

Carla Jacobsen cjacobsen2016@csu.fullerton.edu

Left-To-Right Algorithm:

```
assert(before.is_alternating())
```

```
unsigned numSwaps = 0
```

```
//sc for entire loop:
```

```
while ! is_sorted do
```

```
    { //while
```

```
    for i = 0 to n do
```

```
        { //for
```

```
        if current disk is light and the next is dark then swap
```

```
        if (disk[i] == light) && (disk[i+1] == dark) do
```

```
            { //if
```

```
            ++numSwaps
```

```
            swap disk[i] and disk[i+1]
```

```
            } //if
```

```
        } //for
```

```
    } //while
```

```
return a new sorted_disks
```

Proof:

sc of swap = 13

sc of the if condition = $7 + 7 + 1 = 15$

sc of the if condition if true = $15 + 1 + 13 = 29$

sc of the full if statement = $\text{sc max}(15, 29) = 29$

sc of the for loop condition = n

sc of the entire for loop = $29n$

sc of is_sorted function = $10n + 2$

sc of while condition = $n * (10n + 2) = 10(n^2) + 2n$

sc of entire while loop contents = $(10(n^2) + 2) * (29n) = 290(n^3) + 58(n^2)$

sc of assert(before.is_alternating()) = $11n + 2$

sc of numSwaps initialization = 1

sc of return statement = 2

sc of algorithm = $11n + 2 + 290(n^3) + 58(n^2) + 1 + 2 = 290(n^3) + 58(n^2) + 11n + 5 \rightarrow O(n^3)$

Lawnmower Algorithm:

```
assert(before.is_alternating())
```

```
unsigned numSwaps = 0
```

```
//sc for entire loop:
```

```
while ! is_sorted do
```

```
    { //while
```

```
    for i = 0 to n do
```

```
        { //for
```

```
        if current disk is light and the next is dark then swap
```

```
        if (disk[i] == light) && (disk[i+1] == dark) do
```

```
            { //if
```

```
            ++numSwaps
```

```
            swap disk[i] and disk[i+1]
```

```
            } //if
```

```
        } //for
```

```
    for i = n-1 to 0 do
```

```
        { //for
```

```
        if current disk is dark and the left is light then swap
```

```
        if (disk[i] == dark) && (disk[i-1] == light) do
```

```
            { //if
```

```
            ++numSwaps
```

```
            swap disk[i] and disk[i-1]
```

```
            } //if
```

```
        } //for
```

```
    } //while
```

```
return a new sorted_disks //sc 2
```

Proof:

if statement in n for loop

sc of swap #1 = 13

sc of the if condition #1 = $7 + 7 + 1 = 15$

sc of the if condition if true #1 = $15 + 1 + 13 = 29$

sc of the full if statement #1 = $\text{sc max}(15, 29) = 29$

if statement in n - 1 for loop

sc of swap #2 = 13

sc of the if condition #2 = $7 + 7 + 1 = 15$

sc of the if condition if true #2 = $15 + 1 + 13 = 29$

sc of the full if statement #2 = $\text{sc max}(15, 29) = 29$

n for loop

sc of the for loop condition = n

sc of the entire for loop = $29n$

n - 1 for loop

sc of the for loop condition = n - 1

sc of the entire for loop = $29n - 29$

sc of both for loops = $29n + 29n - 29 = 58n - 29$

sc of is_sorted function = $10n + 2$

sc of while condition = $(n/2) * (10n + 2) = 5(n^2) + n$

sc of entire while loop contents = $(5(n^2) + n) * (58n - 29) = 290(n^3) - 145(n^2) + 58(n^2) - 29n = 290(n^3) - 87(n^2) - 29n$

sc of assert(before.is_alternating()) = $11n + 2$

sc of numSwaps initialization = 1

sc of return statement = 2

sc of algorithm = $11n + 2 + 1 + 2 + 290(n^3) - 87(n^2) - 29n = 290(n^3) - 87(n^2) - 18n + 5 \rightarrow O(n^3)$