

Discussion 07: Orders of Growth and Trees

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Agenda

1. Orders of Growth (OOG)
2. Trees (skip slides)

Announcements

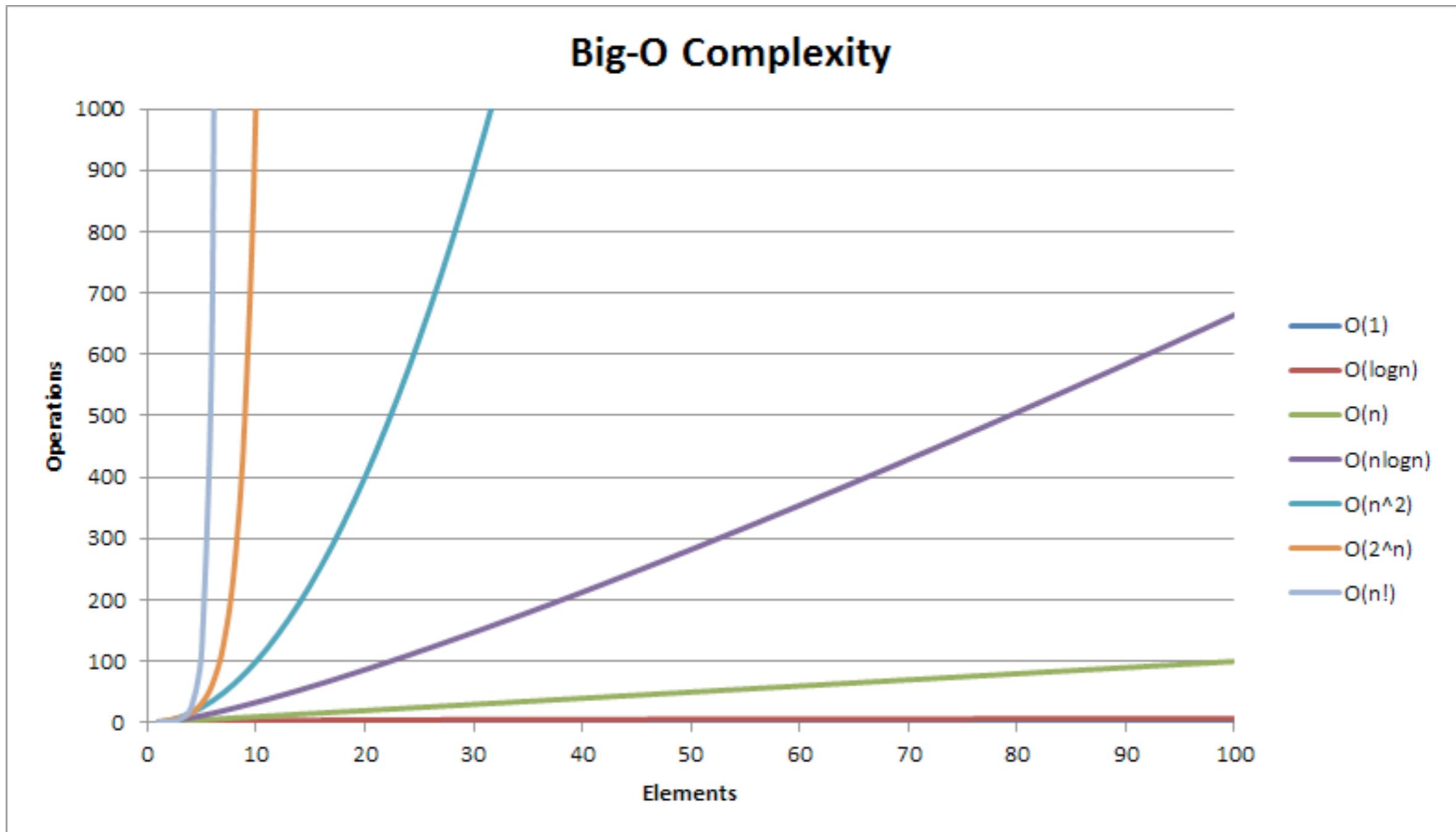
Midterm 2 **Wed 3/15 8-10pm**. Conflict form emailed out, fill out by this Friday!

