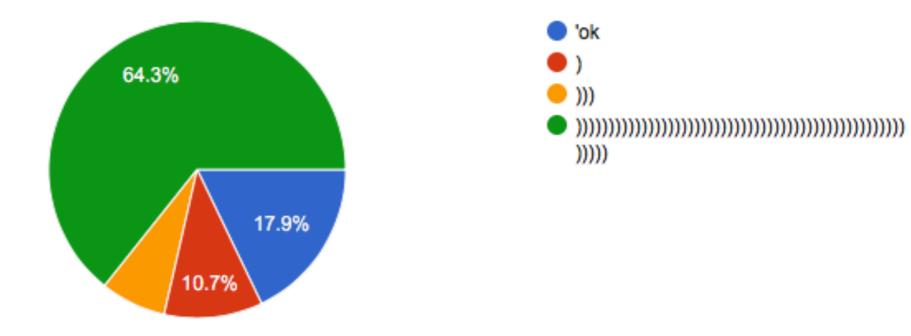
#8 Interpreters and Tail Calls

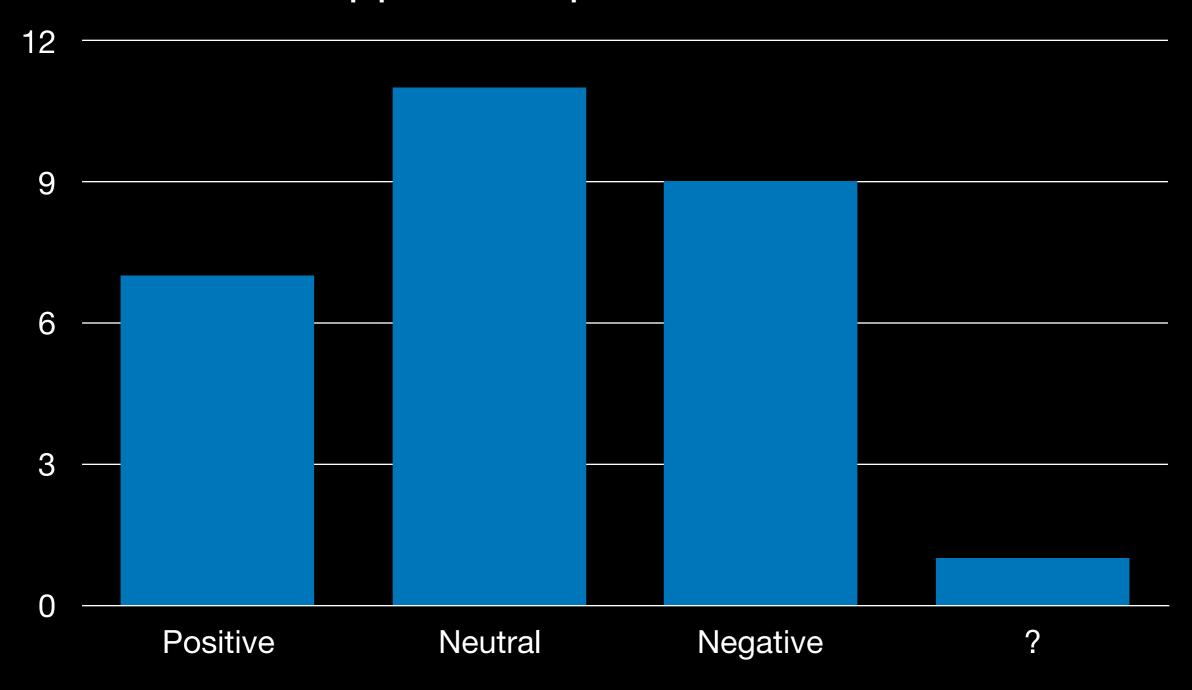
TA: Jerry Chen (jerry.c@berkeley.edu)

How do you actually feel about Scheme?

28 responses



Approx Response Sentiment



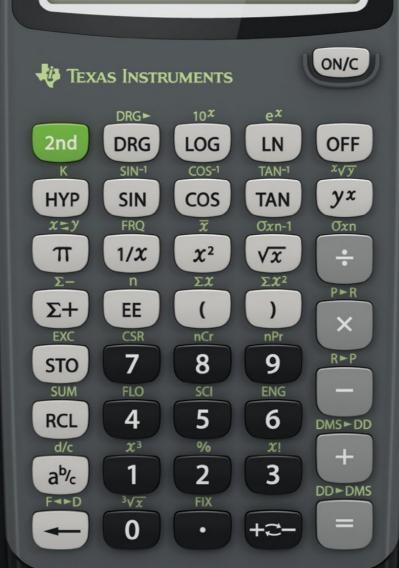
Why Scheme?

