

## Supply & Demand Model

a.)

$$s = 203 + 5.7 * p$$

$$d = 650 - 2.75 * p$$

$$203 + 5.7 * p = 650 - 2.75 * p$$

$$203 + 8.45 * p = 650$$

$$8.45 * p = 447$$

$$p = 52.90$$

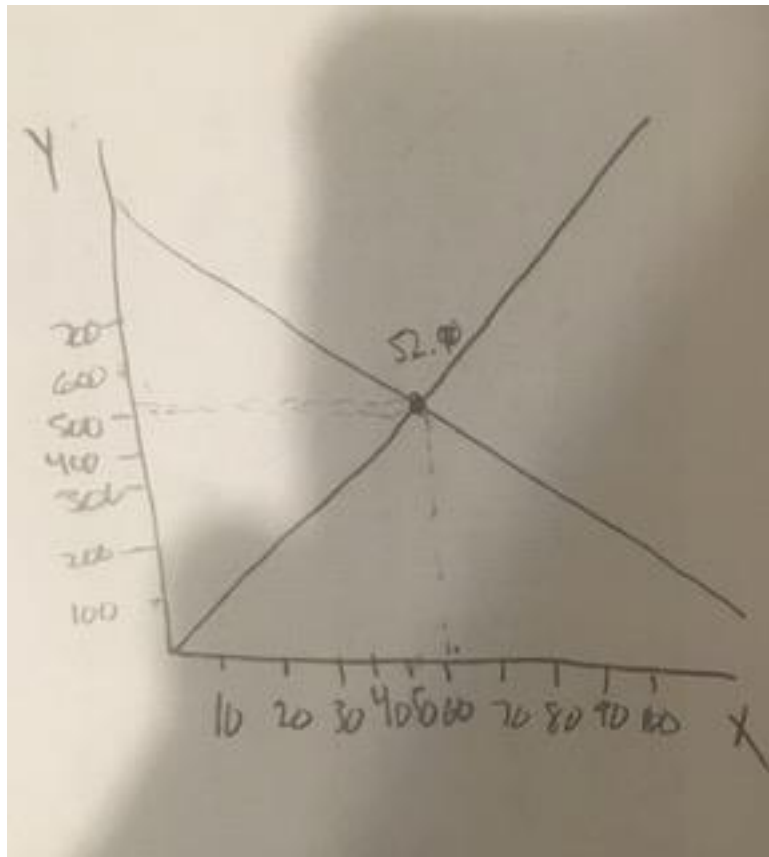
$$s = 203 + 5.7(52.90)$$

$$s = 504.43$$

$$d = 650 - 2.75(52.90)$$

$$d = 504.43$$

$$s = 504.43 = d$$



As shown above through the visual inspection graph and formulas, we can conclude that the economy is stable at the price point of \$52.90.

b.)

```
>> syms p
>> solve(203+5.7*p==650-2.75*p)

ans =

8940/169
>> 8940/169

ans =

52.8994

>> syms s d p
>> sol=solve(s==203+5.7*p,d==650-2.75*p,s==d)

sol =

struct with fields:

    d: [1x1 sym]
    p: [1x1 sym]
    s: [1x1 sym]

>> sol.d

ans =

85265/169
>> 85265/169

ans =

504.5266
>> sol.s

ans =

85265/169
>> 85265/169

ans =

504.5266
>> sol.p

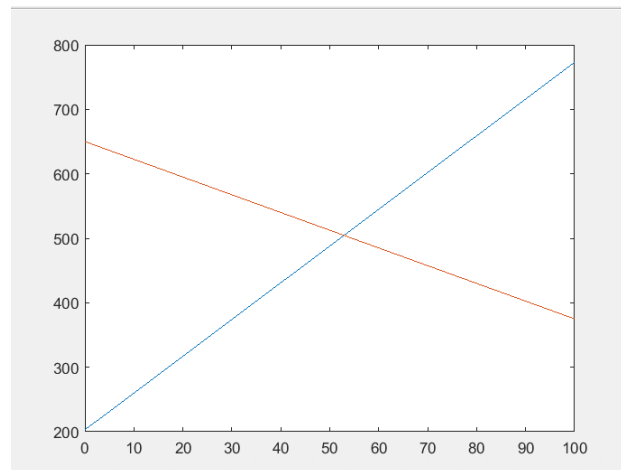
ans =

8940/169
>> 8940/169

ans =

52.8994
```

```
>> x=0:100;
>> plot(x,203+5.7*x)
>> hold on
>> plot(x,650-2.75*x)
```



