## MPFE

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Many of the known mechanisms driving gene regulation fall into the category of epigenomic modifications. DNA methylation is a common epigenomic modification, in which a cytosine (C) in the genomic DNA sequence can be altered by the addition of a methyl group. Methylation patterns can be are detected by treating DNA with bisulphite, which converts unmethylated cytosines to uracils while leaving methylated cytosines intact. This can be carried out at the whole genome level (whole-genome bisulfite sequencing) or at specific loci (PCR amplicons, capture or reduced representation bisulfite sequencing). The resulting reads can be mapped to a reference and methylation patterns inferred.

However, the bisulphite conversion is not 100% efficient, and this introduces errors in the observed distribution of methylation patterns. A second source of errors is the sequencing error. MPFE (for Methylation Patterns Frequency Estimation) [?] calculates the estimated distribution over methylation patterns based on an input of methylation pattern count data, an incomplete conversion rate and site-dependent read error rates.

The main component of the package is the function estimatePatterns(), which generates a table of estimates  $\hat{\theta}_i$  of the distribution over methylation patterns, and a list of patterns identified as spurious. Input to the function is a data frame listing the methylation patterns in the first column followed by a number of columns of count data (one column per sample). Estimation will be performed on all columns by default unless specified by the variable column. The non-conversion and sequencing error rates are specified by the parameters epsilon and eta respectively. The parameter eta can be specified globally or as a site-dependent array with length equal to the number of CpG sites in sequence of interest. The boolean variable fast enables either a fast implementation (default) which ignores those patterns for which the observed read count is zero or a slow implementation. The parameters steps and reltol are passed to the function constrOptim() to control the accuracy of the determination of the maximum log-likelihood.

A second function in the package is plotPatterns(). Input to this function is a data frame, obtained from the output of estimatePatterns(). The output of plotPatterns() is a plot that compares the observed read distribution with the estimated distribution. The parameters yLimit1 and yLimit2 control the range of the y-axis on the plots produced.

In the following example, the input is the table of counts patternsExample. We analyse the second column. The parameter epsilon is 0.01, while the parameter eta is not specified and by default is 0.

- > library(MPFE)
- > data(patternsExample)
- > patternsExample

	mPattern	k1	k2
1	m00000	629	2257
2	m00001	26	90
3	m00010	20	75
4	m00011	2	3
5	m00100	24	82
6	m00101	3	0
7	m00110	1	11
8	m00111	0	0
9	m01000	23	80
10	m01001	0	0
11	m01010	1	1
12	m01011	0	0
13	m01100	1	5
14	m01110	0	0
15	m10000	28	69
16	m10001	1	2
17	m10010	0	2
18	m10011	0	0
19	m10100	0	7
20	m11000	3	1
21	m11001	0	0

> estimatePatterns(patternsExample, epsilon=0.01, column=2)

#### [[1]]

	pattern	${\tt coverage}$	${\tt observedDistribution}$	${\tt estimatedDistribution}$	spurious
1	00000	2257	0.8405959032	0.8841394834	FALSE
2	00001	90	0.0335195531	0.0253622332	FALSE
3	00010	75	0.0279329609	0.0201750634	FALSE
4	00011	3	0.0011173184	0.0005735316	FALSE
5	00100	82	0.0305400372	0.0226431744	FALSE
6	00110	11	0.0040968343	0.0035802381	FALSE
7	01000	80	0.0297951583	0.0217187544	FALSE
8	01010	1	0.0003724395	0.000000000	TRUE

9	01100	5	0.0018621974	0.0013301642	FALSE
10	10000	69	0.0256983240	0.0178634739	FALSE
11	10001	2	0.0007448790	0.0002242079	FALSE
12	10010	2	0.0007448790	0.0002760796	FALSE
13	10100	7	0.0026070764	0.0021135959	FALSE
14	11000	1	0.0003724395	0.000000000	TRUE

Note that in this example two patterns have been identified as spurious; they are patterns 01010 and 11000.