A desperate last ditch attempt to interest you

- A different way of approaching programs
- Programs as data

TI-**30X**a

123456789099





The humble Calculator language

Because algebra is all we need

- Good ol' fashioned arithmetic
- Our favorite Polish prefix notation
- Short circuiting boolean expressions

The humble Calculator language

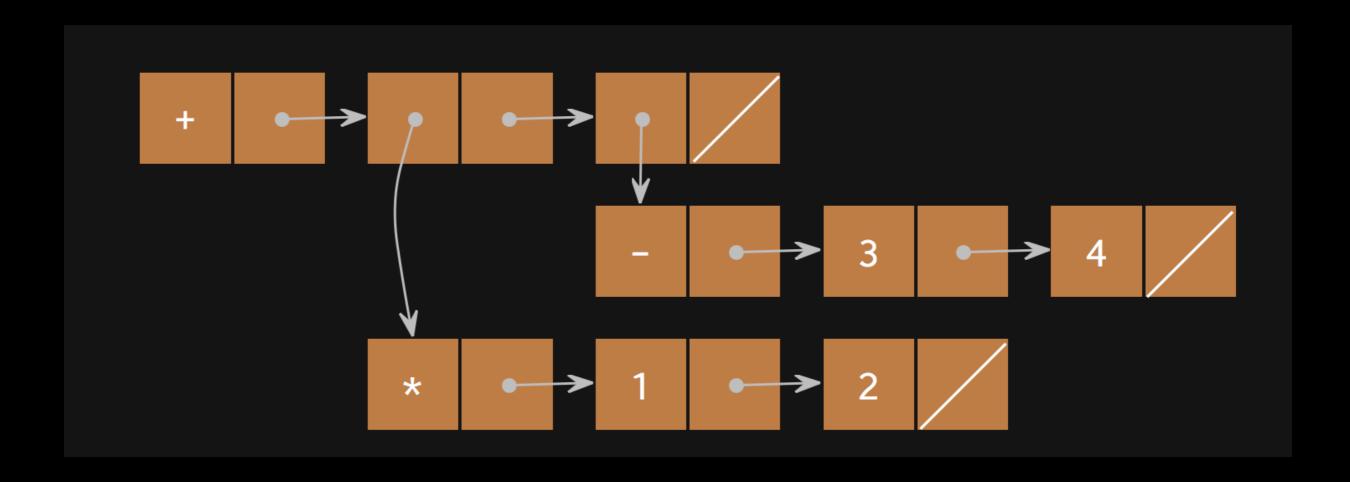
Transforming an expression

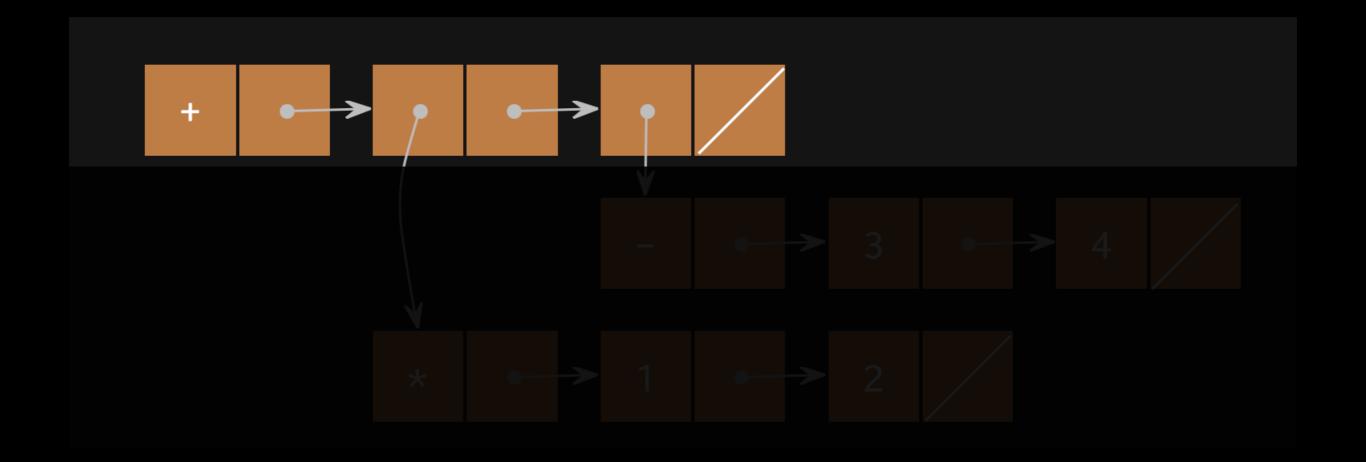
```
> (+ (* 1 2) (- 3 4))
1
```

The humble Calculator language

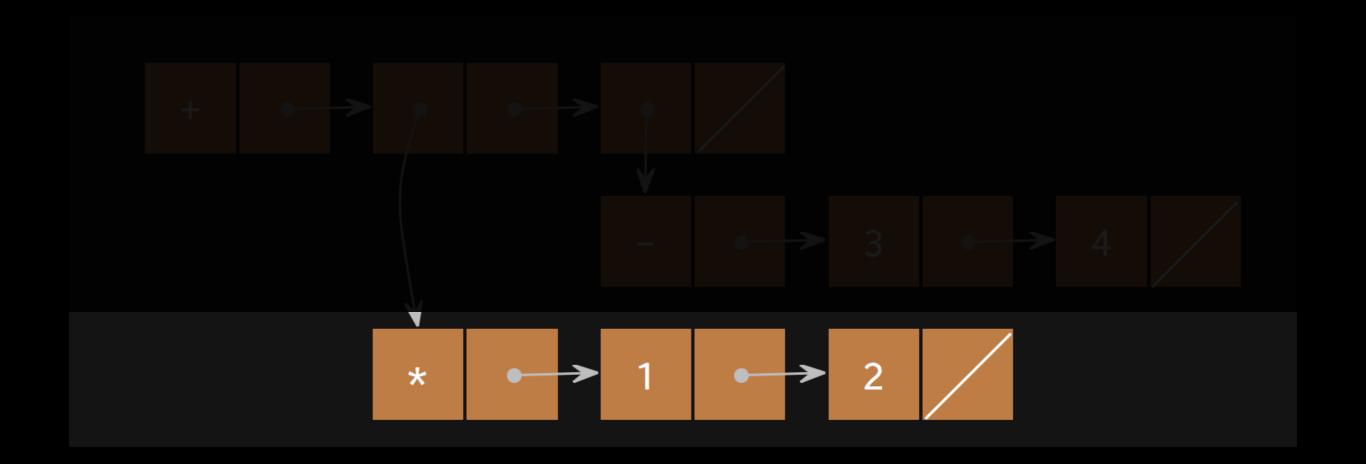
Transforming an expression

(+ (* 1 2) (- 3 4))

