

# Information-Theoretic Probing with Minimum Description Length

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# TLDR

$$\mathcal{L}_{\text{Minimum Description Length}} = \mathcal{L}_{\text{Model}} + \mathcal{L}_{\text{Data}}$$

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Choose the model that gives the shortest description.



$$\mathcal{L}_{\text{Minimum Description Length}} = \mathcal{L}_{\text{Model}} + \mathcal{L}_{\text{Data}}$$

Rissanen, Jorma. "Modeling by shortest data description." *Automatica* 14.5 (1978): 465-471.

# TLDR

Choose the model that gives the shortest description.



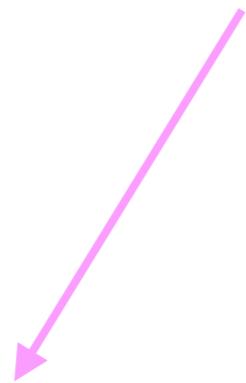
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Variational Inference & Bayesian Learning

# TLDR

$$\mathcal{L}_{\text{Minimum Description Length}} = \mathcal{L}_{\text{Model}} + \mathcal{L}_{\text{Data}}$$



$$\mathcal{L}_{\text{Var}} = \text{KL}(\beta \parallel \alpha)$$

$$- \mathbb{E}_{\theta \sim \beta} \sum_{i=1}^n \log_2 p_\theta(y_i | x_i)$$

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$$\mathcal{L}_{\text{Online}} = t_1 \log_2 K$$

$$- \sum_{i=1}^{S-1} \log_2 p_{\theta_i}(y_{t_i+1:t_{i+1}} | x_{t_i+1:t_{i+1}})$$

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$$- \mathbb{E}_{\theta \sim \beta} \sum_{i=1}^n \log_2 p_\theta(y_i | x_i)$$

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$$\mathcal{L}_{\text{Minimum Description Length}} = \mathcal{L}_{\text{Model}} + \mathcal{L}_{\text{Data}}$$



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# Resources

[mdl paper](#)

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[mdl code](#)

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[mdl blog](#)

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[bayesian layers paper](#)

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[bits-back argument paper](#)

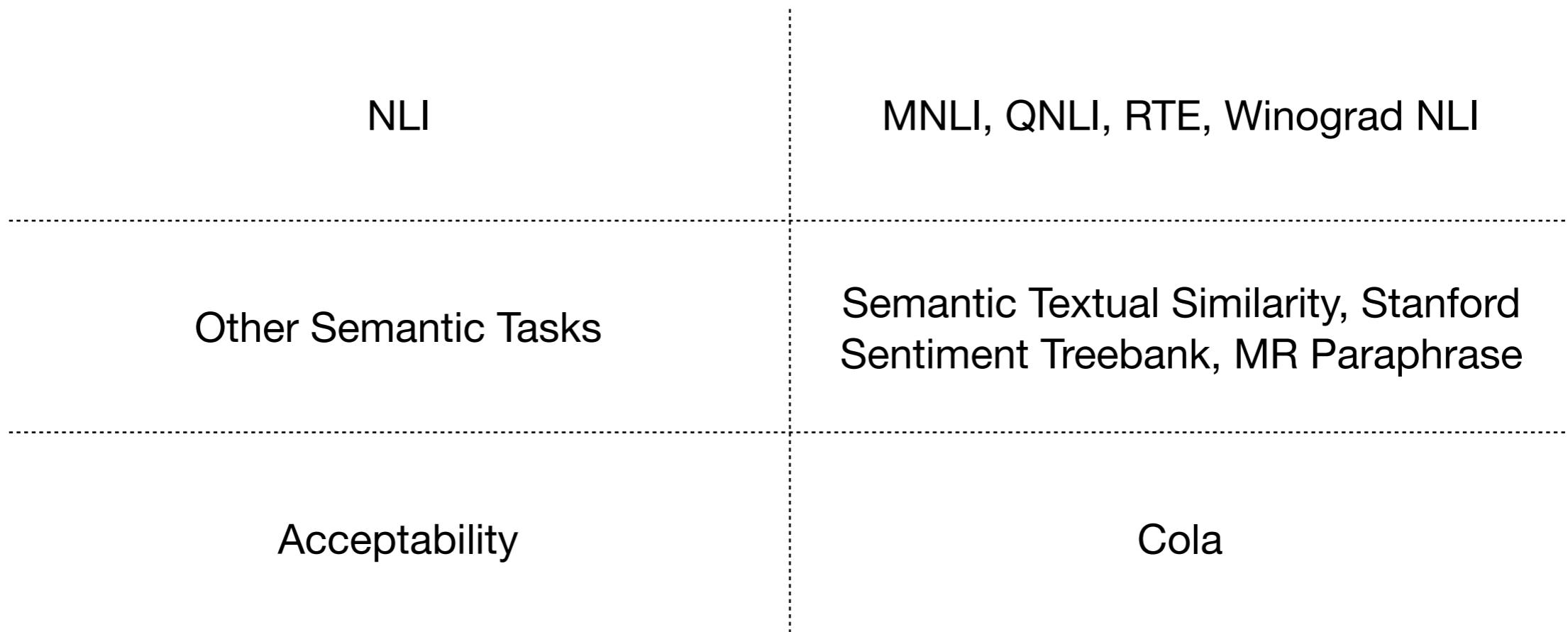
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[probabilistic graphical models course](#)



Models are doing pretty well

# GLUE



# GLUE

|                |      |
|----------------|------|
| T5             | 90.3 |
| Human Baseline | 87.1 |
| BERT++         | 80.5 |
| BERT           | 78.1 |

# SuperGLUE

Multi-Sentence Understanding

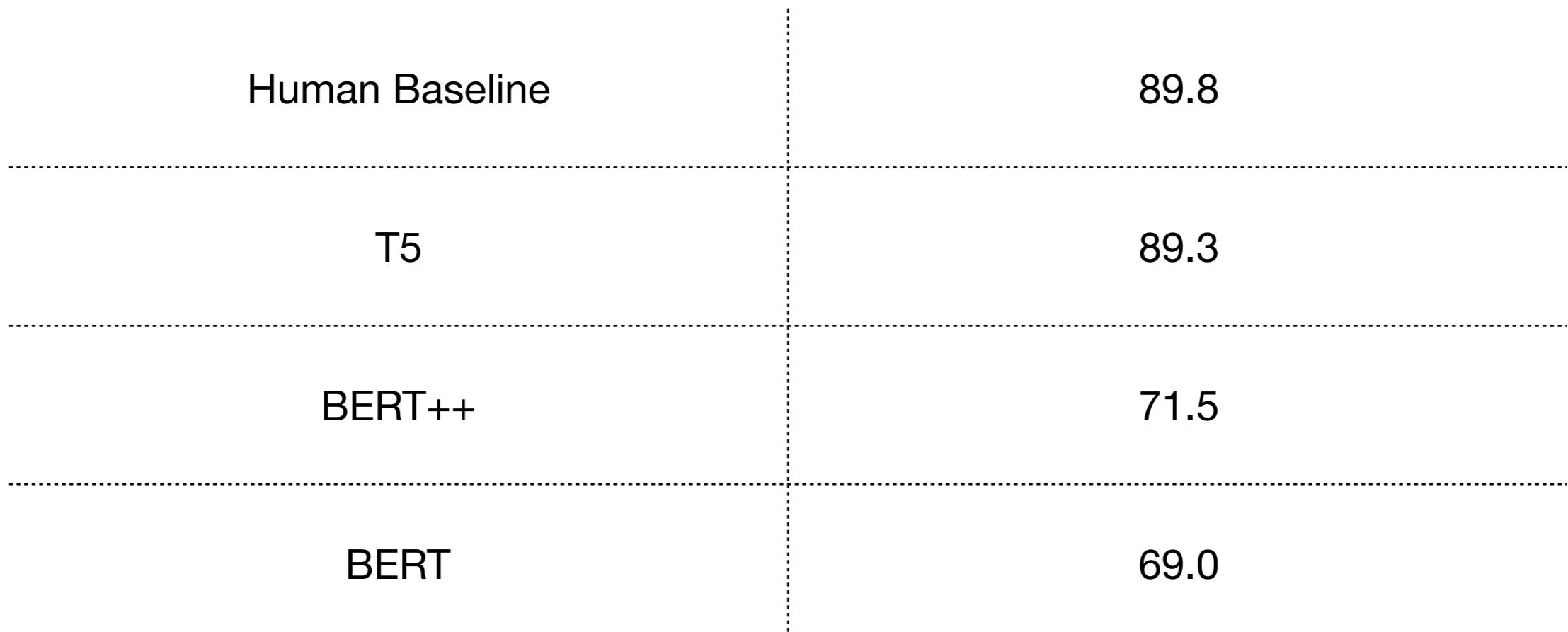
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Common Sense

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Non-trivial QA

# SuperGLUE



Why do the models  
behave the way they do?

