l;
    if(sr==0) return r;
    if(sl*sr>0) return inf;
    while(r-l>eps){
        double mid=(l+r)/2;
        int ss=sign(f(a,n,mid));
        if(ss==0) return mid;
        if(ss*sl>0) l=mid; else r=mid;
    }
}

```

```

}
return l;
}
void solve(int n,double a[],double x[],int &nx){
    if(n==1){
        x[1]=-a[0]/a[1];
        nx=1;
        return;
    }
    double da[10], dx[10];
    int ndx;
    for(int i=n;i>=1;i--) da[i-1]=a[i]*i;
    solve(n-1,da,dx,ndx);
    nx=0;
    if(ndx==0){
        double tmp=binary(-inf,inf,a,n);
        if (tmp<inf) x[++nx]=tmp;
        return;
    }
    double tmp;
    tmp=binary(-inf,dx[1],a,n);
    if(tmp<inf) x[++nx]=tmp;
    for(int i=1;i<=ndx-1;i++){
        tmp=binary(dx[i],dx[i+1],a,n);
        if(tmp<inf) x[++nx]=tmp;
    }
    tmp=binary(dx[ndx],inf,a,n);
    if(tmp<inf) x[++nx]=tmp;
}
int main() {
    scanf("%d",&n);
    for(int i=n;i>=0;i--) scanf("%lf",&a[i]);
    int nx;
    solve(n,a,x,nx);
    for(int i=1;i<=nx;i++) printf("%.6f\n",x[i]);
}

```

2.9 Simplex

```

const int MAXN = 111;
const int MAXM = 111;
const double eps = 1E-10;
double a[MAXN][MAXM], b[MAXN], c[MAXN][MAXM];
double x[MAXN];
int ix[MAXN + MAXM]; // !!! array all indexed from 0
// max{cx} subject to {Ax<=b,x>=0}
// n: constraints, m: vars !!!
// x[] is the optimal solution vector
// usage :
// value = simplex(a, b, c, N, M);
double simplex(double a[MAXN][MAXM], double b[MAXN],
                double c[MAXM], int n, int m){
    ++m;
    int r = n, s = m - 1;
    memset(d, 0, sizeof(d));
    for (int i = 0; i < n + m; ++i) ix[i] = i;
    for (int i = 0; i < n; ++i) {
        for (int j = 0; j < m - 1; ++j) d[i][j] = -a[i][j];
        d[i][m - 1] = 1;
        d[i][m] = b[i];
        if (d[r][m] > d[i][m]) r = i;
    }
    for (int j = 0; j < m - 1; ++j) d[n][j] = c[j];
    d[n + 1][m - 1] = -1;
    for (double dd;; ) {
        if (r < n) {
            int t = ix[s]; ix[s] = ix[r + m]; ix[r + m] = t;
            d[r][s] = 1.0 / d[r][s];
            for (int j = 0; j <= m; ++j)
                if (j != s) d[r][j] *= -d[r][s];
            for (int i = 0; i <= n + 1; ++i) if (i != r) {
                for (int j = 0; j <= m; ++j) if (j != s)
                    d[i][j] += d[r][j] * d[i][s];
                d[i][s] *= d[r][s];
            }
        }
        r = -1; s = -1;
        for (int j = 0; j < m; ++j)
            if (s < 0 || ix[s] > ix[j]) {
                if (d[n + 1][j] > eps ||

```

```

        (d[n + 1][j] > -eps && d[n][j] > eps))
        s = j;
    }
    if (s < 0) break;
    for (int i = 0; i < n; ++i) if (d[i][s] < -eps) {
        if (r < 0 ||
            (dd = d[r][m] / d[r][s] - d[i][m] / d[i][s])
            < -eps ||
            (dd < eps && ix[r + m] > ix[i + m]))
            r = i;
    }
    if (r < 0) return -1; // not bounded
}
if (d[n + 1][m] < -eps) return -1; // not executable
double ans = 0;
for (int i = 0; i < m; ++i) x[i] = 0;
for (int i = m; i < n + m; ++i) { // the missing
    enumerated x[i] = 0
    if (ix[i] < m - 1) {
        ans += d[i - m][m] * c[ix[i]];
        x[ix[i]] = d[i - m][m];
    }
}
return ans;
}
}

```

3 Data Structure

3.1 Disjoint Set

```

class DisjointSet {
public:
    static const int N = 1e5 + 10;
    int p[ N ];
    void Init( int x ) {
        for ( int i = 1; i <= x; ++i ) p[ i ] = i;
    }
    int Find( int x ) { return x == p[ x ] ? x : p[ x ] =
        Find( p[ x ] ); }
    void Union( int x, int y ) { p[ Find( x ) ] = Find( y
        ); }
};

```

3.2 Segement Tree with Lazy Tag

```

#define L( X ) ( X << 1 )
#define R( X ) ( ( X << 1 ) + 1 )
#define mid ( ( l + r ) >> 1 )

class SegmentTree {
public:
    static const int N = 1e5 + 10;
    int arr[ N ], st[ N << 2 ], lazy[ N << 2 ];

    inline void Pull( int now ) { st[ now ] = max( st[ L(
        now ) ], st[ R( now ) ] ); }
    inline void Push( int now, int l, int r ) {
        if ( lazy[ now ] != 0 ) {
            if ( l != r ) {
                st[ L( now ) ] += lazy[ now ];
                st[ R( now ) ] += lazy[ now ];
                lazy[ L( now ) ] += lazy[ now ];
                lazy[ R( now ) ] += lazy[ now ];
            }
            lazy[ now ] = 0;
        }
    }
    void Build( int now, int l, int r ) {
        if ( l == r ) {
            st[ now ] = arr[ l ];
            return;
        }
        Build( L( now ), l, mid );
        Build( R( now ), mid + 1, r );
        Pull( now );
    }
}

```

```

void Update( int ql, int qr, int value, int now, int
    l, int r ) {
    if ( ql > qr || l > qr || r < ql ) return;
    Push( now, l, r );
    if ( l == ql && qr == r ) {
        st[ now ] += value;
        lazy[ now ] += value;
        return;
    }
    if ( qr <= mid )
        Update( ql, qr, value, L( now ), l, mid );
    else if ( mid < ql )
        Update( ql, qr, value, R( now ), mid + 1, r );
    else {
        Update( ql, mid, value, L( now ), l, mid );
        Update( mid + 1, qr, value, R( now ), mid + 1, r
            );
    }
    Pull( now );
}

int Query( int ql, int qr, int now, int l, int r ) {
    if ( ql > qr || l > qr || r < ql ) return 0;
    Push( now, l, r );
    if ( l == ql && qr == r ) return st[ now ];
    if ( qr <= mid )
        return Query( ql, qr, L( now ), l, mid );
    else if ( mid < ql )
        return Query( ql, qr, R( now ), mid + 1, r );
    else {
        int left = Query( ql, mid, L( now ), l, mid );
        int right = Query( mid + 1, qr, R( now ), mid +
            1, r );
        int ans = max( left, right );
        return ans;
    }
}
};

```

3.3 Copy on Write Segement Tree

```

// tested with ASC 29 B
#define mid ( ( l + r ) >> 1 )
class Node {
public:
    int value, l, r, who;
    Node() {}
    Node( int _v ) : value( _v ) { l = r = who = 0; }
};
class SegmentTree {
public:
    static const int N = 1e9;
    vector< Node > st;

    inline void Pull( int now ) {
        int lchild = st[ now ].l;
        int rchild = st[ now ].r;
        if ( lchild != 0 ) {
            st[ now ].value = st[ lchild ].value;
            st[ now ].who = st[ lchild ].who;
        }
        if ( rchild != 0 && st[ rchild ].value > st[ now ].
            value ) {
            st[ now ].value = st[ rchild ].value;
            st[ now ].who = st[ rchild ].who;
        }
    }
    void Build() {
        st.push_back( Node() ); // Null Node
        st.push_back( Node( 0 ) );
    }
    void Update( int ql, int qr, int value, int who, int
        now = 1, int l = 1, int r = N ) {
        if ( ql > qr or qr < l or ql > r ) return;
        if ( l == ql && qr == r ) {
            st[ now ].value = value;
            st[ now ].who = who;
            return;
        }
        if ( qr <= mid ) {
            if ( st[ now ].l == 0 ) {

```



```

        st[ now ].l = st.size();
        st.push_back( Node( 0 ) );
    }
    Update( ql, qr, value, who, st[ now ].l, l, mid )
    ;
}
else if ( mid < ql ) {
    if ( st[ now ].r == 0 ) {
        st[ now ].r = st.size();
        st.push_back( Node( 0 ) );
    }
    Update( ql, qr, value, who, st[ now ].r, mid + 1,
        r );
}
else {
    if ( st[ now ].l == 0 ) {
        st[ now ].l = st.size();
        st.push_back( Node( 0 ) );
    }
    if ( st[ now ].r == 0 ) {
        st[ now ].r = st.size();
        st.push_back( Node( 0 ) );
    }
    Update( ql, mid, value, who, st[ now ].l, l, mid
        );
    Update( mid + 1, qr, value, who, st[ now ].r, mid
        + 1, r );
}
Pull( now );
}
pair< int, int > Query( int ql, int qr, int now = 1,
    int l = 1, int r = N ) {
    if ( ql > qr or qr < l or ql > r ) return { 0, 0 };
    if ( l == ql && qr == r ) {
        return { st[ now ].value, st[ now ].who };
    }
    if ( qr <= mid ) {
        if ( st[ now ].l == 0 ) return { 0, 0 };
        return Query( ql, qr, st[ now ].l, l, mid );
    }
    else if ( mid < ql ) {
        if ( st[ now ].r == 0 ) return { 0, 0 };
        return Query( ql, qr, st[ now ].r, mid + 1, r );
    }
    else {
        pair< int, int > lchild = { 0, 0 };
        if ( st[ now ].l != 0 ) lchild = Query( ql, mid,
            st[ now ].l, l, mid );
        pair< int, int > rchild = { 0, 0 };
        if ( st[ now ].r != 0 ) rchild = Query( mid + 1,
            qr, st[ now ].r, mid + 1, r );
        pair< int, int > ans = { 0, 0 };
        if ( lchild.first > ans.first ) {
            ans.first = lchild.first;
            ans.second = lchild.second;
        }
        if ( rchild.first > ans.first ) {
            ans.first = rchild.first;
            ans.second = rchild.second;
        }
        return ans;
    }
}
};

```

3.4 Persistent Segment Tree

```

// tested with spoj MKTHNUM - K-th Number
#define mid ( ( l + r ) >> 1 )
class Node {
public:
    int value, l, r;
    Node() { value = l = r = 0; }
};
class SegmentTree {
public:
    static const int N = 1e5 + 10;
    int ver_size, st_size;
    vector< int > ver;
    vector< Node > st;

```

```

SegmentTree() {
    ver_size = st_size = 0;
    ver.resize( N );
    st.resize( 70 * N );
    ver[ ver_size++ ] = 1;
    st[ 0 ] = st[ 1 ] = Node();
    st_size = 2;
}
void AddVersion() {
    ver[ ver_size++ ] = st_size++;
    st[ ver[ ver_size - 1 ] ] = st[ ver[ ver_size - 2 ]
        ];
}
inline void Pull( int now ) {
    int lchild = st[ now ].l, rchild = st[ now ].r;
    st[ now ].value = st[ lchild ].value + st[ rchild
        ].value;
}
void Build( int now = 1, int l = 1, int r = N ) {
    if ( l == r ) return;
    st[ now ].l = st_size++;
    st[ now ].r = st_size++;
    Build( st[ now ].l, l, mid );
    Build( st[ now ].r, mid + 1, r );
    Pull( now );
}
void Update( int prv_now, int now, int pos, int l =
    1, int r = N ) {
    if ( l == r ) {
        st[ now ].value += 1;
        return;
    }
    if ( pos <= mid ) {
        st[ now ].l = st_size++;
        st[ st[ now ].l ] = st[ st[ prv_now ].l ];
        Update( st[ prv_now ].l, st[ now ].l, pos, l, mid
            );
    }
    else {
        st[ now ].r = st_size++;
        st[ st[ now ].r ] = st[ st[ prv_now ].r ];
        Update( st[ prv_now ].r, st[ now ].r, pos, mid +
            1, r );
    }
    Pull( now );
}
pair< int, bool > Query( int prv_now, int now, int k,
    int l = 1, int r = N ) {
    int prv_value = st[ prv_now ].value, now_value = st
        [ now ].value;
    if ( l == r && now_value - prv_value == k )
        return make_pair( l, true );
    else if ( now_value - prv_value < k )
        return make_pair( now_value - prv_value, false );
    pair< int, bool > child = Query( st[ prv_now ].l,
        st[ now ].l, k, l, mid );
    if ( child.second == false ) {
        k -= st[ st[ now ].l ].value - st[ st[ prv_now ].
            l ].value;
        child = Query( st[ prv_now ].r, st[ now ].r, k,
            mid + 1, r );
    }
    return child;
}
};

```

3.5 Rope

```

#include<ext/rope>
using namespace __gnu_cxx;
// inserts c before p.
iterator insert(const iterator& p, charT c) :
// inserts n copies of c before p.
iterator insert(const iterator& p, size_t n, charT c) :
// inserts the character c before the ith element.
void insert(size_t i, charT c) :
// erases the element pointed to by p.
void erase(const iterator& p) :
// erases the range [f, l).

```

```

void erase(const iterator& f, const iterator& l) :
// Append a C string.
void append(const charT* s) :
void replace(const iterator& f, const iterator& l,
const rope& x)
void replace(const iterator& f, const iterator& l,
const charT* s)
void replace(const iterator& f1, const iterator& l1,
const charT* f2, const charT* l2)
void replace(const iterator& f1, const iterator& l1,
const iterator& f2, const iterator& l2)
void replace(const iterator& p, const rope& x)
void replace(size_t i, size_t n, const rope& x)
void replace(size_t i, size_t n, charT c)
void replace(size_t i, size_t n, const charT* f, const
charT* l)
void replace(size_t i, size_t n, const iterator& f,
const iterator& l)
rope substr(iterator f, iterator l) const
rope substr(const_iterator f, const_iterator l) const
rope substr(size_t i, size_t n = 1) const

```

3.6 pb_ds

