PartIR

Declarative abstractions for tensor program partitioning

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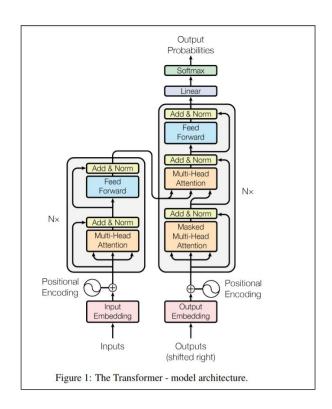
PPDP'20, September 2020



An invited talk about work-in-progress?!?

What is a machine learning model?

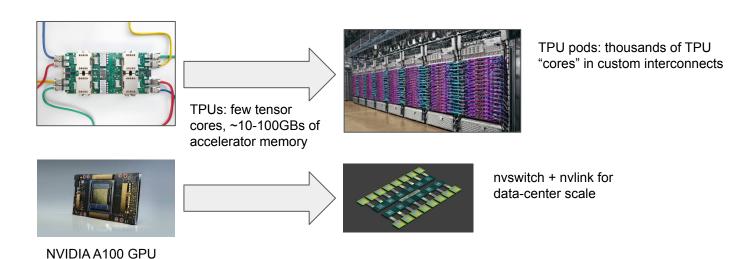
- Typically "beefy" multi-dimensional array programs: tensor programs
- Accept inputs and parameters:
 - Wild variation on input batch size, input spatial dimensions, and parameter size
- Parameters + compute grow:
 - o GPT-3 is a 175B param transformer model
- Ever-growing body of work to reduce parameters and compute:
 - Exploit sparsity [not the topic of this talk]
 - Novel ways to partition these tensor programs to exploit parallelism and make them fit memory constraints



Machine learning hardware: from tensor cores to systems

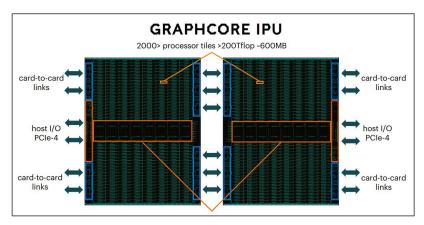
Cannot run a model with 175B parameters on a single machine!

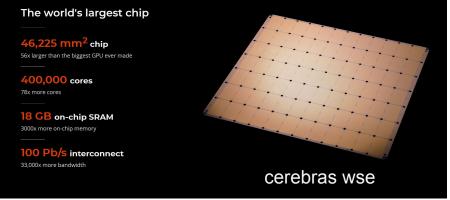
Accelerator trend for scaling: chips => systems of multiple chips => data-centers



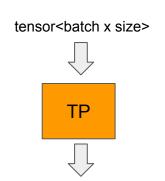
Accelerator scaling trend: lots of wimpy cores

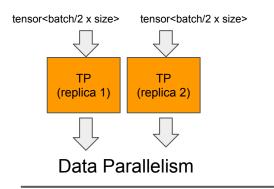
New and cheaper ways to scale compute and memory than monolithic MXU cores

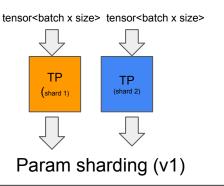




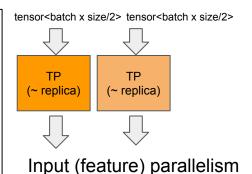
Multiple ways to partition a tensor program

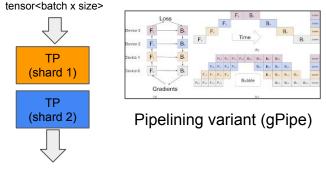






- Partitioning a model is a program transformation
- Often need to additionally mix-and match different forms in the same model
- Beyond Data and Model Parallelism for Deep Neural Networks, SysML'19





Param sharding (v2)

Sounds simple? Still SW in a BAD place for partitioning

- We use data parallelism to reduce input (activation) sizes and scale the available compute flops, assuming model parameters fit on available cores
 - OK for TPUs and small models (~ 8-32GB/core), but new hardware may come with few GBs per device (e.g. Graphcore IPU). How does one map a large transformer model?
- We bake in system assumptions in library code
 - Typically batch parallelism, no model parallelism
- Engineering years on specialized partitions (papers: Megatron, gPipe).
 - New partitioning strategy ~> new research paper!
- System design: manual back-of-the-envelope-calculations for mapping models on new systems. Hard to support a mixture of partitioning strategies

THIS IS MADNESS!!!!!