# What do models learn?

Diagnostic classifiers; “probes”.

# Diagnostic classifiers; “probes”.

Ian Tenney, Patrick Xia, Berlin Chen, Alex Wang, Adam Poliak, R Thomas McCoy, Najoung Kim, Benjamin Van Durme, Sam Bowman, Dipanjan Das, and Ellie Pavlick. 2019. What do you learn from context? probing for sentence structure in contextualized word representations. In International Conference on Learning Representations.

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Tenney, Ian, Dipanjan Das, and Ellie Pavlick. "Bert rediscovers the classical nlp pipeline." arXiv preprint arXiv:1905.05950 (2019).

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Zhang, Kelly W., and Samuel R. Bowman. "Language modeling teaches you more syntax than translation does: Lessons learned through auxiliary task analysis." arXiv preprint arXiv:1809.10040 (2018).

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Kim, Najoung, et al. "Probing what different NLP tasks teach machines about function word comprehension." arXiv preprint arXiv:1904.11544 (2019).

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Warstadt, Alex, et al. "Investigating BERT's Knowledge of Language: Five Analysis Methods with NPIs." arXiv preprint arXiv:1909.02597 (2019).

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Clark, Kevin, et al. "What Does BERT Look At? An Analysis of BERT's Attention." arXiv preprint arXiv:1906.04341 (2019).

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Goldberg, Yoav. "Assessing BERT's Syntactic Abilities." arXiv preprint arXiv:1901.05287 (2019).

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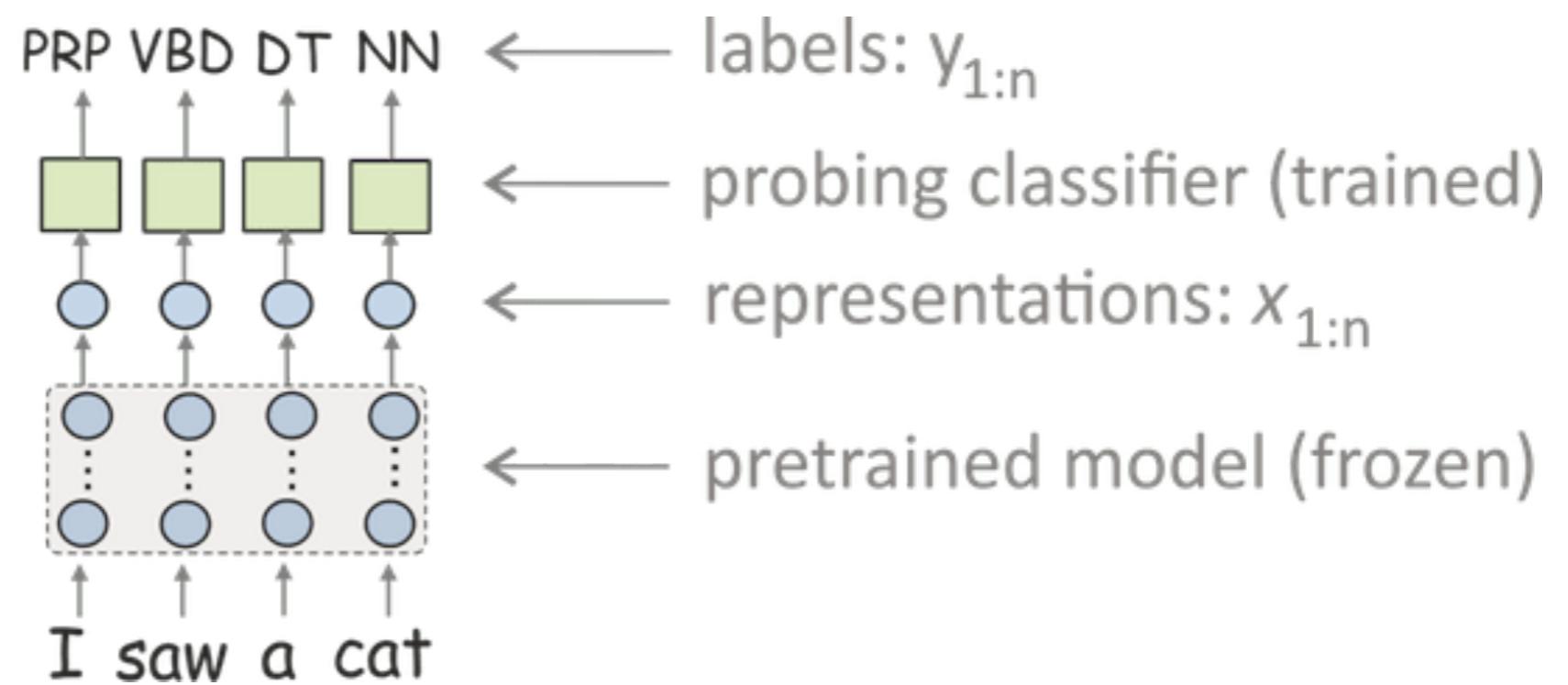
Conneau, Alexis, et al. "What you can cram into a single vector: Probing sentence embeddings for linguistic properties." arXiv preprint arXiv:1805.01070 (2018).