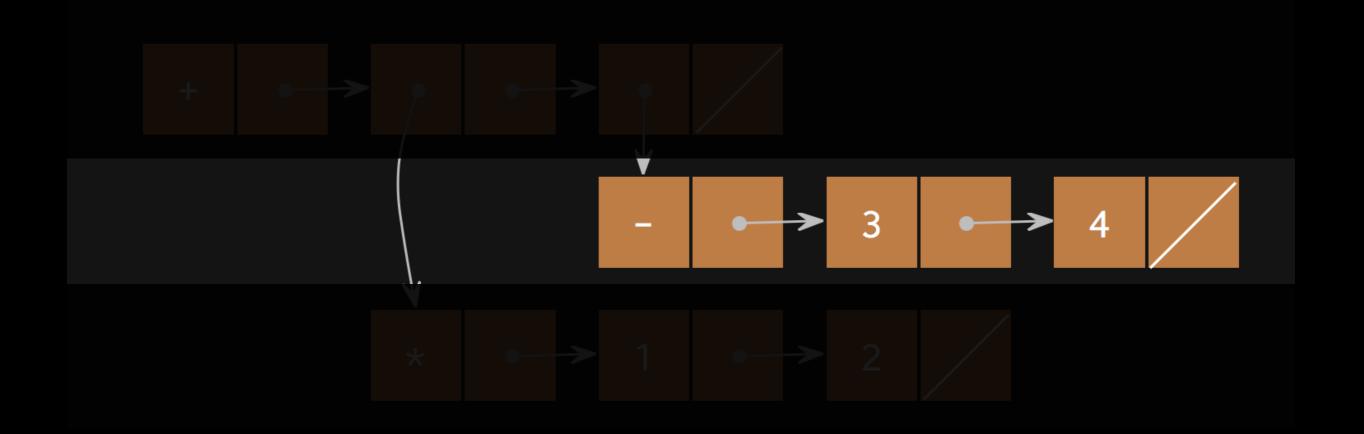




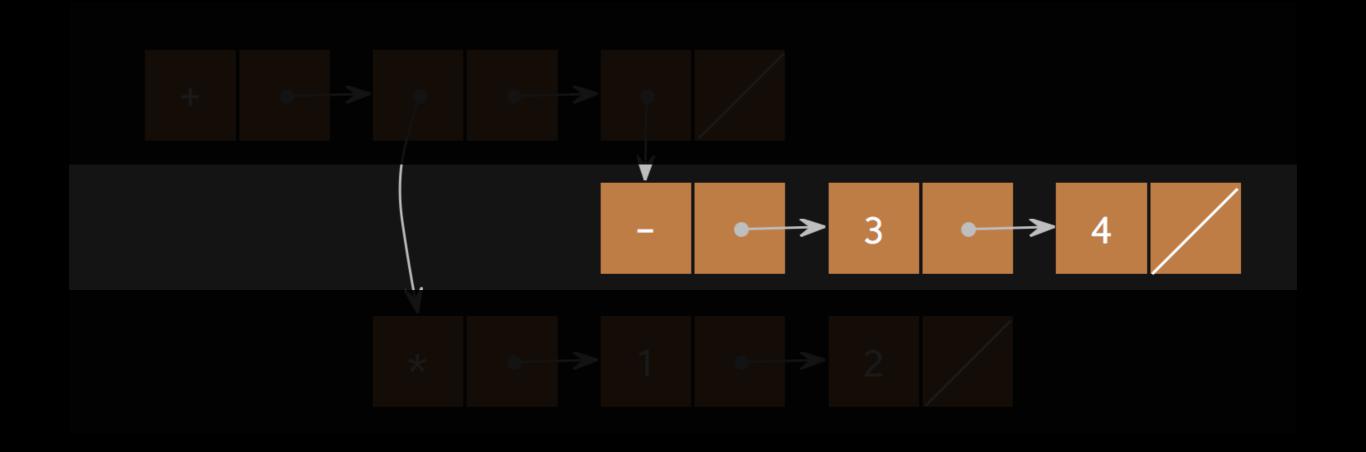
Pair('+', Pair(a, Pair(b, nil)))



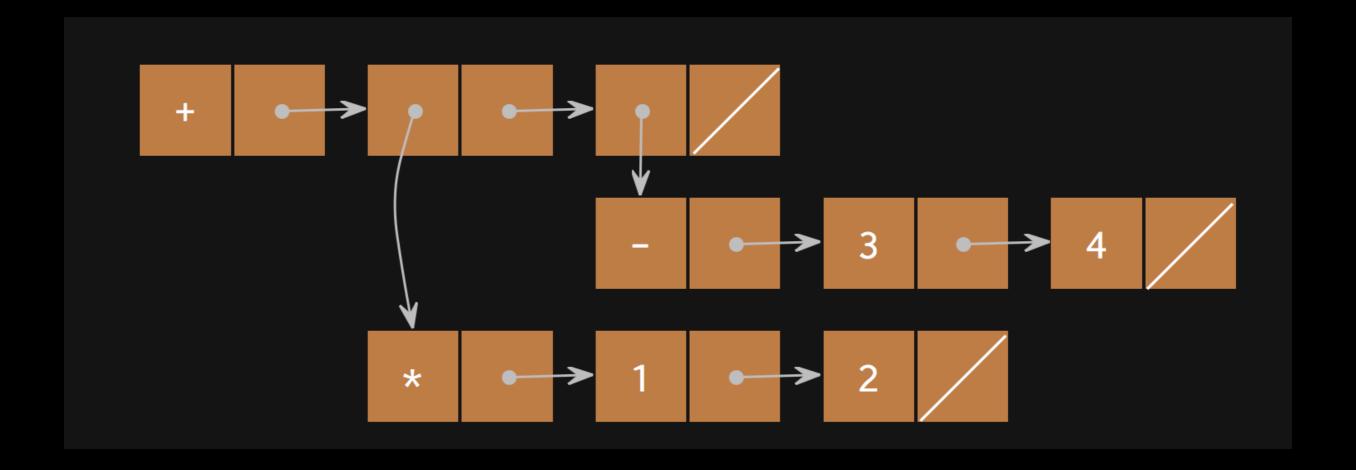
```
Pair('+', Pair(a, Pair(b, nil)))
a = Pair('*', Pair(1, Pair(2, nil)))
```



```
Pair('+', Pair(a, Pair(b, nil)))
a = Pair('*', Pair(1, Pair(2, nil)))
b = Pair('-', Pair(3, Pair(4, nil)))
```



```
Pair('+',
Pair(a,
Pair(b,
nil)))
a = Pair('*', Pair(1, Pair(2, nil)))
b = Pair('-', Pair(3, Pair(4, nil)))
```