The following example uses the same input table. The column variable is not specified, so the function estimatePatterns() by default applies to both columns of counts. The sequencing error rate eta is specified as a site-dependent array.

```
> estimates <- estimatePatterns(patternsExample,
+
                                   epsilon=0.01,
                                   eta=c(0.008, 0.01, 0.01, 0.01, 0.008))
> estimates
[[1]]
   pattern coverage observedDistribution estimatedDistribution spurious
1
     00000
                 629
                               0.825459318
                                                      0.9088748331
                                                                       FALSE
2
     00001
                                                                       FALSE
                  26
                               0.034120735
                                                      0.0200854806
3
     00010
                  20
                               0.026246719
                                                      0.0099129217
                                                                       FALSE
4
     00011
                   2
                               0.002624672
                                                      0.0017646709
                                                                       FALSE
5
     00100
                  24
                                                                       FALSE
                               0.031496063
                                                      0.0155305960
6
     00101
                   3
                               0.003937008
                                                      0.0030002140
                                                                       FALSE
7
                                                                       FALSE
     00110
                   1
                               0.001312336
                                                      0.0004654103
                  23
8
     01000
                               0.030183727
                                                      0.0141238683
                                                                       FALSE
9
     01010
                   1
                               0.001312336
                                                      0.0004935455
                                                                       FALSE
10
     01100
                   1
                               0.001312336
                                                      0.0003809915
                                                                       FALSE
                  28
                                                                       FALSE
11
     10000
                               0.036745407
                                                      0.0221025625
12
                                                      0.0002793763
                                                                       FALSE
     10001
                   1
                               0.001312336
13
     11000
                   3
                               0.003937008
                                                      0.0029855293
                                                                       FALSE
[[2]]
   pattern coverage observedDistribution estimatedDistribution spurious
                2257
1
     00000
                              0.8405959032
                                                      0.9257433597
                                                                       FALSE
2
     00001
                  90
                              0.0335195531
                                                      0.0183957879
                                                                       FALSE
3
                  75
     00010
                              0.0279329609
                                                      0.0115868249
                                                                       FALSE
4
                   3
     00011
                              0.0011173184
                                                      0.0002262905
                                                                       FALSE
5
                  82
                              0.0305400372
                                                                       FALSE
     00100
                                                      0.0141488595
6
     00110
                  11
                              0.0040968343
                                                      0.0032974071
                                                                       FALSE
     01000
                  80
                              0.0297951583
                                                      0.0127240011
                                                                       FALSE
```

#### > plotPatterns(estimates[[2]])

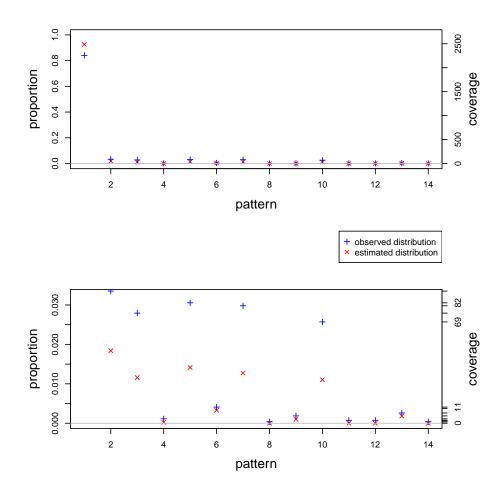


Figure 1: Plot of observed and estimated frequencies with plotPatterns

8	01010	1	0.0003724395	0.000000000	TRUE
9	01100	5	0.0018621974	0.0009915809	FALSE
10	10000	69	0.0256983240	0.0110383332	FALSE
11	10001	2	0.0007448790	0.000000000	TRUE
12	10010	2	0.0007448790	0.000000000	TRUE
13	10100	7	0.0026070764	0.0018475551	FALSE
14	11000	1	0.0003724395	0.000000000	TRUE

The ouput is a list of two data frames. We plot the observed and estimated pattern of the second data frame on figure 1. Two plots are produced: the lower plot is the expanded version of the upper plot.

We can also plot a map of the patterns and their frequencies. For instance, figure 2 illustrates different ways to plot all the patterns with frequency of 50% or less.

```
> par(mfrow=c(2, 2))
> patternMap(estimates[[1]],
               maxFreq=0.5,
               main='Estimated frequencies')
  patternMap(estimates[[1]],
               estimatedDistribution=FALSE,
               maxFreq=0.5,
               topDown=FALSE,
               main='Observed frequencies')
  patternMap(estimates[[1]],
               maxFreq=0.5,
               methCol=colorRampPalette(c('red', 'blue')),
               unMethCol='lightgrey',
               main='Estimated frequencies')
  patternMap(estimates[[1]],
               estimatedDistribution=FALSE,
               maxFreq=0.5,
               methCol=c('bisque4', 'azure4'),
               unMethCol=c('beige', 'azure'),
               main='Observed frequencies')
         Estimated frequencies
                                           Observed frequencies
    0.08
                                      0.15
                                   Proportion
Proportion
                                      0.10
    0.04
                                      0.05
                                      0.00
              2
                  3
                                                 2
          1
                       4
                           5
                                             1
                                                     3
                                                         4
                                                             5
                 CpG
                                                    CpG
         Estimated frequencies
                                           Observed frequencies
    0.08
                                      0.15
Proportion
                                   Proportion
                                      0.10
    0.04
                                      0.05
                                      0.00
    0.00
              2
                  3
                           5
                                                 2
                                                             5
                       4
                                                     3
                                          5
```

Figure 2: Different ways to plot the estimated frequencies with patternMap

CpG

CpG

# References

[1] Lin, P., Forêt, S., Wilson, S.R. and Burden, C.J., Estimation of the methylation pattern distribution from deep sequencing data. BMC Bioinformatics 2015, 16:145 doi:10.1186/s12859-015-0600-6