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Goal:  
predict labels

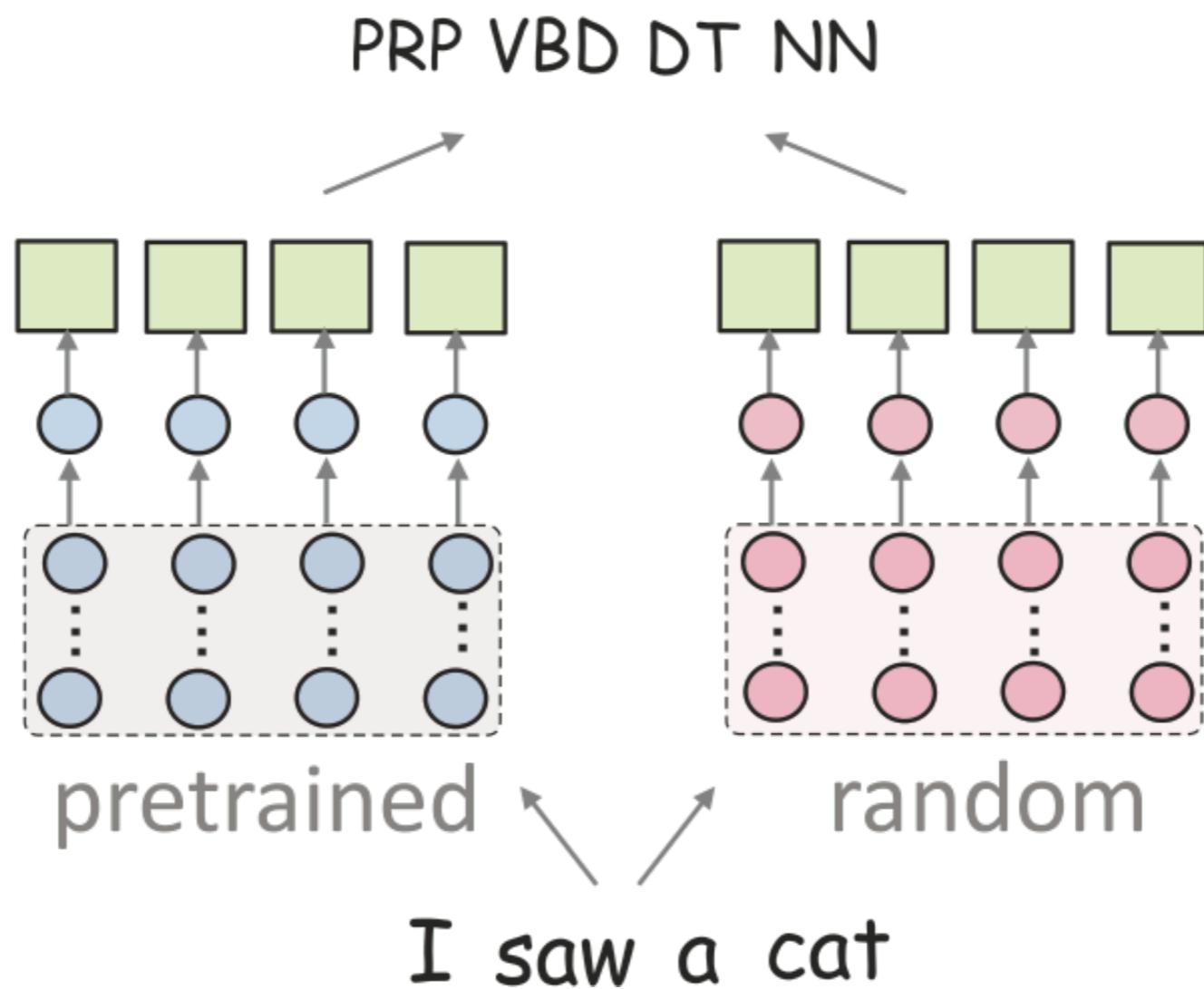
Measure:  
probe accuracy

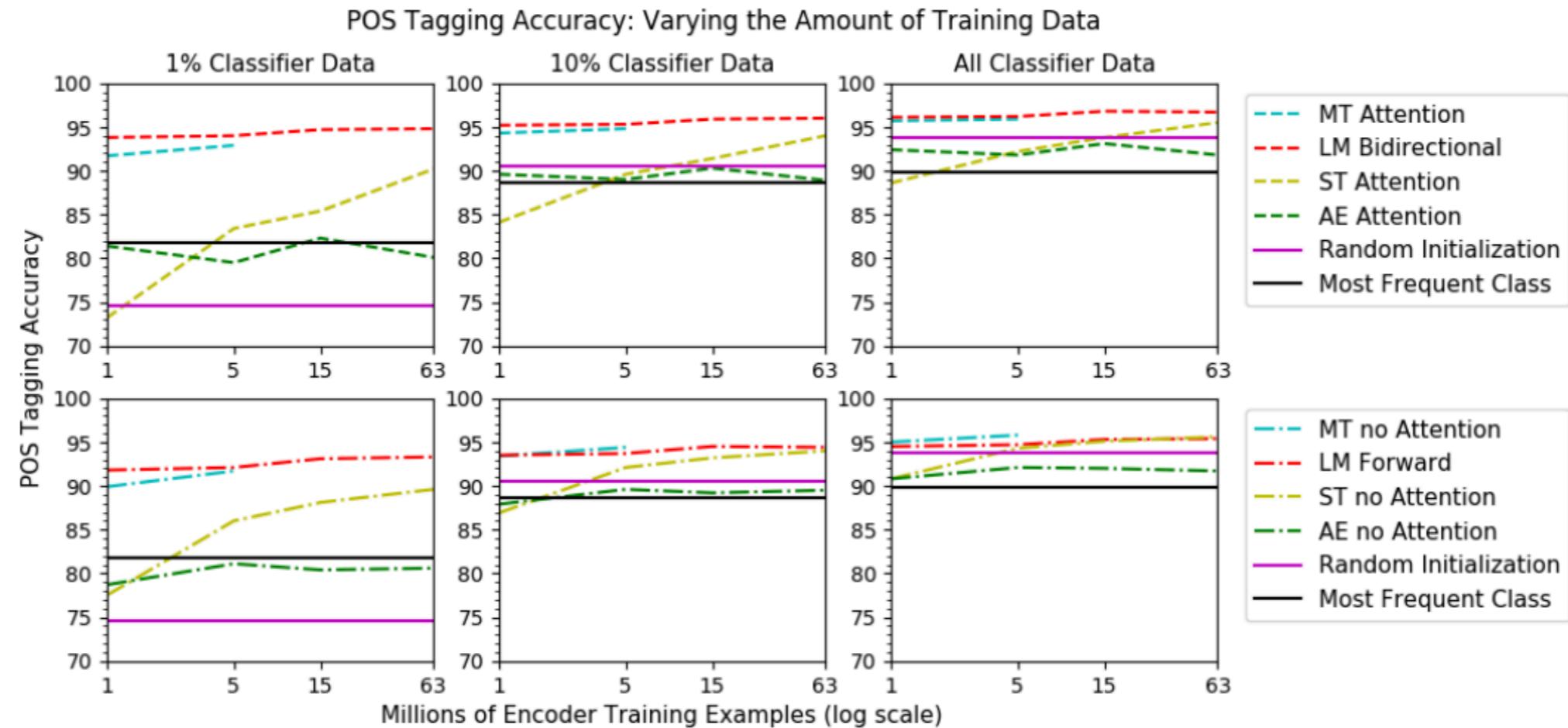


1. Models with random weights  
report similar accuracies to models  
with trained weights.

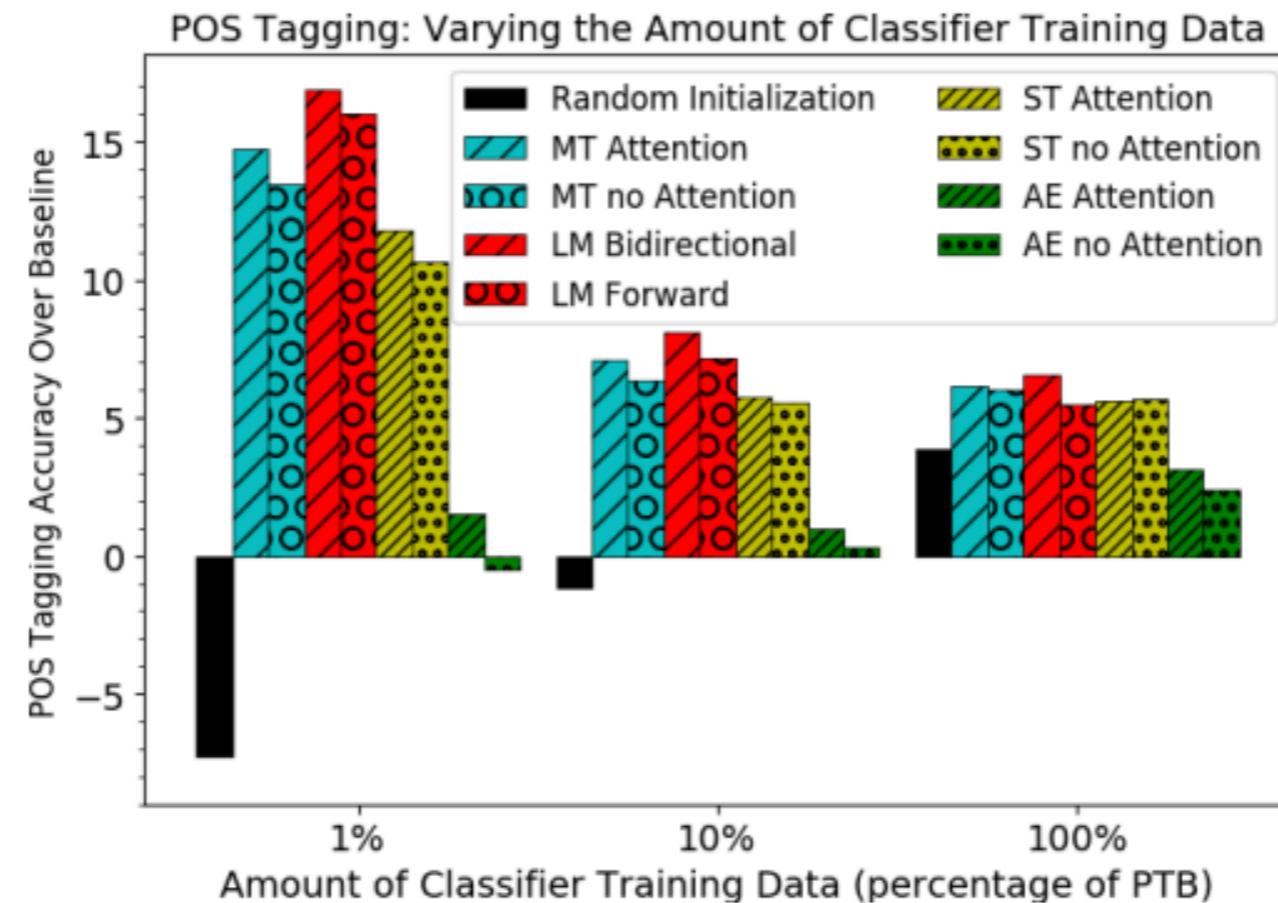
Zhang, Kelly W., and Samuel R. Bowman. "Language modeling teaches you more syntax than translation does: Lessons learned through auxiliary task analysis." *arXiv preprint arXiv:1809.10040* (2018).

# Model: trained vs random





Zhang, Kelly W., and Samuel R. Bowman. "Language modeling teaches you more syntax than translation does: Lessons learned through auxiliary task analysis." *arXiv preprint arXiv:1809.10040* (2018).



