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## âââââââââââââ
   ⢠Learning objectives:
##
      ⢠Learn the R formula interface
      ⢠Specify factor contrasts to test specific hypotheses
##
      ⢠Perform model comparisons
##
      \hat{a}^{\, \boldsymbol{\varsigma}} Run and interpret variety of regression models in R
## Set working directory
## âââââââââââââââââââââ
    It is often helpful to start your R session by setting your working
    directory so you don't have to type the full path names to your data
##
    and other files
# set the working directory
# setwd("~/Desktop/Rstatistics")
# setwd("C:/Users/dataclass/Desktop/Rstatistics")
    You might also start by listing the files in your working directory
getwd() # where am I?
list.files("dataSets") # files in the dataSets folder
## Load the states data
## ââââââââââââââââââââââ
# read the states data
states.data <- readRDS("dataSets/states.rds")</pre>
#get labels
states.info <- data.frame(attributes(states.data)[c("names", "var.labels")])</pre>
#look at last few labels
tail(states.info, 8)
## Linear regression
## ââââââââââââââââââ
## Examine the data before fitting models
Start by examining the data to check for problems.
# summary of expense and csat columns, all rows
sts.ex.sat <- subset(states.data, select = c("expense", "csat"))</pre>
summary(sts.ex.sat)
# correlation between expense and csat
cor(sts.ex.sat)
## Plot the data before fitting models
Plot the data to look for multivariate outliers, non-linear
    relationships etc.
##
# scatter plot of expense vs csat
plot(sts.ex.sat)
## Linear regression example
## âââââââââââââââââââââââââââââââââ
    \hat{a}¢ Linear regression models can be fit with the `lm()' function
    ⢠For example, we can use `lm' to predict SAT scores based on
##
      per-pupal expenditures:
# Fit our regression model
sat.mod <- lm(csat ~ expense, # regression formula</pre>
             data=states.data) # data set
# Summarize and print the results
summary(sat.mod) # show regression coefficients table
## Why is the association between expense and SAT scores /negative/?
Many people find it surprising that the per-capita expenditure on
    students is negatively related to SAT scores. The beauty of multiple
##
    regression is that we can try to pull these apart. What would the
    association between expense and SAT scores be if there were no
##
##
    difference among the states in the percentage of students taking the
summary(lm(csat ~ expense + percent, data = states.data))
## The lm class and methods
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Introduction

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OK, we fit our model. Now what?
    ⢠Examine the model object:
class(sat.mod)
names(sat.mod)
methods(class = class(sat.mod))[1:9]
    ⢠Use function methods to get more information about the fit
confint(sat.mod)
# hist(residuals(sat.mod))
## Linear Regression Assumptions
⢠Ordinary least squares regression relies on several assumptions,
      including that the residuals are normally distributed and
##
      homoscedastic, the errors are independent and the relationships are
##
##
    ⢠Investigate these assumptions visually by plotting your model:
par(mar = c(4, 4, 2, 2), mfrow = c(1, 2)) #optional
plot(sat.mod, which = c(1, 2)) # "which" argument optional
## Comparing models
## ââââââââââââââââââââ
    Do congressional voting patterns predict SAT scores over and above
    expense? Fit two models and compare them:
# fit another model, adding house and senate as predictors
sat.voting.mod <- lm(csat ~ expense + house + senate,</pre>
                    data = na.omit(states.data))
sat.mod <- update(sat.mod, data=na.omit(states.data))</pre>
# compare using the anova() function
anova(sat.mod, sat.voting.mod)
coef(summary(sat.voting.mod))
## Exercise: least squares regression
Use the /states.rds/ data set. Fit a model predicting energy consumed
##
##
    per capita (energy) from the percentage of residents living in
    metropolitan areas (metro). Be sure to
##
    1. Examine/plot the data before fitting the model
    2. Print and interpret the model `summary'
    3. `plot' the model to look for deviations from modeling assumptions
##
    Select one or more additional predictors to add to your model and
##
    repeat steps 1-3. Is this model significantly better than the model
    with /metro/ as the only predictor?
## Interactions and factors
## Modeling interactions
##
    Interactions allow us assess the extent to which the association
    between one predictor and the outcome depends on a second predictor.
##
    For example: Does the association between expense and SAT scores
    depend on the median income in the state?
  #Add the interaction to the model
sat.expense.by.percent <- lm(csat ~ expense*income,</pre>
                           data=states.data)
#Show the results
  coef(summary(sat.expense.by.percent)) # show regression coefficients table
## Regression with categorical predictors
Let's try to predict SAT scores from region, a categorical variable.
    Note that you must make sure R does not think your categorical
##
    variable is numeric.
# make sure R knows region is categorical
str(states.data$region)
states.data$region <- factor(states.data$region)</pre>
\# Add region to the model
sat.region <- lm(csat ~ region,</pre>
               data=states.data)
#Show the results
```

anova(sat.region) # show ANOVA table Again, *make sure to tell R which variables are categorical by converting them to factors!* ## Setting factor reference groups and contrasts In the previous example we use the default contrasts for region. The default in R is treatment contrasts, with the first level as the $% \left(1\right) =\left(1\right) \left(1\right) \left($ ## ## reference. We can change the reference group or use another coding ## scheme using the `C' function. # print default contrasts contrasts(states.data\$region) # change the reference group coef(summary(lm(csat ~ C(region, base=4), data=states.data))) # change the coding scheme coef(summary(lm(csat ~ C(region, contr.helmert), data=states.data))) See also `?contrasts', `?contr.treatment', and `?relevel'. ## Exercise: interactions and factors Use the states data set. ## 1. Add on to the regression equation that you created in exercise 1 by generating an interaction term and testing the interaction. ## ## 2. Try adding region to the model. Are there significant differences

##

across the four regions?

coef(summary(sat.region)) # show regression coefficients table