

# COMPUTER & NETWORK SECURITY

## Lecture 7: Key Management

# CRYPTOBULLETIN: IN THE LAST WEEK

- **OpenSSL Patch to Plug Severe Security Holes**  
<http://krebsonsecurity.com/2015/03/openssl-patch-to-plug-severe-security-holes/>  
also: <http://www.itnews.com.au/News/401891,openssl-patches-denial-of-service-vulnerabilities.aspx>
- **Drupal SQL injection vulnerability attacks persist, despite patch release**  
<http://www.scmagazine.com/trustwave-details-drupal-sql-injection-attack/article/404719/>
- **New BIOS Implant, Vulnerability Discovery Tool to Debut at CanSecWest**  
<https://threatpost.com/new-bios-implant-vulnerability-discovery-tool-to-debut-at-cansecwest/111710>
- **Meet “badBIOS”, the mysterious Mac & PC malware that jumps airgaps (historical)**  
<http://arstechnica.com/security/2013/10/meet-badbios-the-mysterious-mac-and-pc-malware-that-jumps-airgaps/>
- **Shopping for Spy Gear: Catalog Advertises NSA Toolbox (historical)**  
<http://www.spiegel.de/international/world/catalog-reveals-nsa-has-back-doors-for-numerous-devices-a-940994.html>
- **RSA Key Extraction via Low-Bandwidth Acoustic Cryptanalysis (historical)**  
<http://www.cs.tau.ac.il/~tromer/acoustic/>

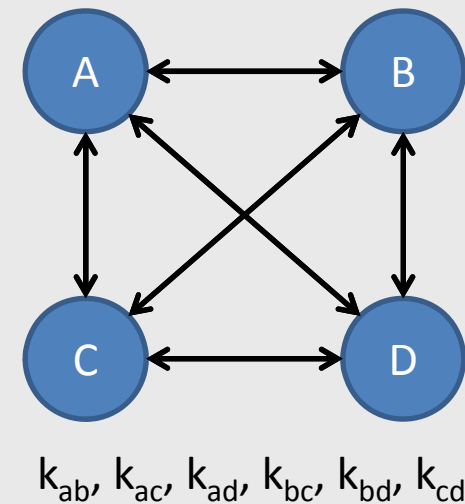
# KEY MANAGEMENT

Suppose we have a symmetric key network:

Alice, Bob, Carol and Dave want to talk to each other  
For secure communication with  $n$  parties, we require

$$\binom{n}{2} = n(n-1) / 2 \text{ keys}$$

Key distribution and management becomes a major issue!



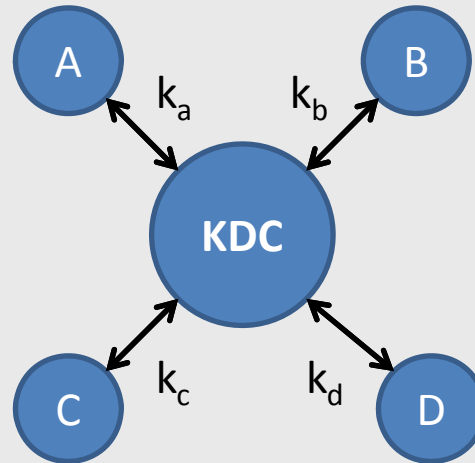
## DEFINITIONS

**Key establishment** is any process whereby a shared key becomes available to two or more parties for subsequent cryptographic use

**Key management** is the set of processes and mechanisms which support key establishment and the maintenance of on-going keying relationships between parties, including replacing older keys with newer ones:

- key agreement
- key transport

## KEY DISTRIBUTION CENTRE: NAIVE

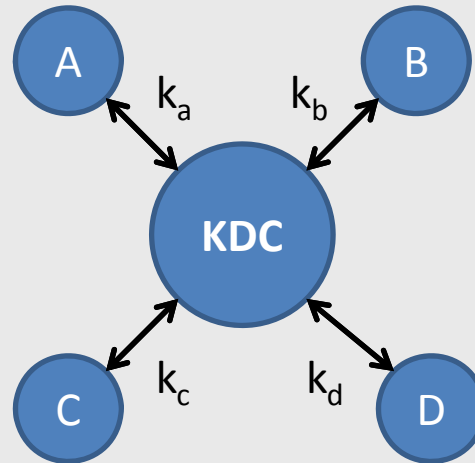


### Protocol:

- (1) Alice  $\rightarrow$  KDC : “want to talk with Bob”
- (2) KDC  $\rightarrow$  Alice : KDC picks random key  $k_{ab}$ , sends  $E_{k_a}[k_{ab}]$ ,  $E_{k_b}[k_{ab}]$ , “ticket a-b”
- (3) Alice  $\rightarrow$  Bob : Alice decrypts  $E_{k_a}[k_{ab}]$ , sends ticket to Bob
- (4) Bob : Bob decrypts ticket