Guerrilla section **Sat 12-3pm in 247 Cory** OOP + Inheritance + Orders of Growth

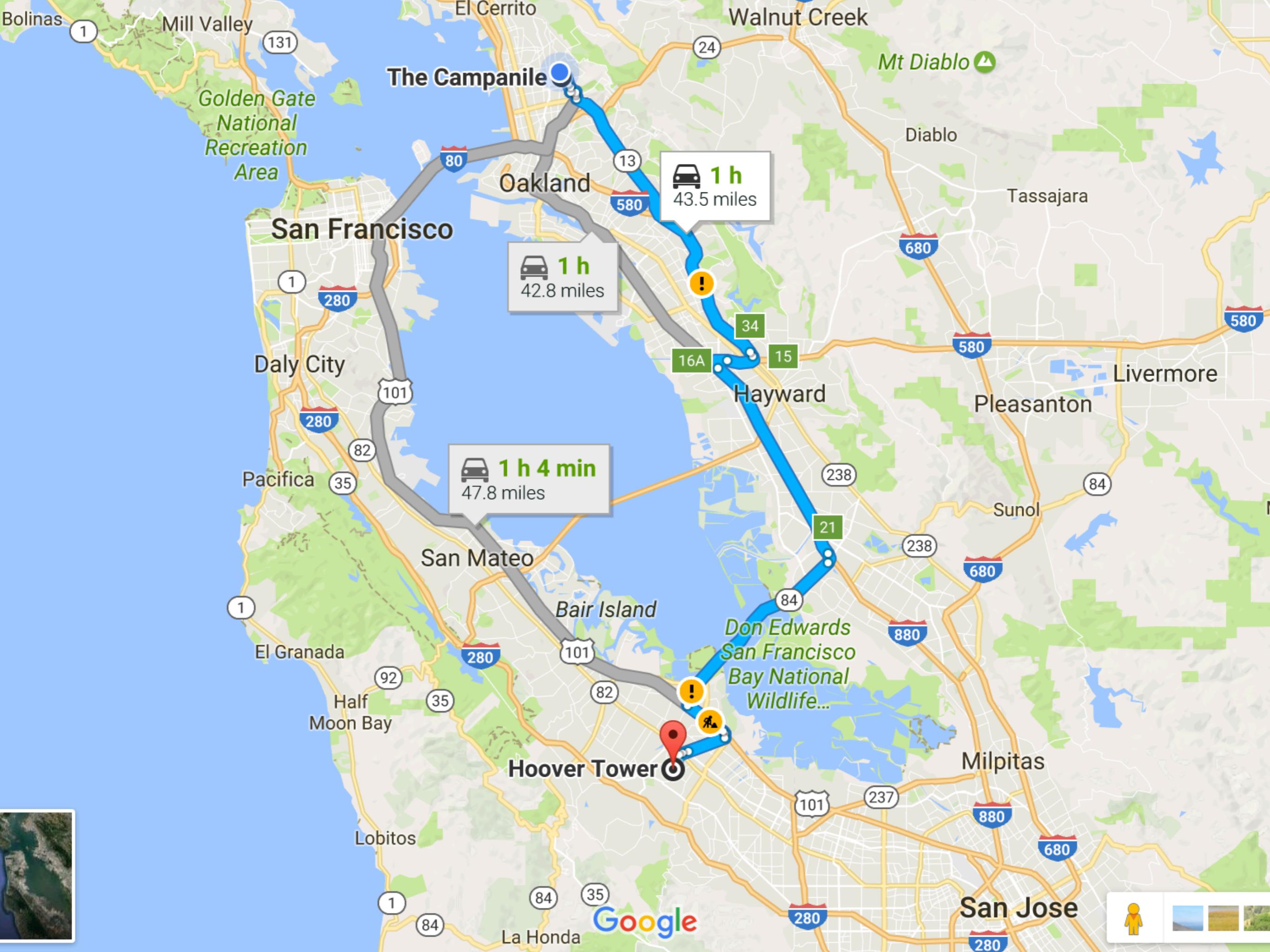
Homework 05 due Monday

- Homework party 6:30-8:30pm

Orders of Growth



<http://bigocheatsheet.com/img/big-o-complexity.png>



Orders of Growth

Why do we care?

In the news



[Google's DeepMind defeats legendary Go player Lee Se-dol in historic victory](#)

[The Verge](#) - 1 day ago

DeepMind founder Demis Hassabis expressed "huge respect for Lee Se-dol and his ..."

[Match 1 - Google DeepMind Challenge Match: Lee Sedol vs AlphaGo](#)

[YouTube](#) - 1 day ago

[Google's Deepmind AI beats Go world champion in first match](#)