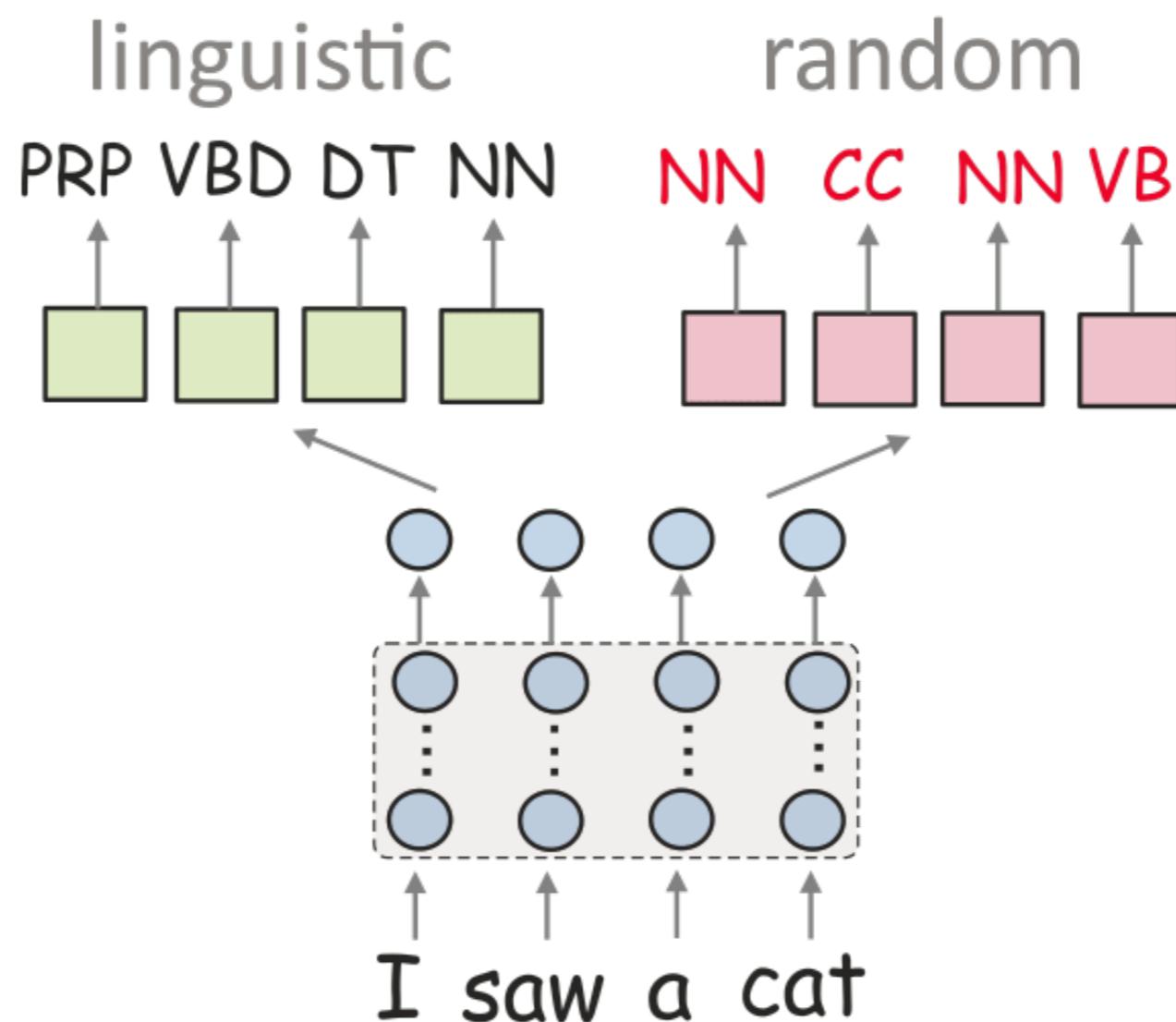
**(a) WC-MFC baselines for different amounts of PTB training data:** 1% PTB: 81.8%; 10% PTB: 88.6%; 100% PTB: 89.9%.

Zhang, Kelly W., and Samuel R. Bowman. "Language modeling teaches you more syntax than translation does: Lessons learned through auxiliary task analysis." *arXiv preprint arXiv:1809.10040* (2018).

2. Models often perform equally well on tasks with randomly assigned variables.

Hewitt, John, and Percy Liang. "Designing and Interpreting Probes with Control Tasks." arXiv preprint arXiv:1909.03368 (2019).