```

/*****PB_DS priority_queue*****/
#include <ext/pb_ds/priority_queue.hpp>
using namespace __gnu_pbds;
typedef priority_queue<T,less<T>,pairing_heap_tag> PQ;
typedef PQ::point_iterator PQit;
point_iterator push(const_reference key)
void modify(point_iterator it, const_reference key)
void erase(point_iterator it)
T top()
void pop()
point_iterator begin()
point_iterator end()
void join(priority_queue &other)
template<class Pred> void split(Pred prd,
priority_queue &other) //Other will contain only
values v for which prd(v) is true. When calling
this method, other's policies must be equivalent to
this object's policies.
template<class Pred> size_type erase_if(Pred prd) //
Erases any value satisfying prd; returns the number
of value erased.
//1. push will return a point_iterator, which can be
saved in a vector and modify or erase afterward.
//2. using begin() and end() can traverse all elements
in the priority_queue.
//3. after join, other will be cleared.
//4. for optimizing Dijkstra, use pairing_heap
//5. binary_heap_tag is better than std::priority_queue
//6. pairing_heap_tag is better than binomial_heap_tag
and rc_binomial_heap_tag
//7. when using only push, pop and join, use
binary_heap_tag
//8. when using modify, use pairing_heap_tag or
thin_heap_tag
/*****PB_DS tree*****/
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
typedef tree<K, T, less<K>, rb_tree_tag, Node_Update>
TREE;
//similar to std::map
//when T = __gnu_pbds::null_type, become std::set
//when Node_Update = tree_order_statistics_node_update,
TREE become a ordered TREE with two new functions:
//1. iterator find_by_order(size_type order) return the
smallest order-th element(e.x. when order = 0,
return the smallest element), when order > TREE.
size(), return end()
//2. size_type order_of_key(const_reference key) return
number of elements smaller than key
void join(tree &other) //other和*this的值域不能相交
void split(const_reference key, tree &other) // 清空
other, 然後把*this當中所有大於key的元素移到other
//自定義Node_Update: 查詢子段和的map<int, int>, 需要紀
圖子樹的mapped_value的和。
template<class Node_CItr, class Node_Itr, class Cmp_Fn,
class _Alloc>

```

```

struct my_nd_upd {
virtual Node_CItr node_begin () const = 0;
virtual Node_CItr node_end () const = 0;
typedef int metadata_type ; //額外信息, 這邊用int
inline void operator()(Node_Itr it,Node_CItr end_it){
Node_Itr l=it.get_l_child(), r=it.get_r_child();
int left = 0 , right = 0;
if(l != end_it) left = l.get_metadata();
if(r != end_it) right = r.get_metadata();
const_cast<metadata_type&>(it.get_metadata())=
left+right+(*it)->second;
}
//operator()功能是把節點it的信息更新, end_it表空節點
//it是Node_Itr, *之後變成iterator, 再取->second變節點
的mapped_value
inline int prefix_sum (int x) {
int ans = 0;
Node_CItr it = node_begin();
while(it!=node_end()){
Node_CItr l = it.get_l_child() , r = it.
get_r_child();
if(Cmp_Fn()(x , (*it)->first)) it = l;
else {
ans += (*it)->second;
if(l != node_end ()) ans += l.get_metadata();
it = r;
}
}
return ans;
}
inline int interval_sum(int l ,int r)
{return prefix_sum(r)-prefix_sum(l-1);}
};
tree<int, int, less<int>, rb_tree_tag, my_nd_upd> T;
printf("%d\n", T.interval_sum(a, b));
/*****PB_DS hash*****/
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/hash_policy.hpp>
__gnu_pbds::cc_hash_table<Key, Mapped>
__gnu_pbds::gp_hash_table<Key, Mapped>
//支援find和operator[]
/*****PB_DS trie*****/
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/trie_policy.hpp>
typedef trie<string, null_type,
trie_string_access_traits<>, pat_trie_tag,
trie_prefix_search_node_update> pref_trie;
pref_trie.insert(const string &str);
auto range = pref_trie.prefix_range(const string &str);
for(auto it = range.first; it != range.second; ++it)
cout << *it << '\n';

```

	push	pop	modify	erase	join
std::priority_queue	lg(n)	lg(n)	n lg(n)	n lg(n)	n lg(n)
pairing_heap_tag	1	lg(n)	lg(n)	lg(n)	1
binary_heap_tag	lg(n)	lg(n)	n	n	n
binomial_heap_tag	1	lg(n)	lg(n)	lg(n)	lg(n)
rc_binomial_heap_tag	1	lg(n)	lg(n)	lg(n)	lg(n)
thin_heap_tag	1	lg(n)	lg(n)[ps]	lg(n)	n

ps: 1 if increased_key only else lg(n)

3.7 Link-Cut Tree

```

const int MXN = 100005;
const int MEM = 100005;
struct Splay {
static Splay nil, mem[MEM], *pmem;
Splay *ch[2], *f;
int val, rev, size;
Splay () : val(-1), rev(0), size(0)
{ f = ch[0] = ch[1] = &nil; }
Splay (int _val) : val(_val), rev(0), size(1)
{ f = ch[0] = ch[1] = &nil; }
bool isr()
{ return f->ch[0] != this && f->ch[1] != this; }
int dir()
{ return f->ch[0] == this ? 0 : 1; }
void setCh(Splay *c, int d){
ch[d] = c;
if (c != &nil) c->f = this;
pull();
}
}

```



```

void push(){
    if( !rev ) return;
    swap(ch[0], ch[1]);
    if (ch[0] != &nil) ch[0]->rev ^= 1;
    if (ch[1] != &nil) ch[1]->rev ^= 1;
    rev=0;
}
void pull(){
    size = ch[0]->size + ch[1]->size + 1;
    if (ch[0] != &nil) ch[0]->f = this;
    if (ch[1] != &nil) ch[1]->f = this;
}
} Splay::nil, Splay::mem[MEM], *Splay::pmem = Splay::
    mem;
Splay *nil = &Splay::nil;
void rotate(Splay *x){
    Splay *p = x->f;
    int d = x->dir();
    if (!p->isr()) p->f->setCh(x, p->dir());
    else x->f = p->f;
    p->setCh(x->ch[d], d);
    x->setCh(p, !d);
    p->pull(); x->pull();
}
vector<Splay*> splayVec;
void splay(Splay *x){
    splayVec.clear();
    for (Splay *q=x;; q=q->f){
        splayVec.push_back(q);
        if (q->isr()) break;
    }
    reverse(begin(splayVec), end(splayVec));
    for (auto it : splayVec) it->push();
    while (!x->isr()) {
        if (x->f->isr()) rotate(x);
        else if (x->dir()==x->f->dir())
            rotate(x->f), rotate(x);
        else rotate(x), rotate(x);
    }
}
Splay* access(Splay *x){
    Splay *q = nil;
    for (;x!=nil;x=x->f){
        splay(x);
        x->setCh(q, 1);
        q = x;
    }
    return q;
}
void evert(Splay *x){
    access(x);
    splay(x);
    x->rev ^= 1;
    x->push(); x->pull();
}
void link(Splay *x, Splay *y){
    // evert(x);
    access(x);
    splay(x);
    evert(y);
    x->setCh(y, 1);
}
void cut(Splay *x, Splay *y){
    // evert(x);
    access(y);
    splay(y);
    y->push();
    y->ch[0] = y->ch[0]->f = nil;
}
int N, Q;
Splay *vt[MXN];
int ask(Splay *x, Splay *y){
    access(x);
    access(y);
    splay(x);
    int res = x->f->val;
    if (res == -1) res=x->val;
    return res;
}
int main(int argc, char** argv){
    scanf("%d%d", &N, &Q);
    for (int i=1; i<=N; i++)

```

```

    vt[i] = new (Splay::pmem++) Splay(i);
while (Q--) {
    char cmd[105];
    int u, v;
    scanf("%s", cmd);
    if (cmd[1] == 'i') {
        scanf("%d%d", &u, &v);
        link(vt[v], vt[u]);
    } else if (cmd[0] == 'c') {
        scanf("%d", &v);
        cut(vt[1], vt[v]);
    } else {
        scanf("%d%d", &u, &v);
        int res=ask(vt[u], vt[v]);
        printf("%d\n", res);
    }
}
}
}

```

3.8 Treap

```

struct Treap{
    int sz, val, pri, tag;
    Treap *l, *r;
    Treap( int _val ){
        val = _val; sz = 1;
        pri = rand(); l = r = NULL; tag = 0;
    }
};
void push( Treap *a ){
    if( a->tag ){
        Treap *swp = a->l; a->l = a->r; a->r = swp;
        int swp2;
        if( a->l ) a->l->tag ^= 1;
        if( a->r ) a->r->tag ^= 1;
        a->tag = 0;
    }
}
int Size( Treap *a ){ return a ? a->sz : 0; }
void pull( Treap *a ){
    a->sz = Size( a->l ) + Size( a->r ) + 1;
}
Treap* merge( Treap *a, Treap *b ){
    if( !a || !b ) return a ? a : b;
    if( a->pri > b->pri ){
        push( a );
        a->r = merge( a->r, b );
        pull( a );
        return a;
    } else {
        push( b );
        b->l = merge( a, b->l );
        pull( b );
        return b;
    }
}
void split( Treap *t, int k, Treap*&a, Treap*&b ){
    if( !t ){ a = b = NULL; return; }
    push( t );
    if( Size( t->l ) + 1 <= k ){
        a = t;
        split( t->r, k - Size( t->l ) - 1, a->r, b );
        pull( a );
    } else {
        b = t;
        split( t->l, k, a, b->l );
        pull( b );
    }
}
}

```

4 Graph

4.1 Dijkstra's Algorithm

```

template< class T >
using MinHeap = priority_queue< T, vector< T >, greater
    < T > >;

```

```
vector< pair< int, int > > v[ N ];
vector< int > Dijkstra( int s ) {
    // n: number of nodes
    vector< int > d( n + 1, 1e9 );
    vector< bool > visit( n + 1, false );
    d[ s ] = 0;

    MinHeap< pair< int, int > > pq;
    pq.push( make_pair( d[ s ], s ) );
    while ( 1 ) {
        int now = -1;
        while ( !pq.empty() and visit[ now = pq.top().
            second ] ) pq.pop();
        if ( now == -1 or visit[ now ] ) break;
        visit[ now ] = true;
        for ( int i = 0; i < v[ now ].size(); ++i ) {
            int child = v[ now ][ i ].first;
            int w = v[ now ][ i ].second;
            if ( !visit[ child ] and ( d[ now ] + w ) < d[
                child ] ) {
                d[ child ] = d[ now ] + w;
                pq.push( make_pair( d[ child ], child ) );
            }
        }
    }
    return d;
}
```

4.2 Tarjan's Algorithm

```
// Build:  $O(V^2)$ , Query:  $O(1)$ 
// n: the number of nodes
int graph[ N ][ N ], lca[ N ][ N ];
vector< bool > visit( N, false );

void tarjan( int now ) {
    if ( visit[ now ] ) return;
    visit[ now ] = true;

    for ( int i = 1; i <= n; ++i )
        if ( visit[ i ] ) lca[ now ][ i ] = lca[ i ][ now ]
            = st.Find( i );

    for ( int i = 1; i <= n; ++i )
        if ( g[ now ][ i ] < 1e9 && !visit[ i ] ) {
            tarjan( i );
            st.Union( i, now );
        }
}
```

4.3 Jump Pointer Algorithm

```
// Build:  $O(V \log V)$ , Query:  $O(\log V)$ 
int tin[ N ], tout[ N ], ancestor[ N ][ 20 ];
vector< int > v[ N ];

void dfs( int now, int pnow ) {
    tin[ now ] = ++now_time;

    ancestor[ now ][ 0 ] = pnow;
    for ( int i = 1; i < 20; ++i )
        ancestor[ now ][ i ] = ancestor[ ancestor[ now ][ i - 1 ] ][ i - 1 ];

    for ( auto child : v[ now ] )
        if ( child != pnow ) dfs( child, now );

    tout[ now ] = ++now_time;
}

bool check_ancestor( int x, int y ) { return ( tin[ x ]
    <= tin[ y ] && tout[ x ] >= tout[ y ] ); }

int find_lca( int x, int y ) {
    if ( check_ancestor( x, y ) ) return x;
    if ( check_ancestor( y, x ) ) return y;

    for ( int i = 19; i >= 0; --i )
```

```
    if ( !check_ancestor( ancestor[ x ][ i ], y ) ) x =
        ancestor[ x ][ i ];
    return ancestor[ x ][ 0 ];
}
```

4.4 Maximum Clique

```
// max N = 64
typedef unsigned long long ll;
struct MaxClique{
    static const int N = 64;
    ll nb[ N ], n, ans;
    void init( ll _n ){
        n = _n;
        for( int i = 0 ; i < n ; i ++ ) nb[ i ] = 0LLU;
    }
    void add_edge( ll _u , ll _v ){
        nb[ _u ] |= ( 1LLU << _v );
        nb[ _v ] |= ( 1LLU << _u );
    }
    void B( ll r , ll p , ll x , ll cnt , ll res ){
        if( cnt + res < ans ) return;
        if( p == 0LLU && x == 0LLU ){
            if( cnt > ans ) ans = cnt;
            return;
        }
        ll y = p | x; y &= -y;
        ll q = p & ( ~nb[ int( log2( y ) ) ] );
        while( q ){
            ll i = int( log2( q & (-q) ) );
            B( r | ( 1LLU << i ) , p & nb[ i ] , x & nb[ i ]
                , cnt + 1LLU , __builtin_popcountll( p & nb[
                    i ] ) );
            q &= ~( 1LLU << i );
            p &= ~( 1LLU << i );
            x |= ( 1LLU << i );
        }
    }
    int solve(){
        ans = 0;
        ll _set = 0;
        if( n < 64 ) _set = ( 1LLU << n ) - 1;
        else{
            for( ll i = 0 ; i < n ; i ++ ) _set |= ( 1LLU <<
                i );
        }
        B( 0LLU , _set , 0LLU , 0LLU , n );
        return ans;
    }
} maxClique;
```

4.5 Heavy-Light Decomposition

```
#define SZ(c) (int)(c).size()
#define ALL(c) (c).begin(), (c).end()
#define REP(i, s, e) for(int i = (s); i <= (e); i++)
#define REPD(i, s, e) for(int i = (s); i >= (e); i--)
typedef tuple< int , int > tii;
const int MAXN = 100010;
const int LOG = 19;
struct HLD{
    int n;
    vector<int> g[MAXN];
    int sz[MAXN], dep[MAXN];
    int ts, tid[MAXN], tdi[MAXN], tl[MAXN], tr[MAXN];
    // ts : timestamp , useless after yutruLi
    // tid[ u ] : pos. of node u in the seq.
    // tdi[ i ] : node at pos i of the seq.
    // tl , tr[ u ] : subtree interval in the seq. of
        node u
    int mom[MAXN][LOG], head[MAXN];
    // head[ u ] : head of the chain contains u
    void dfssz(int u, int p){
        dep[u] = dep[p] + 1;
        mom[u][0] = p;
        sz[u] = 1;
        head[u] = u;
        for(int& v:g[u]) if(v != p){
```