**Alice and Bob now share secret key  $k_{ab}$**

## KEY DISTRIBUTION CENTRE: NAIVE



### Problems:

- The Key Distribution Centre is a single point of failure (likely to be attacked)
- No authentication
- Poor scalability
- Slow

# MERKLE'S PUZZLES

- Ralph Merkle (Stanford, 1974)
- Merkle's puzzles are a way of doing key exchange between Alice and Bob without the need for a KDC

(1) Alice creates lots of puzzles  $P_i = E_{p_i}[\text{"This is puzzle \#X}_i", k_i]$   
where  $i = 1 \dots 220$ ,  $|p_i| = 20$  bits (weak),  $|k_i| = 128$  bits (strong)  
 $X_i$ ,  $p_i$  and  $k_i$  are chosen randomly and different for each  $i$

(2) Alice sends all puzzles  $P_i$  to Bob

(3) Bob picks a random puzzle  $j \in \{1 \dots 220\}$  and solves  $P_j$  by brute force  
(i.e. search on key  $p_j$ ) -- this recovers  $X_j$  and  $k_j$  from the puzzle

(4) Bob sends  $X_j$  to Alice in the clear

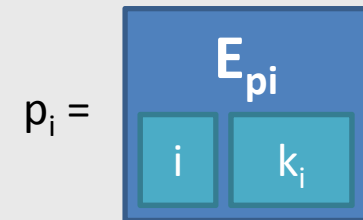
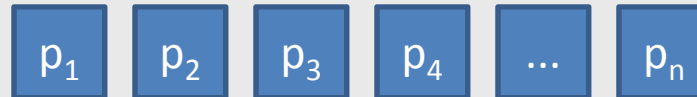
(5) Alice looks up the index  $j$  of  $X_j$  (from a table) to get  $k_j$

**=> Alice and Bob now both share a secret key  $k$**



# MERKLE'S PUZZLES

Alice makes  $2^{20}$  puzzles



Alice sends the puzzles to Bob

Bob selects a random puzzle  $p_j$  retrieving  $(i, k_i)$

Bob sends Alice a message saying he's retrieved the  $i^{\text{th}}$  puzzle

Alice looks up  $k_i$  from her selection of puzzles

Alice and Bob now use the shared key  $k_i$  for all future interaction



# ATTACK ON MERKLE'S PUZZLES

**Eve must break on average half the puzzles to find  $X_j$  (hence  $k_j$ )**

- Time required to do so for  $2^{20}$  puzzles =  $2^{19} \times 2^{19} = 2^{38}$

**If Alice and Bob can try 10,000 keys/second:**

- It will take a minute for each of them to perform their steps ( $2^{19}$  for Bob)
- Plus another minute to communicate the puzzles on a 1.544MB (T1) link

**With comparable resources, it will take Eve about a year to break the system**

Note: Merkle's Puzzles uses a lot of bandwidth (impractical!)

# DIFFIE-HELLMAN KEY EXCHANGE

**Diffie-Hellman (Stanford, 1976)**

**Worldwide standard used in smart cards, SSL, etc.**

Consider the finite field  $Z_p = \langle 0, \dots, p-1 \rangle$  where  $p$  is prime ( $p$  is 300 digits or longer)

Let  $g \in Z_p$  (the generator)