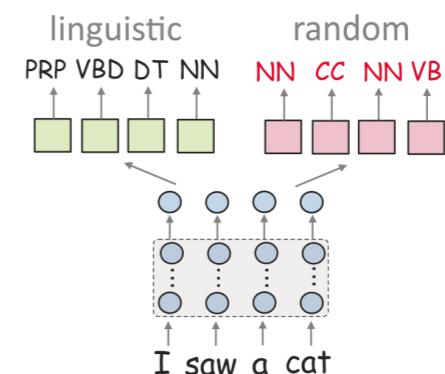
# Labels: linguistic vs random



| <b>Probe</b>                        | <b>PoS</b> | <b>Ctl</b> | <b>Select.</b> |  | <b>Dep</b> | <b>Ctl</b> | <b>Select.</b> |
|-------------------------------------|------------|------------|----------------|--|------------|------------|----------------|
| Probes with Default Hyperparameters |            |            |                |  |            |            |                |
| Linear                              | 97.2       | 71.2       | 26.0           |  | -          | -          | -              |
| Bilinear                            | -          | -          | -              |  | 89.0       | 82.4       | 6.6            |
| MLP-1                               | 97.3       | 92.8       | 4.5            |  | 92.3       | 93.0       | -0.7           |
| MLP-2                               | 97.3       | 93.2       | 4.2            |  | 93.9       | 92.0       | 1.9            |
| Probes with 0.4 Dropout             |            |            |                |  |            |            |                |
| Linear                              | 97.1       | 67.3       | 29.8           |  | -          | -          | -              |
| Bilinear                            | -          | -          | -              |  | 90.4       | 73.7       | 16.7           |
| MLP-1                               | 97.5       | 93.4       | 4.1            |  | 93.8       | 93.1       | 0.7            |
| MLP-2                               | 97.4       | 94.1       | 3.4            |  | 94.7       | 93.5       | 1.3            |
| Probes Designed with Control Tasks  |            |            |                |  |            |            |                |
| Linear                              | 97.0       | 64.0       | 33.0           |  | -          | -          | -              |
| Bilinear                            | -          | -          | -              |  | 91.0       | 83.1       | 7.9            |
| MLP-1                               | 97.2       | 80.6       | 16.6           |  | 90.5       | 84.3       | 6.2            |
| MLP-2                               | 97.2       | 81.7       | 15.4           |  | 92.8       | 89.8       | 3.0            |

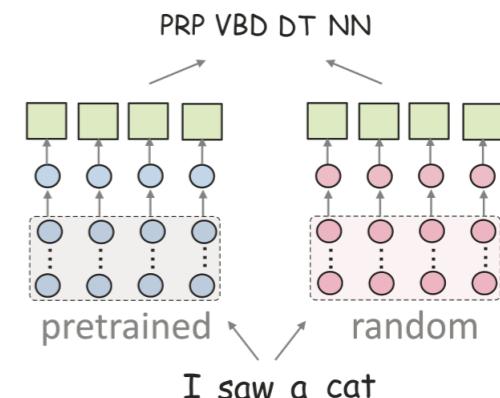
If a random model can solve the linguistic task equally well, what can we say about the model's quality?

Labels: linguistic vs random



If models solve the random task equally well, is there anything we can say about how well the model represents linguistic features?

Model: trained vs random

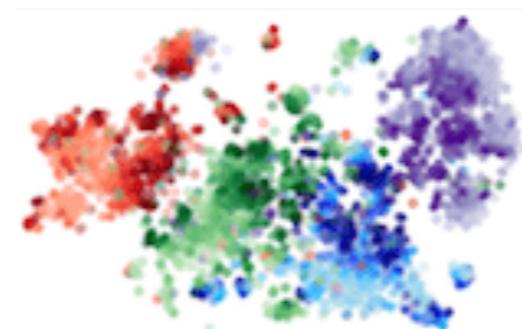


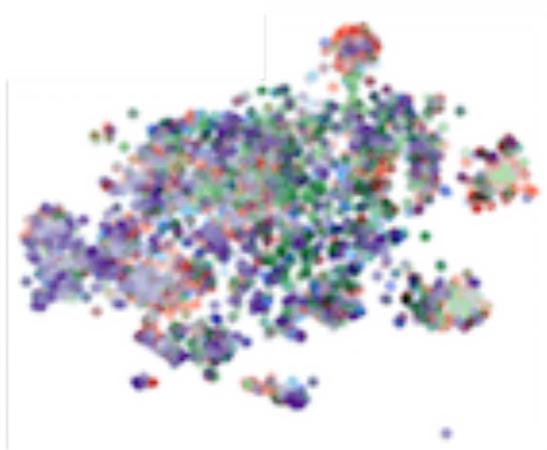
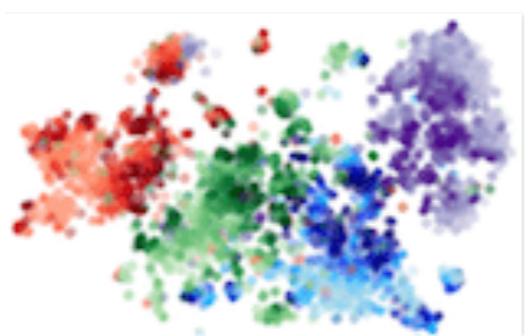


How can we capture how hard it is  
for the probe to learn the task?

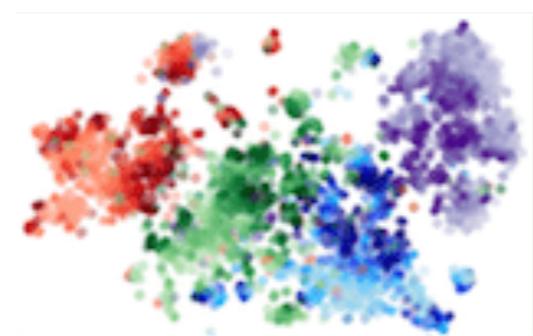
$$\mathcal{D} = \{(x_1, y_1), (x_2, y_2), \dots (x_n, y_n)\}$$

Representations  $x_{1:n}$  and labels  $y_{1:n}$ .

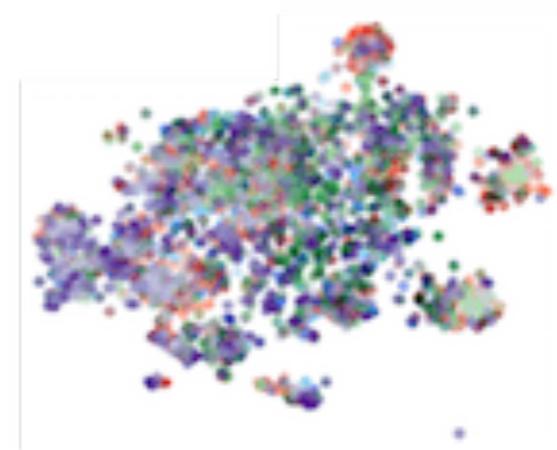




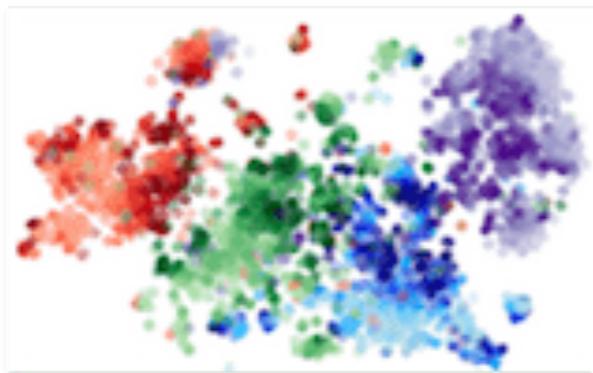
Strong Regularity



Weak Regularity



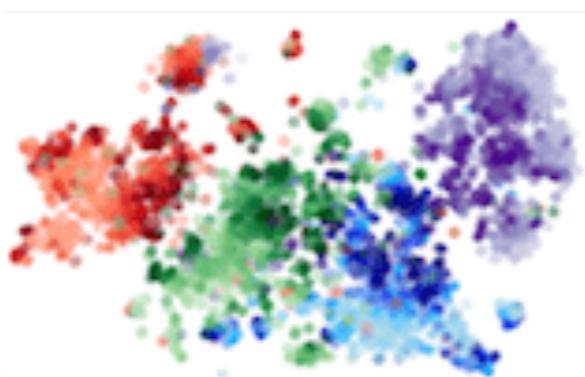
strong regularity



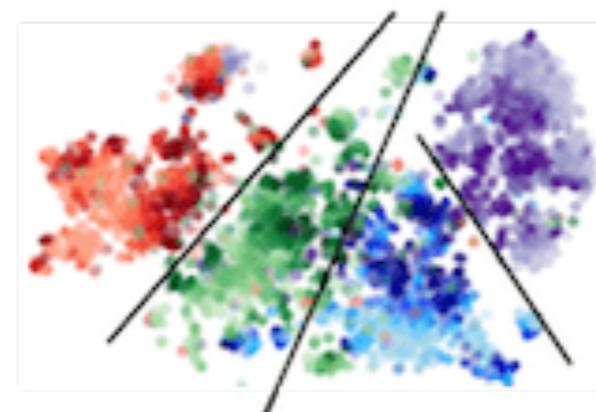
can be revealed  
with a few examples



strong regularity



can be explained  
with a simple “rule”



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$$\begin{aligned}\mathcal{L}_{\text{Online}} &= t_1 \log_2 K \\ &\quad - \sum_{i=1}^{S-1} \log_2 p_{\theta_i}(y_{t_i+1:t_{i+1}} | x_{t_i+1:t_{i+1}})\end{aligned}$$

Rissanen, Jorma. "Universal coding, information, prediction, and estimation." *IEEE Transactions on Information theory* 30.4 (1984): 629-636.