PartIR aspiration: generic partitioning compiler infra

PartIR offers:

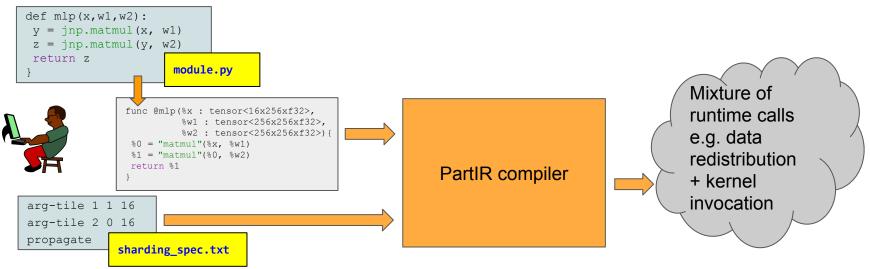
- Declarative abstractions to express partitioned models on accelerator systems
- Declarative transformation rules for partitioning actions and fusion
- Vision: driven by <u>sharding annotations</u>, or <u>interactive tactics</u>, or <u>search + RL</u> (non-exclusive)

Other features:

- POC lowering pass to dataflow graphs of SPMD ops (beyond a single SPMD op)
- Solves the "tiling-on-tensors" problem i.e. a functional specification of tiling
- Useful to explain semantics of related efforts (e.g. XLA sharding propagation, Mesh TF); eventually may increase expressivity (e.g. dataflow and control flow of SPMD ops, pipeline parallelism)
- Close relatives: <u>Dex</u>, <u>Linalg</u>, <u>F-smooth</u> [ICFP'19]
- Relies on some existing tensor op backend compiler and runtime

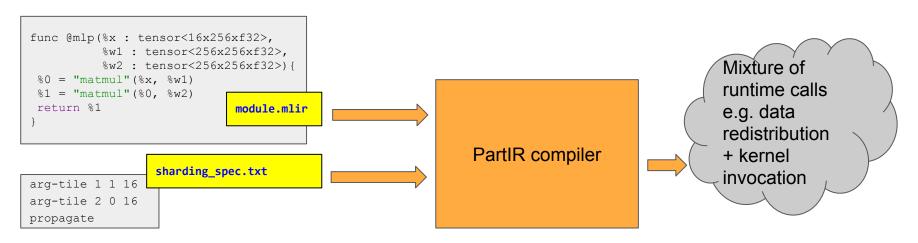
PartIR value; for ML researchers

Reusable math-focused (vs. systems-focused) ML libraries



PartIR value; for compiler infrastructure teams

Reusable partitioning compiler infra; across tensor dialects, different systems of accelerators

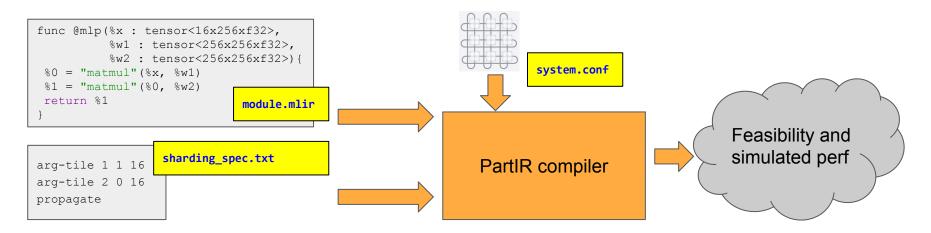


Do not invent a new IR from scratch: we have mature tensor IRs for different needs (e.g. XLA, LinAlg), need common infra to partition across accelerator systems. PartIR is just a generic partitioning framework on top: *it relies on a backend compiler and a runtime, for a given target (e.g. XLA for TPUs)*

PartIR value; to speed up systems design

Systems Design questions: what if 2x memory/core? 2x cores with ½ mem? 2x faster mesh? 2x FLOPS/sec/core?

How can we quickly experiment with partitioning and mapping important models in different ways? At the moment it's months of engineering time but a ton of boilerplate.



A technical tour of PartIR

PartIR sits on top of some other tensor dialect, e.g. XLA:

- Using the MLIR (multi-level IR, https://mlir.llvm.org/) framework this is technically easy to express
- MLIR is infrastructure for representing multiple IRs (*dialects*). Allows programs to span operators from different dialects and features generic binding trees facilities, generic representations of modules, functions, SSA blocks, rewriting APIs, an extensible type system and more
- XLA is a dialect in MLIR and PartIR simply adds a few constructs as a separate dialect

PartIR constructs:

- A range type (partir.range) whose values represent contiguous non-overlapping intervals
- 3 operators specific to partitioning:
 - An op to slice a dimension (partir.slice)
 - An op to tile a dimension (partir.tile)
 - An op to do a tiled reduction (partir.sum)

Not discussed today: a handful of extra operators that allow tensor *building* (as opposed to *partitioning*): out of scope for today's talk, but very useful for e.g. Dex. Such operators were first introduced in the F-smooth paper.

