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1. INTRODUCTION

1.1 General Introduction

A Quadcopter is a multicopter that is propelled and lifted by four propellers (rotors). Opposed to fixed-wing aircraft (most common example is an airplane), a Quadcopter's lift is generated by revolving narrow-chord airfoils, symmetrically placed, are adjusted as a group. Control of motion is attained by altering the pitch and/or rotation rate of one or more propellers.

One reason a Quadcopter is seen as an alternative to some problems in vertical flight is because of torque-induced control issues (mostly the issue dealing with the tail rotor which generates no meaningful lift). Other advantages over a helicopter are: not requiring mechanical linkages to vary the propeller pitch angle as they spin, by using more propellers each individual propeller can be smaller in diameter possessing less kinetic energy, and by using smaller propellers, this reduces the damage done by the propellers should they come into contact with anything. The Helicopters use two propellers to control flight of pitch, roll, and yaw. With four propellers, there are two pairs of propellers and each pair rotates opposite direction. If one pair is slowed down then the Quadcopter will rotate in the same direction of the slowed down propellers, due to the opposite two motors greater speed overpowering the current slower motors.

The Quadcopter can have other applications instead of just a fun recreational model. One use is for the military, instead of sending someone into a dangerous area, the Quadcopter equipped with a camera would fly in and gather valuable reconnaissance information. Small-scale models can lead to the innovations in a full scale Quadcopter potentially solving the aforementioned flight issues presented by helicopters, maybe one-day evening replacing helicopters as a secondary means of air travel (behind airplanes).

The Quadcopter is not as expensive as the larger scale models, which range from a few inches to a few feet in diameter. The models can help people learn how the physics of a Quadcopter work and how it differs from other multicopter technology and other fixed-wing aircraft. The project encompasses many engineering issues and tasks that vary from physics, software, and hardware.

The software side is much different from the hardware. There are various things that need to done in software; for example, controlling the motors, interpreting controller inputs, communicating with the

Quadcopter, and various other algorithms required to fly. Software is also required for semi-autonomous flight, safety systems, and landing.

1.2 Overview of Concept

The Quadcopter as a bare machine is of very little use, but it is the power of algorithms running on integrated hardware that makes the Quadcopter a viable product for industrial and commercial use. Generally, by algorithms, we mean the software platform running on a processor, but Quadcopter falls under embedded system category where algorithms not only maintain the working of central processor which is microcontroller but also of wireless communication devices and IMU (Inertial Measurement Unit) devices. The wireless communication devices itself has a microprocessor which provide error detection and flow control in transmission and also the IMU device has high performance microprocessor to provide reliable data for calculations of yaw, pitch and roll angles for the Quadcopter. The Quadcopter has 4 degrees of freedom i.e. yaw – rotation about axis perpendicular to Quadcopter plane, pitch – rotation about y axis, roll – rotation about x –axis and throttle which is acceleration along the common axis of propellers. Some factors concerning the operation of Quadcopter are:

1.2.1 Weight

Weight is another major consideration for the Quadcopter, which is relative to the size. The design goal is to keep the weight very less, the chassis needs to be made of very lightweight materials, the light metal allows the chassis to be light and has the added benefit of being sturdy enough to support the weight of the motors and batteries. The motors and batteries also add a significant amount of weight to the design, so they must be as light as possible, while continuing to meet other specifications. The motors and batteries account for about half of our target weight limit.

1.2.2 Motors & Propellers

The right electronics are a first step toward creating flight, but a multi-rotor isn't going anywhere without good old-fashioned practical physics to pull it upwards. Your choice in motors plays a pivotal role in the success of a capable setup.

This is also the point when specifications start to get complicated. You'll want to do some research before settling on the right configuration for your quad. And motors are expensive, making it even more important to consider the options carefully.

Motors used these days are almost exclusively of the "brushless" variety. That equates to minimal friction. A cylindrical shell of magnets rotates on precision bearings around a core of tightly and neatly coiled wire. The propeller is fastened atop. Many Tom's Hardware readers already know the composition of an electrical motor, but for enthusiasts dabbling in multi-rotors, the inner workings are unimportant. So long as reasonable care is taken and dirt kept clear of the bearings, brushless motors are famously reliable.



Motors are assigned various notations, the most consequential being the Kv rating. Confusingly, Kv does not refer to kilovolts in this case. Rather, it's a motor velocity constant denoting the revolutions per minute (RPM) that a motor will turn when a 1 V potential difference is applied with zero load. This number is important, as it defines a multi-rotor's flight characteristics based on specifications like battery voltage and take-off weight.

Also vital are the propellers you choose. The variety of props is arguably greater than any other component we discuss; materials, dimensions, and price span a mind-bogglingly wide range. Generally, cheaper props are less precisely manufactured and more prone to creating vibration. This applies especially to the relatively larger end of the prop spectrum, with differences becoming less perceptible for smaller craft. Again, some vibration can be acceptable, bolstering the case for less expensive propellers. But if you're flying a quadcopter with the intention of producing well-shot footage, expect to spend more money on propellers.



It's worth pointing out that a majority of props are designed for airplane, though we're starting to see more optimized for multi-rotors. Graupner is a favorite brand amongst enthusiasts, and the company's E-Props, designed for electric power systems, are often cited as favorites. Other common options include Gemfan, APC, T-Motor, and RCTimer.

There are three simple measurements to keep in mind. The first is length, usually given in inches. The higher the Kv of your motors, the smaller your props need to be. Smaller props allow for greater speeds, but reduced efficiency. A larger prop setup (with correspondingly-low Kv motors) is easier to fly steadily, uses less current, and lifts more weight.

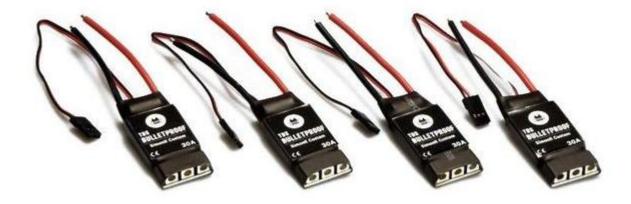
The best way to gauge the right range for motors and props is referring to manufacturer recommendations if you're building an ARTF kit. Or you can simply compare the setups of more experienced builders.

The second measurement, prop pitch, is less important, but of interest to more vigorous hobbyists. Prop dimensions are quoted in the form 9x4.7", as a numerical example. The first number refers to the already-discussed length. The second is pitch, defined as the distance a prop would be pulled forward through a solid in a single full revolution, as if a screw through wood. The greater the pitch, the higher the thrust and necessary motor output. Typically, multi-rotors use props with pitches in the range of 3 to 5". Lower pitches are more efficient, but lend a more sedate flying style.

Finally, we have bore measurement, which is simply the size of the hole in the center of the prop. This must be matched to the shaft of your chosen motors. Adapters are available to downsize a prop's bore. Alternatively, some props, such as those produced by T-Motor, use a direct mounting system whereby screws secure the props directly to the motor head.

1.2.3 Electronic speed controllers (ESCs)

Electronic speed controllers (ESCs) are used in many R/C applications. They translate signal to electrical supply. On a multi-rotor, every motor gets its own ESC, each of which connects to the flight controller. After computing the inputs, the controller directs each ESC to adjust its speed in order for the craft to perform them.



ESC refresh rates vary. For multi-rotors, given the balance of multiple motors critical to the craft's ability to stay airborne, high refresh rates are more important than many other hobbies where ESCs are used.

In essence, we're talking about programmable microcontrollers, and they employ firmware to define and carry out their tasks. In the world of multi-rotors, SimonK is the supreme ruler of ESC firmware, creating revisions optimized for multi-rotor use, stripped of irrelevant features, and sporting refresh rates as high as 400 Hz or so. ESCs can be flashed or purchased with SimonK's optimizations pre-loaded.

The only other major factor to consider is an ESC's maximum current rating, which must exceed the current draw to each motor. Generally, 30 A for medium/large quads and 10 to 12 A for a small quad is plenty.

1.2.4 LiPo Battery

Clearly, those are high current draws. But such is the nature of multi-rotors. A medium-sized hex can easily pull 40 A on a steep ascent. As a result, hefty batteries are a necessity for decent flight times.

The industry standard is lithium-ion polymer (LiPo) batteries. Relatively lightweight, compact, and offering high discharge rates, LiPos are well-suited for multi-rotors.



Ready for another set of specifications? There are three to consider as you start perusing the cyber-aisles of LiPo batteries. The first is voltage. A single cell supplies a nominal voltage of 3.7 V (4.2 V at full charge). Each additional cell wired in series adds 3.7 V to the nominal voltage of that pack. Cell counts are denoted by the number of cells followed by "S". A 4S LiPo, therefore, is a battery of four 3.7 V cells at a summation of 14.8 V.

LiPo packs also have C ratings that indicate the maximum rate at which a pack can be discharged, with C standing for capacity. A 25C pack can be discharged at a rate 25 times its capacity.

Capacity, therefore, is the third important factor. It's measured in milliamp-hours (mAh). Let's say our 20C pack has a capacity of 4000 mAh. Given what we know about C ratings, we can do the math and determine its maximum discharge at up to 80,000 mA, or 80 A. Similar to ESCs, you need a discharge rate that's higher than the combined draw current of your motors.

LiPos connected in parallel add to capacity (rather than affecting voltage). In turn, the aforementioned S notation is modified. A 3S2P arrangement, for example, consists of two three-cell LiPos connected in parallel.

Batteries do not last forever. They vary in cost, and the pricier LiPos typically last for more cycles than the cheaper ones. A pack will "puff" in its plastic wrap as it gets to the end of its rope. Excessive heat after use is another bad sign.

The best way to prolong a LiPo's life is to follow the 80% rule. You should try to avoid discharging more than 80% of the battery's listed capacity (a maximum of 4000 mAh from a 5000 mAh pack, for example). Also, monitor voltage when you're flying, and land before reaching 3.3 V per cell. Voltage falls more rapidly as charge is depleted, and at 3 V per cell, you might drop out of the sky. Some flight controllers have protection mechanisms to help prevent over-discharge.

1.2.5 Safety

Safety is one of the major issues with any flying device. Such devices can become dangerous when traveling at high enough speeds. Though it may not injure someone, it can be painful if one is hit by the Quadcopter. To limit the potential damages, the velocity will be limited to minimum level. This level depends on the final weight of the device, and needs a thorough analysis of the force exerted on collision. Another consideration is the performance under low-voltage conditions. When the battery level reaches a certain point, the Quadcopter must land at a safe speed instead of dropping from an unsafe height.



1.2.6 Reliability of Quadcopter

The Quadcopter needs to be semi-autonomous. This means that the Quadcopter will maintain its current position. It should drift very less. The Quadcopter will be able to self-correct when dropped from a certain height before it reaches the ground. Once the battery reaches a critical level, the Quadcopter will

begin gently landing itself due to less power being supplied to the motors, and thus each motor will turn slower and the unit will descend until it is on ground level. Using the sensor data from the gyro/accelerometer, the Quadcopter will be able to judge its position as well as its velocity. If a large spike in sensor data indicates that a collision has occurred, the Quadcopter will attempt to stabilize itself. Failing to stabilize should result in an immediate shut down of the motors to prevent further harm to the device, and to whatever it happens to be running into.

1.3 Work Done

:

- **Electrical Wiring** Wiring the individual electrical components together during building to ensure that proper communication needs between parts can occur.
- **PCB Design** Schematic designed by Eagle CAD by careful placing of different components required.
- **PCB fabrication** PCB is fabricated by CNC machine via copper clad.
- **Code Structure** Maintain the overall structure of the code. Design how individual modules will interact with one-another, and how communications will occur.
- Scheduler Design a scheduler that allows each module's task to complete within 10ms. If a task runs over the allotted time, the scheduler must run the next scheduled task as soon as possible, and continue this trend until all tasks have caught up to the allocated amount of time they should be running in. No task skips shall occur under any circumstances. If a task completes ahead of the allotted time, then the scheduler shall wait until the proper time to continue execution.
- I2C Communications Implement a system for communication between the AVR and sensors. One sensors currently in use have 3.3-volt I2C communications. The AVR has built in hardware support for I2C, which is available. The accelerometer/gyroscope has a secondary set of I2C lines available for consolidating the sensor data into a single device interface.
- Wireless Communications (Transmission) Implement the transmission of data across the wireless transceiver.

- **SPI Communications** Design the SPI communication between the AVR and the wireless transceiver. The AVR has built in hardware support for SPI; however, there are deep connections to the I2C module. This means that there can be either hardware support for SPI or hardware support for I2C.
- Balancing Systems This module is responsible for determining what corrective actions will
 keep the Quadcopter stable when in the air. This includes determining the percentage of total
 power that each motor will run at.
- **Control Interpretation Systems** This module takes raw data provided by the sensors and turns it into a signal the Quadcopter can use to perform an action (e.g. "Turn Left").
- Reading Sensor Data Communicates with all of the sensors and gathers the data onto the AVR.
 Place data into structures for other modules to process.
- **Input Filtering** Filters input received from sensor modules to remove large outliers on data and smooth the changes between values to reduce jitter.
- **Initial Testing** Responsible for testing the parts received to determine if they meet the requirements needed, and that they are functional. Tests combinations of parts to make sure they are compatible (e.g. Motors and Propellers).
- Wireless Communications (Receiver, Comm. Methods) Implement the receiver of data across the wireless transceiver. Determine methods needed to insure reliable communications with minimal interference.
- PWM Controls This module takes the percentage values for each motor and converts it into a PWM value for the motors.

- Battery & Power Management Determine the optimal batteries available that meet the specifications. This software module is responsible for determining the current battery power available for the safety controls module.
- Controls Connect the Quadcopter to the "Remote Control" AVR via whichever means are required.
- **Control Response Systems** Adjusts the "corrective vectors" provided to the motors based on the control signal sent to the Quadcopter.