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1. Send first block with a uniform code.

$$\begin{aligned}\mathcal{L}_{\text{Online}} = & t_1 \log_2 K \\ & - \sum_{i=1}^{S-1} \log_2 p_{\theta_i}(y_{t_i+1:t_{i+1}} | x_{t_i+1:t_{i+1}})\end{aligned}$$

1. Send first block with a uniform code.
2. Learn model on the sent block(s).

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1. Send first block with a uniform code.
2. Learn model on the sent block(s).
3. Use model to communicate next block (in a shorter way compared to uniform code.)
4. Repeat until all data is sent.

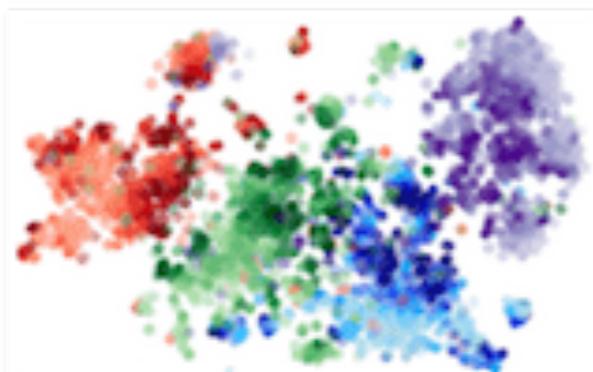
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strong regularity