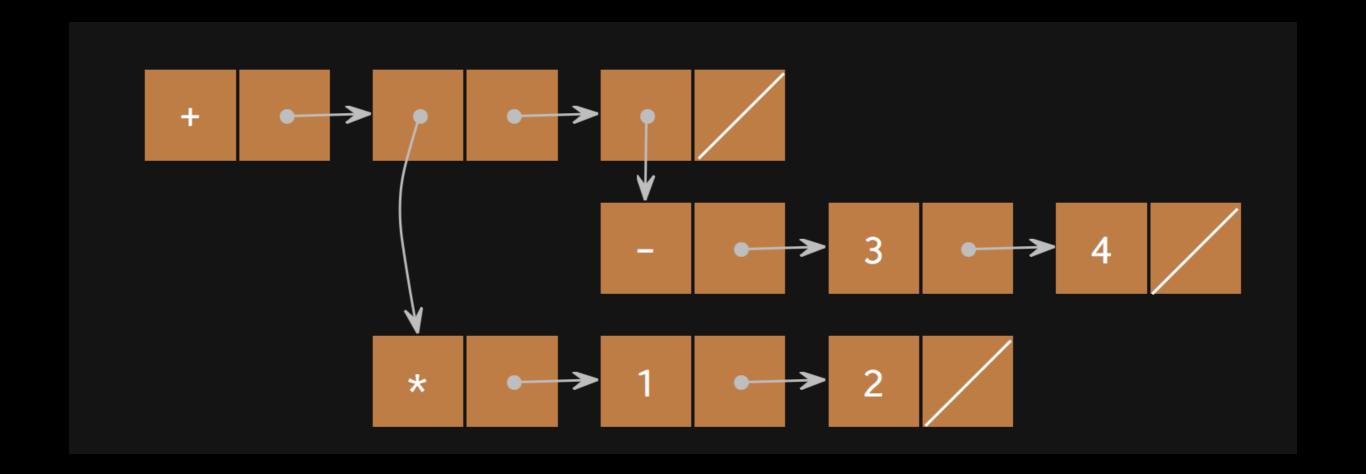
```
Pair('+',
Pair(Pair('*', Pair(1, Pair(2, nil))),
Pair(Pair('-', Pair(3, Pair(4, nil))),
nil)))
a =
b =
```

Calculator Evaluation

Putting our Pair to good use

- Evaluate the operator
- Evaluate the operands
- Apply the operator to the operands

```
1 def calc_eval(exp):
      if isinstance(exp, Pair):
2
          return calc_apply(
3
                   calc_eval(exp.first),
4
                   list(exp.second.map(calc_eval)))
5
      elif exp in OPERATORS:
6
7
          return OPERATORS[exp]
      else: # Primitive expression
8
          return exp
```



```
Pair('+',
Pair(Pair('*', Pair(1, Pair(2, nil))),
Pair(Pair('-', Pair(3, Pair(4, nil))),
nil)))
```

Operators (like '+') and primitives (like 3.1416)

How did we get here?

Started with an expression:

```
> (+ (* 1 2) (- 3 4))
```

Converted to a pair representation:

Used evaluation rules to obtain result:

- Life is about trade offs*
- Recursive calls => non constant space**
- Tail recursive calls => constant space***

^{*} and disclaimers

^{**} usually

^{***} only if you put in the work

Necessary conditions

- Tail context the "last thing" you do in an expression
- Tail call a recursive call in a tail context
- Constant number of frames if all recursive calls are tail
 calls
 - If you depend on other non tail-recursive functions, this might not be sufficient

Valid tail contexts

```
1 (define (fact n)
2  (if (= n 0)
3     1
4     (* n (fact (- n 1)))))
```

Valid tail contexts

Valid tail contexts

More space efficient fact

```
1 (define (fact n)
2  (define (fact-tail n result)
3    (if (= n 0)
4     result
5     (fact-tail (- n 1) (* n result))))
6  (fact-tail n 1))
```

More space efficient fact

More space efficient fact

```
1 (define (fact n)
2 (define (fact-tail n result)
3
     (if (= n 0))
       result
       (fact-tail (- n 1)
5
                  (* n result))))
6
7 (fact-tail n 1))
1 def fact(n):
     result = 1
2
     while n > 0:
3
         n, result = n - 1, result * n
4
5 return result
```

Thanks to Kavi Gupta for this visualization idea

```
1 (define (fact n)
   (define (fact-tail n result)
      (if (= n 0)
3
       result
       (fact-tail (- n 1)
5
                  (* n result))))
6
    (fact-tail n 1))
 def fact(n):
     result = 1
2
while n > 0:
          n, result = n - 1, result * n
4
     return result
5
```

Thanks to Kavi Gupta for this visualization idea