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### **Left-To-Right Algorithm:**

```
def sort_left_to_right(before)
{ //sort_left_to_right

    check disks for alternating

    numSwaps = 0

    newDisks = before

    while the disks are being sorted do
        { //while
            for i = 0 to n - 1 do
                { //for
                    //if current disk is light and the next is dark then swap
                    if (disk[i] == light) && (disk[i+1] == dark) do
                        { //if
                            ++numSwaps

                            swap disk[i] and disk[i+1]
                        } //if
                    } //for
                } //while

            return a new disk object
        } //sort_left_to_right
```

### **Proof for Left-to-Right:**

sc of check disks for alternating =  $n$

sc of numSwaps = 1

sc of newDisks = 1

sc of return = 1

//if statement block:

sc of swap = 1

sc of ++numSwaps = 1

sc of evaluating if condition = 2

sc of then branch =  $1 + 1 = 2$

sc of else branch = 0

sc of if block = sc of evaluating if condition +  $\max(2,0) = 2 + 2 = 4$

//for loop:

sc inside for loop = sc of if block = 4

sc of for loop duration =  $(n - 1) - 0 + 1 = n$

sc of for loop block = (sc of for loop duration) \* (sc inside for loop) =  $4n$

//while loop:

sc of while loop duration =  $n$

sc of while loop block = (while loop duration) \* (for loop block) =  $4(n^2)$

//the entire function:

sc of left\_to\_right =

(sc while block) + (sc check disks) + (sc numSwaps) + (sc newDisks) + (sc return) =

$4(n^2) + n + 1 + 1 + 1 = 4(n^2) + n + 3 =$

**$O(n^2)$**

### Lawnmower Algorithm:

```
def sort_lawnmower(before)
  //sort_lawnmower

  check disks for alternating

  numSwaps = 0

  newDisks = before

  while the disks are being sorted do
    //while
    for i = 0 to n - 1 do    //block a
      //for
      //if current disk is light and the next is dark then swap
      if (disk[i] == light) && (disk[i+1] == dark) do    //block c
        //if
        ++numSwaps

        swap disk[i] and disk[i+1]
      //if
    //for
    for i = n - 1 to 1 do    //block b
      //for
      //if current disk is dark and the left is light then swap
      if(disk[i] == dark) && (disk[i-1] == light) do    //block d
        //if
        ++numSwaps

        swap disk[i] and disk[i-1]
      //if
    //for
  //while

  return a new disk object
//sort_lawnmower
```

### Proof for Lawnmower:

sc of check disks for alternating =  $n$   
sc of numSwaps = 1  
sc of newDisks = 1  
sc of return = 1

//if statement block c:  
sc of swap = 1  
sc of ++numSwaps = 1  
sc of evaluating if condition = 2  
sc of then branch =  $1 + 1 = 2$   
sc of else branch = 0  
sc of if block c = sc of evaluating if condition +  $\max(2,0) = 2 + 2 = 4$

//if statement block d:  
sc of swap = 1  
sc of ++numSwaps = 1  
sc of evaluating if condition = 2  
sc of then branch =  $1 + 1 = 2$   
sc of else branch = 0  
sc of if block d = sc of evaluating if condition +  $\max(2,0) = 2 + 2 = 4$

//for loop block a:  
sc inside for loop = sc of if block c = 4  
sc of for loop duration =  $(n - 1) - 0 + 1 = n$   
sc of for loop block a = (sc of for loop duration) \* (sc inside for loop) =  $4n$

//for loop block b:  
sc inside for loop = sc of if block d = 4  
sc of for loop duration =  $(n - 1) - 1 + 1 = n - 1$   
sc of for loop block b = (sc of for loop duration) \* (sc inside for loop) =  $4(n - 1) = 4n - 4$

//while loop:  
sc of inside while loop = (sc of for loop a) + (sc of for loop b) =  $4n + 4n - 4 = 8n - 4$   
sc of while loop duration =  $n / 2$   
sc of while loop block = (sc of while loop duration) \* (sc of inside while loop) =  
 $(n / 2) * (8n - 4) = 4(n^2) - 2n$

//the entire function:  
sc of lawnmower =  
(sc while block) + (sc check disks) + (sc numSwaps) + (sc newDisks) + (sc return) =  
 $4(n^2) - 2n + n + 1 + 1 + 1 = 4(n^2) - n + 3 =$   
 **$O(n^2)$**