(1) Alice : Alice chooses a random large integer  $a \in Z_p$

(2) Bob : Bob chooses a random large integer  $b \in Z_p$

(3) Alice  $\rightarrow$  Bob : Alice sends Bob  $g^a \pmod{p}$

(4) Bob  $\rightarrow$  Alice : Bob sends Alice  $g^b \pmod{p}$

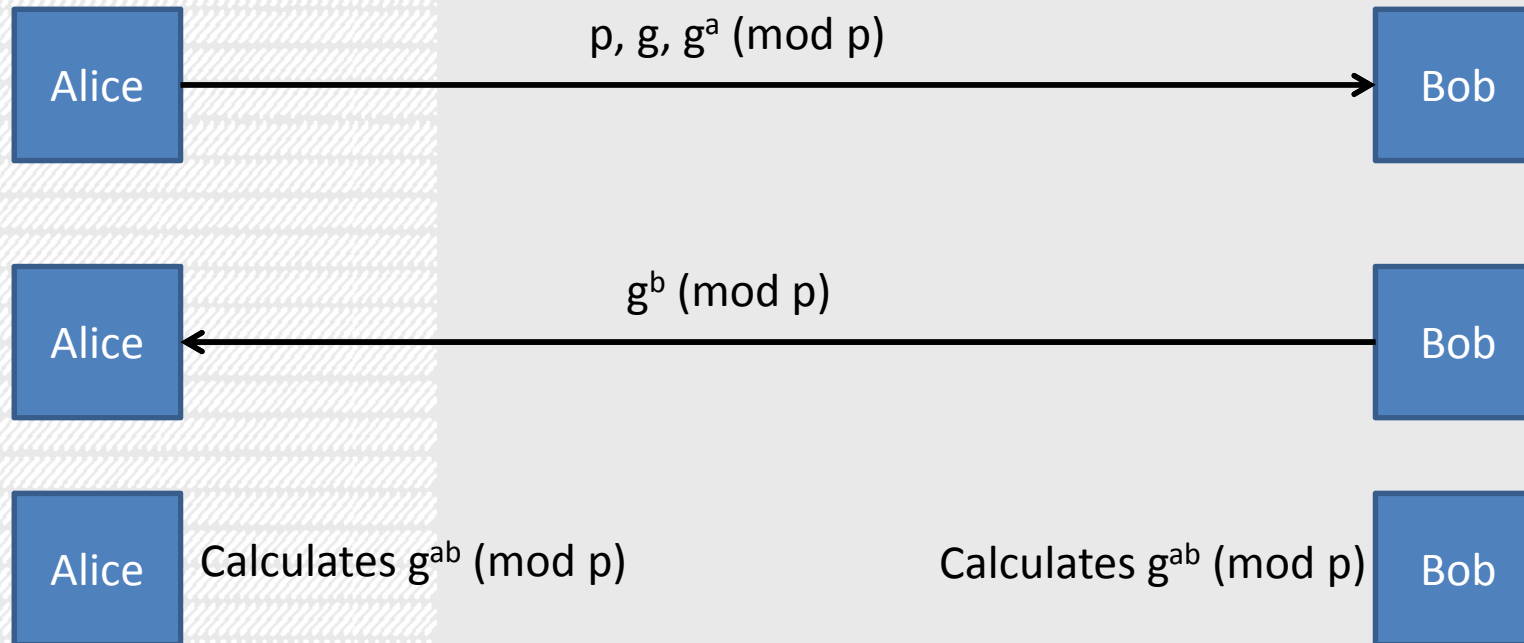
(5) Alice and Bob : compute  $g^{ab}$

: Alice computes  $(g^b)^a = g^{ab} \pmod{p}$

: Bob computes  $(g^a)^b = g^{ab} \pmod{p}$

$\Rightarrow$  Alice and Bob now share secret  $g^{ab}$

# DIFFIE-HELLMAN KEY EXCHANGE



Eve calculates ???  
(only knows  $p, g, g^a, g^b$ )

# STRENGTH OF DIFFIE-HELLMAN

- **The strength of Diffie-Hellman is based upon two issues:**
  - given  $p, g, g^a$ , it is difficult to calculate  $a$  (the discrete logarithm problem)
  - given  $p, g, g^a, g^b$  it is difficult for Eve to calculate  $g^{ab}$  (the Diffie-Hellman problem)
  - we know that  $DL \Rightarrow DH$  but it is not known if  $DH \Rightarrow DL$ .
- **Essentially, the strength of the system is based on the difficulty of factoring numbers the same size as  $p$**
- **The generator,  $g$ , can be small**
- **Do not use the secret  $g^{ab}$  directly as a session key**
  - it is better to either hash it or use it as a seed for a PRNG – not all bits of the secret have a flat distribution

# ■ REFERENCES

## **Handbook of Applied Cryptography**

– read §1, §2-2.4.4, §2.5 - 2.5.3

## **Stallings (3rd Ed)**

– 6.3 – 6.4