2. Problem Domain

The following are the problem encountered during the project:

- Quadcopter as a flying machine is very unstable in air, several methods and algorithms are required to reduce the instability of Quadcopter in free space or air. Quadcopter if unstable is highly dangerous, if not stabilized it can hit anyone and can cause serious injuries, on the other hand this can also critically damage the hardware components
- There is a major problem in wireless communication such as transmitting and receiving of data in packets and hence in acknowledgement of these packets by normal "Remote Control" available in market. The packets sent across a transmission channel via wireless device should be received at the receiving node with no information/data loss since the "Remote Control" has no reliability so data loss can occur and also the acknowledgement along with information such as Battery Level, Yaw, Pitch, Roll and Throttle values etc. cannot be transmitted back by wireless unit at Quadcopter to handheld controller since "Remote Control" available in market is not suitable for this type of use.
- Signal loss is highly probable when using wireless devices or units, which can cause the Quadcopter to relinquish the link or connection from handheld controller. In this case the Quadcopter will continue heading or moving in some direction and thus will be lost from reach of the person controlling it and hence can cause critical damage to property or any individual by injuring him/her.
- Power loss can cause similar effect as signal loss.
- Inertial Measurement Unit (IMU) consist of Accelerometer, Gyroscope if not calibrated on a scale will cause gibberish data as output for calculation of Yaw, Pitch and Roll angular values thus the IMU needs to be calibrated as finer it can be and moreover IMU can give much drift in gyroscopic angular values thus drift needs to be removed otherwise the Quadcopter won't get stabilized.
- Imbalance of Propellers and motors on Quadcopter can produce unwanted vibration in Quadcopter frame and can distort the values coming from IMU i.e. from Accelerometer, Gyroscope and Magnetometer and thus cause instability in Quadcopter. Some methods for reducing these vibrations such as damping etc. have to be introduced.

3. Solution Domain

The following are the solution devised for the above mentioned problems

- In order to stabilize the Quadcopter, PID algorithm is implemented. PID stands for Proportional Integral Derivative. PID algorithm is generally used to stabilize an electrical signal or fluctuating value in field of electronics and aeronautics and thus it is used to stabilize the values of Yaw, Pitch and Roll generated as a result of control values transmitted from handheld controller via wireless units.
- We are using low power chip named "RF24" as wireless unit or device, it is a SPI device. "RF24" is a simplex communication device i.e. the wireless unit can only transmit at a time or receive at a time but advantage is that either wireless unit or RF24 can become transmitter or receiver via a scheduler routine and it supports retransmission, auto acknowledgement and error checking. Thus communication is error free and supports the telemetry operation required for Quadcopter.
- Several complicated algorithms are created to handle the signal loss and power loss situations.
- We are using "MPU9250" a 9DOF sensor as IMU, it has 3-axis Accelerometer, 3-axis Gyroscope and 3-axis Magnetometer on a single chip, it is I2C device.MPU9250 is calibrated by algorithms involving embedded system programming and raw measurement and thus IMU is calibrated successfully. For removing the drift from gyroscopic angular values we have implemented the open source sensor fusion algorithm such as complimentary filter and Madgwick filter in order to stabilize the Yaw, pitch and roll angular measurement
- Several methods are done to remove the vibration from Quadcopter's structure

4. SYSTEM REQUIREMENTS SPECIFICATIONS

4.1 System Domain

The following are the equipment required:

S.No	Equipment	Quantity
1	Arduino Nano	2
2	Electronic Speed Controller	4
3	Brushless DC Motor	4
4	LiPo battery	1
5	Inertial measurement unit	1
6	Quad copter frame	1

• Arduino Nano:



Arduino is a software company, project, and user community that designs and manufactures computer hardware, open, and microcontroller-based kits for building digital devices and interactive objects that can sense and control physical devices.

The project is based on microcontroller board designs, produced by several vendors, using various microcontrollers. These systems provide sets of digital and analog I/O pins that can interface to various expansion boards (termed *shields*) and other circuits. The boards feature serial communication interfaces, including Universal Serial Bus (USB) on some models, for loading programs from personal computers. For programming the microcontrollers, the Arduino project provides an integrated development environment(IDE) based on a programming language named *Processing*, which also supports the languages C and C++.

The first Arduino was introduced in 2005, aiming to provide a low cost, easy way for novices and professionals to create devices that interact with their environment using sensors and actuators. Common examples of such devices intended for beginner hobbyists include simple robots, thermostats, and motion detectors.

Arduino boards are available commercially in preassembled form, or as do-it-yourself kits. The hardware design specifications are openly available, allowing the Arduino boards to be produced by anyone.

• ESC or Electronic Speed Controller

An **electronic speed control** or **ESC** is an electronic circuit with the purpose to vary an electric motor's speed, its direction and possibly also to act as a dynamic brake. ESCs are often used on electrically powered radio controlled models, with the variety most often used for brushless motors essentially providing an electronically generated three-phase electric power low voltage source of energy for the motor.

An ESC can be a stand-alone unit which plugs into the receiver's throttle control channel or incorporated into the receiver itself, as is the case in most toy-grade R/C vehicles. Some R/C manufacturers that install proprietary hobby-grade electronics in their entry-level vehicles, vessels or aircraft use onboard electronics that combine the two on a single circuit.

ESCs are normally rated according to maximum current, for example, 25 amperes or 25 A. Generally, the higher the rating, the larger and heavier the ESC tends to be which is a factor

when calculating mass and balance in airplanes. Many modern ESCs support nickel metal hydride, lithium ion polymer and lithium iron phosphate batteries with a range of input and cut-off voltages. The type of battery and number of cells connected is an important consideration when choosing a Battery eliminator circuit (BEC), whether built into the controller or as a stand-alone unit. A higher number of cells connected will result in a reduced power rating and therefore a lower number of servos supported by an integrated BEC, if it uses a linear voltage regulator. A well designed BEC using a switching regulator should not have a similar limitation.



BLDC Motor:

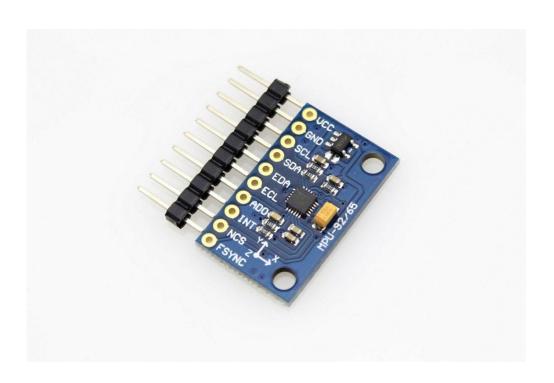
Brushless DC electric motor (BLDC motors, BL motors) also known as electronically commutated motors (ECMs, EC motors) are synchronous that are powered by a DC electric source via an integrated inverter/switching power supply, which produces an AC electric signal to drive the motor. In this context, AC, alternating current, does not imply a sinusoidal waveform, but rather a bi-directional current with no restriction on waveform. Additional sensors and electronics control the inverter output amplitude and waveform (and therefore percent of DC bus usage/efficiency) and frequency (i.e. rotor speed).



• IMU:

An inertial measurement unit (IMU) is an electronic device that measures and reports a body's specific force, angular rate, and sometimes the magnetic field surrounding the body, using a combination of accelerometers and gyroscopes, sometimes also magnetometers. IMUs are typically used to maneuver aircraft, including unmanned aerial vehicles(UAVs), among many others, and spacecraft, including satellites and landers. Recent developments allow for the production of IMU-enabled GPS devices. An IMU allows a GPS receiver to work when GPS-signals are unavailable, such as in tunnels, inside buildings, or when electronic interference is present

The IMU is the main component of inertial navigation systems used in aircraft, spacecraft, watercraft, drones, UAV and guided missiles among others.



5. IMPLEMENTATION

5.1 PID Algorithm

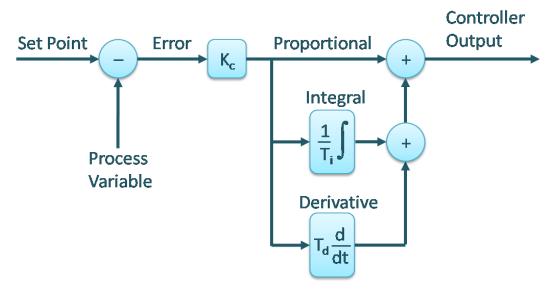


Fig: A block diagram of a PID controller in a feedback loop

A **proportional–integral–derivative controller** (**PID controller**) is a control loop feedback mechanism (controller) commonly used in industrial control systems. A PID controller continuously calculates an error value as the difference between a desired set point and a measured process variable. The controller attempts to minimize the error over time by adjustment of a control variable, such as the position of a control valve, a damper, or the power supplied to a heating element, to a new value determined by a weighted sum:

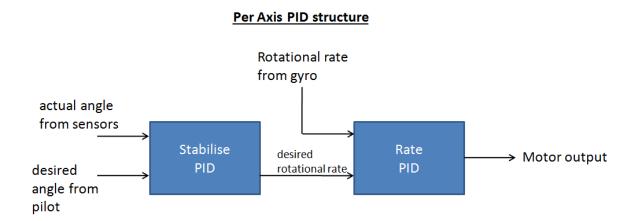
$$u(t) = K_p e(t) + K_i \int_0^t e(\tau) d\tau + K_d \frac{de(t)}{dt}$$

where K_{P} , K_{i} , and K_{d} , all non-negative, denote the coefficients for the proportional, integral, and derivative terms, respectively (sometimes denoted P, I, and D). In this model,

- *P* accounts for present values of the error. For example, if the error is large and positive, the control output will also be large and positive.
- *I* account for past values of the error. For example, if the current output is not sufficiently strong, error will accumulate over time, and the controller will respond by applying a stronger action.
- D accounts for possible future values of the error, based on its current rate of change. [1]

As a PID controller relies only on the measured process variable, not on knowledge of the underlying process, it is broadly applicable. By tuning the three parameters of the model, a PID controller can deal with specific process requirements. The response of the controller can be described in terms of its responsiveness to an error, the degree to which the system overshoots a set point, and the degree of any system oscillation. The use of the PID algorithm does not guarantee optimal control of the system or even its stability.

5.1.1 Control loop structure for Quadcopter



To have any kind of control over the quadcopter or multicopter, we need to be able to measure the quadcopter sensor output (for example the pitch angle), so we can estimate the error (how far we are from the desired pitch angle, e.g. horizontal, 0 degree). We can then apply the 3 control algorithms to the error, to get the next outputs for the motors aiming to correct the error.

The sensed position or angles is the process variable (PV). The desired position or desired angles from pilot/Remote Controller is called the set point (SP). The input to the process (the electric current in the motor) is the output from the PID controller. It is called either the manipulated variable (MV) or the control variable (CV). The difference between the present position and the set point is the error (e), which quantifies whether the angle is too low or too high and by how much.

By measuring the position (PV), and subtracting it from the set point (SP), the error (e) is found, and from it the controller calculates how much electric current to supply to the motor (MV). The obvious method is **proportional** control: the motor current is set in proportion to the existing error. A more complex control may include another term: **derivative** action. This considers the rate of change of error, supplying more or

less electric current depending on how fast the error is approaching zero. Finally, **integral** action adds a third term, using the accumulated position error in the past to detect whether the position of the mechanical arm is settling out too low or too high and to set the electrical current in relation not only to the error but also the time for which it has persisted. An alternative formulation of integral action is to change the electric current in small persistent steps that are proportional to the current error. Over time the steps accumulate and add up dependent on past errors; this is the discrete-time equivalent to integration.

If a controller starts from a stable state with zero error (PV = SP), then further changes by the controller will be in response to changes in other measured or unmeasured inputs to the process that affect the process, and hence the PV. Variables that affect the process other than the MV are known as disturbances. Generally, controllers are used to reject disturbances and to implement set point changes. A change in load on the arm constitutes a disturbance to the robot arm control process.

There are three parameters that a pilot can adjust to improve better quadcopter stability. These are the coefficients to the 3 algorithms we mentioned above. The coefficient basically would change the importance and influence of each algorithm to the output. Here we are going to look at what are the effects of these parameters to the stability of a quadcopter.

5.1.2 PID controller description

The PID control scheme is named after its three correcting terms, whose sum constitutes the manipulated variable (MV). The proportional, integral, and derivative terms are summed to calculate the output of the PID controller. Defining u(t) as the controller output, the final form of the PID algorithm is:

$$\mathbf{u}(t) = \mathbf{MV}(t) = K_p e(t) + K_i \int_0^t e(\tau) d\tau + K_d \frac{de(t)}{dt}$$

Where,

 $K_{p: Proportional gain, a tuning parameter}$

 K_{i} : Integral gain, a tuning parameter

 K_d : Derivative gain, a tuning parameter

e: Error = SP - PV

SP: Set Point

PV: Process Variable

t: Time or instantaneous time (the present)

 τ : Variable of integration; takes on values from time 0 to the present t.

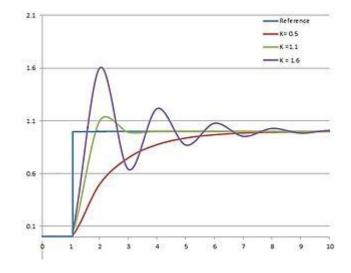
Equivalently, the transfer function in the Laplace Domain of the PID controller is

$$L(s) = K_p + K_i/s + K_d s$$

Where,

s: complex number frequency

5.1.3 Proportional term



Plot of PV vs time, for three values of K_p (K_i and K_d held constant)

The proportional term produces an output value that is proportional to the current error value. The proportional response can be adjusted by multiplying the error by a constant K_p , called the proportional gain constant.

The proportional term is given by:

$$P_{\text{out}} = K_p e(t)$$

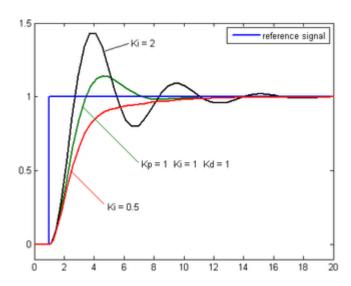
A high proportional gain results in a large change in the output for a given change in the error. If the proportional gain is too high, the system can become unstable. In contrast, a small gain results in a small

output response to a large input error, and a less responsive or less sensitive controller. If the proportional gain is too low, the control action may be too small when responding to system disturbances. Tuning theory and industrial practice indicate that the proportional term should contribute the bulk of the output change.