```

    dep[v] = dep[u] + 1;
    dfssz(v, u);
    sz[u] += sz[v];
}
}
void dfshl(int u){
    //printf("dfshl %d\n", u);
    ts++;
    tid[u] = tl[u] = tr[u] = ts;
    tdi[tid[u]] = u;
    sort(ALL(g[u]),
        [&](int a, int b){return sz[a] > sz[b];});
    bool flag = 1;
    for(int& v:g[u]) if(v != mom[u][0]){
        if(flag) head[v] = head[u], flag = 0;
        dfshl(v);
        tr[u] = tr[v];
    }
}
inline int lca(int a, int b){
    if(dep[a] > dep[b]) swap(a, b);
    //printf("lca %d %d\n", a, b);
    int diff = dep[b] - dep[a];
    REPD(k, LOG-1, 0) if(diff & (1<<k)){
        //printf("b %d\n", mom[b][k]);
        b = mom[b][k];
    }
    if(a == b) return a;
    REPD(k, LOG-1, 0) if(mom[a][k] != mom[b][k]){
        a = mom[a][k];
        b = mom[b][k];
    }
    return mom[a][0];
}
void init( int _n ){
    n = _n;
    REP( i , 1 , n ) g[ i ].clear();
}
void addEdge( int u , int v ){
    g[ u ].push_back( v );
    g[ v ].push_back( u );
}
void yutruli(){
    dfssz(1, 0);
    ts = 0;
    dfshl(1);
    REP(k, 1, LOG-1) REP(i, 1, n)
        mom[i][k] = mom[mom[i][k-1]][k-1];
}
vector< tii > getPath( int u , int v ){
    vector< tii > res;
    while( tid[ u ] < tid[ head[ v ] ] ){
        res.push_back( tii(tid[ head[ v ] ], tid[ v ]) );
        v = mom[ head[ v ] ][ 0 ];
    }
    res.push_back( tii( tid[ u ] , tid[ v ] ) );
    reverse( ALL( res ) );
    return res;
}
/*
 * res : list of intervals from u to v
 * u must be ancestor of v
 * usage :
 * vector< tii >& path = tree.getPath( u , v )
 * for( tii tp : path ) {
 *     int l , r; tie( l , r ) = tp;
 *     upd( l , r );
 *     uu = tree.tdi[ l ] , vv = tree.tdi[ r ];
 *     uu ~> vv is a heavy path on tree
 * }
 */
}
} tree;

```

4.6 Dominator Tree

```

const int MAXN = 100010;
struct DominatorTree{
#define REP(i,s,e) for(int i=(s);i<=(e);i++)
#define REPD(i,s,e) for(int i=(s);i>=(e);i--)

```

```

int n , m , s;
vector< int > g[ MAXN ] , pred[ MAXN ];
vector< int > cov[ MAXN ];
int dfn[ MAXN ] , nfd[ MAXN ] , ts;
int par[ MAXN ];
int sdom[ MAXN ] , idom[ MAXN ];
int mom[ MAXN ] , mn[ MAXN ];
inline bool cmp( int u , int v )
{ return dfn[ u ] < dfn[ v ] ; }
int eval( int u ){
    if( mom[ u ] == u ) return u;
    int res = eval( mom[ u ] );
    if(cmp( sdom[ mn[ mom[ u ] ] ] , sdom[ mn[ u ] ] ))
        mn[ u ] = mn[ mom[ u ] ];
    return mom[ u ] = res;
}
void init( int _n , int _m , int _s ){
    ts = 0; n = _n; m = _m; s = _s;
    REP( i , 1 , n ) g[ i ].clear(), pred[ i ].clear();
}
void addEdge( int u , int v ){
    g[ u ].push_back( v );
    pred[ v ].push_back( u );
}
void dfs( int u ){
    ts++;
    dfn[ u ] = ts;
    nfd[ ts ] = u;
    for( int v : g[ u ] ) if( dfn[ v ] == 0 ){
        par[ v ] = u;
        dfs( v );
    }
}
void build(){
    REP( i , 1 , n ){
        dfn[ i ] = nfd[ i ] = 0;
        cov[ i ].clear();
        mom[ i ] = mn[ i ] = sdom[ i ] = i;
    }
    dfs( s );
    REPD( i , n , 2 ){
        int u = nfd[ i ];
        if( u == 0 ) continue;
        for( int v : pred[ u ] ) if( dfn[ v ] ){
            eval( v );
            if( cmp( sdom[ mn[ v ] ] , sdom[ u ] ) )
                sdom[ u ] = sdom[ mn[ v ] ];
        }
        cov[ sdom[ u ] ].push_back( u );
        mom[ u ] = par[ u ];
        for( int w : cov[ par[ u ] ] ){
            eval( w );
            if( cmp( sdom[ mn[ w ] ] , par[ u ] ) )
                idom[ w ] = mn[ w ];
            else idom[ w ] = par[ u ];
        }
        cov[ par[ u ] ].clear();
    }
    REP( i , 2 , n ){
        int u = nfd[ i ];
        if( u == 0 ) continue;
        if( idom[ u ] != sdom[ u ] )
            idom[ u ] = idom[ idom[ u ] ];
    }
}
} domT;

```

4.7 Number of Maximal Clique

```

// bool g[][] : adjacent array indexed from 1 to n
void dfs(int sz){
    int i , j , k , t , cnt , best = 0;
    if(ne[sz]==ce[sz]){ if (ce[sz]==0) ++ans; return; }
    for(t=0, i=1; i<=ne[sz]; ++i){
        for(cnt=0, j=ne[sz]+1; j<=ce[sz]; ++j)
            if (!g[lst[sz][i]][lst[sz][j]]) ++cnt;
        if (t==0 || cnt<best) t=i, best=cnt;
    } if (t && best<=0) return;
    for (k=ne[sz]+1; k<=ce[sz]; ++k) {
        if (t>0){ for (i=k; i<=ce[sz]; ++i)

```

```

        if (!g[lst[sz][t]][lst[sz][i]]) break;
        swap(lst[sz][k], lst[sz][i]);
    } i=lst[sz][k]; ne[sz+1]=ce[sz+1]=0;
    for (j=1; j<k; ++j) if (g[i][lst[sz][j]])
        lst[sz+1][++ne[sz+1]]=lst[sz][j];
    for (ce[sz+1]=ne[sz+1], j=k+1; j<=ce[sz]; ++j)
        if (g[i][lst[sz][j]]) lst[sz+1][++ce[sz+1]]=lst[sz][j];
    dfs(sz+1); ++ne[sz]; --best;
    for (j=k+1, cnt=0; j<=ce[sz]; ++j) if (!g[i][lst[sz][j]]) ++cnt;
    if (t==0 || cnt<best) t=k, best=cnt;
    if (t && best<=0) break;
}
}
void work(){
    ne[0]=0; ce[0]=0;
    for(int i=1; i<=n; ++i) lst[0][++ce[0]]=i;
    ans=0; dfs(0);
}
}

```

4.8 Strongly Connected Component

```

struct Scc{
    int n, nScc, vst[MXN], bln[MXN];
    vector<int> E[MXN], rE[MXN], vec;
    void init(int _n){
        n = _n;
        for (int i=0; i<MXN; i++){
            E[i].clear();
            rE[i].clear();
        }
    }
    void add_edge(int u, int v){
        E[u].PB(v);
        rE[v].PB(u);
    }
    void DFS(int u){
        vst[u]=1;
        for (auto v : E[u])
            if (!vst[v]) DFS(v);
        vec.PB(u);
    }
    void rDFS(int u){
        vst[u] = 1;
        bln[u] = nScc;
        for (auto v : rE[u])
            if (!vst[v]) rDFS(v);
    }
    void solve(){
        nScc = 0;
        vec.clear();
        FZ(vst);
        for (int i=0; i<n; i++)
            if (!vst[i]) DFS(i);
        reverse(vec.begin(), vec.end());
        FZ(vst);
        for (auto v : vec){
            if (!vst[v]){
                rDFS(v);
                nScc++;
            }
        }
    }
}
};

```

4.9 Dynamic MST

```

/* Dynamic MST O( Q lg^2 Q )
(qx[i], qy[i]) -> chg weight of edge No.qx[i] to qy[i]
delete an edge: (i, -infy)
add an edge: change from -infy to specific value
*/
const int SZ=M+3*MXQ;
int a[N],*tz;
int find(int xx){
    int root=xx; while(a[root]) root=a[root];
    int next; while((next=a[xx])){a[xx]=root; xx=next; }
    return root;
}

```

```

}
bool cmp(int aa,int bb){ return tz[aa]<tz[bb]; }
int kx[N],ky[N],kt, vd[N],id[M], app[M];
bool extra[M];
void solve(int *qx,int *qy,int Q,int n,int *x,int *y,
    int *z,int m1,long long ans){
    if(Q==1){
        for(int i=1;i<=n;i++) a[i]=0;
        z[ qx[0] ]=qy[0]; tz = z;
        for(int i=0;i<m1;i++) id[i]=i;
        sort(id,id+m1,cmp); int ri,rj;
        for(int i=0;i<m1;i++){
            ri=find(x[id[i]]); rj=find(y[id[i]]);
            if(ri!=rj){ ans+=z[id[i]]; a[ri]=rj; }
        }
        printf("%lld\n",ans);
        return;
    }
    int ri,rj;
    //contract
    kt=0;
    for(int i=1;i<=n;i++) a[i]=0;
    for(int i=0;i<Q;i++){
        ri=find(x[qx[i]]); rj=find(y[qx[i]]); if(ri!=rj) a[ri]=rj;
    }
    int tm=0;
    for(int i=0;i<m1;i++) extra[i]=true;
    for(int i=0;i<Q;i++) extra[ qx[i] ]=false;
    for(int i=0;i<m1;i++) if(extra[i]) id[tm++]=i;
    tz=z; sort(id,id+tm,cmp);
    for(int i=0;i<tm;i++){
        ri=find(x[id[i]]); rj=find(y[id[i]]);
        if(ri!=rj){
            a[ri]=rj; ans += z[id[i]];
            kx[kt]=x[id[i]]; ky[kt]=y[id[i]]; kt++;
        }
    }
    for(int i=1;i<=n;i++) a[i]=0;
    for(int i=0;i<kt;i++) a[ find(kx[i]) ]=find(ky[i]);
    int n2=0;
    for(int i=1;i<=n;i++) if(a[i]==0)
        vd[i]++;n2++;
    for(int i=1;i<=n;i++) if(a[i])
        vd[i]=vd[find(i)];
    int m2=0, *Nx=x+m1, *Ny=y+m1, *Nz=z+m1;
    for(int i=0;i<m1;i++) app[i]=-1;
    for(int i=0;i<Q;i++) if(app[qx[i]]==-1){
        Nx[m2]=vd[ x[ qx[i] ] ]; Ny[m2]=vd[ y[ qx[i] ] ];
        Nz[m2]=z[ qx[i] ];
        app[qx[i]]=m2; m2++;
    }
    for(int i=0;i<Q;i++){ z[ qx[i] ]=qy[i]; qx[i]=app[qx[i]]; }
    for(int i=1;i<=n2;i++) a[i]=0;
    for(int i=0;i<tm;i++){
        ri=find(vd[ x[id[i]] ]); rj=find(vd[ y[id[i]] ]);
        if(ri!=rj){
            a[ri]=rj; Nx[m2]=vd[ x[id[i]] ];
            Ny[m2]=vd[ y[id[i]] ]; Nz[m2]=z[id[i]]; m2++;
        }
    }
    int mid=Q/2;
    solve(qx,qy,mid,n2,Nx,Ny,Nz,m2,ans);
    solve(qx+mid,qy+mid,Q-mid,n2,Nx,Ny,Nz,m2,ans);
}
int x[SZ],y[SZ],z[SZ],qx[MXQ],qy[MXQ],n,m,Q;
void init(){
    scanf("%d%d",&n,&m);
    for(int i=0;i<m;i++) scanf("%d%d%d",x+i,y+i,z+i);
    scanf("%d",&Q);
    for(int i=0;i<Q;i++){ scanf("%d%d",qx+i,qy+i); qx[i]--; }
}
void work(){ if(Q) solve(qx,qy,Q,n,x,y,z,m,0); }
int main(){init(); work(); }

```

4.10 General Matching

```

const int N = 514, E = (2e5) * 2;

```

```

struct Graph{
    int to[E],bro[E],head[N],e;
    int lnk[N],vis[N],stp,n;
    void init( int _n ){
        stp = 0; e = 1; n = _n;
        for( int i = 1 ; i <= n ; i ++ )
            lnk[i] = vis[i] = 0;
    }
    void add_edge(int u,int v){
        to[e]=v,bro[e]=head[u],head[u]=e++;
        to[e]=u,bro[e]=head[v],head[v]=e++;
    }
    bool dfs(int x){
        vis[x]=stp;
        for(int i=head[x];i;i=bro[i]){
            int v=to[i];
            if(!lnk[v]){
                lnk[x]=v,lnk[v]=x;
                return true;
            }else if(vis[lnk[v]]<stp){
                int w=lnk[v];
                lnk[x]=v,lnk[v]=x,lnk[w]=0;
                if(dfs(w)){
                    return true;
                }
                lnk[w]=v,lnk[v]=w,lnk[x]=0;
            }
        }
        return false;
    }
    int solve(){
        int ans = 0;
        for(int i=1;i<=n;i++){
            if(!lnk[i]){
                stp++; ans += dfs(i);
            }
        }
        return ans;
    }
} graph;

```

4.11 Minimum General Weighted Matching

```

struct Graph {
    // Minimum General Weighted Matching (Perfect Match)
    static const int MXN = 105;
    int n, edge[MXN][MXN];
    int match[MXN],dis[MXN],onstk[MXN];
    vector<int> stk;
    void init(int _n) {
        n = _n;
        for( int i = 0 ; i < n ; i ++ )
            for( int j = 0 ; j < n ; j ++ )
                edge[ i ][ j ] = 0;
    }
    void add_edge(int u, int v, int w)
    { edge[u][v] = edge[v][u] = w; }
    bool SPFA(int u){
        if (onstk[u]) return true;
        stk.pb(u);
        onstk[u] = 1;
        for (int v=0; v<n; v++){
            if (u != v && match[u] != v && !onstk[v]){
                int m = match[v];
                if (dis[m] > dis[u] - edge[v][m] + edge[u][v]){
                    dis[m] = dis[u] - edge[v][m] + edge[u][v];
                    onstk[v] = 1;
                    stk.pb(v);
                    if (SPFA(m)) return true;
                    stk.pop_back();
                    onstk[v] = 0;
                }
            }
        }
        onstk[u] = 0;
        stk.pop_back();
        return false;
    }
    int solve() {
        // find a match
        for (int i=0; i<n; i+=2){

```

```

            match[i] = i+1;
            match[i+1] = i;
        }
        while (true){
            int found = 0;
            for( int i = 0 ; i < n ; i ++ )
                onstk[ i ] = dis[ i ] = 0;
            for (int i=0; i<n; i++){
                stk.clear();
                if (!onstk[i] && SPFA(i)){
                    found = 1;
                    while (SZ(stk)>=2){
                        int u = stk.back(); stk.pop_back();
                        int v = stk.back(); stk.pop_back();
                        match[u] = v;
                        match[v] = u;
                    }
                }
                if (!found) break;
            }
            int ret = 0;
            for (int i=0; i<n; i++)
                ret += edge[i][match[i]];
            ret /= 2;
            return ret;
        }
    }
}graph;

```

4.12 Maximum General Weighted Matching