2 variables

a.)

$$\begin{aligned} 2x - 3y &= 1 \\ -4x + 8y &= 4 \\ E2(2) \\ 2x - 3y &= 1 \\ 0 + 2y &= 6 \\ E2\left(\frac{1}{2}\right) \\ 2x - 3y &= 1 \\ 0 + 1y &= 3 \\ E12(3) \\ 2x - 0 &= 10 \\ 0 + 1y &= 3 \\ E1\left(\frac{1}{2}\right) \\ 1x - 0 &= 5 \\ 0 + 1y &= 3 \\ x &= 5 \\ y &= 3 \end{aligned}$$

b.)

$$\begin{aligned} 2x - 3y &= 5 \\ 3x - 8y &= 4 \\ E2\left(-\frac{3}{2}\right) \\ 2x - 3y &= 5 \\ 0 - 3.5y &= 3.5 \\ E2\left(-\frac{1}{3.5}\right) \\ 2x - 3y &= 5 \\ 0 + 1y &= 1 \\ E12(3) \\ 2x - 0 &= 8 \\ 0 + 1y &= 1 \\ E1\left(\frac{1}{2}\right) \\ 1x - 0 &= 4 \\ 0 + 1y &= 1 \\ x &= 4 \\ y &= 1 \end{aligned}$$

2 variables - Augmented

a.)

$$\begin{aligned} 4) \text{ a) } & \begin{cases} 2x - 3y = 1 \\ -4x + 8y = 4 \end{cases} \\ & \text{augmented} \\ & \begin{array}{cc|c} 2 & -3 & 1 \\ -4 & 8 & 4 \end{array} \\ & E2(2) \\ & \begin{array}{cc|c} 2 & -3 & 1 \\ 0 & 2 & 6 \end{array} \\ & E2(\frac{1}{2}) \\ & \begin{array}{cc|c} 2 & -3 & 1 \\ 0 & 1 & 3 \end{array} \\ & E1(2(3)) \\ & \begin{array}{cc|c} 2 & 0 & 10 \\ 0 & 1 & 3 \end{array} \\ & E1(\frac{1}{2}) \\ & \begin{array}{cc|c} 1 & 0 & 5 \\ 0 & 1 & 3 \end{array} \\ & x=5 \\ & y=3 \end{aligned}$$

b.)

$$\begin{aligned} 6) & \begin{cases} 2x - 3y = 5 \\ 3x - 8y = 4 \end{cases} \\ & \text{augmented} \\ & \begin{array}{cc|c} 2 & -3 & 5 \\ 3 & -8 & 4 \end{array} \\ & E2(1(\frac{2}{3})) \\ & \begin{array}{cc|c} 2 & -3 & 5 \\ 0 & -5 & -35 \end{array} \\ & E2(-\frac{1}{55}) \\ & \begin{array}{cc|c} 2 & -3 & 5 \\ 0 & 1 & 1 \end{array} \\ & E1(2(3)) \\ & \begin{array}{cc|c} 2 & 0 & 8 \\ 0 & 1 & 1 \end{array} \\ & E1(\frac{1}{2}) \\ & \begin{array}{cc|c} 1 & 0 & 4 \\ 0 & 1 & 1 \end{array} \\ & x=4 \\ & y=1 \end{aligned}$$