5.1.4 Steady-state error

Because a non-zero error is required to drive it, a proportional controller generally operates with a so-called *steady-state error*. Steady-state error (SSE) is proportional to the process gain and inversely proportional to proportional gain. SSE may be mitigated by adding a compensating bias term to the set point or output, or corrected dynamically by adding an integral term.

5.1.5 Integral term



Plot of PV vs time, for three values of K_i (K_p and K_d held constant)

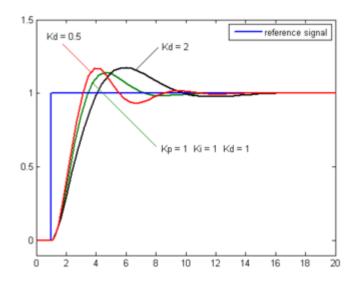
The contribution from the integral term is proportional to both the magnitude of the error and the duration of the error. The integral in a PID controller is the sum of the instantaneous error over time and gives the accumulated offset that should have been corrected previously. The accumulated error is then multiplied by the integral gain (K_i) and added to the controller output.

The integral term is given by:

$$I_{\text{out}} = K_i \int_0^t e(\tau) \, d\tau$$

The integral term accelerates the movement of the process towards set point and eliminates the residual steady-state error that occurs with a pure proportional controller. However, since the integral term responds to accumulated errors from the past, it can cause the present value to overshoot the set point value (see the section on loop tuning).

5.1.6 Derivative term



Plot of PV vs time, for three values of K_d (K_p and K_i held constant)

The derivative of the process error is calculated by determining the slope of the error over time and multiplying this rate of change by the derivative gain K_d . The magnitude of the contribution of the derivative term to the overall control action is termed the derivative gain, K_d .

The derivative term is given by:

$$D_{\rm out} = K_d \frac{de(t)}{dt}$$

Derivative action predicts system behavior and thus improves settling time and stability of the system. An ideal derivative is not causal, so that implementations of PID controllers include an additional low pass filtering for the derivative term, to limit the high frequency gain and noise Derivative action is seldom used in practice though - by one estimate in only 25% of deployed controllers- because of its variable impact on system stability in real-world applications

5.1.7 The effect of each parameter

The variation of each of these parameters alters the effectiveness of the stabilization. Generally, there are 3 PID loops with their own P I D coefficients, one per axis, so will have to set P, I and D values for each axis (pitch, roll and yaw).

To a quadcopter, these parameters can cause these behaviors.

- **Proportional Gain coefficient** Your quadcopter can fly relatively stable without other parameters but this one. This coefficient determines which is more important, human control or the values measured by the gyroscopes. The higher the coefficient, the higher the quadcopter seems more sensitive and reactive to angular change. If it is too low, the quadcopter will appear sluggish and will be harder to keep steady. You might find the multicopter starts to oscillate with a high frequency when P gain is too high.
- Integral Gain coefficient this coefficient can increase the precision of the angular position. For example, when the quadcopter is disturbed and its angle changes 20 degrees, in theory it remembers how much the angle has changed and will return 20 degrees. In practice if you make your quadcopter go forward and the force it to stop, the quadcopter will continue for some time to counteract the action. Without this term, the opposition does not last as long. This term is especially useful with irregular wind, and ground effect (turbulence from motors). However, when the I value gets too high your quadcopter might begin to have slow reaction and a decrease effect of the Proportional gain as consequence, it will also start to oscillate like having high P gain, but with a lower frequency.
- **Derivative Gain coefficient** this coefficient allows the quadcopter to reach more quickly the desired attitude. Some people call it the accelerator parameter because it amplifies the user input. It also decreases control action fast when the error is decreasing fast. In practice it will increase the reaction speed and in certain cases an increase the effect of the P gain.

5.1.8 Stability

If the PID controller parameters (the gains of the proportional, integral and derivative terms) are chosen incorrectly, the controlled process input can be unstable, i.e., its output diverges, with or without

oscillation, and is limited only by saturation or mechanical breakage. Instability is caused by *excess* gain, particularly in the presence of significant lag.

Generally, stabilization of response is required and the process must not oscillate for any combination of process conditions and set points, though sometimes marginal stability (bounded oscillation) is acceptable or desired.

Mathematically, the origins of instability can be seen in the Laplace domain.^[15] The total loop transfer function is:

$$H(s) = \frac{K(s)G(s)}{1 + K(s)G(s)}$$

where

K(s): PID transfer function

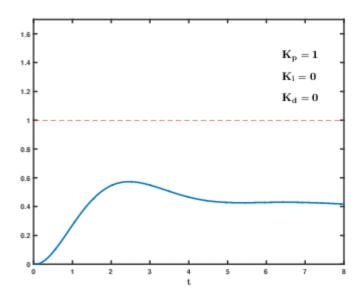
G(s): Plant transfer function

The system is called unstable where the closed loop transfer function diverges for some s.^[15] This happens for situations where K(s)G(s) = -1. Typically, this happens when |K(s)G(s)| = 1with a 180 degree phase shift. Stability is guaranteed when K(s)G(s) < 1for frequencies that suffer high phase shifts. A more general formalism of this effect is known as the Nyquist stability criterion.

5.1.9 Manual tuning

If the system must remain online, one tuning method is to first set K_i and K_d values to zero. Increase the K_p until the output of the loop oscillates, then the K_p should be set to approximately half of that value for a "quarter amplitude decay" type response. Then increase K_i until any offset is corrected in sufficient time for the process. However, too much K_i will cause instability. Finally, increase K_d , if required, until the loop is acceptably quick to reach its reference after a load disturbance. However, too much K_d will cause excessive response and overshoot. A fast PID loop tuning usually overshoots slightly to reach the set point more quickly; however, some systems cannot accept overshoot, in which case an

over-damped closed-loop system is required, which will require a K_{P} setting significantly less than half that of the K_{P} setting that was causing oscillation.



Effects of varying PID parameters (K_p,K_i,K_d) on the step response of a system.

Effects of increasing a parameter independently							
Parameter	Rise time	Overshoot	Settling time	Steady-state error	Stability		
K_p	Decrease	Increase	Small change	Decrease	Degrade		
K_i	Decrease	Increase	Increase	Eliminate	Degrade		
K_d	Minor change	Decrease	Decrease	No effect in theory	Improve if K_d small		

These gains apply to the ideal, parallel form of the PID controller. When applied to the standard PID form, the integral and derivative time parameters T_{i} and T_{d} are only dependent on the oscillation period T_{u} .

5.1.10 Tuning of quadcopter PID Gains

It is usually tune one parameter at a time start with P gain, I and then D gain.

For **P gain**, first start low and work way up, until noticing it producing oscillation. Fine tune it until you get to a point it's not sluggish and there is not oscillation.

For the **I gain**, again start low, and increase slowly. Roll and pitch your quad left and right, pay attention to the how long does it take to stop and stabilize. You want to get to a point where it stabilizes very quickly as you release the stick and it doesn't wander around for too long. You might also want to test it under windy condition to get a reliable I-value.

For **D** gain, it can get into a complicated interaction with P and I value. When using D gain, you need to go back and fine tune P and I to keep the plant well stabilized.

Quadcopters are symmetric so you can set the same PID Gain values for Pitch, and Roll. The value for Yaw is not as important as those of Pitch and Roll so it's probably OK to set the same values as for Pitch/Roll to start with (even it might not be the best). After your multicopter is relatively stable, you can start alter the Yaw gains. For non-symmetric multicopter like hexcopter or tricopter, you might want to fine tune the pitch and roll separately, after you have some flight experience.

5.1.11 IMU Data Fusing: Complementary, Madgwick Filter

An **inertial measurement unit**, or IMU, measures accelerations and rotation rates, and possibly earth's magnetic field, in order to determine a body's attitude. Two basic filter approaches are discussed, the **complementary filter** and the **Madgwick filter**. The article starts with some preliminaries, which I find relevant. It then considers the case of a single axis (called one dimensional or 1D). First the simplest method is discussed, where gyro bias is not estimated (called 1st order). Then gyro bias estimation is included (called 2nd order). Finally, the complete situation of three axes (called 3D) is considered, and some approximations and improvements are evaluated.

Notation: The discrete time step is denoted as Δt , and nor k is used as time-step index. The estimate of a quantity is indicated by a hat, e.g. \hat{x} , which will however often be dropped for simplicity, whenever confusion seems impossible. Bold symbols represent vectors or matrices in \mathbb{R}^3 (vectors and matrices in e.g. state space won't be bold), and quaternions.

5.1.12 Preliminaries

5.1.12.1 Kinematics and IMU Algorithms

The task of attitude estimation corresponds to evaluating (computationally) the kinematic equation for the rotation of a body:

$$\mathbf{\Omega}_{\times} = \boldsymbol{\omega} \mathbf{J} = \begin{pmatrix} 0 & -\omega_z & \omega_y \\ \omega_z & 0 & -\omega_x \\ -\omega_y & \omega_x & 0 \end{pmatrix}, \quad \text{Eq. (1.1)}$$

where $\boldsymbol{\omega} = (\omega_x, \omega_y, \omega_z)^T$ is the measured rotation rate vector. The rotation **R**represents the orientation of the body-fixed reference frame as observed in the earth reference frame. For any vector \mathbf{v} , the coordinates \mathbf{v}_{earth} with respect to the earth frame become in the body-fixed frame $\mathbf{v}_{body} = \mathbf{R}^T \mathbf{v}_{earth}$, which evolve as $\dot{\mathbf{v}}_{body} = \mathbf{\Omega}_{\times}^T \mathbf{v}_{body} = -(\boldsymbol{\omega} \times \mathbf{v}_{body})$ (the minus sign comes in here since $\boldsymbol{\omega}$ represents the rotation of the body-fixed coordinate system).

As simple as it may appear, equation Eq. (1.1) presents us with some fundamental issues:

- (1) Equation (1.1) is non-linear. This can complicate filter design enormously.
- (2) Equation (1.1) is susceptible to numerical errors. Well, numerical errors are present in any calculation performed on a microprocessor, but in most cases they are well-behaved in the sense that they do not accumulate. However, for Eq. (1) the errors continuously grow if no counter-measures are taken, and Reventually ceases to represent a rotation. Importantly, this is related to the global non-commutativity of rotations (in 3 dimensions) and hence is fundamental. It is here where cool buzz words such as direction cosine matrix (DCM) or quaternions enter the game.
- (3) The rotation **R** can be represented in several ways [RO], and each representation has its own set of advantages and disadvantages. Most well-known are the representations by a rotation matrix or DCM, Euler angles and related angles (Cardan, Tait-Brian), axis and angle, and

quaternions, but some more exist. Obviously, the algorithm will depend a lot on which representation is chosen.

You may note, no words were yet spent on measurement noise and data fusing; I haven't added it to the list since it's not really rooted in Eq. (1.1), although it's of course an important point – and in fact the topic of this article.

Anyhow, since the challenges are alike, all algorithms presented by the above authors exhibit a similar structure:

5.1.12.2 Discretization and Implementation Issues

Well, it's not big news that for a given system, described by e.g. a continuous-time transfer function G(s), there are many different possible implementations in computer code, and that they do not all show identical performance even though they are derived from one and the same function G(s).

One reason for arriving at different implementations is that there is no universal rule for converting a continuous- time transfer function G(s) to a discrete-time transfer function H(z), since it's approximate. The conversion from G(s) to H(z) is thus not unique, and typical choices are:

backward difference:
$$s = \frac{1}{\Delta t}(1 - z^{-1})$$
 Eq. (1.2)

bilinear transformation, expansion of
$$ln(z)$$
: $s = \frac{2}{\Delta t} \frac{1 - z^{-1}}{1 + z^{-1}}$, Eq. (1.3)

impulse invariance transformation:
$$\frac{G(z)}{1-z^{-1}} = Z\left(\frac{G(s)}{s}\right), \text{ Eq. (1.4)}$$

Another reason is that a given discrete-time transfer function H(z) can be implemented in different ways, and the different implementations possibly show different behavior in various aspects, such as stability and high-frequency noise. The topic is not simple, and is beyond my competences, but the basic principle is clear.

Let's consider as an example, since it's familiar, PID controller the $G(s) = K_p + \frac{1}{s}K_i + sK_d$ Using backward difference finds one $H(z)=K_p+rac{K_i\Delta t}{1-z^{-1}}+rac{K_d}{\Delta t}(1-z^{-1})$, which can be implemented by first evaluating $I_n = \frac{K_t \Delta t}{1-z^{-1}} x_{n}$ and then $y_n = K_p x_n + I_n + \frac{K_d}{\Delta t} (1-z^{-1}) x_n$, or by directly solving $y_n = H(z) x_n$. In the first case one obtains the **positional PID algorithm**

$$I_n = I_{n-1} + K_i \Delta t x_n$$
 Eq.(1.5a)

$$y_n = K_p x_n + I_n + \frac{K_d}{\Delta t} (x_n - x_{n-1})$$
 Eq. (1.5b)

while the second case leads to the velocity PID algorithm

$$y_n = y_{n-1} + K_p(x_n - x_{n-1}) + K_i \Delta t x_n + \frac{K_d}{\Delta t}(x_n + 2x_{n-1} - x_{n-2})$$
 Eq. (1.6)

Both derive from the same function H(z), or G(s), but differ e.g. with regards to wind up, overflow of internal variables, number of storage elements and so on.

Corollary #1: In the positional PID algorithm, Eq. (1.5), the order of the two equations can be reversed,

$$y_n = K_p x_n + I_{n-1} + \frac{K_d}{\Delta t} (x_n - x_{n-1})$$
 Eq.(1.7a)
 $I_n = I_{n-1} + K_i \Delta t x_n$ Eq.(1.7b)

with an irrelevant change of the parameter $K_p \to K_p + K_i \Delta t$. That is, the order of their execution or implementation in code is irrelevant.