```

struct WeightGraph {
    static const int INF = INT_MAX;
    static const int N = 514;
    struct edge{
        int u,v,w; edge(){}
        edge(int ui,int vi,int wi)
            :u(ui),v(vi),w(wi){}
    };
    int n,n_x;
    edge g[N*2][N*2];
    int lab[N*2];
    int match[N*2],slack[N*2],st[N*2],pa[N*2];
    int flo_from[N*2][N+1],S[N*2],vis[N*2];
    vector<int> flo[N*2];
    queue<int> q;
    int e_delta(const edge &e){
        return lab[e.u]+lab[e.v]-g[e.u][e.v].w*2;
    }
    void update_slack(int u,int x){
        if(!slack[x]||e_delta(g[u][x])<e_delta(g[slack[x]][x]))slack[x]=u;
    }
    void set_slack(int x){
        slack[x]=0;
        for(int u=1;u<=n;++u)
            if(g[u][x].w>0&&st[u]!=x&&S[st[u]]==0)
                update_slack(u,x);
    }
    void q_push(int x){
        if(x<=n)q.push(x);
        else for(size_t i=0;i<flo[x].size();i++)
            q_push(flo[x][i]);
    }
    void set_st(int x,int b){
        st[x]=b;
        if(x>n)for(size_t i=0;i<flo[x].size();++i)
            set_st(flo[x][i],b);
    }
    int get_pr(int b,int xr){
        int pr=find(flo[b].begin(),flo[b].end(),xr)-flo[b].begin();
        if(pr%2==1){
            reverse(flo[b].begin()+1,flo[b].end());
            return (int)flo[b].size()-pr;
        }else return pr;
    }
    void set_match(int u,int v){
        match[u]=g[u][v].v;
        if(u<=n) return;

```



```

    edge e=g[u][v];
    int xr=flo_from[u][e.u],pr=get_pr(u,xr);
    for(int i=0;i<pr;++i)set_match(flo[u][i],flo[u][i
    ^1]);
    set_match(xr,v);
    rotate(flo[u].begin(),flo[u].begin()+pr,flo[u].end
    ());
}
void augment(int u,int v){
    for(;;){
        int xnv=st[match[u]];
        set_match(u,v);
        if(!xnv)return;
        set_match(xnv,st[pa[xnv]]);
        u=st[pa[xnv]],v=xnv;
    }
}
int get_lca(int u,int v){
    static int t=0;
    for(++t;u!=v;swap(u,v)){
        if(u==0)continue;
        if(vis[u]==t)return u;
        vis[u]=t;
        u=st[match[u]];
        if(u)u=st[pa[u]];
    }
    return 0;
}
void add_blossom(int u,int lca,int v){
    int b=n+1;
    while(b<=n_x&&st[b]++b;
    if(b>n_x)++n_x;
    lab[b]=0,S[b]=0;
    match[b]=match[lca];
    flo[b].clear();
    flo[b].push_back(lca);
    for(int x=u,y; x!=lca; x=st[pa[y]])
        flo[b].push_back(x),flo[b].push_back(y=st[match[x
        ]]),q_push(y);
    reverse(flo[b].begin()+1,flo[b].end());
    for(int x=v,y; x!=lca; x=st[pa[y]])
        flo[b].push_back(x),flo[b].push_back(y=st[match[x
        ]]),q_push(y);
    set_st(b,b);
    for(int x=1;x<=n_x;++x)g[b][x].w=g[x][b].w=0;
    for(int x=1;x<=n;++x)flo_from[b][x]=0;
    for(size_t i=0;i<flo[b].size();++i){
        int xs=flo[b][i];
        for(int x=1;x<=n_x;++x)
            if(g[b][x].w==0||e_delta(g[xs][x])<e_delta(g[b
            ][x]))
                g[b][x]=g[xs][x],g[x][b]=g[x][xs];
        for(int x=1;x<=n;++x)
            if(flo_from[xs][x])flo_from[b][x]=xs;
    }
    set_slack(b);
}
void expand_blossom(int b){
    for(size_t i=0;i<flo[b].size();++i)
        set_st(flo[b][i],flo[b][i]);
    int xr=flo_from[b][g[b][pa[b]].u],pr=get_pr(b,xr);
    for(int i=0;i<pr;i+=2){
        int xs=flo[b][i],xns=flo[b][i+1];
        pa[xs]=g[xns][xs].u;
        S[xs]=1,S[xns]=0;
        slack[xs]=0,set_slack(xns);
        q_push(xns);
    }
    S[xr]=1,pa[xr]=pa[b];
    for(size_t i=pr+1;i<flo[b].size();++i){
        int xs=flo[b][i];
        S[xs]=-1,set_slack(xs);
    }
    st[b]=0;
}
bool on_found_edge(const edge &e){
    int u=st[e.u],v=st[e.v];
    if(S[v]==-1){
        pa[v]=e.u,S[v]=1;
        int nu=st[match[v]];
        slack[v]=slack[nu]=0;
        S[nu]=0,q_push(nu);
    }
}

```

```

    }else if(S[v]==0){
        int lca=get_lca(u,v);
        if(!lca)return augment(u,v),augment(v,u),true;
        else add_blossom(u,lca,v);
    }
    return false;
}
bool matching(){
    memset(S+1,-1,sizeof(int)*n_x);
    memset(slack+1,0,sizeof(int)*n_x);
    q=queue<int>();
    for(int x=1;x<=n_x;++x)
        if(st[x]==x&&!match[x])pa[x]=0,S[x]=0,q_push(x);
    if(q.empty())return false;
    for(;;){
        while(q.size()){
            int u=q.front();q.pop();
            if(S[st[u]]==1)continue;
            for(int v=1;v<=n;++v)
                if(g[u][v].w>0&&st[u]!=st[v]){
                    if(e_delta(g[u][v])==0){
                        if(on_found_edge(g[u][v]))return true;
                    }else update_slack(u,st[v]);
                }
        }
        int d=INF;
        for(int b=n+1;b<=n_x;++b)
            if(st[b]==b&&S[b]==1)d=min(d,lab[b]/2);
        for(int x=1;x<=n_x;++x)
            if(st[x]==x&&slack[x]){
                if(S[x]==-1)d=min(d,e_delta(g[slack[x]][x]));
                else if(S[x]==0)d=min(d,e_delta(g[slack[x]][x
                ])/2);
            }
        for(int u=1;u<=n;++u){
            if(S[st[u]]==0){
                if(lab[u]<=d)return 0;
                lab[u]-=d;
            }else if(S[st[u]]==1)lab[u]+=d;
        }
        for(int b=n+1;b<=n_x;++b)
            if(st[b]==b){
                if(S[st[b]]==0)lab[b]+=d*2;
                else if(S[st[b]]==1)lab[b]-=d*2;
            }
        q=queue<int>();
        for(int x=1;x<=n_x;++x)
            if(st[x]==x&&slack[x]&&st[slack[x]]!=x&&e_delta
            (g[slack[x]][x])==0)
                if(on_found_edge(g[slack[x]][x]))return true;
        for(int b=n+1;b<=n_x;++b)
            if(st[b]==b&&S[b]==1&&lab[b]==0)expand_blossom(
            b);
    }
    return false;
}
pair<long long,int> solve(){
    memset(match+1,0,sizeof(int)*n);
    n_x=n;
    int n_matches=0;
    long long tot_weight=0;
    for(int u=0;u<=n;++u)st[u]=u,flo[u].clear();
    int w_max=0;
    for(int u=1;u<=n;++u)
        for(int v=1;v<=n;++v){
            flo_from[u][v]=(u==v?u:0);
            w_max=max(w_max,g[u][v].w);
        }
    for(int u=1;u<=n;++u)lab[u]=w_max;
    while(matching())++n_matches;
    for(int u=1;u<=n;++u)
        if(match[u]&&match[u]<u)
            tot_weight+=g[u][match[u]].w;
    return make_pair(tot_weight,n_matches);
}
void add_edge( int ui , int vi , int wi ){
    g[ui][vi].w = g[vi][ui].w = wi;
}
void init( int _n ){
    n = _n;
    for(int u=1;u<=n;++u)
        for(int v=1;v<=n;++v)

```

```

        g[u][v]=edge(u,v,0);
    }
} graph;

```

4.13 Minimum Steiner Tree

```

// Minimum Steiner Tree
// O(V^3AT + V^2 2^AT)
struct SteinerTree{
#define V 33
#define T 8
#define INF 1023456789
    int n, dst[V][V], dp[1 << T][V], tdst[V];
    void init( int _n ){
        n = _n;
        for( int i = 0 ; i < n ; i ++ ){
            for( int j = 0 ; j < n ; j ++ ){
                dst[ i ][ j ] = INF;
                dst[ i ][ i ] = 0;
            }
        }
        void add_edge( int ui , int vi , int wi ){
            dst[ ui ][ vi ] = min( dst[ ui ][ vi ] , wi );
            dst[ vi ][ ui ] = min( dst[ vi ][ ui ] , wi );
        }
        void shortest_path(){
            for( int k = 0 ; k < n ; k ++ )
                for( int i = 0 ; i < n ; i ++ )
                    for( int j = 0 ; j < n ; j ++ )
                        dst[ i ][ j ] = min( dst[ i ][ j ],
                            dst[ i ][ k ] + dst[ k ][ j ] );
        }
        int solve( const vector<int>& ter ){
            int t = (int)ter.size();
            for( int i = 0 ; i < ( 1 << t ) ; i ++ )
                for( int j = 0 ; j < n ; j ++ )
                    dp[ i ][ j ] = INF;
            for( int i = 0 ; i < n ; i ++ )
                dp[ 0 ][ i ] = 0;
            for( int msk = 1 ; msk < ( 1 << t ) ; msk ++ ){
                if( msk == ( msk & (-msk) ) ){
                    int who = __lg( msk );
                    for( int i = 0 ; i < n ; i ++ )
                        dp[ msk ][ i ] = dst[ ter[ who ] ][ i ];
                    continue;
                }
                for( int i = 0 ; i < n ; i ++ )
                    for( int submsk = ( msk - 1 ) & msk ; submsk ;
                        submsk = ( submsk - 1 ) & msk )
                        dp[ msk ][ i ] = min( dp[ msk ][ i ],
                            dp[ submsk ][ i ] +
                            dp[ msk ^ submsk ][ i ] );
                for( int i = 0 ; i < n ; i ++ ){
                    tdst[ i ] = INF;
                    for( int j = 0 ; j < n ; j ++ )
                        tdst[ i ] = min( tdst[ i ],
                            dp[ msk ][ j ] + dst[ j ][ i ] );
                }
                for( int i = 0 ; i < n ; i ++ )
                    dp[ msk ][ i ] = tdst[ i ];
            }
            int ans = INF;
            for( int i = 0 ; i < n ; i ++ )
                ans = min( ans , dp[ ( 1 << t ) - 1 ][ i ] );
            return ans;
        }
    } solver;
}

```

4.14 BCC based on Vertex

```

struct BccVertex {
    int n,nScc,step,dfn[MXN],low[MXN];
    vector<int> E[MXN],sccv[MXN];
    int top,stk[MXN];
    void init(int _n) {
        n = _n;
        nScc = step = 0;
        for( int i=0; i<n; i++) E[i].clear();
    }
}

```

```

}
void add_edge(int u, int v) {
    E[u].PB(v);
    E[v].PB(u);
}
void DFS(int u, int f) {
    dfn[u] = low[u] = step++;
    stk[top++] = u;
    for( auto v:E[u] ) {
        if (v == f) continue;
        if (dfn[v] == -1) {
            DFS(v,u);
            low[u] = min(low[u], low[v]);
            if (low[v] >= dfn[u]) {
                int z;
                sccv[nScc].clear();
                do {
                    z = stk[--top];
                    sccv[nScc].PB(z);
                } while (z != v);
                sccv[nScc].PB(u);
                nScc++;
            }
        } else {
            low[u] = min(low[u],dfn[v]);
        }
    }
}
vector<vector<int>> solve() {
    vector<vector<int>> res;
    for( int i=0; i<n; i++) {
        dfn[i] = low[i] = -1;
    }
    for( int i=0; i<n; i++) {
        if (dfn[i] == -1) {
            top = 0;
            DFS(i,i);
        }
    }
    REP(i,nScc) res.PB(sccv[i]);
    return res;
}
}graph;

```

5 Flow

5.1 Bipartite Matching

```

struct BipartiteMatching { // O( ( V + E ) * sqrt( V ) )
    vector< int > G[ N ]; // N = total number of
        nodes = n + m
    int n, m, match[ N ], dist[ N ];
    // n: number of nodes on left side, nodes are
        numbered 1 to n
    // m: number of nodes on right side, nodes are
        numbered n+1 to n+m
    // G = NIL[0] u G1[G[1---n]] u G2[G[n+1---n+m]]
    bool BFS() {
        queue< int > Q;
        for ( int i = 1; i <= n; i++ ) {
            if ( match[ i ] == 0 ) {
                dist[ i ] = 0;
                Q.push( i );
            }
            else
                dist[ i ] = INF;
        }
        dist[ 0 ] = INF;
        while ( !Q.empty() ) {
            int u = Q.front();
            Q.pop();
            if ( dist[ u ] < dist[ 0 ] )
                for ( int v : G[ u ] )
                    if ( dist[ match[ v ] ] == INF ) {
                        dist[ match[ v ] ] = dist[ u ] + 1;
                        Q.push( match[ v ] );
                    }
        }
    }
}

```

```

    return ( dist[ 0 ] != INF );
}
bool DFS( int u ) {
    if ( u != 0 ) {
        for ( int v : G[ u ] )
            if ( dist[ match[ v ] ] == dist[ u ] + 1 && DFS
                ( match[ v ] ) ) {
                match[ v ] = u;
                match[ u ] = v;
                return true;
            }
        dist[ u ] = INF;
        return false;
    }
    return true;
}
int Max_Match() {
    int matching = 0;
    fill_n( match, n + m + 1, 0 );
    while ( BFS() )
        for ( int i = 1; i <= n; i++ )
            if ( match[ i ] == 0 && DFS( i ) ) matching++;
    return matching;
}
void AddEdge( int u, int v ) { G[ u ].push_back( n +
    v ); }
void DFS2( int u ) {
    dist[ u ] = 1;
    for ( int v : G[ u ] )
        if ( v != match[ u ] ) {
            dist[ v ] = 1;
            if ( match[ v ] != 0 ) DFS2( match[ v ] );
        }
}
void Min_Vertex_Cover( vector< int > &lrtn, vector<
    int > &rrtn ) {
    // after calling Max_Match
    fill_n( dist + 1, n + m, 0 );
    for ( int i = 1; i <= n; i++ )
        if ( match[ i ] == 0 ) DFS2( i );
    for ( int i = 1; i <= n; i++ )
        if ( dist[ i ] == 0 ) lrtn.push_back( i );
    for ( int i = n + 1; i <= n + m; i++ )
        if ( dist[ i ] == 1 ) rrtn.push_back( i - n );
}
} ob;

```

5.2 MaxFlow (ISAP)

