HW2-REPORT

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1 MLQP Analyse

1.1 Forward

$$x_i^k = f^k(n_i^k)$$

$$n_i^k = b_i^k + \sum_{j=1}^{N^{k-1}} (u_{i,j}^k (x_j^{k-1})^2 + v_{i,j}^k x_j^{k-1})$$

1.2 Backpropagation

Let:

$$s_i^k = \frac{\partial F}{\partial n_i^k}$$

Then:

$$u_{i,j}^{k}(l+1) = u_{i,j}^{k}(l) - \alpha s_{i}^{k} \frac{\partial n_{i}^{k}}{\partial u_{i,j}^{k}} = u_{i,j}^{k}(l) - \alpha s_{i}^{k}(x_{j}^{k-1})^{2}$$

$$v_{i,j}^{k}(l+1) = v_{i,j}^{k}(l) - \alpha s_{i}^{k} \frac{\partial n_{i}^{k}}{\partial v_{i,j}^{k}} = v_{i,j}^{k}(l) - \alpha s_{i}^{k} x_{j}^{k-1}$$

$$b_{i,j}^{k}(l+1) = b_{i,j}^{k}(l) - \alpha s_{i}^{k} \frac{\partial n_{i}^{k}}{\partial b_{i,j}^{k}} = b_{i,j}^{k}(l) - \alpha s_{i}^{k}$$

Now calculate s^k :

$$s^k = \frac{\partial F}{\partial n^k} = \frac{\partial F}{\partial n^{k+1}} \frac{\partial n^{k+1}}{\partial n^k} = s^{k+1} \frac{\partial n^{k+1}}{\partial n^k}$$

To calculate the Jacobbi's matrix

$$J^k = \frac{\partial n^{k+1}}{\partial n^k}$$

We have:

$$J_{i,j}^k = \frac{\partial n_i^{k+1}}{\partial n_j^k} = \frac{\partial (b_i^{k+1} + \sum_{l=1}^{N^k} (u_{i,l}^{k+1}(x_l^k)^2 + v_{i,l}^{k+1}x_l^k))}{\partial n_j^k} = (2x_j^k u_{i,j}^{k+1} + v_{i,j}^{k+1}) \frac{\partial x_j^k}{\partial n_j^k}$$

At last, calculate s^m:

$$s_i^m = \frac{\partial \sum_{j=1}^{N^m} (t_j - x_j^m)^2}{\partial n_i^m} = 2(x_i^m - t_i) \frac{\partial x_i^m}{\partial n_i^m}$$

Let

$$\dot{F}^{k}{}_{i,j} = \begin{cases} \dot{f}^{k}(x_{i}^{k}), & i = j \\ 0, & i \neq j \end{cases}$$
$$X_{i,j}^{k} = \begin{cases} x_{i}^{k}, & i = j \\ 0, & i \neq j \end{cases}$$

Then

$$s^{m} = 2(x^{m} - t)\dot{F}^{m}$$

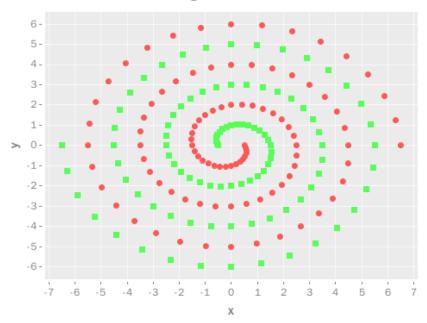
$$s^{k} = s^{k+1}J^{k} = s^{k+1}(\dot{F}^{k}V^{k+1} + 2\dot{F}^{k}X^{k}U^{k+1})$$

2 Two-spirals problem

2.1 Problem

The two-spirals problem is defined as follow:

Origin Data



It is extremely hard for traditional network to regress such a pattern. In the following I will try to use MLQP to solve this problem.

2.2 Net Structure

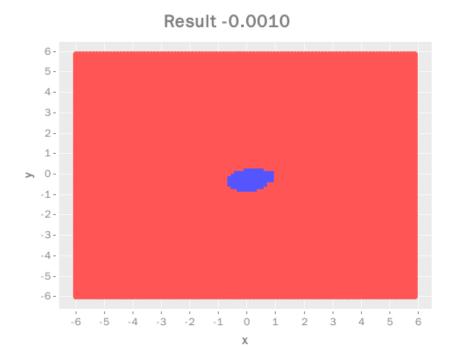
I try to use a two-layer MLQP network to solve the problem. The first layer contains 10 neurons with sigmoid function as transport function. The second layer contains 1 neuron with purelin function as transport function.

To avoid the weight matrixes always being symmetry, I gave each cell of them random initial values between -1 and 1.

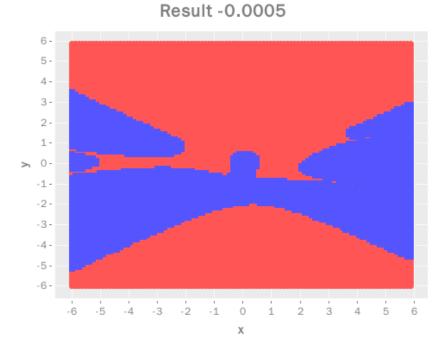
As sigmoid function almost become a constant when x > 5, I use very small α s from 0.0001 to 0.001.

2.3 Result

The training result when $\alpha = 0.01$:

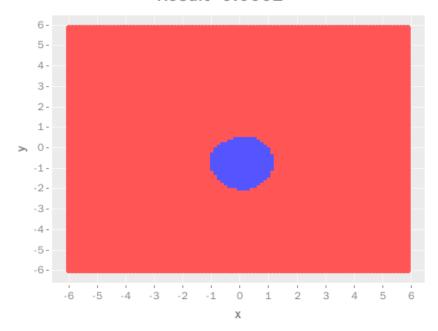


The training result when $\alpha = 0.005$:



The training result when $\alpha = 0.001$:

Result -0.0001



Each result use a random net and looped for 1000 times