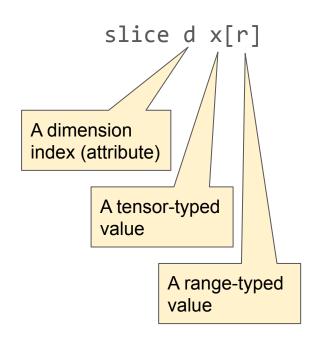
PartIR range type and its values: range<n,w>

A range type $\frac{\text{range} < n_{\text{JW}}}{\text{range}}$ denotes the set of contiguous non-overlapping intervals of a range n, each interval being of width w.

- Assume (x:range<16,8>). Then x is one of: [0..8), [8..16)
- Non-overlapped and perfectly divisible, for now. (n `mod` w == 0)
- We can nest ranges in a monoid fashion (will skip for this talk)

PartIR constructs: slicing a dimension with a range value

Key idea: use range values directly in slicing



x : tensor<64x32x64xf32>

r: range < 64,4 >

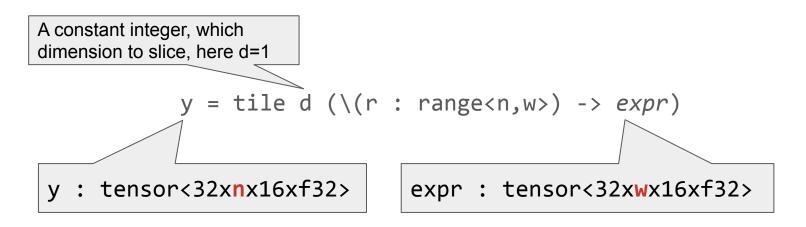
slice $0 \times [r]$: tensor< $4\times32\times64\timesf32$ >

slice 1 x[r] : TYPE-ERROR

slice $2 \times [r]$: tensor<64x32x4xf32>

PartIR constructs: tiling a dimension with a range

PartIR introduces a higher-order loop-like expression for this:



Semantics: a generator expression for the slices of a bigger array. It can be given either parallel or sequential semantics (depends on lowering)

PartIR constructs: reductions

A similar higher-order operator:



Semantics: sum together all the <32x16xf32> chunks to a single tensor of the same shape. Can be implemented with all-reduce in a distributed setting (see later)

Partitioning = progressive application of rewrite rules

```
x : tensor<nxmxf32>, y : tensor<mxoxf32>
matmul-tile-0:
    matmul(x, y) <~~> tile 0 (\r:range(n,nw) -> matmul(slice 0 x[r], y))
matmul-tile-1:
    matmul(x, y) <~~> tile 1 (\r:range(o,ow) -> matmul(x, slice 1 y[r]))
matmul-sum:
    matmul(x, y) <~~>
        sum (\r:range(m,mw) -> matmul(slice 1 x[r], slice 0 y[r]))
```

- Rewrite rules preserve types and semantics
- Each tensor operator from our base dialect is equipped with annotations that inform how each dimension could be partitioned, and how this propagates to argument slicing.
- Opportunity: given the mathematical definition of an op or even a sub-program search for valid rewrites + validate through a theorem prover. Reminiscent of TASO [SOSP'19])

Producer-consumer fusion = when slice met tile

```
s : range<64,32>
fuse:
    slice 0 (tile 0 (\r:range<64,32> -> expr)[s] ~~> expr{s/r}
```

Analogous to the build-slice fusion rule from F-smooth paper [ICFP'19]

Slicing function arguments or values (aka "dumb tiling")

```
x : tensor<64x32xf32>
x <--> tile 0 (\r:range(64,4) -> slice 0 x[r])
x <--> tile 1 (\r:range(32,4) -> slice 1 x[r])
```

Propagation tactics - push slicing in

```
slice 0 (matmul(x, y))[r] ~~> matmul(slice 0 x[r], y)
slice 1 (matmul(x, y))[r] ~~> matmul(x, slice 1 y[r])
```

Intuition: do not compute a big matmul only to take a slice out of it! Instead, directly compute the slice. Also note: these are derived rules from fusion + the specialized matmul ops, but useful on their own!