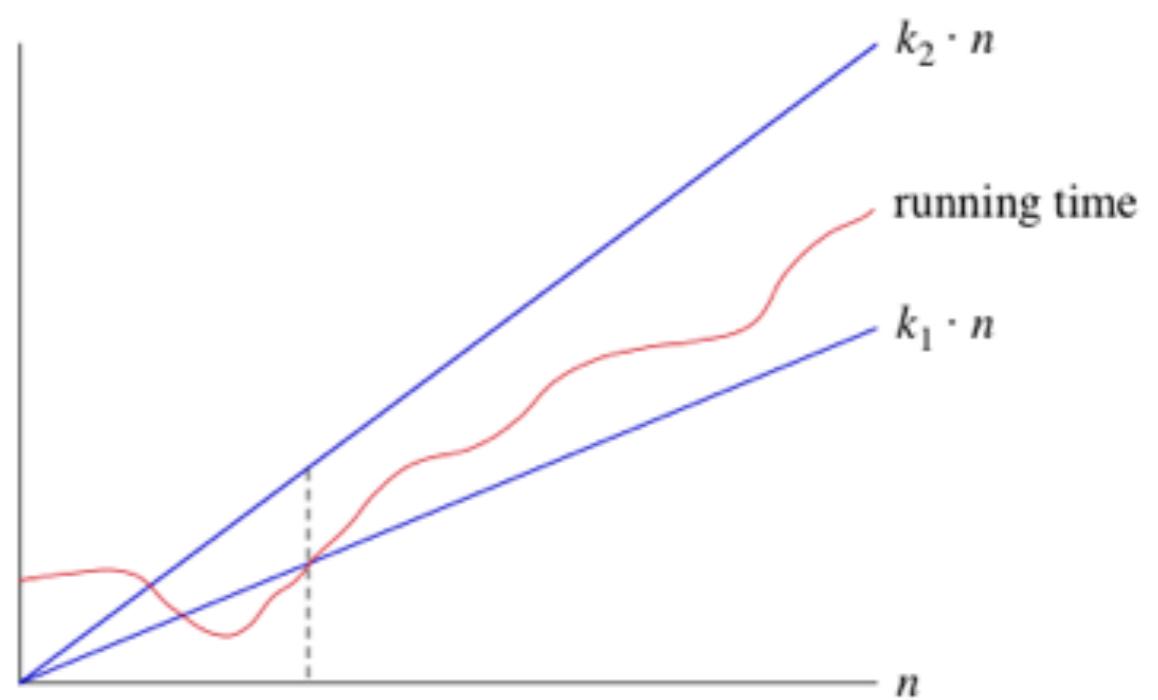
[Engadget](#) - 23 hours ago

[More news for deepmind](#)

Orders of Growth

How do we describe how fast a program is?

Orders of growth — "as input size changes, how does run time?"



Orders of Growth

Time (μsec) for problem size N	1 second	Max N Possible in 1 hour	1 month	1 century
$\lg N$	10^{300000}	$10^{1000000000}$	$10^{8 \cdot 10^{11}}$	$10^{9 \cdot 10^{14}}$
N	10^6	$3.6 \cdot 10^9$	$2.7 \cdot 10^{12}$	$3.2 \cdot 10^{15}$
$N \lg N$	63000	$1.3 \cdot 10^8$	$7.4 \cdot 10^{10}$	$6.9 \cdot 10^{13}$
N^2	1000	60000	$1.6 \cdot 10^6$	$5.6 \cdot 10^7$
N^3	100	1500	14000	150000
2^N	20	32	41	51

Orders of Growth

Simplify

Answer

$$\Theta(3n)$$

$\Theta(n)$ — ignore const factors

$$\Theta(n^3 + 1000n^2)$$

$\Theta(n^3)$ — larger term dominates

$$\Theta(\log n + n)$$

$\Theta(n)$ — larger term dominates

$$\Theta(n \log n + n)$$

$\Theta(n \log n)$ — larger term dominates

Caveat — **these are NOT mathematically precise ways of describing growth relationships!

Just for "Fun"

Question**

$$\Theta(\log_2 n) > \Theta(\log_{10} n)$$

Answer

No — Use change of base formula.

$$\Theta(n \log(n^8)) > \Theta(n^2 \log(n^3))$$

No — use log rules to get $\Theta(n \log n)$ vs $\Theta(n^2 \log n)$

$$\Theta(n \log n) < \Theta((\log n)^{\log n})$$

Yes — RHS is $n^{\log \log n}$. Or take log of both sides.