5.1.12.3 1D IMU Data Fusing – 1st Order (without Drift Estimation)

In this chapter we will consider the simplest case of IMU data fusing, namely that of fusing the angles for a single axis as determined from the time-integrated rotation rate and accelerometer data, without explicitly estimating the gyro's drift. It has relevance for applications, but here it is of interest mainly as a "warm up", and because it provides some insight which will help us to better understand the more advanced cases below.

In the following, θ denotes the estimated angle), athe angle calculated from the accelerometer measurements, and ω the rotation rate measured by the gyro.

Complementary Filter

The complementary filter fuses the accelerometer and integrated gyro data by passing the former through a 1st-order low pass and the latter through a 1st-order high pass filter and adding the outputs. The transfer function reads

$$\theta = \frac{1}{1+Ts}a + \frac{Ts}{1+Ts}\frac{1}{s}\omega = \frac{a+T\omega}{1+Ts}$$
Eq. (2.1)

where T determines the filter cut-off frequencies. Using backward difference yields.

$$1 + Ts = (1 + \frac{T}{\Delta t}) - \frac{T}{\Delta t}z^{-1}$$

Insertion into Eq. (2.1) and rearrangement leads to our final result

$$\theta_k = \alpha(\theta_{k-1} + \omega_k \Delta t) + (1 - \alpha)a_k$$
 Eq. (2.2)

where $\alpha = \frac{T}{\Delta t}/(1 + \frac{T}{\Delta t})$. This relation can be implemented in code in several ways; three of them were discussed in [SC] (though only #3 makes sense). For better comparison with the other cases below, the result is reformulated as

$$\theta_k = \alpha \theta_{k-1} + (1 - \alpha)a_k + \alpha \omega_k \Delta t$$
 Eq. (2.3)

• Madgwick Filter

Here data fusing is done with a P controller and an integrating process, where the "accelerometer" angle abecomes the set point and the rotation rate ω a disturbance (of type d_1). The transfer function is thus

$$\theta = K_p \frac{1}{s} (a - \theta) + \frac{1}{s} \omega$$
 Eq. (2.7)

where $a - \theta$ is the error input to the P controller. Rearranging this equation for θ yields exactly the transfer function of the complementary filter, Eq. (2.1), which from standard arguments of control theory is however not surprising.

The controller Eq. (2.7) is usually implemented by first rearranging it to $\theta = \frac{1}{s} [K_p(a-\theta) + \omega]$, then separating it into $e = a - \theta$ and $\theta = \frac{1}{s} (K_p e + \omega)$, and finally discretizing it as

$$e_k = a_k - \theta_{k-1}$$

 $\theta_k = \theta_{k-1} + (K_p e_k + \omega_k) \Delta t$ Eq. (2.8)

That is, for the Madgwick filter one arrives at the update law

$$\theta_k = \alpha \theta_{k-1} + (1 - \alpha)a_k + \omega_k \Delta t$$
 Eq. (2.9)

with $\alpha = 1 - K_p \Delta t$.

It is worthwhile to elaborate a bit further on the controller aspect. For a (simple) controller on finds in general that

$$y = \frac{G_c G_p}{1 + G_c G_p} r + \frac{G_p}{1 + G_c G_p} d_1 + \frac{1}{1 + G_c G_p} d_2$$
 Eq. (2.10)

where $G_c(s)$ and $G_p(s)$ are the controller and process transfer functions, respectively (the other symbols should be obvious). The conversion of the complementary filter transfer function, Eq. (2.1), into the controller form, Eq. (2.7), is accomplished by multiplying the nominator and denominator in Eq. (2.1) by 1/s:

$$\theta = \frac{1}{1 + Ts} a + \frac{Ts}{1 + Ts} \frac{1}{s} \omega = \frac{K_p \frac{1}{s}}{1 + K_p \frac{1}{s}} a + \frac{\frac{1}{s}}{1 + K_p \frac{1}{s}} \omega$$
 Eq. (2.11)

and identifying $G_c(s) = K_p = 1/T_{\text{and}} G_p(s) = 1/s$. Equations (2.1) and (2.7) are identical, but the former is expressed in terms of polynomials in swhile the latter is expressed in terms of polynomials in 1/s.

• Comparison and Conclusions

A couple of observations can be made from the above findings.

- (1) The complementary and Madgwick filters are described by identical transfer functions.
- (2) From (1) it follows that all three filters are identical at the level of the transfer function.
- (3) Despite the algorithm of the Madgwick filter is **not** identical to that of the complementary and/ see Eq. (2.9) and Eqs. (2.2), (2.6).

It is worthwhile to discuss the last point further. For convenience the two update laws are reproduced:

$$\theta_k = \alpha \theta_{k-1} + (1 - \alpha)a_k + \alpha \omega_k \Delta t$$
 Eqs. (2.2),(2.6)
$$\theta_k = \alpha \theta_{k-1} + (1 - \alpha)a_k + \omega_k \Delta t$$
 Eq. (2.9)

One can look at the difference in two ways. Firstly, Eqs. (2.2,6) may be read to say that the angle is first advanced by integrating the rotation rate to give an updated angle and then filtered with a_k to give an improved angle. This may be expressed by the bracketing $\theta_k = \alpha[\theta_{k-1} + \omega_k \Delta t] + (1-\alpha)a_k$. In contrast, Eq. (2.9) may be read to say that the angle is first filtered with a_k and then advanced by integrating the rotation rate, corresponding to the bracketing $\theta_k = [\alpha \theta_{k-1} + (1-\alpha)a_k] + \omega_k \Delta t$. Secondly, the equations can be rearranged into the algorithms.

complementary filter (1D, 1st order) Madgwick filter (1D, 1st order)

$$\theta_k^- = \theta_{k-1} + \omega_k \Delta t \qquad \text{Eq. (2.12)}$$

$$\theta_k^- = \theta_{k-1} + \omega_k \Delta t \qquad \text{Eq. (2.13)}$$

$$e_k^- = a_k - \theta_k^- \qquad \qquad e_k = a_k - \theta_{k-1}$$

$$\theta_k = \theta_k^- + K_0 e_k^- \qquad \qquad \theta_k = \theta_k^- + K_p \Delta t e_k$$

They are essentially identical, except of the important difference that on the left the feedback error uses the updated angle θ_k^- while on the right it uses the previous angle estimate θ_{k-1} ! The two algorithms cannot be directly converted into each other, even though they derive from the

same transfer function, which should be considered a characteristic feature expressing the different underlying "philosophies".

5.1.12.4 1D IMU Data Fusing – 2nd Order (with Drift Estimation)

In this chapter the single-axis filters will be improved by explicitly taking into account the bias/drift of the gyro sensors. To the best of my knowledge, a complementary filter accomplishing this task has not been described before, and hence the order of the discussion of the filters is changed as compared to Chapter 2.

Madgwick Filter

The gyro drift estimation is facilitated by using a PI controller [RM08], and the transfer function is accordingly

$$\theta = \left(K_p + K_i \frac{1}{s}\right) \frac{1}{s} (a - \theta) + \frac{1}{s} \omega$$
Eq. (3.5)

Following again the standard implementation (positional PID algorithm) one separates Eq. (3.5) into $e = a - \theta$, $I = K_i \frac{1}{s} e$, and $\theta = \frac{1}{s} (K_p e + I + \omega)$, and discretizes it as

$$e_k = a_k - \theta_{k-1}$$

$$I_k = I_{k-1} + K_i \Delta t e_k$$

$$\theta_k = \theta_{k-1} + (K_p e_k + I_k + \omega_k) \Delta t$$
Eq. (3.6)

This results in the update laws

$$I_k = I_{k-1} + K_i \Delta t (a_k - \theta_{k-1})$$

$$\theta_k = \alpha \theta_{k-1} + (1 - \alpha) a_k + (\omega_k + I_k) \Delta t$$
 Eq. (3.7)

with $\alpha = 1 - K_p \Delta t$.

Here Corollary #1 is recalled, which tells that the sequence of the two equations in Eq. (3.7) can be reversed (with an insignificant parameter change).

Complementary Filter

A complementary filter is easily derived by solving the transfer function of the Madgwick filter for the angle θ , which yields

$$\theta = \frac{1 + \frac{K_p}{K_i}s}{1 + \frac{K_p}{K_i}s + \frac{1}{K_i}s^2} a + \frac{\frac{1}{K_i}s^2}{1 + \frac{K_p}{K_i}s + \frac{1}{K_i}s^2} \frac{1}{s} \omega$$
 Eq. (3.10)

Obviously, and not unexpectedly, this complementary filter is built from 2nd order filters. Note that the filter acting on the acceleration data actually consists of a low-pass plus band-pass filter.

This result has interesting consequences. Being 2^{nd} order filters, the frequency response of the acceleration and rotation rate filters are characterized by the resonance frequency and damping factor

$$\xi = \frac{K_p}{2\sqrt{K_i}}$$
 Eq. (3.11)

The damping factor determines the overshoot at the resonance frequency. For high-pass (and low-pass) filters the frequency response is flat (and the step response non-oscillatory) for $\xi \ge 1$. This suggests the criterion

$$K_i \le \frac{1}{4}K_p^2$$
 Eq. (3.12)

in order to avoid overshoot in the gyro channel. In order to minimize also overshoot in the accelerometer channel, the damping should be somewhat larger than that; $\xi \approx 2$ might be a good compromise between smooth frequency response and fast bias estimation. Accordingly, as a rule of thumb $K_i \approx 0.05 \dots 0.1 \, K_p^2$.

Note that – unless K_i is set to very small values – the crossover frequency is determined now by K_i (or the inverse square root of it), and not by K_p in the 1st order case! It could in fact be appropriate to use the parameters ω_{00} $T = 2\pi/\sqrt{K_i}$ and $\xi_{instead}$ of K_p and K_i ; the tuning of the filter might be more intuitive to the user.

The complementary filter may be implemented as in Eq. (3.6), or with any of the algorithms used with advantage for digital filters. The direct form II would be a typical choice

• Summary on 1D Filters

As lengthy as it was, the above detailed discussion in chapters 2 and 3 of different approaches to the data fusing for a single axis result in a very short summary:

The three considered different approaches are in fact not that different, even in the 2nd order case.

As a bonus a criterion for the choice of the bias estimator gain K_i or K_1 , respectively, has been obtained, as well as a potentially easier and/or more flexible direct implementation as a complementary filter.

There is a difference between the Kalman and Mahony&Madgwick filters in how the error is calculated. This may be interpreted as conceptually different "philosophies", but besides that it's not clear to me if this has also practical consequences, such as different stability properties or high-frequency noise. (Does anyone know?)

5.1.12.5 Further 3D Filters

Madgwick's IMU Filter

Madgwick has presented an interesting approach, which is based on formulating task T3 as a minimization problem and solving it with a gradient technique [SM]. I will argue here that this approach is – IMHO – not appropriate for IMUs which are using only gyro and accelerometer data (6DOF IMU).

Madgwick uses a quaternion approach to represent the attitude, which immediately poses the problem of how to convert the measured acceleration vector ainto a quaternion. Madgwick has described the problem in clear detail: A body's attitude (quaternion) cannot be unambiguously represented by a direction (vector) since any rotation of the body around that

direction gives the same vector but a different quaternion. The solution manifold is a "line "and not a "point ". Or plainly: The body's yaw angle is totally undetermined.

To tackle this problem he suggested to determine that rotation, which brings the gravity vector $\mathbf{g}^{earth} = -\mathbf{e}_z$ in the earth frame in coincidence with the measured acceleration $\mathbf{g}^{body} = \mathbf{a}$ in the body frame, that is to find the rotation \mathbf{R}_a for which $\mathbf{a} = -\mathbf{R}_a^T \mathbf{e}_z$, or the quaternion \mathbf{q}_a for which $\mathbf{a} = -\mathbf{q}_a^{-1} \mathbf{e}_z \mathbf{q}_a$, respectively. Converting the measured vector to a quaternion is very desirable since then data fusing could be done directly on quaternions, which has favorable mathematical properties [RO2]. In order to determine this rotation computationally, Madgwick suggested to formulate it as minimization problem and to solve it iteratively by the method of steepest decent.

This approach has two problems. The exact solution is not unique but there are infinitely many, and not the exact solution is calculated. One can hence expect that the yaw angle in the computed attitude \mathbf{q}_{ais} not only arbitrary, but determined by the noise introduced by the incomplete steepest decent. The yaw angle fluctuates.

At this point one could analyze the algorithm by asking: Let's assume that our gyro and accelerometer data is perfect and exact, what is then the algorithm doing? Clearly, one would expect the algorithm to produce the exact attitude, and the data fusing filter not to introduce any corrections. For the filters described in the above this is obviously fulfilled. In Madgwick's filter, the correction step δs however not zero (since $a = -q^{-1}e_zq$). That is, the filter in fact pushes the estimated attitude away from the correct attitude. In conclusion this is a signature of the noise mentioned before.

6 TESTING METHODOLOGY

6.1 Range Test

Range test was conducted to check the signal range between the remote controller and Quadcopter. In the test performed, various obstacles are introduced between wireless units on Quadcopter and Remote Controller, in which the communication seems to be unaffected with respect to clean line of sight communication.

6.2 IMU Test

IMU or Inertial measurement unit is tested while it is being calibrated. In testing phase, a number of tests were carried out to calibrate the IMU (3 – axis Accelerometer, 3- axis Gyroscope) by placing it on perpendicular and parallel surfaces with respect to ground. And also various sensitivity factors were varied (i.e. sensitivity factors of Accelerometer and Gyroscope) were varied to produce optimum readings from gyroscope and accelerometer.

6.3 PID Tuning

The various gain coefficients like proportional gain, derivative gain and Integral gain coefficients were adjusted to stabilize the vibrations and angular values such as Yaw, Pitch and Roll.

6.4 Propeller Balancing

Various methods were applied to remove imbalance in propellers which includes setting of Digital Low Pass Filter in IMU at 5 Hz.

7 CONCLUSION

7.1 Summary

Our Quadcopter was able to fly with stable angular values of Yaw, Pitch and Roll. We have used Arduino Nano board which has ATMEGA 328P microcontroller which does all the implemented operations despite operating on very low power.