**Back Substitution / Gauss Jordan / Gaussian**

$$\begin{array}{rrcrcl}
 -2x + 6y & -3z & -w & = & 8 \\
 & 5y & +z & -6w & = & 1 \\
 & & z & +5w & = & 2 \\
 & & & 4w & = & 4
 \end{array}$$

a.) augmented matrix M

$$\begin{array}{rrrrr}
 -2 & 6 & -3 & -1 & 8 \\
 0 & 5 & 1 & -6 & 1 \\
 0 & 0 & 1 & 5 & 2 \\
 0 & 0 & 0 & 4 & 4
 \end{array}$$

b.)

$$\begin{array}{l}
 E4(1/4)| \\
 \begin{array}{rrrrr}
 -2 & 6 & -3 & -1 & 8 \\
 0 & 5 & 1 & -6 & 1 \\
 0 & 0 & 1 & 5 & 2 \\
 0 & 0 & 0 & 1 & 1
 \end{array}
 \end{array}$$

$$\begin{array}{l}
 E34(-5) \\
 \begin{array}{rrrrr}
 -2 & 6 & -3 & -1 & 8 \\
 0 & 5 & 1 & -6 & 1 \\
 0 & 0 & 1 & 0 & -3 \\
 0 & 0 & 0 & 1 & 1
 \end{array}
 \end{array}$$

$$\begin{array}{l}
 E24(6) \\
 \begin{array}{rrrrr}
 -2 & 6 & -3 & -1 & 8 \\
 0 & 5 & 1 & 0 & 7 \\
 0 & 0 & 1 & 0 & -3 \\
 0 & 0 & 0 & 1 & 1
 \end{array}
 \end{array}$$

$$\begin{array}{l}
 E14(1) \\
 \begin{array}{rrrrr}
 -2 & 6 & -3 & 0 & 9 \\
 0 & 5 & 1 & 0 & 7 \\
 0 & 0 & 1 & 0 & -3 \\
 0 & 0 & 0 & 1 & 1
 \end{array}
 \end{array}$$

$$\begin{array}{l}
 E23(-1) \\
 \begin{array}{rrrrr}
 -2 & 6 & -3 & 0 & 9 \\
 0 & 5 & 0 & 0 & 10 \\
 0 & 0 & 1 & 0 & -3 \\
 0 & 0 & 0 & 1 & 1
 \end{array}
 \end{array}$$

$$\begin{array}{l}
 E13(3) \\
 \begin{array}{rrrrr}
 -2 & 6 & 0 & 0 & 0 \\
 0 & 5 & 0 & 0 & 10 \\
 0 & 0 & 1 & 0 & -3 \\
 0 & 0 & 0 & 1 & 1
 \end{array}
 \end{array}$$

$$\begin{array}{l}
 E2(1/5) \\
 \begin{array}{rrrrr}
 -2 & 6 & 0 & 0 & 0 \\
 0 & 1 & 0 & 0 & 2 \\
 0 & 0 & 1 & 0 & -3 \\
 0 & 0 & 0 & 1 & 1
 \end{array}
 \end{array}$$

$$\begin{array}{l}
 E12(-6) \\
 \begin{array}{rrrrr}
 -2 & 0 & 0 & 0 & -12 \\
 0 & 1 & 0 & 0 & 2 \\
 0 & 0 & 1 & 0 & -3 \\
 0 & 0 & 0 & 1 & 1|
 \end{array}
 \end{array}$$

$$\begin{array}{l}
 E1(-1/2) \\
 \begin{array}{rrrrr}
 1 & 0 & 0 & 0 & 6 \\
 0 & 1 & 0 & 0 & 2 \\
 0 & 0 & 1 & 0 & -3 \\
 0 & 0 & 0 & 1 & 1
 \end{array}
 \end{array}$$

c.)