Trees

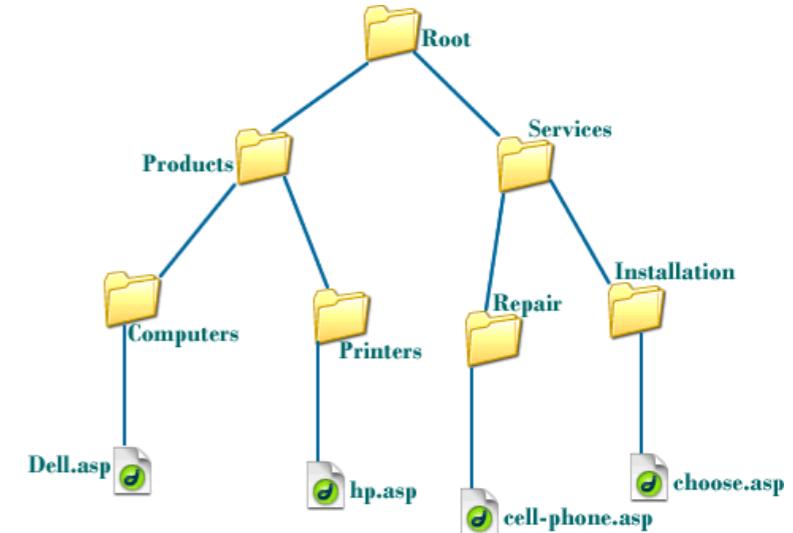


Trees

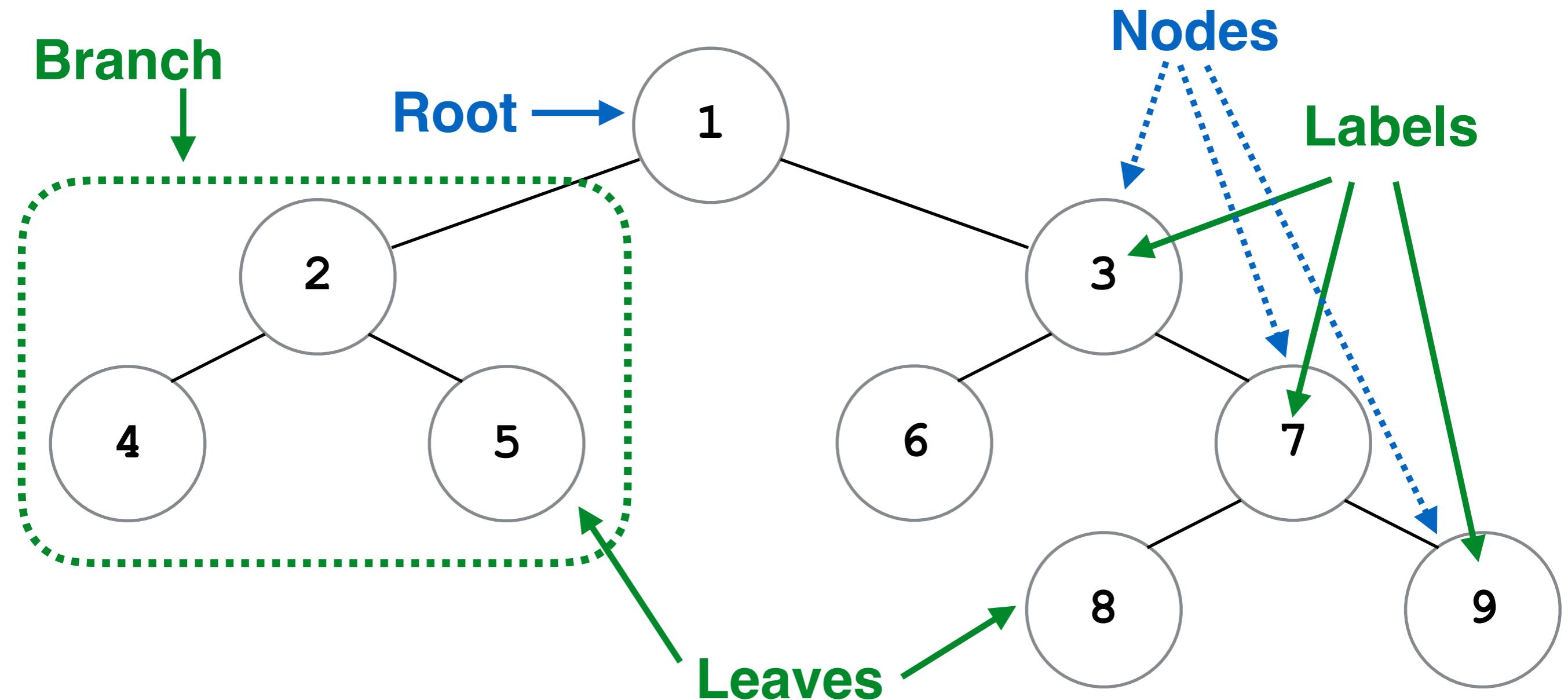
Storing things in order like a list is boring...

In real life, you **see trees everywhere!**

- Taking notes
- Directory structure on your computer
- Nature and stuff, I guess



Trees



Trees (OOP)

Constructor:

```
Tree(label, branches=[])
```

Selectors:

```
t.label, t.branches, t.is_leaf()
```

Trees (OOP)

Can now also modify labels (and branches)!