We have used NRF24L01+ wireless chip which works on low power with consuming only 3.3 Volts which produce a feasible result that is the range test is done successfully.

We have used a single chip Inertial Measurement Unit (IMU) to measure the angular values which results in stable operations of Quadcopter.

7.2 Limitations

Because the microcontrollers internal flash memory is 32K in which bootloader acquires 1K and a code acquires approximately 29K and rest of the memory is used for dynamic memory allocation for variables the algorithms such as power loss and impulse detection were not yet implemented.

7.3 Recommended for future work

In future version of our Quadcopter the power loss and impulse detection algorithm will be implemented and also we will attach computer vision based processing to the Quadcopter which will use some Artificial Intelligence algorithms to do certain tasks.

8 CODE

```
9 #include "quadcopter_config.h"
10 #include <PID v1.h>
11 #include <Servo.h>
12 #include <Wire.h>
13 #include"RF24.h"
14
15
16 float angleX, angleY, angleZ = 0.0;
17
18 int throttle=THROTTLE RMIN;
19
20
21
22 double pid roll in, pid roll out, pid roll setpoint = 0;
23 double pid_pitch_in, pid_pitch_out, pid_pitch_setpoint = 0;
24 double pid yaw in, pid yaw out, pid yaw setpoint = 0;
25
26
27 int m0, m1, m2, m3;
28
29
30
31 void setup()
32 {
33
34
     Serial.begin(115200);
35
      if(Serial.available())
36
       Serial.println("Debug Output ON");
37
38
   motors initialize();
39
40
41
   pinMode(PIN LED, OUTPUT);
42
   digitalWrite(PIN LED, LOW);
43
44
45
46
   rx Initialize();
47 pid initialize();
48
   motors arm();
49
    imu setup();
50
51 }
52
53 void loop()
54 {
55
   receiver update();
56
   imu loop();
57
    control update();
58
59
```

```
60 }
61 void control update(){
62
      throttle=map(packet rx.throttle, THROTTLE RMIN, THROTTLE RMAX, MOTOR ZER
      O LEVEL, MOTOR MAX LEVEL);
63
64
65
     setpoint update();
66
     pid update();
67
     pid compute();
68
69
     m0 = throttle + pid pitch out - pid roll out + pid yaw out;
     m1 = throttle + pid pitch out + pid roll out - pid yaw out;
70
71
     m2 = throttle - pid pitch out + pid roll out + pid yaw out;
72
     m3 = throttle - pid pitch out - pid roll out - pid yaw out;
73
74
     if(throttle < THROTTLE SAFE SHUTOFF)</pre>
75
76
         m0 = m1 = m2 = m3 = MOTOR ZERO LEVEL;
77
78
79
    update motors (m0, m1, m2, m3);
80
     m0=0;
81
     m1=0;
82
     m2=0;
     m3=0;
83
84 }
85
86
87 void setpoint update() {
88
89
     if(packet rx.roll > 508 - 20 && packet rx.roll < 508 + 20)
90
       pid roll setpoint = 0;
91
     else
92
       pid roll setpoint =
     map(packet rx.roll,ROLL_RMIN,ROLL_RMAX,ROLL_WMIN,ROLL_WMAX);
93
94
95
96
     if(packet rx.pitch > 508 - 20 && packet rx.pitch < 508 + 20)
97
       pid pitch setpoint = 0;
98
     else
99
       pid pitch setpoint =
     map(packet rx.pitch,PITCH RMIN,PITCH RMAX,PITCH WMIN,PITCH WMAX);
100
101
102
     if(packet rx.yaw > 522 - 20 && packet rx.yaw < 522 + 20)</pre>
103
       pid yaw setpoint = 0;
104
     else
105
       pid yaw setpoint =
      map(packet rx.yaw,YAW RMIN,YAW RMAX,YAW WMIN,YAW WMAX);
106
107
       Serial.println();
```

```
Serial.println(pid roll setpoint);
108
109
       Serial.println(pid pitch setpoint);
       Serial.println(pid yaw setpoint);
110
111 }
112
113
114 Servo motor0;
115 Servo motor1;
116 Servo motor2;
117 Servo motor3;
118
119 void motors initialize() {
120 motor0.attach(PIN MOTOR0);
121 motor1.attach(PIN MOTOR1);
122 motor2.attach(PIN MOTOR2);
123 motor3.attach(PIN MOTOR3);
124 motor0.writeMicroseconds(MOTOR_ZERO_LEVEL);
125 motor1.writeMicroseconds(MOTOR ZERO LEVEL);
126 motor2.writeMicroseconds(MOTOR ZERO LEVEL);
    motor3.writeMicroseconds(MOTOR ZERO LEVEL);
127
128 }
129
130 void motors arm() {
131 motor0.writeMicroseconds (MOTOR ZERO LEVEL);
132 motor1.writeMicroseconds(MOTOR ZERO LEVEL);
133 motor2.writeMicroseconds(MOTOR ZERO LEVEL);
134 motor3.writeMicroseconds (MOTOR ZERO LEVEL);
135
     delay(3000);
136 }
137
138 void update motors (int m0, int m1, int m2, int m3)
139 {
140
    /*motor0.writeMicroseconds(m0);
141
     motor1.writeMicroseconds(m1);
142 motor2.writeMicroseconds(m2);
143
    motor3.writeMicroseconds(m3);
144
    Serial.print("\t Front left :");
145
146
    Serial.print(m0);
147
     Serial.print("\t Front Right :");
148 Serial.print(m1);
     Serial.print("\t Rear left :");
149
150 Serial.print(m3);
     Serial.print("\t Rear Right :");
151
152
     Serial.print(m2);
153
     Serial.println();
154 }
155
156
157
158
159
160
```

```
161 #include < SPI.h >
162
163
164
165 RF24 rx(7,8);
166 byte addresses[][6]={"tx","rx"};
167
168 struct packet
169 {
170
    int throttle;
171 int yaw;
172
    int roll;
173 int pitch;
174 } packet rx;
175
176 void rx Initialize() {
177 // Serial.begin(115200); used for debugging
178
179 rx.begin();
180 rx.setChannel(115);
181 rx.setDataRate(RF24 250KBPS);
182 rx.setPALevel(RF24 PA LOW);
183 rx.openWritingPipe(addresses[1]);
184 rx.openReadingPipe(1,addresses[0]);
185 rx.startListening();
186 rx.setAutoAck(0);
187 rx.setCRCLength(RF24_CRC_16);
188
189 }
190
191
192 void receiver update(){
193
     if(rx.available())
194
       while(rx.available())
195
196
         {rx.read(&packet rx, sizeof(packet rx));
197
     }
198
199
200
     }
201
202
     Serial.print(packet rx.throttle);
203 Serial.print("\t");
204
     Serial.print(packet rx.yaw);
     Serial.print("\t");
205
206 Serial.print(packet rx.pitch);
207
    Serial.print("\t");
208
     Serial.print(packet rx.roll);
209
     Serial.print("\t");
210
211 }
212
213
```

```
214
215:
216
217 // MPU9250 VCC - Arduino VCC
218 // MPU9250 GND - Arduino GND
219 // MPU9250 I2C SCL - Arduino I2C SCL
220 // MPU9250 I2C SCL - Arduino I2C SDA
221
222
223
224
225 // Arduino code ( GYRO + Accelerometer)
226
227 #include <SPI.h>
228 #include <Wire.h>
229
230 #define AK8963 ADDRESS
                             0x0C
231 #define WHO AM I AK8963 0x00 // should return 0x48
232 #define INFO
                             0x01
233 #define AK8963 ST1
                             0x02
                                  // data ready status bit 0
234 \#define AK8963 XOUT L 0x03 // data
235 #define AK8963 XOUT H 0x04
236 #define AK8963 YOUT L 0x05
237 #define AK8963 YOUT H 0x06
238 #define AK8963 ZOUT L
                          0 \times 07
239 #define AK8963 ZOUT H 0x08
240 #define AK8963 ST2
                             0x09 // Data overflow bit 3 and data read
      error status bit 2
241 #define AK8963 CNTL
                             0x0A // Power down (0000), single-measurement
      (0001), self-test (1000) and Fuse ROM (1111) modes on bits 3:0
                             0x0C // Self test control
242 #define AK8963 ASTC
243 #define AK8963 I2CDIS
                             0x0F // I2C disable
244 #define AK8963 ASAX
                             0x10 // Fuse ROM x-axis sensitivity adjustment
      value
245 #define AK8963 ASAY
                             0x11
                                  // Fuse ROM y-axis sensitivity adjustment
      value
                             0x12 // Fuse ROM z-axis sensitivity adjustment
246 #define AK8963 ASAZ
247 #define XG OFFSET H 0x13 // User-defined trim values for gyroscope
248 #define XG OFFSET L 0x14
249 #define YG OFFSET H 0x15
250 #define YG OFFSET L 0x16
251 #define ZG OFFSET H 0x17
252 #define ZG OFFSET L 0x18
253 #define SMPLRT DIV 0x19
254 #define CONFIG 0x1A
255 #define GYRO CONFIG 0x1B
256 #define ACCEL CONFIG 0x1C
257 #define ACCEL CONFIG2 0x1D
258 #define LP ACCEL ODR 0x1E
259 #define WOM THR 0x1F
260 #define MOT DUR 0x20 // Duration counter threshold for motion interrupt
      generation, 1 kHz rate, LSB = 1 ms
```

```
261 #define ZMOT THR 0x21 // Zero-motion detection threshold bits [7:0]
262 #define ZRMOT DUR 0x22 // Duration counter threshold for zero motion
      interrupt generation, 16 Hz rate, LSB = 64 ms
263 #define FIFO EN 0x23
264 #define I2C MST CTRL 0x24
265 #define I2C SLV0 ADDR 0x25
266 #define I2C SLV0 REG 0x26
267 #define I2C SLV0 CTRL 0x27
268 #define I2C SLV1 ADDR 0x28
269 #define I2C SLV1 REG 0x29
270 #define I2C SLV1 CTRL 0x2A
271 #define I2C SLV2 ADDR 0x2B
272 #define I2C SLV2 REG 0x2C
273 #define I2C SLV2 CTRL 0x2D
274 #define I2C SLV3 ADDR 0x2E
275 #define I2C SLV3 REG 0x2F
276 #define I2C SLV3 CTRL 0x30
277 #define I2C SLV4 ADDR 0x31
278 #define I2C SLV4 REG 0x32
279 #define I2C SLV4 DO 0x33
280 #define I2C SLV4 CTRL 0x34
281 #define I2C SLV4 DI 0x35
282 #define I2C MST STATUS 0x36
283 #define INT PIN CFG 0x37
284 #define INT ENABLE 0x38
285 #define DMP INT STATUS 0x39 // Check DMP interrupt
286 #define INT STATUS 0x3A
287 #define ACCEL XOUT H 0x3B
288 #define ACCEL XOUT L 0x3C
289 #define ACCEL YOUT H 0x3D
290 #define ACCEL YOUT L 0x3E
291 #define ACCEL ZOUT_H 0x3F
292 #define ACCEL ZOUT L 0x40
293 #define TEMP OUT H 0x41
294 #define TEMP OUT L 0x42
295 #define GYRO XOUT H 0x43
296 #define GYRO XOUT L 0x44
297 #define GYRO YOUT H 0x45
298 #define GYRO YOUT L 0x46
299 #define GYRO ZOUT H 0x47
300 #define GYRO ZOUT L 0x48
301 #define EXT SENS DATA 00 0x49
302 #define EXT SENS DATA 01 0x4A
303 #define EXT SENS DATA 02 0x4B
304 #define EXT SENS DATA 03 0x4C
305 #define EXT SENS DATA 04 0x4D
306 #define EXT SENS DATA 05 0x4E
307 #define EXT SENS DATA 06 0x4F
308 #define EXT SENS DATA 07 0x50
309 #define EXT SENS DATA 08 0x51
310 #define EXT SENS DATA 09 0x52
311 #define EXT SENS DATA 10 0x53
312 #define EXT SENS DATA 11 0x54
```

```
313 #define EXT SENS DATA 12 0x55
314 #define EXT SENS DATA 13 0x56
315 #define EXT SENS DATA 14 0x57
316 #define EXT SENS DATA 15 0x58
317 #define EXT SENS DATA 16 0x59
318 #define EXT SENS DATA 17 0x5A
319 #define EXT SENS DATA 18 0x5B
320 #define EXT SENS DATA 19 0x5C
321 #define EXT SENS DATA 20 0x5D
322 #define EXT SENS DATA 21 0x5E
323 #define EXT SENS DATA 22 0x5F
324 #define EXT SENS DATA 23 0x60
325 #define MOT DETECT STATUS 0x61
326 \# define I2C SLV0 DO 0x63
327 #define I2C SLV1 DO 0x64
328 #define I2C SLV2 DO 0x65
329 #define I2C SLV3 DO 0x66
330 #define I2C MST DELAY CTRL 0x67
331 #define SIGNAL PATH RESET 0x68
332 #define MOT DETECT CTRL 0x69
333 #define USER CTRL 0x6A // Bit 7 enable DMP, bit 3 reset DMP
334 #define PWR MGMT 1 0x6B // Device defaults to the SLEEP mode
335 #define PWR MGMT 2 0x6C
336 \#define DMP BANK 0x6D // Activates a specific bank in the DMP
337 \#define DMP RW PNT 0x6E // Set read/write pointer to a specific start
      address in specified DMP bank
338 #define DMP REG 0x6F // Register in DMP from which to read or to which
      to write
339 \# define DMP REG 1 0x70
340 #define DMP REG 2 0x71
341 #define FIFO COUNTH 0x72
342 #define FIFO COUNTL 0x73
343 #define FIFO R W 0x74
344 #define WHO AM I MPU9250 0x75 // Should return 0x71
345 #define XA OFFSET H 0x77
346 #define XA OFFSET L 0x78
347 #define YA OFFSET H 0x7A
348 #define YA OFFSET L 0x7B
349 #define ZA OFFSET H 0x7D
350 #define ZA OFFSET L 0x7E
             MPU9250 ADDRESS
                                           0x68
351 #define
352
353
354
355 #define
            GYRO FULL SCALE 250 DPS
                                           0x00
356 #define GYRO FULL SCALE 500 DPS
                                           0x08
             GYRO FULL SCALE 1000 DPS
357 #define
                                           0x10
358 #define
             GYRO FULL SCALE 2000 DPS
                                          0x18
359
             ACC FULL SCALE 2 G
360 #define
                                          0x00
361 #define
            ACC FULL SCALE 4 G
                                          0x08
             ACC FULL SCALE 8 G
362 #define
                                          0x10
363 #define
              ACC FULL SCALE 16 G