```

// O( V^2 * E ) V up to 2w
#define SZ( c ) ( (int)( c ).size() )
class MaxFlow {
public:
    static const int MAXV = 5e3 + 10;
    static const int INF = 1e18;
    struct Edge {
        int v, c, r;
        Edge( int _v, int _c, int _r ) : v( _v ), c( _c ),
            r( _r ) {}
    };
    int s, t;
    vector< Edge > G[ MAXV * 2 ];
    int iter[ MAXV * 2 ], d[ MAXV * 2 ], gap[ MAXV * 2 ],
        tot;
    void Init( int x ) {
        tot = x + 2;
        s = x + 1, t = x + 2;
        for ( int i = 0; i <= tot; i++ ) {
            G[ i ].clear();
            iter[ i ] = d[ i ] = gap[ i ] = 0;
        }
    }
    void AddEdge( int u, int v, int c ) {
        G[ u ].push_back( Edge( v, c, SZ( G[ v ] ) ) );
        G[ v ].push_back( Edge( u, 0, SZ( G[ u ] ) - 1 ) );
    }
    int DFS( int p, int flow ) {
        if ( p == t ) return flow;
        for ( int &i = iter[ p ]; i < SZ( G[ p ] ); i++ ) {
            Edge &e = G[ p ][ i ];

```

```

            if ( e.c > 0 && d[ p ] == d[ e.v ] + 1 ) {
                int f = DFS( e.v, min( flow, e.c ) );
                if ( f ) {
                    e.c -= f;
                    G[ e.v ][ e.r ].c += f;
                    return f;
                }
            }
        }
        if ( ( --gap[ d[ p ] ] ) == 0 )
            d[ s ] = tot;
        else {
            d[ p ]++;
            iter[ p ] = 0;
            ++gap[ d[ p ] ];
        }
        return 0;
    }
    int Solve() {
        int res = 0;
        gap[ 0 ] = tot;
        for ( res = 0; d[ s ] < tot; res += DFS( s, INF ) )
            ;
        return res;
    }
};

```

5.3 MinCostMaxFlow

```

// O( V^2 * F )
class MinCostMaxFlow {
public:
    static const int MAXV = 2000;
    static const int INF = 1e9;
    struct Edge {
        int v, cap, w, rev;
        Edge() {}
        Edge( int t2, int t3, int t4, int t5 ) : v( t2 ),
            cap( t3 ), w( t4 ), rev( t5 ) {}
    };
    int V, s, t;
    vector< Edge > g[ MAXV ];
    void Init( int n ) {
        V = n + 4; // total number of nodes
        s = n + 1, t = n + 4; // s = source, t = sink
        for ( int i = 1; i <= V; i++ ) g[ i ].clear();
    }
    // cap: capacity, w: cost
    void AddEdge( int a, int b, int cap, int w ) {
        g[ a ].push_back( Edge( b, cap, w, (int)g[ b ].size() ) );
        g[ b ].push_back( Edge( a, 0, -w, (int)g[ a ].size() - 1 ) );
    }
    int d[ MAXV ], id[ MAXV ], mom[ MAXV ];
    bool inqu[ MAXV ];
    int qu[ 2000000 ], ql, qr;
    // the size of qu should be much large than MAXV
    int MncMxf() {
        int INF = INF;
        int mxf = 0, mnc = 0;
        while ( 1 ) {
            fill( d + 1, d + 1 + V, INF );
            fill( inqu + 1, inqu + 1 + V, 0 );
            fill( mom + 1, mom + 1 + V, -1 );
            mom[ s ] = s;
            d[ s ] = 0;
            ql = 1, qr = 0;
            qu[ ++qr ] = s;
            inqu[ s ] = 1;
            while ( ql <= qr ) {
                int u = qu[ ql++ ];
                inqu[ u ] = 0;
                for ( int i = 0; i < (int)g[ u ].size(); i++ ) {
                    Edge &e = g[ u ][ i ];
                    int v = e.v;
                    if ( e.cap > 0 && d[ v ] > d[ u ] + e.w ) {
                        d[ v ] = d[ u ] + e.w;
                        mom[ v ] = u;

```

```

        id[ v ] = i;
        if ( !inqu[ v ] ) qu[ ++qr ] = v, inqu[ v ]
            = 1;
    }
}
if ( mom[ t ] == -1 ) break;
int df = INF;
for ( int u = t; u != s; u = mom[ u ] ) df = min(
    df, g[ mom[ u ] ][ id[ u ] ].cap );
for ( int u = t; u != s; u = mom[ u ] ) {
    Edge &e = g[ mom[ u ] ][ id[ u ] ];
    e.cap -= df;
    g[ e.v ][ e.rev ].cap += df;
}
mxf += df;
mnc += df * d[ t ];
}
return mnc;
}
};

```

5.4 BoundedMaxFlow

```

// node from 0 ~ size - 1
class Graph {
public:
    Graph( const int &size )
        : size_( size + 2 ),
          source_( size ),
          sink_( size + 1 ),
          edges_( size_ ),
          capacity_( size_, vector< int >( size_, 0 ) ),
          lower_bound_( size_, vector< int >( size_, 0 ) ),
          lower_bound_sum_( size_, 0 ) {}
    void AddEdge( int from, int to, int lower_bound, int
        capacity ) {
        edges_[ from ].push_back( to );
        edges_[ to ].push_back( from );

        capacity_[ from ][ to ] += capacity - lower_bound;
        lower_bound_[ from ][ to ] += lower_bound;

        lower_bound_sum_[ from ] += lower_bound;
        lower_bound_sum_[ to ] -= lower_bound;
    }
    int MaxFlow() {
        int expected_source = 0, expected_sink = 0;
        for ( int i = 0; i < source_; ++i )
            if ( lower_bound_sum_[ i ] > 0 ) {
                capacity_[ i ][ sink_ ] = lower_bound_sum_[ i ];
                edges_[ i ].push_back( sink_ );
                edges_[ sink_ ].push_back( i );
                expected_sink += lower_bound_sum_[ i ];
            }
            else if ( lower_bound_sum_[ i ] < 0 ) {
                capacity_[ source_ ][ i ] = -lower_bound_sum_[ i ];
                edges_[ source_ ].push_back( i );
                expected_source -= lower_bound_sum_[ i ];
            }
        int Flow = 0;
        while ( BFS( source_, sink_ ) )
            for ( auto &from : edges_[ sink_ ] ) {
                if ( from_[ from ] == -1 ) continue;

                from_[ sink_ ] = from;
                int current_Flow = numeric_limits< int >::max();
                for ( int i = sink_; i != source_; i = from_[ i ] )
                    current_Flow = min( current_Flow, capacity_[
                        from_[ i ] ][ i ] );
                if ( not current_Flow ) continue;
                for ( int i = sink_; i != source_; i = from_[ i ] ) {
                    capacity_[ from_[ i ] ][ i ] -= current_Flow;
                    capacity_[ i ][ from_[ i ] ] += current_Flow;

```

```

                }
                Flow += current_Flow;
            }
            if ( Flow != expected_source ) return -1;
            return Flow;
        }
        int Flow( int from, int to ) { return lower_bound_[
            from ][ to ] + capacity_[ to ][ from ]; }

private:
        bool BFS( int source, int sink ) {
            queue< int > Q;
            Q.push( source );
            from_ = vector< int >( size_, -1 );
            from_[ source ] = source;

            while ( !Q.empty() ) {
                int node = Q.front();
                Q.pop();
                if ( node == sink ) continue;
                for ( auto &neighbour : edges_[ node ] )
                    if ( from_[ neighbour ] == -1 && capacity_[
                        node ][ neighbour ] > 0 ) {
                        from_[ neighbour ] = node;
                        Q.push( neighbour );
                    }
            }
            return from_[ sink ] != -1;
        }
        int size_, source_, sink_;
        vector< vector< int > > edges_;
        vector< vector< int > > capacity_;
        vector< vector< int > > lower_bound_;
        vector< int > lower_bound_sum_;
        vector< int > from_;
    };

```

5.5 Dinic

```

struct Dinic{
    static const int MXN = 10000;
    struct Edge{ int v,f,re; };
    int n,s,t,level[MXN];
    vector<Edge> E[MXN];
    void init(int _n, int _s, int _t){
        n = _n; s = _s; t = _t;
        for (int i=0; i<n; i++) E[i].clear();
    }
    void add_edge(int u, int v, int f){
        E[u].PB({v,f,SZ(E[v])});
        E[v].PB({u,0,SZ(E[u])-1});
    }
    bool BFS(){
        for (int i=0; i<n; i++) level[i] = -1;
        queue<int> que;
        que.push(s);
        level[s] = 0;
        while (!que.empty()){
            int u = que.front(); que.pop();
            for (auto it : E[u]){
                if (it.f > 0 && level[it.v] == -1){
                    level[it.v] = level[u]+1;
                    que.push(it.v);
                }
            }
        }
        return level[t] != -1;
    }
    int DFS(int u, int nf){
        if (u == t) return nf;
        int res = 0;
        for (auto &it : E[u]){
            if (it.f > 0 && level[it.v] == level[u]+1){
                int tf = DFS(it.v, min(nf,it.f));
                res += tf; nf -= tf; it.f -= tf;
                E[it.v][it.re].f += tf;
                if (nf == 0) return res;
            }
        }
        return 0;
    }
    int Flow(){
        while (BFS())
            for (int i=s; i<t; i++)
                if (level[i] < level[i+1])
                    DFS(i, INF);
        return level[t] == -1 ? 0 : Flow();
    }
};

```

```

    return res;
}
int flow(int res=0){
    while ( BFS() )
        res += DFS(s,2147483647);
    return res;
}
}flow;

```

5.6 DMST

```

/*
 * Edmond's algoirthm for Directed MST
 * runs in O(VE)
 */
const int MAXV = 10010;
const int MAXE = 10010;
const int INF = 2147483647;
struct Edge{
    int u, v, c;
    Edge(){}
    Edge(int x, int y, int z) :
        u(x), v(y), c(z){}
};
int V, E, root;
Edge edges[MAXE];
inline int newV(){
    V++;
    return V;
}
inline void addEdge(int u, int v, int c){
    E++;
    edges[E] = Edge(u, v, c);
}
bool con[MAXV];
int mnInW[MAXV], prv[MAXV], cyc[MAXV], vis[MAXV];
inline int DMST(){
    fill(con, con+V+1, 0);
    int r1 = 0, r2 = 0;
    while(1){
        fill(mnInW, mnInW+V+1, INF);
        fill(prv, prv+V+1, -1);
        REP(i, 1, E){
            int u=edges[i].u, v=edges[i].v, c=edges[i].c;
            if(u != v && v != root && c < mnInW[v])
                mnInW[v] = c, prv[v] = u;
        }
        fill(vis, vis+V+1, -1);
        fill(cyc, cyc+V+1, -1);
        r1 = 0;
        bool jf = 0;
        REP(i, 1, V){
            if(con[i]) continue;
            if(prv[i] == -1 && i != root) return -1;
            if(prv[i] > 0) r1 += mnInW[i];
            int s;
            for(s = i; s != -1 && vis[s] == -1; s = prv[s])
                vis[s] = i;
            if(s > 0 && vis[s] == i){
                // get a cycle
                jf = 1;
                int v = s;
                do{
                    cyc[v] = s, con[v] = 1;
                    r2 += mnInW[v];
                    v = prv[v];
                }while(v != s);
                con[s] = 0;
            }
        }
        if(!jf) break;
        REP(i, 1, E){
            int &u = edges[i].u;
            int &v = edges[i].v;
            if(cyc[v] > 0) edges[i].c -= mnInW[edges[i].v];
            if(cyc[u] > 0) edges[i].u = cyc[edges[i].u];
            if(cyc[v] > 0) edges[i].v = cyc[edges[i].v];
            if(u == v) edges[i--] = edges[E--];
        }
    }
}

```

```

    return r1+r2;
}

```

5.7 SW min-cut

```

// global min cut
struct SW{ // O(V^3)
    static const int MXN = 514;
    int n,vst[MXN],del[MXN];
    int edge[MXN][MXN],wei[MXN];
    void init(int _n){
        n = _n;
        FZ(edge);
        FZ(del);
    }
    void add_edge(int u, int v, int w){
        edge[u][v] += w;
        edge[v][u] += w;
    }
    void search(int &s, int &t){
        FZ(vst); FZ(wei);
        s = t = -1;
        while (true){
            int mx=-1, cur=0;
            for (int i=0; i<n; i++){
                if (!del[i] && !vst[i] && mx<wei[i])
                    cur = i, mx = wei[i];
            }
            if (mx == -1) break;
            vst[cur] = 1;
            s = t;
            t = cur;
            for (int i=0; i<n; i++){
                if (!vst[i] && !del[i]) wei[i] += edge[cur][i];
            }
        }
    }
    int solve(){
        int res = 2147483647;
        for (int i=0,x,y; i<n-1; i++){
            search(x,y);
            res = min(res,wei[y]);
            del[y] = 1;
            for (int j=0; j<n; j++){
                edge[x][j] = (edge[j][x] += edge[y][j]);
            }
        }
        return res;
    }
}graph;

```

5.8 Theorem

```

/*
Lucas' Theorem:
For non-negative integer n,m and prime P,
C(m,n) mod P = C(m/M,n/M) * C(m%M,n%M) mod P
= mult_i ( C(m_i,n_i) )
where m_i is the i-th digit of m in base P.

