

## Question 2

(a)

```
maxSumMemo(A, j, T):
    if(j == 0):
        return A[0]
    if(T[j] != -infinity):
        return T[j]
    prev_max = maxSumMemo(A, j - 1, T) + A[j]
    T[j] = max(prev_max, A[j])
    return T[j]

maxSum(A):
    n = A.length
    T is a table/array of length n, whose values are all initialised to -infinity
    max = maxSumMemo(A, n - 1, T)
    for(k = n - 2; k >= 0; k--):
        curr = maxSumMemo(A, k, T)
        if(curr > max):
            max = curr
    return max
```

(b)

In `maxSum()`, when `maxSumMemo()` is called for the first time outside the for-loop, it recursively iterates through all  $n$  entries of  $A$ , filling up the table  $T$  with their maximum subarray sums. This takes  $n$  steps.

Then in `maxSum()`, the for-loop iterates approximately  $n$  times, calling `maxSumMemo()` each time. However, this time `maxSumMemo()` will only take a fixed number of steps, since the table  $T$  has already been filled out. So, the for-loop takes  $n$  steps.

So, the number of steps is approximately  $n + n$ . Which is a  $\Theta(n)$  cost.