                                          0x18
```

```
364
365 enum Ascale {
366 \, AFS \, 2G = 0,
367 AFS 4G,
368 AFS 8G,
369 AFS 16G
370 };
371 enum Gscale {
372 \, \text{GFS} \, 250 \, \text{DPS} = 0,
373 GFS 500DPS,
374 GFS 1000DPS,
375 GFS 2000DPS
376 };
377
378 enum Mscale {
379 MFS 14BITS = 0, // 0.6 mG per LSB
380 MFS_16BITS // 0.15 mG per LSB
381 };
382
383
384
385 uint8 t Gscale = GFS 250DPS;
386 uint8 t Ascale = AFS 2G;
387 uint8 t Mscale = MFS 16BITS; // Choose either 14-bit or 16-bit
      magnetometer resolution
                                 // 2 for 8 Hz, 6 for 100 Hz continuous
388 uint8 t Mmode = 0x02;
      magnetometer data read
389 float aRes, gRes, mRes;
                              // scale resolutions per LSB for the
      sensors
390
391
392
393
394
395 int16 t magCount[3]; // Stores the 16-bit signed magnetometer sensor
      output
396
     // Factory mag calibration
397 int16 t accelCount[3]; // Stores the 16-bit signed accelerometer sensor
      output
398 int16 t gyroCount[3]; // Stores the 16-bit signed gyro sensor output
399 float magCalibration[3] = {0,0,0};
400 float magBias[3] = \{290.71, 111.07, -76.17\};
401//float magBias[3] = \{150.61, 165.72, -160.80\};
402 \text{ float gyroBias}[3] = \{1.09, -1.8, 2.4\}, \text{ accelBias}[3] = \{0.01013, 0.01801, 0.01801\}
      -0.00537}; // Bias corrections for gyro and accelerometer
403
404
405 float GyroMeasError = PI * (40.0f / 180.0f); // gyroscope measurement
      error in rads/s (start at 40 deg/s)
406 float GyroMeasDrift = PI * (0.0f / 180.0f); // gyroscope measurement
      drift in rad/s/s (start at 0.0 deg/s/s)
407 // There is a tradeoff in the beta parameter between accuracy and
      response speed.
```

```
408 // In the original Madgwick study, beta of 0.041 (corresponding to
      GyroMeasError of 2.7 degrees/s) was found to give optimal accuracy.
409 // However, with this value, the LSM9SD0 response time is about 10
      seconds to a stable initial quaternion.
410 // Subsequent changes also require a longish lag time to a stable
      output, not fast enough for a quadcopter or robot car!
411 // By increasing beta (GyroMeasError) by about a factor of fifteen, the
      response time constant is reduced to ~2 sec
412 // I haven't noticed any reduction in solution accuracy. This is
      essentially the I coefficient in a PID control sense;
413 // the bigger the feedback coefficient, the faster the solution
      converges, usually at the expense of accuracy.
414 // In any case, this is the free parameter in the Madgwick filtering and
      fusion scheme.
415 float beta = sqrt(3.0f / 4.0f) * GyroMeasError; // compute beta
416 float zeta = sqrt(3.0f / 4.0f) * GyroMeasDrift; // compute zeta, the
      other free parameter in the Madgwick scheme usually set to a small or
      zero value
417 #define Kp 2.0f * 5.0f // these are the free parameters in the Mahony
      filter and fusion scheme, Kp for proportional feedback, Ki for
      integral
418 #define Ki 0.0f
419
420 float pitch, yaw, roll;
421
422
                                       // integration interval for
423 \text{ float deltat} = 0.0 \text{f, sum} = 0.0 \text{f;}
      both filter schemes
424 uint32 t lastUpdate = 0, firstUpdate = 0; // used to calculate
      integration interval
425 \text{ uint} 32 \text{ t Now} = 0;
426 \text{ uint } 32 \text{ t delt t = 0, count = 0, sumCount = 0; } // \text{ used to control}
      display output rate
427 double ax=0, ay=0, az=0, gx=0, gy=0, gz=0, pitch1, roll1, gxint=0,
      qyint=0,xf,yf,zf,mx, my, mz;; // variables to hold latest sensor data
      values
428 double yawc;
429 float q[4] = \{1.0f, 0.0f, 0.0f, 0.0f\}; // vector to hold quaternion 430 float eInt[3] = \{0.0f, 0.0f, 0.0f\}; // vector to hold integral
      error for Mahony method
431 void imu setup()
432 {
433
434 Wire.begin();
435 //Serial.begin(115200);
436 getAres();
437 getGres();
438
      getMres();
439 Serial.println(" Calibrate gyro and accel");
440 // calibrateMPU9250 (gyroBias, accelBias);
441 //Serial.println("accel biases (mg)");
      Serial.println(1000.*accelBias[0]);
```

```
Serial.println(1000.*accelBias[1]);
      Serial.println(1000.*accelBias[2]);
442 //Serial.println("gyro biases (dps)"); Serial.println(gyroBias[0]);
      Serial.println(gyroBias[1]); Serial.println(gyroBias[2]);
443 initMPU9250();
444
      initAK8963(magCalibration);
445
446
447 }
448
449
450
451
452 void imu loop()
453 {
454
455 if (readByte(MPU9250 ADDRESS, INT STATUS) & 0x01) { // check if data
      ready interrupt
456 // if (digitalRead(intPin)) { // On interrupt, read data
457 readAccelData(accelCount); // Read the x/y/z adc values
458 // Now we'll calculate the accleration value into actual g's
459 ax = (float)accelCount[0]*aRes - accelBias[0]; // get actual g value,
      this depends on scale being set
460 ay = (float)accelCount[1] *aRes - accelBias[1];
461 az = (float)accelCount[2]*aRes - accelBias[2];
462
463
464
465 readGyroData(gyroCount); // Read the x/y/z adc values
466 // Calculate the gyro value into actual degrees per second
467 \, \text{gx} = (\text{float}) \, \text{gyroCount}[0] \, \text{*gRes}; // \, \text{get actual gyro value, this depends on}
      scale being set
468 gy = (float)gyroCount[1] *gRes;
469 gz = (float)gyroCount[2]*gRes;
470
471 readMagData(magCount); // Read the x/y/z adc values
472
473
474
       // Calculate the magnetometer values in milliGauss
475
       // Include factory calibration per data sheet and user environmental
      corrections
476
       mx = (float)magCount[0]*mRes*magCalibration[0] - magBias[0];
                                                                        // get
      actual magnetometer value, this depends on scale being set
477
       my = (float)magCount[1]*mRes*magCalibration[1] - magBias[1];
478
       mz = (float)magCount[2]*mRes*magCalibration[2] - magBias[2];
479
480 }
481 Now = micros();
482 deltat = ((Now - lastUpdate)/1000000.0f); // set integration time by
      time elapsed since last filter update
483 lastUpdate = Now;
484
485 sum += deltat; // sum for averaging filter update rate
```

```
486 sumCount++;
487 MadgwickQuaternionUpdate(ax, ay, az, gx*PI/180.0f, gy*PI/180.0f,
      gz*PI/180.0f, my, mx, mz);
         = atan2(2.0f * (q[1] * q[2] + q[0] * q[3]), q[0] * q[0] + q[1] *
      q[1] - q[2] * q[2] - q[3] * q[3]);
         *= 180.0f / PI;
489 yawc
          -= 0.17f; // Declination at Danville, California is 13 degrees 48
490 yawc
      minutes and 47 seconds on 2014-04-04
491 \text{ pitch1} = \text{atan2}(\text{ay,sqrt}(\text{ax*ax} + \text{az*az}))*180/PI;
492 \text{ roll1} = atan2(-ax,az)*180/PI;
493 / \text{headx} = \text{mx} * \cos(\text{pitch1*PI}/180) + \text{my} * \sin(\text{pitch1*PI}/180) *
      sin(roll1*PI/180) + mz * sin(pitch1*PI/180) * cos(roll1*PI/180);
494 //heady =my * cos(roll1*PI/180) - mz * sin(roll1*PI/180);
495 //yawc = atan2 (-heady, headx) *180/PI;
496
497
498 xf = .90 * (roll1 + gx * deltat) + .10 * ax;
499 \text{ yf} = .90 * (pitch1+ gy * deltat) + .10 * ay;
500 //zf = .90 * (qz * deltat) + .10 * mz;
501
502 //Serial.print("ax = "); Serial.print((int)1000*ax);
503 // Serial.print(" ay = "); Serial.print((int)1000*ay);
504 //Serial.print(" az = "); Serial.print((int)1000*az);
505 //Serial.print("\troll = "); Serial.print((int)roll1);
506 //Serial.print("\tpitch = "); Serial.print((int)pitch1);
507 //Serial.print("\tgx = "); Serial.print( gxint, 2);
508 // Serial.print("\tqy = "); Serial.print( qyint, 2);
509 Serial.print("\txf = "); Serial.print( xf, 2);
510 Serial.print("\tyf = "); Serial.print( yf, 2);
511 Serial.print("\tzf = "); Serial.print( qz, 2);
512
513 //Serial.print("\taccel bias x "); Serial.print(accelBias[0] , 2);
514 // Serial.print("\taccel bias y "); Serial.print( , 2);
515 Serial.println("");
516 Serial.println(deltat);
517 \text{ sumCount} = 0;
518 \, \text{sum} = 0;
519 delay (100);
520 }
521 void getMres() {
522
     switch (Mscale)
523
524
      // Possible magnetometer scales (and their register bit settings)
      // 14 bit resolution (0) and 16 bit resolution (1)
525
526
        case MFS 14BITS:
527
              mRes = 10.*4912./8190.; // Proper scale to return milliGauss
528
              break;
529
        case MFS 16BITS:
530
              mRes = 10.*4912./32760.0; // Proper scale to return milliGauss
531
              break;
532
    }
533 }
```

```
534 void getGres() {
535 switch (Gscale)
536 {
537 // Possible gyro scales (and their register bit settings) are:
538 // 250 DPS (00), 500 DPS (01), 1000 DPS (10), and 2000 DPS (11).
539 // Here's a bit of an algorith to calculate DPS/(ADC tick) based on that
      2-bit value:
540 case GFS 250DPS:
541 \, \text{gRes} = 250.0/32768.0;
542 break;
543 case GFS 500DPS:
544 \, \text{qRes} = 500.0/32768.0;
545 break;
546 case GFS 1000DPS:
547 \, \text{gRes} = 1000.0/32768.0;
548 break;
549 case GFS 2000DPS:
550 \text{ gRes} = 2000.0/32768.0;
551 break;
552 }
553 }
554 void getAres() {
555 switch (Ascale)
556 {
557 // Possible accelerometer scales (and their register bit settings) are:
558 / / 2 Gs (00), 4 Gs (01), 8 Gs (10), and 16 Gs (11).
559 // Here's a bit of an algorith to calculate DPS/(ADC tick) based on that
      2-bit value:
560 case AFS 2G:
561 \text{ aRes} = 2.0/32768.0;
562 break;
563 case AFS 4G:
564 \text{ aRes} = 4.0/32768.0;
565 break;
566 case AFS 8G:
567 \, aRes = 8.0/32768.0;
568 break;
569 case AFS 16G:
570 \text{ aRes} = 16.0/32768.0;
571 break;
572 }
573 }
574 void readAccelData(int16 t * destination)
576 uint8 t rawData[6]; // x/y/z accel register data stored here
577 readBytes (MPU9250 ADDRESS, ACCEL XOUT H, 6, &rawData[0]); // Read the
      six raw data registers into data array
578 \text{ destination}[0] = -((int16 t) rawData[0] << 8) | rawData[1] ; // Turn the
      MSB and LSB into a signed 16-bit value
579 \text{ destination}[1] = ((int16 t) rawData[2] << 8) | rawData[3];
580 \text{ destination}[2] = ((int16 t) rawData[4] << 8) | rawData[5];
582 void readGyroData(int16 t * destination)
```

```
583 {
584 uint8 t rawData[6]; // x/y/z gyro register data stored here
585 readBytes (MPU9250 ADDRESS, GYRO XOUT H, 6, &rawData[0]); // Read the six
     raw data registers sequentially into data array
586 \text{ destination}[0] = -((int16 t) rawData[0] << 8) | rawData[1]; // Turn the
     MSB and LSB into a signed 16-bit value
587 \text{ destination}[1] = ((int16 t) rawData[2] << 8) | rawData[3];
588 \text{ destination}[2] = ((int16 t) rawData[4] << 8) | rawData[5];
590 void readMagData(int16 t * destination)
591 {
592
     uint8 t rawData[7]; // x/y/z gyro register data, ST2 register stored
     here, must read ST2 at end of data acquisition
     if (readByte (AK8963 ADDRESS, AK8963 ST1) & 0x01) { // wait for
593
     magnetometer data ready bit to be set
     readBytes(AK8963 ADDRESS, AK8963 XOUT L, 7, &rawData[0]); // Read the
     six raw data and ST2 registers sequentially into data array
595
     uint8 t c = rawData[6]; // End data read by reading ST2 register
596
       if(!(c & 0x08)) { // Check if magnetic sensor overflow set, if not
     then report data
597
       destination[0] = ((int16 t) rawData[1] << 8) | rawData[0]; // Turn
     the MSB and LSB into a signed 16-bit value
598
       destination[1] = ((int16 t)rawData[3] << 8) | rawData[2] ; // Data
     stored as little Endian
599
       destination[2] = ((int16 t) rawData[5] << 8) | rawData[4];
600
601
602 }
603
604
605 void initAK8963 (float * destination)
606 {
607
     // First extract the factory calibration for each magnetometer axis
608
     uint8 t rawData[3]; // x/y/z gyro calibration data stored here
609
     writeByte(AK8963 ADDRESS, AK8963 CNTL, 0x00); // Power down
     magnetometer
610
     delay(10);
     writeByte(AK8963 ADDRESS, AK8963 CNTL, 0x0F); // Enter Fuse ROM access