can be revealed  
with a few examples

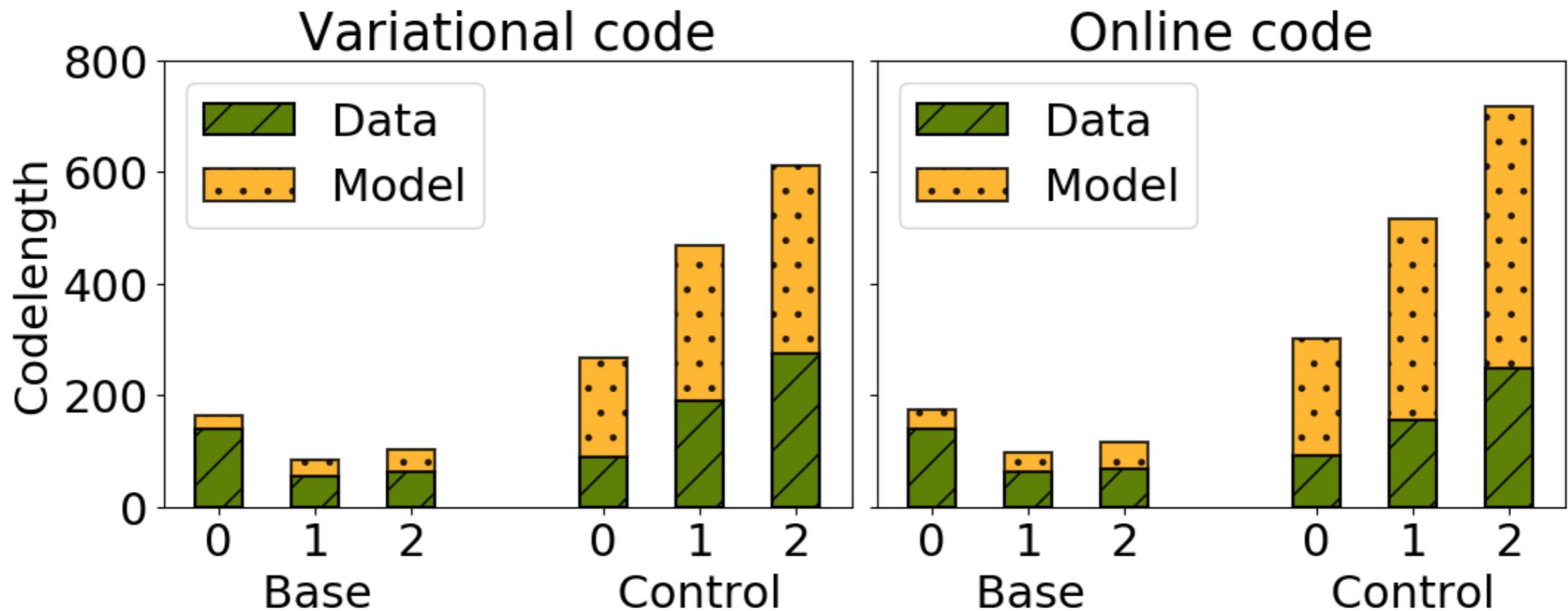




# Results

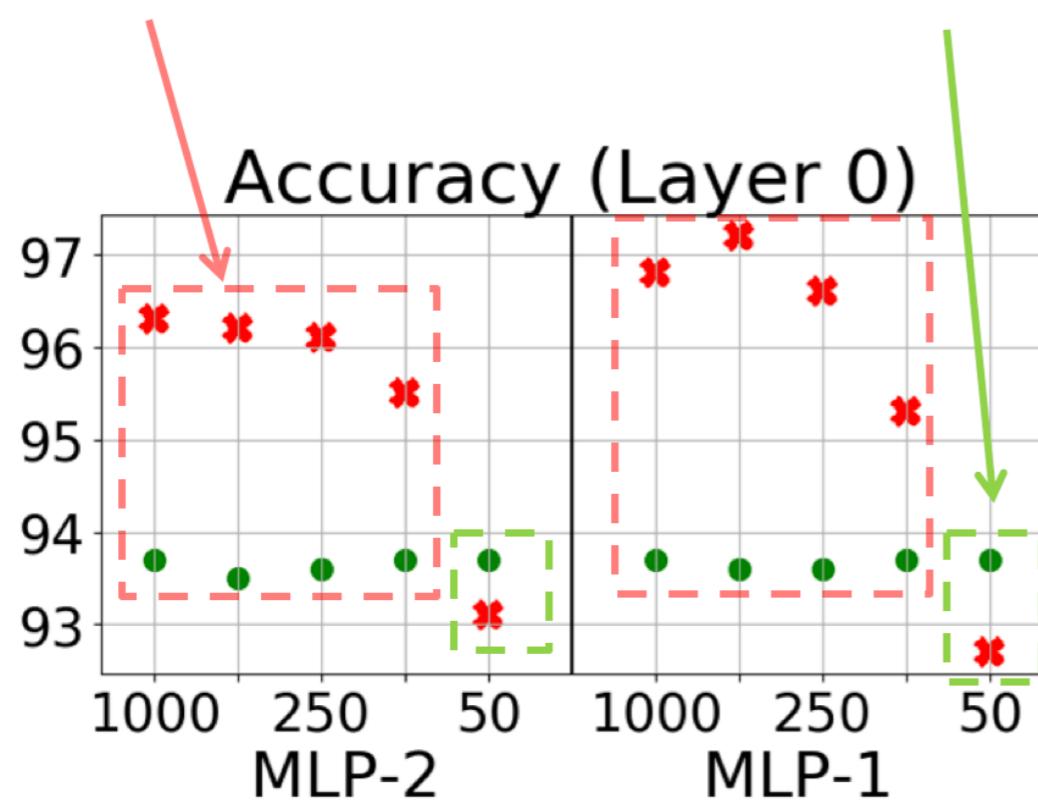
# Variational & Online Codes

## Report Similar Behavior



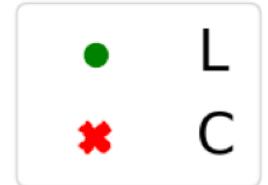
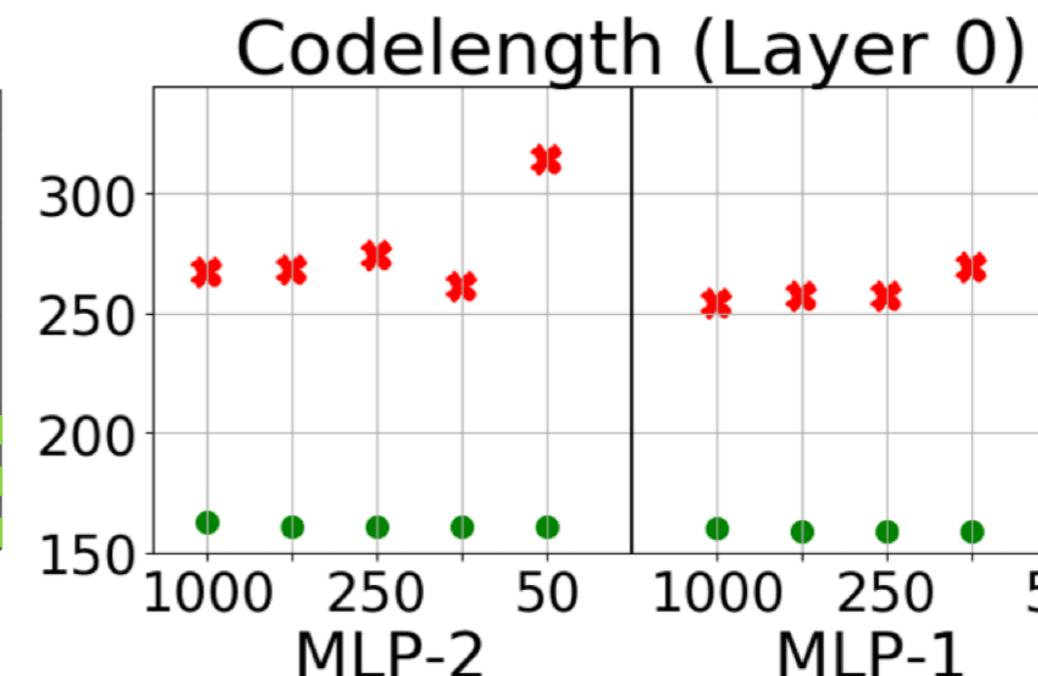
# Across HPs, Accuracy Unclear; MDL Clear

Control is better



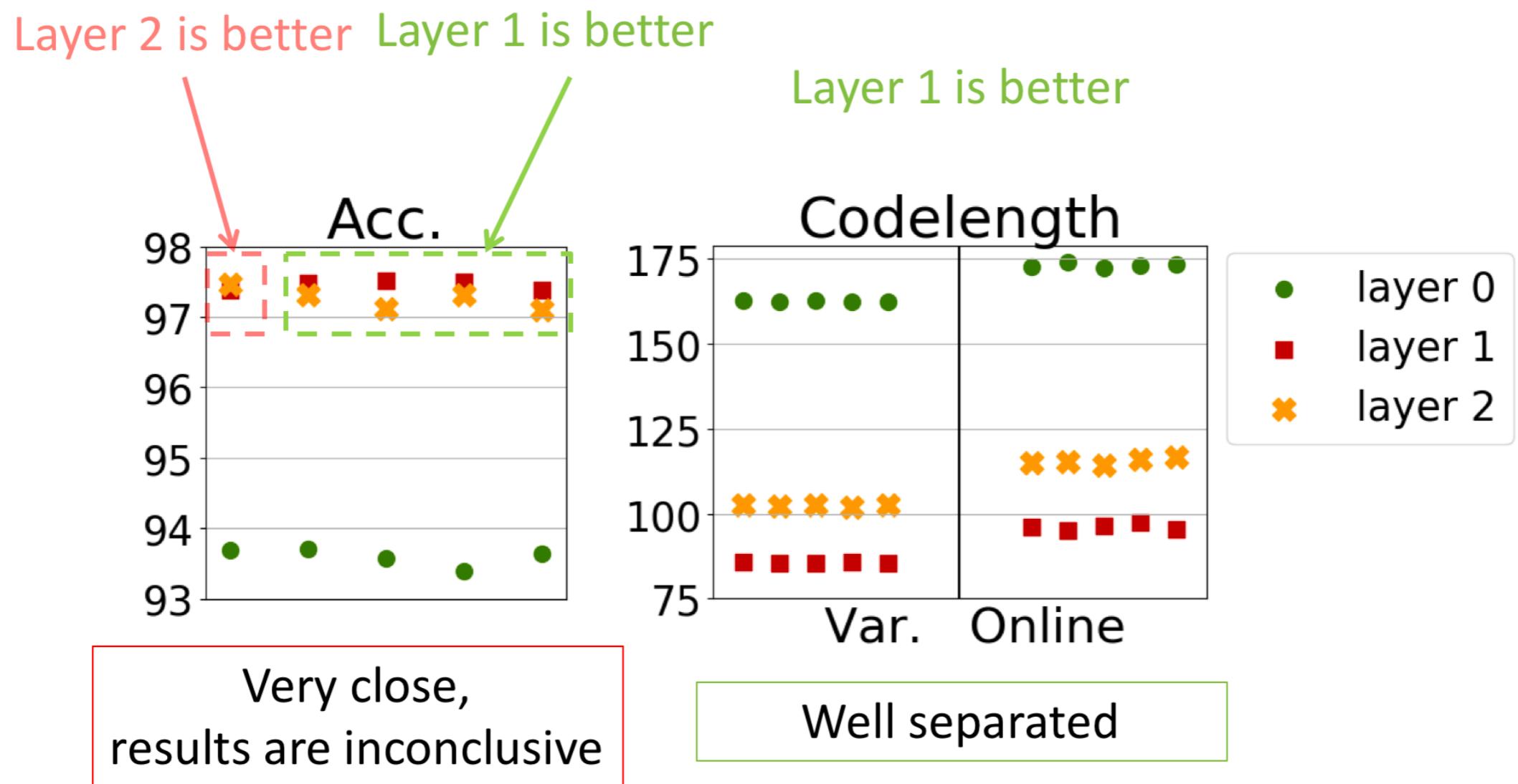
Linguistic is better

Linguistic is better

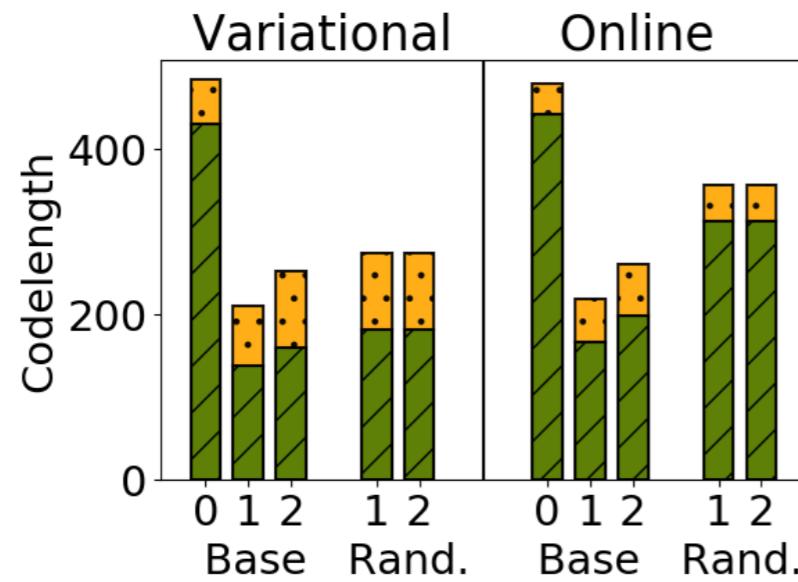


Accuracy is wrong for 8 out of 10 settings, MDL is always correct  
(for accuracy higher is better, for codelength – lower)