Propagation tactics - pulling tiling out

Intuition: try to expose looping constructs at the top-level

But needs to be done carefully: we are pulling "y" **into** the tiling construct, hence likely to increase the local memory requirements on every compute core!

A space of user-controlled actions + propagation

-> tensor<16x256xf32> {
 %0 = partir.tile 0 (%r : !partir.range<16,8>) {
 %1 = partir.slice 0 %x[%r]
 %2 = matmul(%1, %w)
 %3 = matmul(%2, %u)
 partir.yield %3
 }
 return %0
}

arg-tile 0 0 8.



propagate.

```
arg-tile 1 1 128;
arg-tile 2 0 128;
propagate.
```

func @mlp(%x: tensor<16x256xf32>, %w: tensor<256x256xf32>, %u: tensor<256x256xf32>)

Lowering PartIR

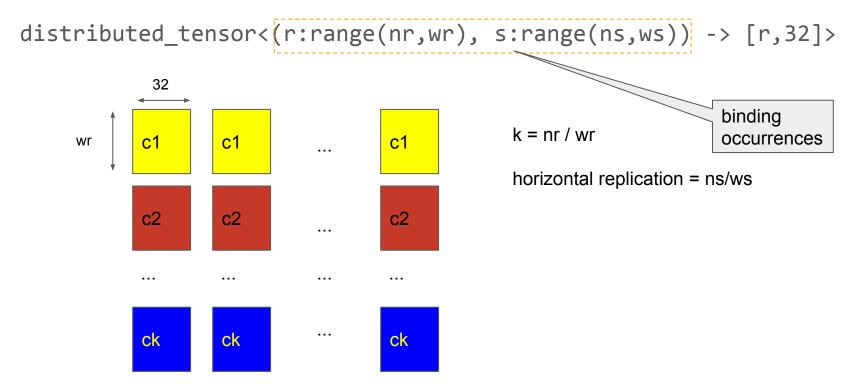
Since many accelerators offer facilities for:

- data transfers between devices and re-distribution
- SPMD-style ops across a number of available cores

we sketch out a translation of PartIR programs to such an SPMD dialect, which we call PartIR:SPMD. This entails several steps:

- Introducing the type system of PartIR:SPMD
- Introducing the ops of PartIR:SPMD
- Introducing progressive lowering to PartIR:SPMD

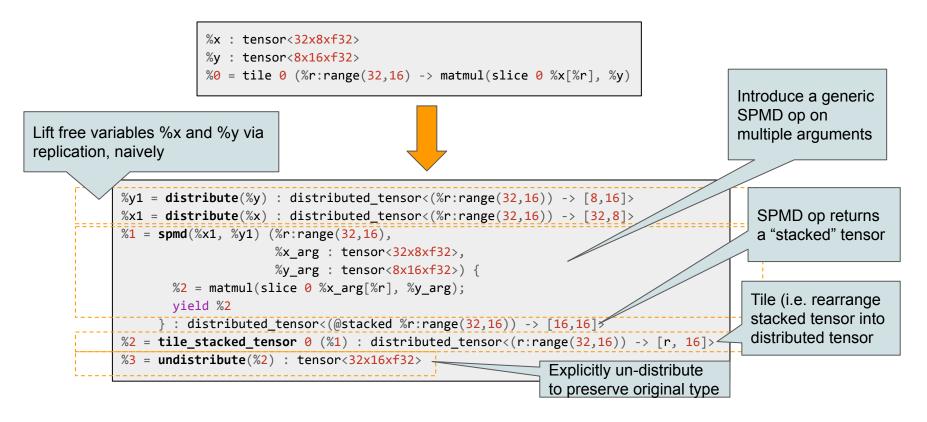
PartIR:SPMD Distributed tensor types



PartIR:SPMD Stacked tensor types

```
distributed_tensor<(r:range(nr,wr), @stacked s:range(ns,ws)) -> [r,32]>
        32
                                                   k = nr / wr
                c12
                                                   s = ns / ws
       c21
                                         Summary: distributed tensor<(rs) -> shape>
                                              Chunks = \Pi(|r.size/r.tilesize| for r in rs)
                                              stacked r ∉ rangeVars(shape) => stacking
                                              non stacked r ∉ rangeVars(shape) => replication
```

Lowering step 1: introduce SPMD op + lift free variables



Lowering step 2: transform replication to distribution

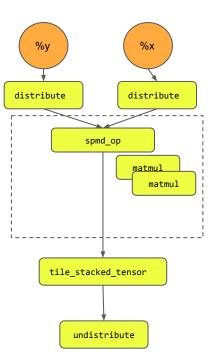


More lowering details (known and unknown)