611
     mode
612
     delay(10);
613
     readBytes(AK8963 ADDRESS, AK8963 ASAX, 3, &rawData[0]); // Read the
     x-, y-, and z-axis calibration values
614
     destination[0] = (float)(rawData[0] - 128)/256. + 1.; // Return x-
     axis sensitivity adjustment values, etc.
615
     destination[1] = (float)(rawData[1] - 128)/256. + 1.;
616
     destination[2] = (float)(rawData[2] - 128)/256. + 1.;
617
     writeByte(AK8963 ADDRESS, AK8963 CNTL, 0x00); // Power down
     magnetometer
618
     delay(10);
     // Configure the magnetometer for continuous read and highest
619
     resolution
620
    // set Mscale bit 4 to 1 (0) to enable 16 (14) bit resolution in CNTL
     register,
```

```
621 // and enable continuous mode data acquisition Mmode (bits [3:0]),
     0010 for 8 Hz and 0110 for 100 Hz sample rates
     writeByte(AK8963 ADDRESS, AK8963 CNTL, Mscale << 4 | Mmode); // Set
622
     magnetometer data resolution and sample ODR
623
     delay(10);
624 }
625 void initMPU9250()
626 {
627 // wake up device
628 writeByte (MPU9250 ADDRESS, PWR MGMT 1, 0x00); // Clear sleep mode bit
      (6), enable all sensors
629 delay(100); // Wait for all registers to reset
630 // get stable time source
631 writeByte (MPU9250 ADDRESS, PWR MGMT 1, 0x01); // Auto select clock
      source to be PLL gyroscope reference if ready else
632 delay (200);
633 // Configure Gyro and Thermometer
634 // Disable FSYNC and set thermometer and gyro bandwidth to 41 and 42 Hz,
      respectively;
635 // minimum delay time for this setting is 5.9 ms, which means sensor
      fusion update rates cannot
636 // \text{ be higher than 1 } / 0.0059 = 170 \text{ Hz}
637 // DLPF CFG = bits 2:0 = 011; this limits the sample rate to 1000 Hz for
638 \, / / With the MPU9250, it is possible to get gyro sample rates of 32 kHz
      (!), 8 kHz, or 1 kHz
639 writeByte (MPU9250 ADDRESS, CONFIG, 0x03);
640 // Set sample rate = gyroscope output rate/(1 + SMPLRT DIV)
641 writeByte (MPU9250 ADDRESS, SMPLRT DIV, 0x04); // Use a 200 Hz rate; a
      rate consistent with the filter update rate
642 // determined inset in CONFIG above
643 // Set gyroscope full scale range
644 // Range selects FS SEL and AFS SEL are 0 - 3, so 2-bit values are left-
      shifted into positions 4:3
645 uint8 t c = readByte(MPU9250 ADDRESS, GYRO CONFIG); // get current
      GYRO CONFIG register value
646 // c = c \& \sim 0xE0; // Clear self-test bits [7:5]
647 c = c \& \sim 0 \times 02; // Clear Fchoice bits [1:0]
648 c = c \& ~0x18; // Clear AFS bits [4:3]
649 c = c | Gscale << 3; // Set full scale range for the gyro
650 // c = | 0x00; // Set Fchoice for the gyro to 11 by writing its inverse
      to bits 1:0 of GYRO CONFIG
651 writeByte (MPU9250 ADDRESS, GYRO CONFIG, c); // Write new GYRO CONFIG
      value to register
652 // Set accelerometer full-scale range configuration
653c = readByte(MPU9250 ADDRESS, ACCEL CONFIG); // get current ACCEL CONFIG
      register value
654 // c = c & ~0xE0; // Clear self-test bits [7:5]
655c = c \& ~0x18; // Clear AFS bits [4:3]
656c = c \mid Ascale << 3; // Set full scale range for the accelerometer
657 writeByte (MPU9250 ADDRESS, ACCEL CONFIG, c); // Write new ACCEL CONFIG
      register value
658 // Set accelerometer sample rate configuration
```

```
659 // It is possible to get a 4 kHz sample rate from the accelerometer by
      choosing 1 for
660 // accel fchoice b bit [3]; in this case the bandwidth is 1.13 kHz
661 c = readByte (MPU9250 ADDRESS, ACCEL CONFIG2); // get current
     ACCEL CONFIG2 register value
662 c = c \& \sim 0 \times 0F; // Clear accel fchoice b (bit 3) and A DLPFG (bits [2:0])
663 \, \text{c} = \text{c} \mid 0 \times 03; \text{ // Set accelerometer rate to 1 kHz and bandwidth to 41 Hz}
664 writeByte (MPU9250 ADDRESS, ACCEL CONFIG2, c); // Write new ACCEL CONFIG2
      register value
665 // The accelerometer, gyro, and thermometer are set to 1 kHz sample
      rates,
666 // but all these rates are further reduced by a factor of 5 to 200 Hz
      because of the SMPLRT DIV setting
667 // Configure Interrupts and Bypass Enable
668 // Set interrupt pin active high, push-pull, hold interrupt pin level
      HIGH until interrupt cleared,
669 // clear on read of INT STATUS, and enable I2C BYPASS EN so additional
      chips
670 // can join the I2C bus and all can be controlled by the Arduino as
      master
671 writeByte (MPU9250 ADDRESS, INT PIN CFG, 0x22);
672 writeByte (MPU9250 ADDRESS, INT ENABLE, 0x01); // Enable data ready (bit
      0) interrupt
673 delay (100);
674 }
675
676
677
678 void calibrateMPU9250(float * dest1, float * dest2)
680 uint8 t data[12]; // data array to hold accelerometer and gyro x, y, z,
      data
681 uint16 t ii, packet count, fifo count;
682 int32_t gyro_bias[3] = \{0, 0, 0\}, accel bias[3] = \{0, 0, 0\};
683 // reset device
684 writeByte (MPU9250 ADDRESS, PWR MGMT 1, 0x80); // Write a one to bit 7
      reset bit; toggle reset device
685 delay (100);
686 // get stable time source; Auto select clock source to be PLL gyroscope
      reference if ready
687// else use the internal oscillator, bits 2:0 = 001
688 writeByte (MPU9250 ADDRESS, PWR MGMT 1, 0x01);
689 writeByte (MPU9250 ADDRESS, PWR MGMT 2, 0x00);
690 delay(200);
691 // Configure device for bias calculation
692 writeByte (MPU9250 ADDRESS, INT ENABLE, 0x00); // Disable all interrupts
693 writeByte (MPU9250 ADDRESS, FIFO EN, 0x00); // Disable FIFO
694 writeByte (MPU9250 ADDRESS, PWR MGMT_1, 0x00); // Turn on internal clock
695 writeByte (MPU9250 ADDRESS, I2C MST CTRL, 0x00); // Disable I2C master
696 writeByte (MPU9250 ADDRESS, USER CTRL, 0x00); // Disable FIFO and I2C
      master modes
697 writeByte (MPU9250 ADDRESS, USER CTRL, 0x0C); // Reset FIFO and DMP
```

```
698 delay (15);
699 // Configure MPU6050 gyro and accelerometer for bias calculation
700 writeByte (MPU9250 ADDRESS, CONFIG, 0x01); // Set low-pass filter to 188
701 writeByte (MPU9250 ADDRESS, SMPLRT DIV, 0x00); // Set sample rate to 1
      kHz
702 writeByte (MPU9250 ADDRESS, GYRO CONFIG, 0x00); // Set gyro full-scale to
      250 degrees per second, maximum sensitivity
703 writeByte (MPU9250 ADDRESS, ACCEL CONFIG, 0x00); // Set accelerometer
      full-scale to 2 g, maximum sensitivity
704 uint16 t gyrosensitivity = 131; // = 131 LSB/degrees/sec
705 uint16 t accelsensitivity = 16384; // = 16384 LSB/g
706 // Configure FIFO to capture accelerometer and gyro data for bias
      calculation
707 writeByte (MPU9250 ADDRESS, USER CTRL, 0x40); // Enable FIFO
708 writeByte (MPU9250 ADDRESS, FIFO EN, 0x78); // Enable gyro and
      accelerometer sensors for FIFO (max size 512 bytes in MPU-9150)
709 delay(40); // accumulate 40 samples in 40 milliseconds = 480 bytes
710 // At end of sample accumulation, turn off FIFO sensor read
711 writeByte (MPU9250 ADDRESS, FIFO EN, 0x00); // Disable gyro and
      accelerometer sensors for FIFO
712 readBytes (MPU9250 ADDRESS, FIFO COUNTH, 2, &data[0]); // read FIFO
      sample count
713 fifo count = ((uint16 t)data[0] << 8) | data[1];
714 packet count = fifo count/12;// How many sets of full gyro and
      accelerometer data for averaging
715 for (ii = 0; ii < packet count; ii++) {
716 int16 t accel temp[3] = \{0, 0, 0\}, gyro temp[3] = \{0, 0, 0\};
717 readBytes (MPU9250 ADDRESS, FIFO R W, 12, &data[0]); // read data for
      averaging
718 accel temp[0] = (int16 t) (((int16 t)data[0] << 8) | data[1] ); // Form
      signed 16-bit integer for each sample in FIFO
719 accel temp[1] = (int16 t) (((int16 t)data[2] << 8) | data[3] );
720 \ accel \ temp[2] = (int16 \ t) (((int16 \ t) data[4] << 8) \ | \ data[5] ) ;
721 \text{ gyro temp}[0] = (int16 t) (((int16 t) data[6] << 8) | data[7]);
722 gyro temp[1] = (int16 t) (((int16 t)data[8] << 8) | data[9] );
723 gyro temp[2] = (int16 t) (((int16 t) data[10] << 8) | data[11]) ;
724 accel bias[0] += (int32 t) accel temp[0]; // Sum individual signed 16-
      bit biases to get accumulated signed 32-bit biases
725 \, \text{accel bias}[1] += (int32 \, t) \, \text{accel temp}[1];
726 \operatorname{accel} \operatorname{bias}[2] += (\operatorname{int} 32 t) \operatorname{accel} \operatorname{temp}[2];
727 gyro bias[0] += (int32 t) gyro temp[0];
728 gyro bias[1] += (int32 t) gyro temp[1];
729 gyro bias[2] += (int32 t) gyro temp[2];
730 }
731 accel bias[0] /= (int32 t) packet count; // Normalize sums to get
      average count biases
732 accel bias[1] /= (int32 t) packet count;
733 accel bias[2] /= (int32 t) packet count;
734 gyro bias[0] /= (int32 t) packet count;
735 gyro bias[1] /= (int32 t) packet count;
736 gyro bias[2] /= (int32 t) packet count;
```

```
737 if (accel bias[2] > 0L) {accel bias[2] -= (int32 t) accelsensitivity;} //
      Remove gravity from the z-axis accelerometer bias calculation
738 else {accel bias[2] += (int32 t) accelsensitivity;}
739 // Construct the gyro biases for push to the hardware gyro bias
      registers, which are reset to zero upon device startup
740 \text{ data}[0] = (-\text{gyro bias}[0]/4 >> 8) \& 0xFF; // Divide by 4 to get 32.9 LSB
      per deg/s to conform to expected bias input format
741 data[1] = (-gyro bias[0]/4) \& 0xFF; // Biases are additive, so change
      sign on calculated average gyro biases
742 \, \text{data}[2] = (-\text{gyro bias}[1]/4 >> 8) \& 0xFF;
743 data[3] = (-gyro bias[1]/4) \& 0xFF;
744 \, \text{data}[4] = (-\text{gyro bias}[2]/4 >> 8) \& 0xFF;
745 \, data[5] = (-gyro \, bias[2]/4) \& 0xFF;
746 // Push gyro biases to hardware registers
747 writeByte (MPU9250 ADDRESS, XG OFFSET H, data[0]);
748 writeByte (MPU9250 ADDRESS, XG OFFSET L, data[1]);
749 writeByte (MPU9250 ADDRESS, YG OFFSET H, data[2]);
750 writeByte (MPU9250 ADDRESS, YG OFFSET L, data[3]);
751 writeByte (MPU9250 ADDRESS, ZG OFFSET H, data[4]);
752 writeByte (MPU9250 ADDRESS, ZG OFFSET_L, data[5]);
753 // Output scaled gyro biases for display in the main program
754 dest1[0] = (float) gyro bias[0]/(float) gyrosensitivity;
755 dest1[1] = (float) gyro bias[1]/(float) gyrosensitivity;
756 dest1[2] = (float) gyro bias[2]/(float) gyrosensitivity;
757 // Construct the accelerometer biases for push to the hardware
      accelerometer bias registers. These registers contain
758 // factory trim values which must be added to the calculated
      accelerometer biases; on boot up these registers will hold
759 // non-zero values. In addition, bit 0 of the lower byte must be
      preserved since it is used for temperature
760 // compensation calculations. Accelerometer bias registers expect bias
      input as 2048 LSB per g, so that
761 // the accelerometer biases calculated above must be divided by 8.
762 int32 t accel bias reg[3] = \{0, 0, 0\}; // A place to hold the factory
      accelerometer trim biases
763 readBytes (MPU9250 ADDRESS, XA OFFSET H, 2, &data[0]); // Read factory
      accelerometer trim values
764 \, \text{accel bias reg}[0] = (int32 \, t) \, (((int16 \, t) \, data[0] << 8) \, | \, data[1]);
765 readBytes (MPU9250 ADDRESS, YA OFFSET H, 2, &data[0]);
766 accel_bias_reg[1] = (int32_t) (((int16_t)data[0] << 8) | data[1]);
767 readBytes (MPU9250 ADDRESS, ZA OFFSET H, 2, &data[0]);
768 accel bias reg[2] = (int32 t) (((int16 t)data[0] << 8) | data[1]);
769 uint 32 t mask = 1uL; // Define mask for temperature compensation bit 0
      of lower byte of accelerometer bias registers
770 uint8 t mask bit[3] = \{0, 0, 0\}; // Define array to hold mask bit for
      each accelerometer bias axis
771 for (ii = 0; ii < 3; ii++) {
772 if((accel bias reg[ii] & mask)) mask bit[ii] = 0x01; // If temperature
      compensation bit is set, record that fact in mask bit
773 }
774 // Construct total accelerometer bias, including calculated average
      accelerometer bias from above
```

```
775 accel bias reg[0] -= (accel bias[0]/8); // Subtract calculated averaged