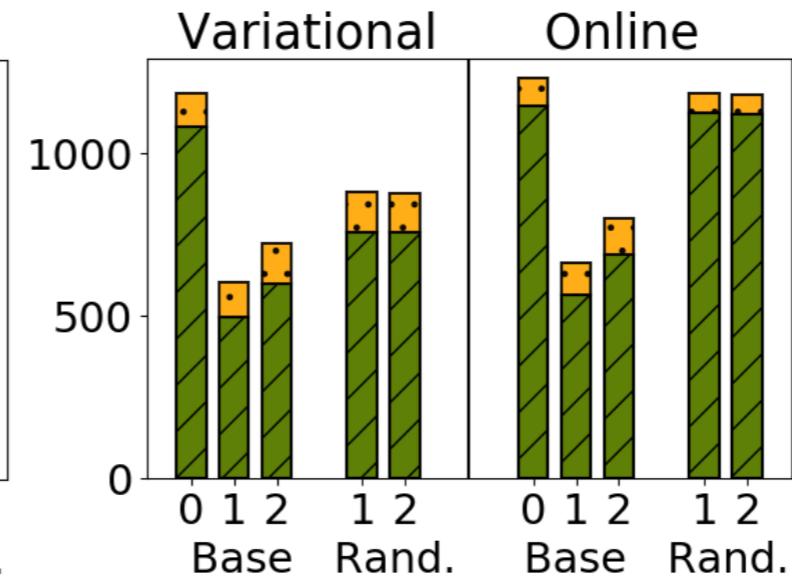
# Across Random Seeds, Acc Unstable; MDL Stable



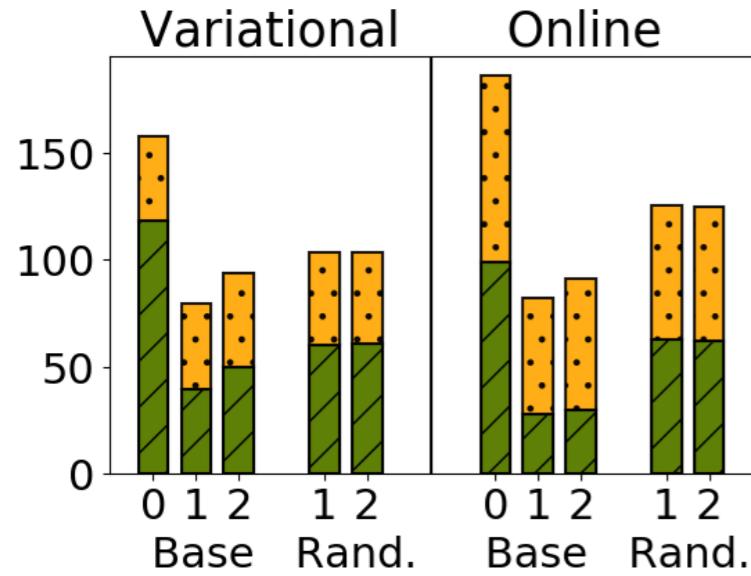
## Part of Speech



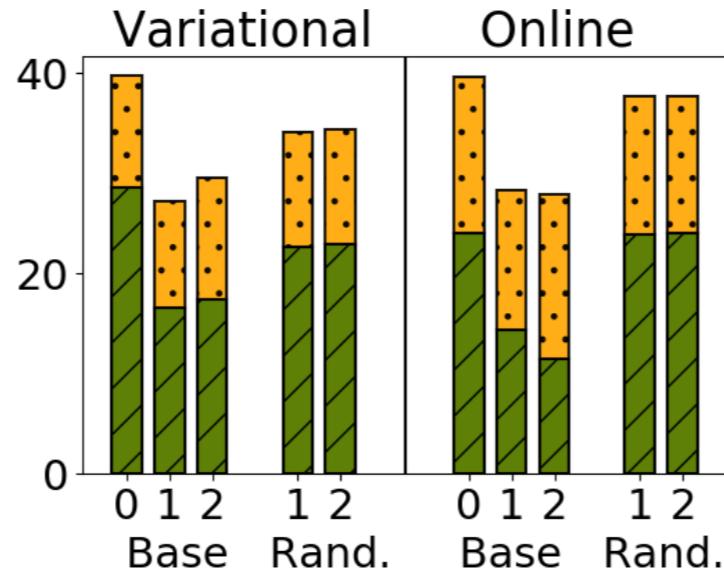
## Constituents



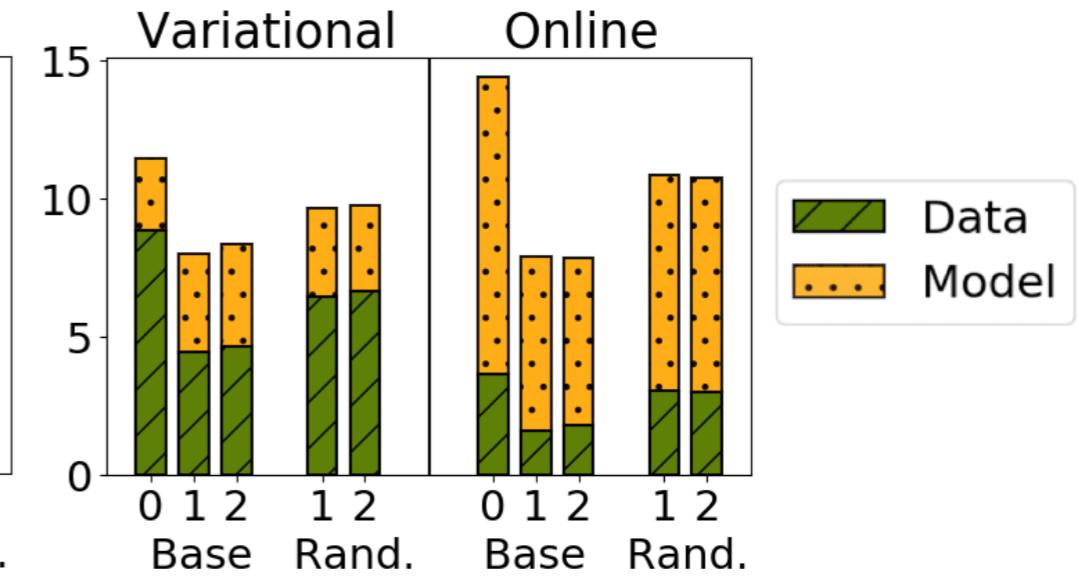
## Dependencies



## NER



## Relation classification



## Author Take-Aways

1. Layer 0 vs. Contextual: Even random contextual is better.
2. Code-lengths for randomly initialized models are higher.
3. Randomly initialized layers don't evolve.

## My Take-Aways

1. Seems better than accuracy.
2. Seems not that much better and requires accuracy for context.
  1. The HPs that “failed” for accuracy were very small.
  2. The separation across random seeds for MDL shows a difference, but we can’t readily interpret that difference.



# Small Experiments For Building Intuition