$$x=6$$

$$y=2$$

$$z=-3$$

$$w=1$$

## 2 Variables / 2 Variables Augmented & Back Substitution / Gauss Jordan / Gaussian in Matlab

a.)

```
>> M(2,:) = M(2,:) * (1/2)

M =

     2     -3     1
     0      1     3

>> %E2(1/2)
>> M(2,:) = M(2,:) * (1/2)

M =

     2.0000    -3.0000     1.0000
         0     0.5000     1.5000

>> M = [2 -3 1; -4 8 4]

M =

     2     -3     1
    -4      8     4

>> %E21(2)
>> M(2,:) = M(2,:) + 2*M(1,:)

M =

     2     -3     1
     0      2     6

>> %E2(1/2)
>> M(2,:) = M(2,:) * (1/2)

M =
|
     2     -3     1
     0      1     3

>> %E12(3)
>> M(1,:) = M(1,:) + 3*M(2,:)

M =

     2      0    10
     0      1     3

>> %E1(1/2)
>> M(1,:) = M(1,:) * (1/2)

M =

     1      0     5
     0      1     3
```

b.)

```
>> M = [2 -3 5; 3 -8 4]

M =

     2     -3     5
     3     -8     4

>> %E21(2)
>> M(2,:) = M(2,:) - (3/2)*M(1,:)

M =
|
     2.0000    -3.0000     5.0000
         0    -3.5000    -3.5000

>> %E2(1/2)
>> M(2,:) = M(2,:) * (-1/3.5)

M =

     2     -3     5
     0      1      1

>> %E12(3)
>> M(1,:) = M(1,:) + 3*M(2,:)

M =

     2      0      8
     0      1      1

>> %E1(1/2)
>> M(1,:) = M(1,:) * (1/2)

M =

     1      0      4
     0      1      1

x >> |
```

5.)

```
>> M=[-2 6 -3 -1 8;0 5 1 -6 1;0 0 1 5 2;0 0 0 4 4]
```

```
M =
```

```

-2    6    -3    -1    8
 0    5     1   -6     1
 0     0     1    5     2
 0     0     0    4     4

```

```
>> %E4(1/4)
```

```
>> M(4,:)=M(4,:)*(1/4)
```

```
M =
```

```

-2    6    -3    -1    8
 0    5     1   -6     1
 0     0     1    5     2
 0     0     0    1     1

```

```
>> %E34(-5)
```

```
>> M(3,:)=M(3,:)-5*M(4,:)
```

```
M =
```

```

-2    6    -3    -1    8
 0    5     1   -6     1
 0     0     1    0   -3
 0     0     0    1     1

```

```
>> %E24(6)
```

```
>> M(2,:)=M(2,:)+6*M(4,:)
```

```
M =
```

```

-2    6    -3    -1    8
 0    5     1    0     7
 0     0     1    0   -3
 0     0     0    1     1

```

```
>> %E14(1)
```

```
>> M(1,:)=M(1,:)+1*M(4,:)
```

```
M =
```

```

-2    6    -3     0     9
 0    5     1     0     7
 0     0     1     0   -3
 0     0     0     1     1

```

```
>> %E23(-1)
```

```
>> M(2,:)=M(2,:)-1*M(3,:)
```

```
M =
```

```

-2    6    -3     0     9
 0    5     0     0    10
 0     0     1     0   -3
 0     0     0     1     1

```

```
>> %E13(3)
```

```
>> M(1,:)=M(1,:)+3*M(3,:)
```

```
M =
```

```

-2    6     0     0     0
 0    5     0     0    10
 0     0     1     0   -3
 0     0     0     1     1

```

```
>> %E2(1/5)
```

```
>> M(2,:)=M(2,:)*(1/5)
```

```
M =
```

```

-2    6     0     0     0
 0     1     0     0     2
 0     0     1     0   -3
 0     0     0     1     1

```

```
>> %E12(-6)
```

```
>> M(1,:)=M(1,:)-6*M(2,:)
```

```
M =
```

```

-2     0     0     0   -12
 0     1     0     0     2
 0     0     1     0   -3
 0     0     0     1     1

```

```
>> %E1(-1/2)
```

```
>> M(1,:)=M(1,:)*(-1/2)
```

```
M =
```

```

 1     0     0     0     6
 0     1     0     0     2
 0     0     1     0   -3
 0     0     0     1     1

```