      accelerometer bias scaled to 2048 LSB/g (16 g full scale)
776 accel bias reg[1] -= (accel bias[1]/8);
777 accel bias reg[2] \rightarrow (accel bias[2]/8);
778 data[0] = (accel bias reg[0] >> 8) & 0xFF;
779 data[1] = (accel bias reg[0]) & 0xFF;
780 data[1] = data[1] | mask bit[0]; // preserve temperature compensation
      bit when writing back to accelerometer bias registers
781 \text{ data}[2] = (accel bias reg[1] >> 8) & 0xFF;
782 \, \text{data}[3] = (\text{accel bias reg}[1]) \& 0xFF;
783 data[3] = data[3] | mask bit[1]; // preserve temperature compensation
      bit when writing back to accelerometer bias registers
784 \text{ data}[4] = (\text{accel bias reg}[2] >> 8) & 0xFF;
785 \, \text{data}[5] = (\text{accel bias reg}[2]) \& 0xFF;
786 data[5] = data[5] | mask bit[2]; // preserve temperature compensation
      bit when writing back to accelerometer bias registers
787 // Apparently this is not working for the acceleration biases in the
      MPU-9250
788 // Are we handling the temperature correction bit properly?
789 // Push accelerometer biases to hardware registers
790 writeByte (MPU9250 ADDRESS, XA OFFSET H, data[0]);
791 writeByte (MPU9250 ADDRESS, XA OFFSET L, data[1]);
792 writeByte (MPU9250 ADDRESS, YA OFFSET H, data[2]);
793 writeByte (MPU9250 ADDRESS, YA OFFSET L, data[3]);
794 writeByte (MPU9250 ADDRESS, ZA OFFSET H, data[4]);
795 writeByte (MPU9250 ADDRESS, ZA OFFSET L, data[5]);
796 // Output scaled accelerometer biases for display in the main program
797 dest2[0] = (float)accel bias[0]/(float)accelsensitivity;
798 dest2[1] = (float)accel bias[1]/(float)accelsensitivity;
799 dest2[2] = (float)accel bias[2]/(float)accelsensitivity;
800 }
801
802 void writeByte(uint8 t address, uint8 t subAddress, uint8 t data)
804 Wire.beginTransmission(address); // Initialize the Tx buffer
805 Wire.write(subAddress); // Put slave register address in Tx buffer
806 Wire.write(data); // Put data in Tx buffer
807 Wire.endTransmission(); // Send the Tx buffer
808}
809 uint8 t readByte(uint8 t address, uint8 t subAddress)
811 uint8 t data; // `data` will store the register data
812 Wire.beginTransmission(address); // Initialize the Tx buffer
813 Wire.write(subAddress); // Put slave register address in Tx buffer
814 Wire.endTransmission(); // Send the Tx buffer, but send a restart to
      keep connection alive
815 // Wire.endTransmission(false); // Send the Tx buffer, but send a
      restart to keep connection alive
816 // Wire.requestFrom(address, 1); // Read one byte from slave register
      address
817 Wire.requestFrom(address, (size t) 1); // Read one byte from slave
      register address
818 data = Wire.read(); // Fill Rx buffer with result
```

```
819 return data; // Return data read from slave register
821 void readBytes (uint8 t address, uint8 t subAddress, uint8 t count,
      uint8 t * dest)
822 {
823 Wire.beginTransmission(address); // Initialize the Tx buffer
824 Wire.write(subAddress); // Put slave register address in Tx buffer
825 Wire.endTransmission(); // Send the Tx buffer, but send a restart to
      keep connection alive
826 // Wire.endTransmission(false); // Send the Tx buffer, but send a
      restart to keep connection alive
827 \text{ uint } 8 \text{ t i } = 0;
828 // Wire.requestFrom(address, count); // Read bytes from slave register
      address
829 Wire.requestFrom(address, (size t) count); // Read bytes from slave
      register address
830 while (Wire.available()) {
831 dest[i++] = Wire.read(); } // Put read results in the Rx buffer
833 void MadgwickQuaternionUpdate(float ax, float ay, float az, float gx,
      float gy, float gz, float mx, float my, float mz)
834
835
                float q1 = q[0], q2 = q[1], q3 = q[2], q4 = q[3]; // short
      name local variable for readability
836
                float norm;
837
                float hx, hy, 2bx, 2bz;
838
                float s1, s2, s3, s4;
839
                float qDot1, qDot2, qDot3, qDot4;
840
841
               // Auxiliary variables to avoid repeated arithmetic
               float _2q1mx;
842
843
               float _2q1my;
844
                float 2q1mz;
                float 2q2mx;
845
846
               float 4bx;
                float _4bz;
847
                float 2q1 = 2.0f * q1;
848
849
                float 2q2 = 2.0f * q2;
               float 2q3 = 2.0f * q3;
850
851
                float 2q4 = 2.0f * q4;
                float 2q1q3 = 2.0f * q1 * q3;
852
                float 2q3q4 = 2.0f * q3 * q4;
853
854
               float q1q1 = q1 * q1;
855
               float q1q2 = q1 * q2;
856
                float q1q3 = q1 * q3;
857
               float q1q4 = q1 * q4;
858
               float q2q2 = q2 * q2;
859
               float q2q3 = q2 * q3;
               float q2q4 = q2 * q4;
860
861
               float q3q3 = q3 * q3;
862
                float q3q4 = q3 * q4;
863
                float q4q4 = q4 * q4;
864
```

```
865
                                            // Normalise accelerometer measurement
866
                                            norm = sqrt(ax * ax + ay * ay + az * az);
867
                                            if (norm == 0.0f) return; // handle NaN
868
                                            norm = 1.0f/norm;
869
                                            ax *= norm;
870
                                            ay *= norm;
871
                                            az *= norm;
872
873
                                            // Normalise magnetometer measurement
874
                                            norm = sqrt(mx * mx + my * my + mz * mz);
875
                                            if (norm == 0.0f) return; // handle NaN
876
                                            norm = 1.0f/norm;
877
                                            mx *= norm;
878
                                            my *= norm;
879
                                           mz *= norm;
880
881
                                            // Reference direction of Earth's magnetic field
882
                                             2q1mx = 2.0f * q1 * mx;
                                              2q1my = 2.0f * q1 * my;
883
                                            2q1mz = 2.0f * q1 * mz;
884
885
                                             2q2mx = 2.0f * q2 * mx;
886
                                            hx = mx * q1q1 - 2q1my * q4 + 2q1mz * q3 + mx * q2q2 +
                 2q2 * my * q3 + 2q2 * mz * q4 - mx * q3q3 - mx * q4q4;
                                           hy = 2q1mx * q4 + my * q1q1 - 2q1mz * q2 + 2q2mx * q3 -
887
                my * q2q2 + my * q3q3 + 2q3 * mz * q4 - my * q4q4;
                                            _2bx = sqrt(hx * hx + hy * hy);
888
                                               2bz = -2q1mx * q3 + 2q1my * q2 + mz * q1q1 + 2q2mx * q4
889
                 - mz * q2q2 + _2q3 * my * q4 - <math>mz * q3q3 + mz * q4q4;
                                             _4bx = 2.0f * _2bx;
_4bz = 2.0f * _2bz;
890
891
892
893
                                            // Gradient decent algorithm corrective step
                                            s1 = -2q3 * (2.0f * q2q4 - 2q1q3 - ax) + 2q2 * (2.0f *
894
                 q1q2 + _2q3q4 - ay) - _2bz * q3 * (_2bx * (0.5f - q3q3 - q4q4) + _2bz
                * (q2q4 - q1q3) - mx) + (-_2bx * q4 + _2bz * q2) * (_2bx * (q2q3 - q1q4) + _2bz * (q1q2 + q3q4) - my) + _2bx * q3 * (_2bx * (q1q3 +
                 q2q4) + 2bz * (0.5f - q2q2 - q3q3) - mz);
                                            s2 = 2q4 * (2.0f * q2q4 - 2q1q3 - ax) + 2q1 * (2.0f *
895
                 q1q2 + 2q3q4 - ay) - 4.0f * q2 * (1.0f - 2.0f * q2q2 - 2.0f * q3q3 -
                 az) + \frac{1}{2}bz * q4 * (\frac{1}{2}bx * (0.5f - q3q3 - q4q4) + \frac{1}{2}bz * (q2q4 - q1q3)
                 -mx) + (2bx * q3 + 2bz * q1) * (2bx * (q2q3 - q1q4) + 2bz *
                 (q1q2 + q3q4) - my) + (_2bx * q4 - _4bz * q2) * (_2bx * (q1q3 + q2q4)
                 + _2bz * (0.5f - q2q2 - q3q3) - mz);
                                            s3 = -2q1 * (2.0f * q2q4 - _2q1q3 - ax) + _2q4 * (2.0f * _2q4 + _2q4 +
896
                q1q2 + _2q3q4 - ay) - 4.0f * q3 * (1.0f - 2.0f * q2q2 - 2.0f * q3q3 -
                 az) + (-4bx * q3 - 2bz * q1) * (2bx * (0.5f - q3q3 - q4q4) + _2bz
                 * (q2q4 - q1q3) - mx) + (_2bx * q2 + _2bz * q4) * (_2bx * (q2q3 -
                 q1q4) + 2bz * (q1q2 + q3q4) - my) + (2bx * q1 - 4bz * q3) * (2bx
                 * (q1q3 + q2q4) + 2bz * (0.5f - q2q2 - q3q3) - mz);
                 s4 = 2q2 * (2.0f * q2q4 - 2q1q3 - ax) + 2q3 * (2.0f * q1q2 + 2q3q4 - ay) + (-4bx * q4 + 2bz * q2) * (2bx * (0.5f - q3q3) * (2.0f * q1q2 + 2p3q4 - ay) + (-4bx * q4 + 2bz * q2) * (2bx * (0.5f - q3q3) * (2.0f * q1q2 + 2p3q4 - ay) * (2.0f * q1q2 + ay) * (
897
                 -q4q4) + 2bz * (q2q4 - q1q3) - mx) + (-2bx * q1 + 2bz * q3) *
```

```
(2bx * (q2q3 - q1q4) + 2bz * (q1q2 + q3q4) - my) + 2bx * q2 * (2bx * (q1q3 + q2q4) + 2bz * (0.5f - q2q2 - q3q3) - mz);
                norm = sqrt(s1 * s1 + s2 * s2 + s3 * s3 + s4 * s4);
898
      normalise step magnitude
899
                norm = 1.0f/norm;
900
                s1 *= norm;
901
                s2 *= norm;
902
                s3 *= norm;
903
                s4 *= norm;
904
905
                // Compute rate of change of quaternion
                qDot1 = 0.5f * (-q2 * gx - q3 * gy - q4 * gz) - beta * s1;
906
907
                qDot2 = 0.5f * (q1 * gx + q3 * gz - q4 * gy) - beta * s2;
                qDot3 = 0.5f * (q1 * gy - q2 * gz + q4 * gx) - beta * s3;
908
909
                qDot4 = 0.5f * (q1 * qz + q2 * qy - q3 * qx) - beta * s4;
910
911
                // Integrate to yield quaternion
912
                q1 += qDot1 * deltat;
913
                q2 += qDot2 * deltat;
                q3 += qDot3 * deltat;
914
915
                q4 += qDot4 * deltat;
916
                norm = sqrt(q1 * q1 + q2 * q2 + q3 * q3 + q4 * q4);
      normalise quaternion
917
                norm = 1.0f/norm;
918
                q[0] = q1 * norm;
919
                q[1] = q2 * norm;
920
                q[2] = q3 * norm;
921
                q[3] = q4 * norm;
922
923
            }
924
925
926
927
928
929
930 PID roll controller(&pid roll in,
                                         &pid roll out,
                                                           &pid roll setpoint,
      ROLL PID KP, ROLL PID KI, ROLL PID KD, REVERSE);
931 PID pitch controller (&pid pitch in, &pid pitch out, &pid pitch setpoint,
      PITCH PID KP , PITCH PID KI, PITCH PID KD, REVERSE);
932 PID yaw controller (&pid yaw in,
                                        &pid yaw out,
                                                           &pid yaw setpoint,
      YAW PID KP, YAW PID KI, YAW PID KD, DIRECT);
933
934
935 void pid initialize() {
936
     roll controller.SetOutputLimits (ROLL PID MIN, ROLL PID MAX);
937
     pitch controller.SetOutputLimits(PITCH PID MIN, PITCH PID MAX);
     yaw_controller.SetOutputLimits(YAW PID MIN,YAW PID MAX);
938
939
     roll controller.SetMode(AUTOMATIC);
940
     pitch controller.SetMode(AUTOMATIC);
941
     yaw controller.SetMode(AUTOMATIC);
942
     roll controller.SetSampleTime(PID SAMPLE TIME );
     pitch controller.SetSampleTime(PID SAMPLE TIME );
943
```

```
944 yaw_controller.SetSampleTime(PID_SAMPLE_TIME );
945 }
946
947 void pid update(){
948 pid roll in = xf;
949 pid_{pitch_{in}} = yf;
950 pid yaw in = gz;
951 }
952
953 void pid compute() {
954
      roll controller.Compute();
955
      pitch controller.Compute();
956
      yaw_controller.Compute();
957
958 }
```

9. REFERENCES(Website) www.playground.arduino.cc Nrf24L01+ datasheets **Invensense MPU9250 datasheet** 63