- For translating partir.sum we introduce spmd + partir.all_reduce op
- Nested partir.tile and partir.sum
- Non-perfectly nested code inside partir.tile/partir.sum
 - Need to choose between creating distributed versions of intermediates, or inlining in inner loops and replicating computation. Expose option to programmers
- Fusion of distribution operators:
 - o undistribute(distribute[t](%x) ~> %x
 - o distribute[T](undistribute(%x) ~> %x
 when type(%x) == T
 - o distribute[τ](undistribute(%x) ~> redistribute %x
 when globalType(type(%x) == globalType(τ)

Execution

- Compile all bodies of spmd_op using the backend compiler
- Literally execute the data-flow graph using the backend runtime (must support the redistribution operators and SPMD execution)

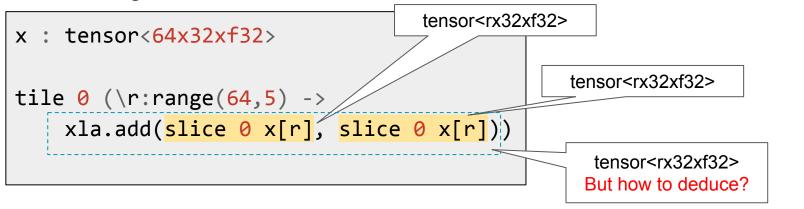


Range widths that do not divide the dimension?

I.e. let the last interval have a Proposal: use dependent types smaller width Semantics: Range(16, 5) = [0..4), [5..10), [10..15), [15,16)Introduce dependent types: **BEFORE** slice d %x[%r] : <n1, n2, ..., %r, ..., n k> Type partir.tile using dependent types: v : tensor<32xnx16xf32> x : tensor<32xwx16xf32> $%y = tile d (%r : range<n,w>) { ... stuff ... ; yield %x }$ **NOW** : tensor<32xnx16xf32> x : tensor<32x%rx16xf32>

More expressive (dependent) types annoyance

- XLA dialect only has static shape: not dependent types on range values!
- How to type check a PartIR + XLA program with dependent types?
- Solution: specialization
 - o range<32,5> has values with in-effect 2 widths: 5 and 2
 - type-check existing XLA ops for the two different assignments of widths
 - can lead to exponential blow-up for deeply nested tiles/sum, but we don't really expect a nesting level of > 2-3



An active research & engineering effort in DeepMind

- Testing strengths and weaknesses of PartIR on a set of mission-important models (XLA generated from Tensorflow or Jax high-level programs)
- Introduced "tiling specifications" for a substantial subset of of XLA ops
- Working through lowering and execution for TPU/GPU environments
- Started work on exposing the state of a partir program and an action space as a reinforcement-learning environment to tap onto the big pool of ML researchers in DeepMind. Example actions:
 - Application of a rewrite rule
 - Navigation
 - Effective inlining of a tile op inside another
 - Pushing tiling out
- Work towards approximate cost models for evaluating solutions (e.g. minimize data redistribution, subject to memory fit) and learnt cost models from data (Ithemal, [ICML'19])
- Identifying architectural modifications to MLIR pass and rewriting APIs needed for RL

What we do not know: how much declarative is enough?

- How to best express even higher-level abstractions, most notably: pipelining
- Input ("feature") partitioning when we can't exactly partition in the boundaries:
 - o halo exchanges and convolutions require extra data to be communicated
- Is a tile-based IR on top of a tensor IR already too low level? Do we need higher-level combinators -- for instance "map over data" or "map over parameters" or "pipeline"?
- How to enhance numpy-style tensor programs with PartIR concepts:
 - Expose PartIR constructs directly, let people program with those (not portable code)
 - Numpy + interactive environment to partition a program (nice but also niche!)
 - Numpy + sharding annotations on variables (a bit better but limits library usability)
 - Numpy + sharding annotations on inputs and outputs only + ML/search for intermediates?

Thank you!

- We desperately need abstractions for partitioning in our compiler stacks
 Types, Operators, Transformations
- PartIR offers a principled approach to partitioning via semantics preserving sequences of really simple transforms, rooted in deforestation and fusion ideas from declarative programming
- Great value for understanding the partitioning problem and having an executable semantics of partitioned programs
- But many things we do not know and need to learn; e.g. what has the HPC/MPI community been doing in this space?

The work is really just starting, keen to engage and collaborate!

Extra material

Notation convention: SSA vs. expressions

We use expression-based notation instead of SSA cause it's shorter.

```
tile d (\r:range<n,w> -> expr)
```

expr here can be thought of as the body of a region that yields a value.