Pick' s Theorem
A = i + b/2 - 1

Kirchhoff's theorem
A_{ii} = deg(i), A_{ij} = (i,j) \in E ? -1 : 0
Deleting any one row, one column, and cal the det(A)
*/

```

6 Geometry

6.1 Half Plane Intersection

6.2 Intersection of 2 Lines

```

#define N 100010
#define EPS 1e-8
#define SIDE 1000000

```



```

struct PO{ double x , y ; } p[ N ] , o ;
struct LI{
    PO a , b ;
    double angle ;
    void in( double x1 , double y1 , double x2 , double
        y2 ){
        a.x = x1 ; a.y = y1 ; b.x = x2 ; b.y = y2 ;
    }
} li[ N ] , deq[ N ] ;
int n , m , cnt ;
inline int dc( double x ){
    if ( x > EPS ) return 1 ;
    else if ( x < -EPS ) return -1 ;
    return 0 ;
}
inline PO operator-( PO a , PO b ){
    PO c ;
    c.x = a.x - b.x ; c.y = a.y - b.y ;
    return c ;
}
inline double cross( PO a , PO b , PO c ){
    return ( b.x - a.x ) * ( c.y - a.y ) - ( b.y - a.y )
        * ( c.x - a.x ) ;
}
inline bool cmp( const LI &a , const LI &b ){
    if( dc( a.angle - b.angle ) == 0 ) return dc( cross(
        a.a , a.b , b.a ) ) < 0 ;
    return a.angle > b.angle ;
}
inline PO getpoint( LI &a , LI &b ){
    double k1 = cross( a.a , b.b , b.a ) ;
    double k2 = cross( a.b , b.a , b.b ) ;
    PO tmp = a.b - a.a , ans ;
    ans.x = a.a.x + tmp.x * k1 / ( k1 + k2 ) ;
    ans.y = a.a.y + tmp.y * k1 / ( k1 + k2 ) ;
    return ans ;
}
inline void getcut(){
    sort( li + 1 , li + 1 + n , cmp ) ; m = 1 ;
    for( int i = 2 ; i <= n ; i ++ )
        if( dc( li[ i ].angle - li[ m ].angle ) != 0 )
            li[ ++ m ] = li[ i ] ;
    deq[ 1 ] = li[ 1 ] ; deq[ 2 ] = li[ 2 ] ;
    int bot = 1 , top = 2 ;
    for( int i = 3 ; i <= m ; i ++ ){
        while( bot < top && dc( cross( li[ i ].a , li[ i ].
            b , getpoint( deq[ top ] , deq[ top - 1 ] ) ) )
            < 0 ) top -- ;
        while( bot < top && dc( cross( li[ i ].a , li[ i ].
            b , getpoint( deq[ bot ] , deq[ bot + 1 ] ) ) )
            < 0 ) bot ++ ;
        deq[ ++ top ] = li[ i ] ;
    }
    while( bot < top && dc( cross( deq[ bot ].a , deq[
        bot ].b , getpoint( deq[ top ] , deq[ top - 1 ] ) )
        ) < 0 ) top -- ;
    while( bot < top && dc( cross( deq[ top ].a , deq[
        top ].b , getpoint( deq[ bot ] , deq[ bot + 1 ] ) )
        ) < 0 ) bot ++ ;
    cnt = 0 ;
    if( bot == top ) return ;
    for( int i = bot ; i < top ; i ++ ) p[ ++ cnt ] =
        getpoint( deq[ i ] , deq[ i + 1 ] ) ;
    if( top - 1 > bot ) p[ ++ cnt ] = getpoint( deq[ bot
        ] , deq[ top ] ) ;
}
double px[ N ] , py[ N ] ;
void read( int rm ) {
    for( int i = 1 ; i <= n ; i ++ ) px[ i + n ] = px[ i
        ] , py[ i + n ] = py[ i ] ;
    for( int i = 1 ; i <= n ; i ++ ){
        // half-plane from li[ i ].a -> li[ i ].b
        li[ i ].a.x = px[ i + rm + 1 ] ; li[ i ].a.y = py[ i
            + rm + 1 ] ;
        li[ i ].b.x = px[ i ] ; li[ i ].b.y = py[ i ] ;
        li[ i ].angle = atan2( li[ i ].b.y - li[ i ].a.y ,
            li[ i ].b.x - li[ i ].a.x ) ;
    }
}
inline double getarea( int rm ){
    read( rm ) ; getcut() ;
    double res = 0.0 ;

```

```

    p[ cnt + 1 ] = p[ 1 ] ;
    for( int i = 1 ; i <= cnt ; i ++ ) res += cross( o ,
        p[ i ] , p[ i + 1 ] ) ;
    if( res < 0.0 ) res *= -1.0 ;
    return res ;
}

```

6.3 Intersection of 2 Segments

```

int ori( const PLL& o , const PLL& a , const PLL& b ){
    LL ret = ( a - o ) ^ ( b - o ) ;
    return ret / max( 1ll , abs( ret ) ) ;
}
// p1 == p2 || q1 == q2 need to be handled
bool banana( const PLL& p1 , const PLL& p2 ,
    const PLL& q1 , const PLL& q2 ){
    if( ( ( p2 - p1 ) ^ ( q2 - q1 ) ) == 0 ){ // parallel
        if( ori( p1 , p2 , q1 ) ) return false ;
        return ( ( p1 - q1 ) * ( p2 - q1 ) ) <= 0 ||
            ( ( p1 - q2 ) * ( p2 - q2 ) ) <= 0 ||
            ( ( q1 - p1 ) * ( q2 - p1 ) ) <= 0 ||
            ( ( q1 - p2 ) * ( q2 - p2 ) ) <= 0 ;
    }
    return ( ori( p1 , p2 , q1 ) * ori( p1 , p2 , q2 ) <= 0 ) &&
        ( ori( q1 , q2 , p1 ) * ori( q1 , q2 , p2 ) <= 0 ) ;
}

```

6.4 Intersection of Circle and Segment

```

bool Inter( const Pt& p1 , const Pt& p2 , Circle& cc ){
    Pt dp = p2 - p1 ;
    double a = dp * dp ;
    double b = 2 * ( dp * ( p1 - cc.o ) ) ;
    double c = cc.o * cc.o + p1 * p1 - 2 * ( cc.o * p1 )
        - cc.R * cc.R ;
    double bb4ac = b * b - 4 * a * c ;
    return !( fabs( a ) < eps or bb4ac < 0 ) ;
}

```

6.5 Intersection of Polygon and Circle

```

Pt ORI , info[ N ] ;
D r ; int n ;
// Divides into multiple triangle, and sum up
// oriented area
D area2( Pt pa , Pt pb ){
    if( norm( pa ) < norm( pb ) ) swap( pa , pb ) ;
    if( norm( pb ) < eps ) return 0 ;
    D S , h , theta ;
    D a = norm( pb ) , b = norm( pa ) , c = norm( pb - pa ) ;
    D cosB = ( pb * ( pb - pa ) ) / a / c , B = acos( cosB ) ;
    D cosC = ( pa * pb ) / a / b , C = acos( cosC ) ;
    if( a > r ){
        S = ( C / 2 ) * r * r ;
        h = a * b * sin( C ) / c ;
        if ( h < r && B < PI / 2 ) S -= ( acos( h / r ) * r * r - h * sqrt
            ( r * r - h * h ) ) ;
    } else if( b > r ){
        theta = PI - B - asin( sin( B ) / r * a ) ;
        S = .5 * a * r * sin( theta ) + ( C - theta ) / 2 * r * r ;
    } else S = .5 * sin( C ) * a * b ;
    return S ;
}
D area() {
    D S = 0 ;
    for( int i = 0 ; i < n ; ++i )
        S += abs( area2( info[ i ] , info[ i + 1 ] ) ) * sign( det(
            info[ i ] , info[ i + 1 ] ) ) ;
    return fabs( S ) ;
}

```

6.6 Intersection of 2 Circles

6.7 Circle Cover

```

#define N 1021
struct CircleCover{
    int C; Circle c[ N ];
    bool g[ N ][ N ], overlap[ N ][ N ];
    // Area[i] : area covered by at least i circles
    D Area[ N ];
    void init( int _C ){ C = _C; }
    bool CCinter( Circle& a , Circle& b , Pt& p1 , Pt& p2
    ){
        Pt o1 = a.O , o2 = b.O;
        D r1 = a.R , r2 = b.R;
        D d2 = ( o1 - o2 ) * ( o1 - o2 );
        D d = sqrt(d2);
        if( d > r1 + r2 ) return false;
        Pt u = (o1+o2)*0.5 + (o1-o2)*((r2*r2-r1*r1)/(2*d2))
        ;
        D A = sqrt((r1+r2+d)*(r1-r2+d)*(r1+r2-d)*(-r1+r2+d)
        );
        Pt v = Pt( o1.Y-o2.Y , -o1.X + o2.X ) * A / (2*d2);
        p1 = u + v; p2 = u - v;
        return true;
    }
    struct Tevent {
        Pt p; D ang; int add;
        Tevent() {}
        Tevent(Pt _a, D _b, int _c): p(_a), ang(_b), add(_c
        ) {}
        bool operator<(const Tevent &a)const
        {return ang < a.ang;}
    }eve[ N * 2 ];
    // strict: x = 0, otherwise x = -1
    bool disjunct( Circle& a, Circle &b, int x ){
        return sign( norm( a.O - b.O ) - a.R - b.R ) > x;
    }
    bool contain( Circle& a, Circle &b, int x ){
        return sign( a.R - b.R - norm( a.O - b.O ) ) > x;
    }
    bool contain(int i, int j){ /* c[j] is non-strictly
        in c[i]. */
        return (sign(c[i].R - c[j].R) > 0 ||
            (sign(c[i].R - c[j].R) == 0 && i < j) ) &&
            contain(c[i], c[j], -1);
    }
    void solve(){
        for( int i = 0 ; i <= C + 1 ; i ++ )
            Area[ i ] = 0;
        for( int i = 0 ; i < C ; i ++ )
            for( int j = 0 ; j < C ; j ++ )
                overlap[i][j] = contain(i, j);
        for( int i = 0 ; i < C ; i ++ )
            for( int j = 0 ; j < C ; j ++ )
                g[i][j] = !(overlap[i][j] || overlap[j][i] ||
                    disjunct(c[i], c[j], -1));
        for( int i = 0 ; i < C ; i ++ ){
            int E = 0, cnt = 1;
            for( int j = 0 ; j < C ; j ++ )
                if( j != i && overlap[j][i] )
                    cnt ++;
            for( int j = 0 ; j < C ; j ++ )
                if( i != j && g[i][j] ){
                    Pt aa, bb;
                    CCinter(c[i], c[j], aa, bb);
                    D A = atan2(aa.Y - c[i].O.Y, aa.X - c[i].O.X)
                    ;
                    D B = atan2(bb.Y - c[i].O.Y, bb.X - c[i].O.X)
                    ;
                    eve[E ++] = Tevent(bb, B, 1);
                    eve[E ++] = Tevent(aa, A, -1);
                    if(B > A) cnt ++;
                }
            if( E == 0 ) Area[ cnt ] += pi * c[i].R * c[i].R;
            else{
                sort( eve , eve + E );
                eve[E] = eve[0];
                for( int j = 0 ; j < E ; j ++ ){
                    cnt += eve[j].add;
                    Area[cnt] += (eve[j].p ^ eve[j + 1].p) * .5;
                    D theta = eve[j + 1].ang - eve[j].ang;
                    if (theta < 0) theta += 2. * pi;
                    Area[cnt] += ( theta - sin(theta) ) * c[i].R
                        * c[i].R * .5;
                }
            }
        }
    }
}

```

```

    }
}
};

```

6.8 Tangent Line of 2 Circles

```

vector<Line> go( const Circle& c1 , const Circle& c2 ){
    vector<Line> ret;
    double d_sq = norm2( c1.O - c2.O );
    if( d_sq < eps ) return ret;
    double d = sqrt( d_sq );
    Pt v = ( c2.O - c1.O ) / d;
    for( int sign1 = 1 ; sign1 >= -1 ; sign1 -= 2 ){
        double c = ( c1.R - sign1 * c2.R ) / d;
        if( c * c > 1 ) continue;
        double h = sqrt( max( 0.0 , 1.0 - c * c ) );
        for( int sign2 = 1 ; sign2 >= -1 ; sign2 -= 2 ){
            Pt n;
            n.X = v.X * c - sign2 * h * v.Y;
            n.Y = v.Y * c + sign2 * h * v.X;
            Pt p1 = c1.O + n * c1.R;
            Pt p2 = c2.O + n * ( c2.R * sign1 );
            if( fabs( p1.X - p2.X ) < eps and
                fabs( p1.Y - p2.Y ) < eps )
                p2 = p1 + perp( c2.O - c1.O );
            ret.push_back( { p1 , p2 } );
        }
    }
    return ret;
}

```

6.9 KD Tree

```

const int MXN = 100005;
struct KDTree {
    struct Node {
        int x,y,x1,y1,x2,y2;
        int id,f;
        Node *L, *R;
    }tree[MXN];
    int n;
    Node *root;
    LL dis2(int x1, int y1, int x2, int y2) {
        LL dx = x1-x2;
        LL dy = y1-y2;
        return dx*dx+dy*dy;
    }
    static bool cmpx(Node& a, Node& b){ return a.x<b.x; }
    static bool cmpy(Node& a, Node& b){ return a.y<b.y; }
    void init(vector<pair<int,int>> ip) {
        n = ip.size();
        for (int i=0; i<n; i++) {
            tree[i].id = i;
            tree[i].x = ip[i].first;
            tree[i].y = ip[i].second;
        }
        root = build_tree(0, n-1, 0);
    }
    Node* build_tree(int L, int R, int dep) {
        if (L>R) return nullptr;
        int M = (L+R)/2;
        tree[M].f = dep%2;
        nth_element(tree+L, tree+M, tree+R+1, tree[M].f ?
            cmpy : cmpx);
        tree[M].x1 = tree[M].x2 = tree[M].x;
        tree[M].y1 = tree[M].y2 = tree[M].y;

        tree[M].L = build_tree(L, M-1, dep+1);
        if (tree[M].L) {
            tree[M].x1 = min(tree[M].x1, tree[M].L->x1);
            tree[M].x2 = max(tree[M].x2, tree[M].L->x2);
            tree[M].y1 = min(tree[M].y1, tree[M].L->y1);
            tree[M].y2 = max(tree[M].y2, tree[M].L->y2);
        }
        tree[M].R = build_tree(M+1, R, dep+1);
        if (tree[M].R) {
            tree[M].x1 = min(tree[M].x1, tree[M].R->x1);

```

```

    tree[M].x2 = max(tree[M].x2, tree[M].R->x2);
    tree[M].y1 = min(tree[M].y1, tree[M].R->y1);
    tree[M].y2 = max(tree[M].y2, tree[M].R->y2);
}
return tree+M;
}
int touch(Node* r, int x, int y, LL d2){
    LL dis = sqrt(d2)+1;
    if (x<r->x1-dis || x>r->x2+dis ||
        y<r->y1-dis || y>r->y2+dis)
        return 0;
    return 1;
}
void nearest(Node* r, int x, int y,
             int &mID, LL &md2){
    if (!r || !touch(r, x, y, md2)) return;
    LL d2 = dis2(r->x, r->y, x, y);
    if (d2 < md2 || (d2 == md2 && mID < r->id)) {
        mID = r->id;
        md2 = d2;
    }
    // search order depends on split dim
    if ((r->f == 0 && x < r->x) ||
        (r->f == 1 && y < r->y)) {
        nearest(r->L, x, y, mID, md2);
        nearest(r->R, x, y, mID, md2);
    } else {
        nearest(r->R, x, y, mID, md2);
        nearest(r->L, x, y, mID, md2);
    }
}
int query(int x, int y) {
    int id = 1029384756;
    LL d2 = 102938475612345678LL;
    nearest(root, x, y, id, d2);
    return id;
}
}tree;

```

6.10 Lower Concave Hull

```

/****
maintain a "concave hull" that support the following
1. insertion of a line
2. query of height(y) on specific x on the hull
****/
/* set as needed */
typedef long double LD;
const LD eps=1e-9;
const LD inf=1e19;
class Seg {
public:
    LD m,c,x1,x2; // y=mx+c
    bool flag;
    Seg(
        LD _m,LD _c,LD _x1=-inf,LD _x2=inf,bool _flag=0)
        :m(_m),c(_c),x1(_x1),x2(_x2),flag(_flag) {}
    LD evaly(LD x) const {
        return m*x+c;
    }
    const bool operator<(LD x) const {
        return x2-eps<x;
    }
    const bool operator<(const Seg &b) const {
        if(flag||b.flag) return *this<b.x1;
        return m+eps<b.m;
    }
};
class LowerConcaveHull { // maintain a hull like: \_/_/
public:
    set<Seg> hull;
    /* functions */
    LD xintersection(Seg a,Seg b) {
        return (a.c-b.c)/(b.m-a.m);
    }
    inline set<Seg>::iterator replace(set<Seg> &
        hull,set<Seg>::iterator it,Seg s) {
        hull.erase(it);
        return hull.insert(s).first;
    }
}

```

```

void insert(Seg s) {
    // insert a line and update hull
    set<Seg>::iterator it=hull.find(s);
    // check for same slope
    if(it!=hull.end()) {
        if(it->c+eps>=s.c) return;
        hull.erase(it);
    }
    // check if below whole hull
    it=hull.lower_bound(s);
    if(it!=hull.end()&&
        s.evaly(it->x1)<=it->evaly(it->x1)+eps) return;
    // update right hull
    while(it!=hull.end()) {
        LD x=xintersection(s,*it);
        if(x>=it->x2-eps) hull.erase(it++);
        else {
            s.x2=x;
            it=replace(hull,it,Seg(it->m,it->c,x,it->x2));
            break;
        }
    }
    // update left hull
    while(it!=hull.begin()) {
        LD x=xintersection(s,*(--it));
        if(x<=it->x1+eps) hull.erase(it--);
        else {
            s.x1=x;
            it=replace(hull,it,Seg(it->m,it->c,it->x1,x));
            break;
        }
    }
    // insert s
    hull.insert(s);
}
void insert(LD m,LD c) { insert(Seg(m,c)); }
LD query(LD x) { // return y @ given x
    set<Seg>::iterator it =
        hull.lower_bound(Seg(0.0,0.0,x,x,1));
    return it->evaly(x);
}
};

```

6.11 Delaunay Triangulation

```

/* Delaunay Triangulation:
Given a sets of points on 2D plane, find a
triangulation such that no points will strictly
inside circumcircle of any triangle.

find : return a triangle contain given point
add_point : add a point into triangulation

A Triangle is in triangulation iff. its has_chd is 0.
Region of triangle u: iterate each u.edge[i].tri,
each points are u.p[(i+1)%3], u.p[(i+2)%3]

calculation involves O(|V|^6) */
const int N = 100000 + 5;
const type inf = 2e3;
type eps = 1e-6; // 0 when integer
type sqr(type x) { return x*x; }
// return p4 is in circumcircle of tri(p1,p2,p3)
bool in_cc(const Pt& p1, const Pt& p2, const Pt& p3,
           const Pt& p4){
    type u11 = p1.X - p4.X; type u12 = p1.Y - p4.Y;
    type u21 = p2.X - p4.X; type u22 = p2.Y - p4.Y;
    type u31 = p3.X - p4.X; type u32 = p3.Y - p4.Y;
    type u13 = sqr(p1.X)-sqr(p4.X)+sqr(p1.Y)-sqr(p4.Y);
    type u23 = sqr(p2.X)-sqr(p4.X)+sqr(p2.Y)-sqr(p4.Y);
    type u33 = sqr(p3.X)-sqr(p4.X)+sqr(p3.Y)-sqr(p4.Y);
    type det = -u13*u22*u31 + u12*u23*u31 + u13*u21*u32
        - u11*u23*u32 - u12*u21*u33 + u11*u22*u33;
    return det > eps;
}
type side(const Pt& a, const Pt& b, const Pt& p)
{ return (b - a) ^ (p - a); }
typedef int SdRef;
struct Tri;
typedef Tri* TriRef;

```

```

struct Edge {
    TriRef tri; SdRef side;
    Edge():tri(0), side(0){}
    Edge(TriRef _tri, SdRef _side):tri(_tri), side(_side)
    {}
};

struct Tri {
    Pt p[3];
    Edge edge[3];
    TriRef chd[3];
    Tri() {}
    Tri(const Pt& p0, const Pt& p1, const Pt& p2) {
        p[0] = p0; p[1] = p1; p[2] = p2;
        chd[0] = chd[1] = chd[2] = 0;
    }
    bool has_chd() const { return chd[0] != 0; }
    int num_chd() const {
        return chd[0] == 0 ? 0
            : chd[1] == 0 ? 1
            : chd[2] == 0 ? 2 : 3;
    }
    bool contains(Pt const& q) const {
        for( int i = 0 ; i < 3 ; i ++ )
            if( side(p[i], p[(i + 1) % 3] , q) < -eps )
                return false;
        return true;
    }
} pool[ N * 10 ], *tris;

void edge( Edge a, Edge b ){
    if(a.tri) a.tri->edge[a.side] = b;
    if(b.tri) b.tri->edge[b.side] = a;
}

struct Trig { // Triangulation
    Trig(){
        the_root = // Tri should at least contain all
                    points
                    new(tris++)Tri(Pt(-inf,-inf),Pt(+inf+inf,-inf),Pt
                    (-inf,+inf+inf));
    }
    TriRef find(Pt p)const{ return find(the_root,p); }
    void add_point(const Pt& p){ add_point(find(the_root,
        p),p); }
    TriRef the_root;
    static TriRef find(TriRef root, const Pt& p) {
        while( true ){
            if( !root->has_chd() )
                return root;
            for( int i = 0; i < 3 && root->chd[i] ; ++i )
                if (root->chd[i]->contains(p)) {
                    root = root->chd[i];
                    break;
                }
        }
        assert( false ); // "point not found"
    }
    void add_point(TriRef root, Pt const& p) {
        TriRef tab,tbc,tca;
        /* split it into three triangles */
        tab=new(tris++) Tri(root->p[0],root->p[1],p);
        tbc=new(tris++) Tri(root->p[1],root->p[2],p);
        tca=new(tris++) Tri(root->p[2],root->p[0],p);
        edge(Edge(tab,0), Edge(tbc,1));
        edge(Edge(tbc,0), Edge(tca,1));
        edge(Edge(tca,0), Edge(tab,1));
        edge(Edge(tab,2), root->edge[2]);
        edge(Edge(tbc,2), root->edge[0]);
        edge(Edge(tca,2), root->edge[1]);
        root->chd[0] = tab;
        root->chd[1] = tbc;
        root->chd[2] = tca;
        flip(tab,2);
        flip(tbc,2);
        flip(tca,2);
    }
    void flip(TriRef tri, SdRef pi) {
        TriRef trj = tri->edge[pi].tri;
        int pj = tri->edge[pi].side;
        if (!trj) return;
        if (!in_cc(tri->p[0],tri->p[1],tri->p[2],trj->p[pj]
            )) return;
        /* flip edge between tri,trj */

```

```

        TriRef trk = new(tris++) Tri(tri->p[(pi+1)%3], trj
            ->p[pj], tri->p[pi]);
        TriRef trl = new(tris++) Tri(trj->p[(pj+1)%3], tri
            ->p[pi], trj->p[pj]);
        edge(Edge(trk,0), Edge(trl,0));
        edge(Edge(trk,1), tri->edge[(pi+2)%3]);
        edge(Edge(trk,2), trj->edge[(pj+1)%3]);
        edge(Edge(trl,1), trj->edge[(pj+2)%3]);
        edge(Edge(trl,2), tri->edge[(pi+1)%3]);
        tri->chd[0]=trk; tri->chd[1]=trl; tri->chd[2]=0;
        trj->chd[0]=trk; trj->chd[1]=trl; trj->chd[2]=0;
        flip(trk,1); flip(trk,2);
        flip(trl,1); flip(trl,2);
    }
};
vector<TriRef> triang;
set<TriRef> vst;
void go( TriRef now ){
    if( vst.find( now ) != vst.end() )
        return;
    vst.insert( now );
    if( !now->has_chd() ){
        triang.push_back( now );
        return;
    }
    for( int i = 0 ; i < now->num_chd() ; i ++ )
        go( now->chd[ i ] );
}

void build( int n , Pt* ps ){
    tris = pool;
    random_shuffle(ps, ps + n);
    Trig tri;
    for(int i = 0; i < n; ++ i)
        tri.add_point(ps[i]);
    go( tri.the_root );
}

```

6.12 Min Enclosing Circle

```

struct Mec{
    // return pair of center and r
    static const int N = 101010;
    int n;
    Pt p[ N ], cen;
    double r2;
    void init( int _n , Pt _p[] ){
        n = _n;
        memcpy( p , _p , sizeof(Pt) * n );
    }
    double sqr(double a){ return a*a; }
    Pt center(Pt p0, Pt p1, Pt p2) {
        Pt a = p1-p0;
        Pt b = p2-p0;
        double c1=norm2( a ) * 0.5;
        double c2=norm2( b ) * 0.5;
        double d = a ^ b;
        double x = p0.X + (c1 * b.Y - c2 * a.Y) / d;
        double y = p0.Y + (a.X * c2 - b.X * c1) / d;
        return Pt(x,y);
    }
    pair<Pt,double> solve(){
        random_shuffle(p,p+n);
        r2=0;
        for (int i=0; i<n; i++){
            if (norm2(cen-p[i]) <= r2) continue;
            cen = p[i];
            r2 = 0;
            for (int j=0; j<i; j++){
                if (norm2(cen-p[j]) <= r2) continue;
                cen=Pt((p[i].X+p[j].X)/2,(p[i].Y+p[j].Y)/2);
                r2 = norm2(cen-p[j]);
                for (int k=0; k<j; k++){
                    if (norm2(cen-p[k]) <= r2) continue;
                    cen = center(p[i],p[j],p[k]);
                    r2 = norm2(cen-p[k]);
                }
            }
        }
        return {cen,sqrt(r2)};
    }
}

```

```
} mec;
```

6.13 Heart of Triangle

```
Pt inCenter( Pt &A, Pt &B, Pt &C) { // 内心
    double a = norm(B-C), b = norm(C-A), c = norm(A-B);
    return (A * a + B * b + C * c) / (a + b + c);
}
Pt circumCenter( Pt &a, Pt &b, Pt &c) { // 外心
    Pt bb = b - a, cc = c - a;
    double db=norm2(bb), dc=norm2(cc), d=2*(bb ^ cc);
    return a-Pt(bb.Y*dc-cc.Y*db, cc.X*db-bb.X*dc) / d;
}
Pt othroCenter( Pt &a, Pt &b, Pt &c) { // 垂心
    Pt ba = b - a, ca = c - a, bc = b - c;
    double Y = ba.Y * ca.Y * bc.Y,
           A = ca.X * ba.Y - ba.X * ca.Y,
           x0= (Y+ca.X*ba.Y*bc.X-ba.X*ca.Y*c.X) / A,
           y0= -ba.X * (x0 - c.X) / ba.Y + ca.Y;
    return Pt(x0, y0);
}
```

6.14 Min/Max Enclosing Rectangle.cpp

```
/****** NEED REVISION *****/
/* uva819 - gifts large and small */
#define MAXN 100005
const double eps=1e-8;
const double inf=1e15;
class Coor {
public:
    double x,y;
    Coor() {}
    Coor(double xi,double yi) { x=xi; y=yi; }
    Coor& operator+=(const Coor &b) { x+=b.x; y+=b.y;
        return *this; }
    const Coor operator+(const Coor &b) const { return (
        Coor)*this+=b; }
    Coor& operator-=(const Coor &b) { x-=b.x; y-=b.y;
        return *this; }
    const Coor operator-(const Coor &b) const { return (
        Coor)*this-=b; }
    Coor& operator*=(const double b) { x*=b; y*=b; return
        *this; }
    const Coor operator*(const double b) const { return (
        Coor)*this*=b; }
    Coor& operator/=(const double b) { x/=b; y/=b; return
        *this; }
    const Coor operator/(const double b) const { return (
        Coor)*this/=b; }
    const bool operator<(const Coor& b) const { return y<
        b.y-eps||fabs(y-b.y)<eps&&x<b.x; }
    const double len2() const { return x*x+y*y; }
    const double len() const { return sqrt(len2()); }
    const Coor perp() const { return Coor(y,-x); }
    Coor& standardize() {
        if(y<0||y==0&&x<0) {
            x=-x;
            y=-y;
        }
        return *this;
    }
    const Coor standardize() const { return ((Coor)*this)
        .standardize(); }
};
double dot(const Coor &a,const Coor &b) { return a.x*b.
    x+a.y*b.y; }
double dot(const Coor &o,const Coor &a,const Coor &b) {
    return dot(a-o,b-o); }
double cross(const Coor &a,const Coor &b) { return a.x*
    b.y-a.y*b.x; }
double cross(const Coor &o,const Coor &a,const Coor &b)
    { return cross(a-o,b-o); }
Coor cmpo;
const bool cmpf(const Coor &a,const Coor &b) {
    return cross(cmpo,a,b)>eps||fabs(cross(cmpo,a,b))<eps
        &&
        dot(a,cmpo,b)<-eps;
```

```
}
class Polygon {
public:
    int pn;
    Coor p[MAXN];
    void convex_hull() {
        int i,tn=pn;
        for(i=1;i<pn;++i) if(p[i]<p[0]) swap(p[0],p[i]);
        cmpo=p[0];
        std::sort(p+1,p+pn,cmpf);
        for(i=pn=1;i<tn;++i) {
            while(pn>2&&cross(p[pn-2],p[pn-1],p[i])<=eps) --
                pn;
            p[pn++]=p[i];
        }
        p[pn]=p[0];
    }
};
Polygon pol;
double minarea,maxarea;
int slpn;
Coor slope[MAXN*2];
Coor lrec[MAXN*2],rrec[MAXN*2],trec[MAXN*2],brec[MAXN
    *2];
inline double xproject(Coor p,Coor slp) { return dot(p,
    slp)/slp.len(); }
inline double yproject(Coor p,Coor slp) { return cross(
    p,slp)/slp.len(); }
inline double calcarea(Coor lp,Coor rp,Coor bp,Coor tp,
    Coor slp) {
    return (xproject(rp,slp)-xproject(lp,slp))*(yproject(
        tp,slp)-yproject(bp,slp)); }
inline void solve() {
    int i,lind,rind,tind,bind,tn;
    double pro,area1,area2,l,r,m1,m2;
    Coor s1,s2;
    pol.convex_hull();
    slpn=0; /* generate all critical slope */
    slope[slpn++]=Coor(1.0,0.0);
    slope[slpn++]=Coor(0.0,1.0);
    for(i=0;i<pol.pn;i++) {
        slope[slpn]=(pol.p[i+1]-pol.p[i]).standardize();
        if(slope[slpn].x>0) slpn++;
        slope[slpn]=(pol.p[i+1]-pol.p[i]).perp().
            standardize();
        if(slope[slpn].x>0) slpn++;
    }
    cmpo=Coor(0,0);
    std::sort(slope,slope+slpn,cmpf);
    tn=slpn;
    for(i=slpn=1;i<tn;i++)
        if(cross(cmpo,slope[i-1],slope[i])>0) slope[slpn
            ++]=slope[i];
    lind=rind=0; /* find critical touchpoints */
    for(i=0;i<pol.pn;i++) {
        pro=xproject(pol.p[i],slope[0]);
        if(pro<xproject(pol.p[lind],slope[0])) lind=i;
        if(pro>xproject(pol.p[rind],slope[0])) rind=i;
    }
    tind=bind=0;
    for(i=0;i<pol.pn;i++) {
        pro=yproject(pol.p[i],slope[0]);
        if(pro<yproject(pol.p[bind],slope[0])) bind=i;
        if(pro>yproject(pol.p[tind],slope[0])) tind=i;
    }
    for(i=0;i<slpn;i++) {
        while(xproject(pol.p[lind+1],slope[i])<=xproject(
            pol.p[lind],slope[i])+eps)
            lind=(lind==pol.pn-1?0:lind+1);
        while(xproject(pol.p[rind+1],slope[i])>=xproject(
            pol.p[rind],slope[i])-eps)
            rind=(rind==pol.pn-1?0:rind+1);
        while(yproject(pol.p[bind+1],slope[i])<=yproject(
            pol.p[bind],slope[i])+eps)
            bind=(bind==pol.pn-1?0:bind+1);
        while(yproject(pol.p[tind+1],slope[i])>=yproject(
            pol.p[tind],slope[i])-eps)
            tind=(tind==pol.pn-1?0:tind+1);
        lrec[i]=pol.p[lind];
        rrec[i]=pol.p[rind];
        brecc[i]=pol.p[bind];
        trec[i]=pol.p[tind];
    }
}
```



```

    }
    minarea=inf; /* find minimum area */
    for(i=0; i<slpn; i++) {
        area1=calcareal(lrec[i], rrec[i], brec[i], trec[i],
            slope[i]);
        if(area1<minarea) minarea=area1;
    }
    maxarea=minarea; /* find maximum area */
    for(i=0; i<slpn-1; i++) {
        l=0.0; r=1.0;
        while(l<r-eps) {
            m1=l+(r-l)/3;
            m2=l+(r-l)*2/3;
            s1=slope[i]*(1.0-m1)+slope[i+1]*m1;
            area1=calcareal(lrec[i], rrec[i], brec[i], trec[i],
                s1);
            s2=slope[i]*(1.0-m2)+slope[i+1]*m2;
            area2=calcareal(lrec[i], rrec[i], brec[i], trec[i],
                s2);
            if(area1<area2) l=m1;
            else r=m2;
        }
        s1=slope[i]*(1.0-l)+slope[i+1]*l;
        area1=calcareal(lrec[i], rrec[i], brec[i], trec[i], s1);
        if(area1>maxarea) maxarea=area1;
    }
}

int main(){
    int i, casenum=1;
    while(scanf("%d", &pol.pn)==1 && pol.pn) {
        for(i=0; i<pol.pn; i++)
            scanf("%lf %lf", &pol.p[i].x, &pol.p[i].y);
        solve();
        //minarea, maxarea
    }
}

```

6.15 Union of Polynomials

```

#define eps 1e-8
class PY{ public:
    int n;
    Pt pt[5];
    Pt& operator[](const int x){ return pt[x]; }
    void input(){
        int i; n=4;
        for(i=0; i<n; i++) scanf("%lf%lf", &pt[i].x, &pt[i].y);
    }
    double getArea(){
        int i; double s=pt[n-1]^pt[0];
        for(i=0; i<n-1; i++) s+=pt[i]^pt[i+1];
        return s/2;
    }
};

PY py[500];
pair<double, int> c[5000];
inline double segP(Pt &p, Pt &p1, Pt &p2){
    if(SG(p1.x-p2.x)==0) return (p.y-p1.y)/(p2.y-p1.y);
    return (p.x-p1.x)/(p2.x-p1.x);
}

double polyUnion(int n){
    int i, j, ii, jj, ta, tb, r, d;
    double z, w, s, sum, tc, td;
    for(i=0; i<n; i++) py[i][py[i].n]=py[i][0];
    sum=0;
    for(i=0; i<n; i++){
        for(ii=0; ii<py[i].n; ii++){
            r=0;
            c[r++]=make_pair(0.0, 0);
            c[r++]=make_pair(1.0, 0);
            for(j=0; j<n; j++){
                if(i==j) continue;
                for(jj=0; jj<py[j].n; jj++){
                    ta=SG(tri(py[i][ii], py[i][ii+1], py[j][jj]));
                    tb=SG(tri(py[i][ii], py[i][ii+1], py[j][jj+1]));
                    if(ta==0 && tb==0){
                        if((py[j][jj+1]-py[j][jj])*(py[i][ii+1]-py[i][ii])>0 && j<i){

```

```

                        c[r++]=make_pair(segP(py[j][jj], py[i][ii],
                            py[i][ii+1]), 1);
                        c[r++]=make_pair(segP(py[j][jj+1], py[i][ii],
                            py[i][ii+1]), -1);
                    }
                }else if(ta>0 && tb<0){
                    tc=tri(py[j][jj], py[j][jj+1], py[i][ii]);
                    td=tri(py[j][jj], py[j][jj+1], py[i][ii+1]);
                    c[r++]=make_pair(tc/(tc-td), 1);
                }else if(ta<0 && tb>0){
                    tc=tri(py[j][jj], py[j][jj+1], py[i][ii]);
                    td=tri(py[j][jj], py[j][jj+1], py[i][ii+1]);
                    c[r++]=make_pair(tc/(tc-td), -1);
                }
            }
        }
        sort(c, c+r);
        z=min(max(c[0].first, 0.0), 1.0);
        d=c[0].second; s=0;
        for(j=1; j<r; j++){
            w=min(max(c[j].first, 0.0), 1.0);
            if(!d) s+=w-z;
            d+=c[j].second; z=w;
        }
        sum+=(py[i][ii]^py[i][ii+1])*s;
    }
}

return sum/2;
}

int main(){
    int n, i, j, k;
    double sum, ds;
    scanf("%d", &n); sum=0;
    for(i=0; i<n; i++){
        py[i].input();
        ds=py[i].getArea();
        if(ds<0){
            for(j=0, k=py[i].n-1; j<k; j++, k--) swap(py[i][j],
                py[i][k]);
            ds=-ds;
        }
        sum+=ds;
    }
    printf("%.9f\n", sum/polyUnion(n));
}

```

7 String

7.1 Knuth-Morris-Pratt Algorithm

```

// test with CF 471 D
template< typename T >
vector< int > KMP( vector< T > target, vector< T >
    pattern ) {
    vector< int > match;
    if ( pattern.size() > target.size() ) return match;
    vector< int > failure_function( (int)target.size(),
        -1 );
    for ( int i = 1, j = failure_function[ 0 ] = -1; i <
        (int)pattern.size(); ++i ) {
        while ( j >= 0 and pattern[ j + 1 ] != pattern[ i ] )
            j = failure_function[ j ];
        if ( pattern[ j + 1 ] == pattern[ i ] ) j++;
        failure_function[ i ] = j;
    }
    // KMP
    int pos = i, prv = failure_function[ pos ];
    while ( pos + 1 < (int)pattern.size() and pattern[
        pos + 1 ] == pattern[ prv + 1 ] ) {
        if ( failure_function[ pos ] == -1 ) break;
        pos = prv;
        prv = failure_function[ prv ];
    }
    failure_function[ i ] = prv;
}

for ( int i = 0, j = -1; i < (int)target.size(); ++i ) {
    while ( j >= 0 and pattern[ j + 1 ] != target[ i ] )
        j = failure_function[ j ];
    if ( pattern[ j + 1 ] == target[ i ] ) j++;
}

```

```

    if ( j == (int)pattern.size() - 1 ) {
        match.push_back( i - pattern.size() + 1 );
        j = failure_function[ j ];
    }
}
return match;
}

```

7.2 Z Value

```

void Z_value( string& s, vector< int >& z ) {
    z.resize( s.size() );
    int i, j, left, right, len = s.size();
    left = right = 0; z[ 0 ] = len;
    for ( i = 1; i < (int)s.size(); ++i ) {
        j = max( min( z[ i - left ], right - i ), 0 );
        for( ; i + j < len && s[ i + j ] == s[ j ]; ++j );
        z[ i ] = j;
        if( i + z[ i ] > right ) {
            left = i;
            right = i + z[ i ];
        }
    }
}

```

7.3 Z Value Palindrome

```

const int N = 1000 + 10;
int len, zv[ N * 2 ];
char op[ N * 2 ];
string ip;
int main(){
    cin >> ip; len = ip.size();
    int l2 = len * 2 + 1;
    for ( int i = 0; i < l2; ++i ) {
        if ( i & 1 ) op[ i ] = ip[ i / 2 ];
        else op[ i ] = '@';
    }
    int l = 0, r = 0;
    zv[ 0 ] = 1;
    for ( int i = 1; i < l2; ++i ) {
        if ( i > r ) {
            l = r = i;
            while ( l > 0 and r < l2 - 1 and op[ l - 1 ] == op[ r + 1 ] )
                --l, ++r;
            zv[ i ] = r - l + 1;
        }
        else {
            int md = ( l + r ) / 2, j = md + md - i;
            zv[ i ] = zv[ j ];
            int q = zv[ i ] / 2, nr = i + q;
            if ( nr == r ) {
                l = i + i - r;
                while ( l > 0 and r < l2 - 1 and op[ l - 1 ] == op[ r + 1 ] )
                    --l, ++r;
                zv[ i ] = r - l + 1;
            }
            else if ( nr > r )
                zv[ i ] = ( r - i ) * 2 + 1;
        }
    }
}

```

7.4 Suffix Array

```

class SuffixArray {
public:
    static const int N = 1e5 + 10;
    string st;
    int SA[ N ], RA[ N ], tempSA[ N ], tempRA[ N ],
        counting[ N ], n;
    int LCP[ N ], PLCP[ N ], Phi[ N ];
}

```

```

void build( string& s ) { st = s + '.'; n = st.size();
    constructSA(); constructLCP(); }
void countingSort( int k ) {
    int maxRange = max( 260, n );
    memset( counting, 0, sizeof counting );
    for ( int i = 0; i < n; i++ )
        counting[ i + k < n ? RA[ i + k ] : 0 ]++;

    int sum = 0;
    for ( int i = 0; i < maxRange; ++i ) {
        int temp = counting[ i ];
        counting[ i ] = sum;
        sum += temp;
    }

    for ( int i = 0; i < n; ++i )
        tempSA[ counting[ SA[ i ] + k < n ? RA[ SA[ i ] + k ] : 0 ]++ ] = SA[ i ];
    for ( int i = 0; i < n; ++i )
        SA[ i ] = tempSA[ i ];
}
void constructSA() {
    for ( int i = 0; i < n; ++i ) {
        SA[ i ] = i;
        RA[ i ] = st[ i ];
    }

    for ( int k = 1; k < n; k <= 1 ) {
        countingSort( k ); countingSort( 0 );
        int rank;
        tempRA[ SA[ 0 ] ] = rank = 0;
        for ( int i = 1; i < n; ++i )
            tempRA[ SA[ i ] ] = ( RA[ SA[ i - 1 ] ] == RA[ SA[ i ] ] && RA[ SA[ i - 1 ] + k ] == RA[ SA[ i ] + k ] ) ? rank : ++rank;
        for ( int i = 0; i < n; ++i ) RA[ i ] = tempRA[ i ];
        if ( RA[ SA[ n - 1 ] ] == n - 1 ) break;
    }
}
void constructLCP() {
    Phi[ SA[ 0 ] ] = -1;
    for ( int i = 1; i < n; ++i )
        Phi[ SA[ i ] ] = SA[ i - 1 ];
    int L = 0;
    for ( int i = 0; i < n; ++i ) {
        if ( Phi[ i ] == -1 ) {
            PLCP[ i ] = 0;
            continue;
        }
        while ( st[ i + L ] == st[ Phi[ i ] + L ] ) L++;
        PLCP[ i ] = L;
        L = max( L - 1, 0 );
    }
    for ( int i = 0; i < n; ++i ) LCP[ i ] = PLCP[ SA[ i ] ];
}

```

7.5 Palindrome Tree

```

const int MAXN = 200010;
struct PalT{
    struct Node{
        int nxt[ 33 ], len, fail;
        ll cnt;
    };
    int tot, lst;
    Node nd[ MAXN * 2 ];
    char* s;
    int newNode( int l, int _fail ){
        int res = ++tot;
        memset( nd[ res ].nxt, 0, sizeof nd[ res ].nxt );
        nd[ res ].len = l;
        nd[ res ].cnt = 0;
        nd[ res ].fail = _fail;
        return res;
    }
    void push( int p ){

```

```

int np = lst;
int c = s[ p ] - 'a';
while( p - nd[ np ].len - 1 < 0
    || s[ p ] != s[ p - nd[ np ].len - 1 ] )
    np = nd[ np ].fail;

if( nd[ np ].nxt[ c ] ){
    nd[ nd[ np ].nxt[ c ] ].cnt++;
    lst = nd[ np ].nxt[ c ];
    return ;
}
int nq = newNode( nd[ np ].len + 2 , 0 );
nd[ nq ].cnt++;
nd[ np ].nxt[ c ] = nq;
lst = nq;
if( nd[ nq ].len == 1 ){
    nd[ nq ].fail = 2;
    return ;
}
int tf = nd[ np ].fail;
while( p - nd[ tf ].len - 1 < 0
    || s[ p ] != s[ p - nd[ tf ].len - 1 ] )
    tf = nd[ tf ].fail;

nd[ nq ].fail = nd[ tf ].nxt[ c ];
return ;
}
void init( char* _s ){
    s = _s;
    tot = 0;
    newNode( -1 , 1 );
    newNode( 0 , 1 );
    lst = 2;
    for( int i = 0 ; s[ i ] ; i++ )
        push( i );
}
void yutruli(){
#define REPD(i, s, e) for(int i = (s); i >= (e); i--)
    REPD( i , tot , 1 )
        nd[ nd[ i ].fail ].cnt += nd[ i ].cnt;
    nd[ 1 ].cnt = nd[ 2 ].cnt = 0ll;
}
} pA;
int main(){ pA.init( sa ); }

```

7.6 Suffix Automata

```

const int MAXM = 1000010;
struct SAM{
    int tot, root, lst, mom[MAXM], mx[MAXM];
    int acc[MAXM], nxt[MAXM][33];
    int newNode(){
        int res = ++tot;
        fill(nxt[res], nxt[res]+33, 0);
        mom[res] = mx[res] = acc[res] = 0;
        return res;
    }
    void init(){
        tot = 0;
        root = newNode();
        mom[root] = 0, mx[root] = 0;
        lst = root;
    }
    void push(int c){
        int p = lst;
        int np = newNode();
        mx[np] = mx[p]+1;
        for(; p && nxt[p][c] == 0; p = mom[p])
            nxt[p][c] = np;
        if(p == 0) mom[np] = root;
        else{
            int q = nxt[p][c];
            if(mx[p]+1 == mx[q]) mom[np] = q;
            else{
                int nq = newNode();
                mx[nq] = mx[p]+1;
                for(int i = 0; i < 33; i++)
                    nxt[nq][i] = nxt[q][i];
                mom[nq] = mom[q];
                mom[q] = nq;
            }
        }
    }
}

```

```

        mom[np] = nq;
        for(; p && nxt[p][c] == q; p = mom[p])
            nxt[p][c] = nq;
    }
    lst = np;
}
void push(char *str){
    for(int i = 0; str[i]; i++)
        push(str[i]-'a'+1);
}
} sam;

```

7.7 Smallest Rotation

```

string mcp(string s){
    int n = s.length();
    s += s;
    int i=0, j=1;
    while (i<n && j<n){
        int k = 0;
        while (k < n && s[i+k] == s[j+k]) k++;
        if (s[i+k] <= s[j+k]) j += k+1;
        else i += k+1;
        if (i == j) j++;
    }
    int ans = i < n ? i : j;
    return s.substr(ans, n);
}

```