Analysis of Covariance Tutorials: Oneway and Factorial Analyses

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```
# Load in Required Libraries
library(psych)
library(tidyverse)
library(jmv)
library(ggpubr)
library(apaTables)
library(ez)
library(rstatix)
```

ANCOVA | One-Way Research Context Prompt

Research Context:

Researchers investigated the effect of exercises in reducing anxiety levels. Anxiety scores were measured from three groups of individuals practicing physical exercises at different levels (low, moderate, and high).

The anxiety score was measured pre- and 6-months post-exercise training programs. It is expected that any reduction in the anxiety by the exercises programs would also depend on the participant's baseline level of anxiety.

In this analysis we use the pre-test anxiety score as the covariate and are interested in possible differences between group with respect to the post-test anxiety score.

One-way ANCOVA | Data

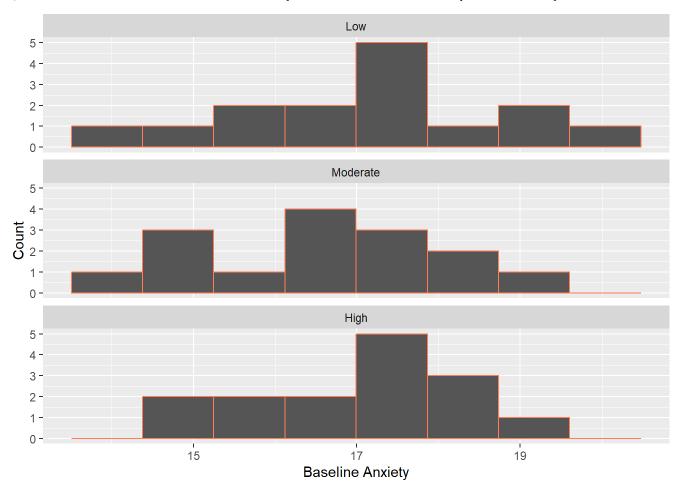
```
dat_anx <- read.csv("ancova1.csv")</pre>
```

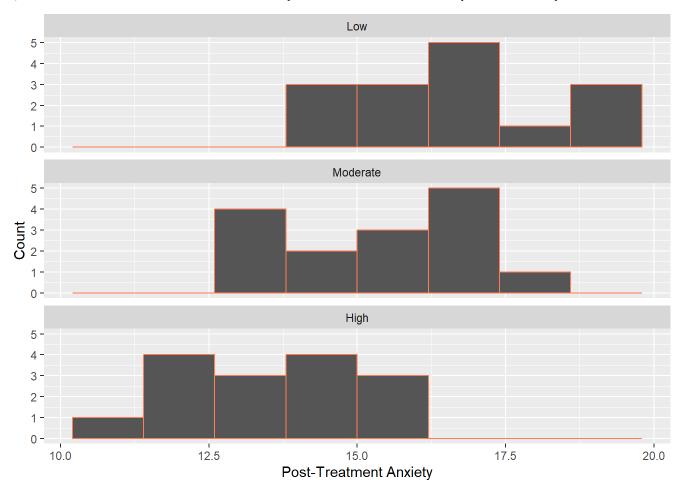
ANCOVA | Descriptive Stats (Baseline-test)

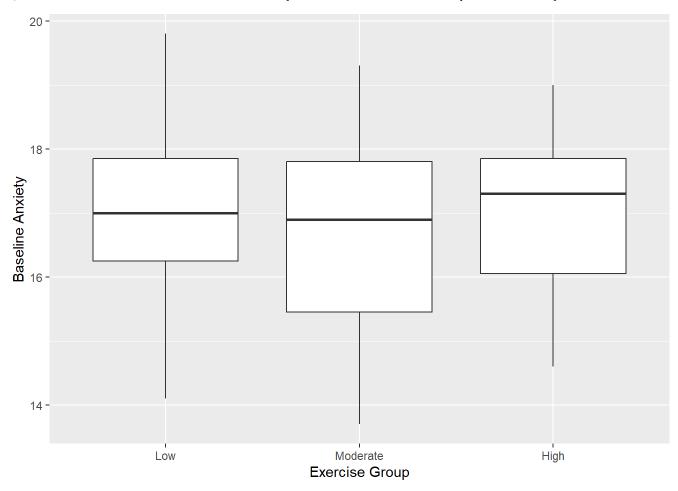
```
##
             group1 vars n
                                           sd median trimmed
      item
                                mean
                                                                  mad min max
                       1 15 17.08667 1.628701
                                                17.0 17.10769 1.33434 14.1 19.8
## X11
         1
                Low
## X12
          2 Moderate
                       1 15 16.64667 1.565643
                                                16.9 16.66923 1.63086 13.7 19.3
## X13
               High
                       1 15 17.01333 1.321183
                                                17.3 17.04615 1.33434 14.6 19.0
##
                  skew
                         kurtosis
      range
## X11
         5.7 -0.1029298 -0.8254734 0.4205288
## X12
         5.6 -0.2002025 -1.0718963 0.4042473
## X13
        4.4 -0.3718028 -1.1608155 0.3411279
```

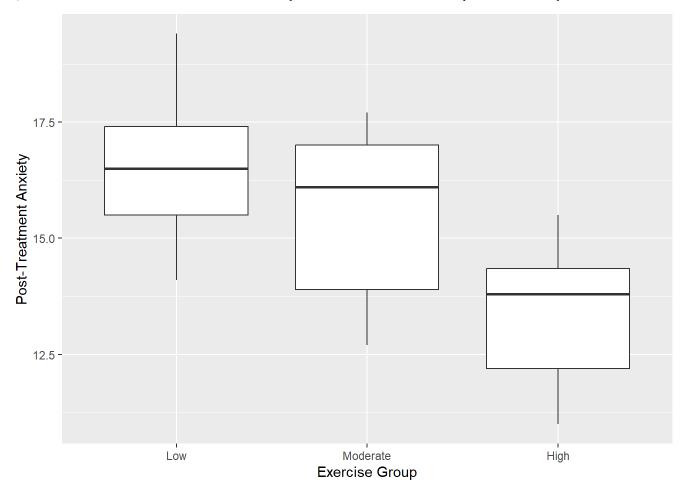
```
##
             group1 vars n
                                mean
                                           sd median trimmed
                                                                  mad min max
## X11
                       1 15 16.62000 1.675538
                                                16.5 16.60000 1.48260 14.1 19.4
         1
                                                16.1 15.57692 1.77912 12.7 17.7
## X12
         2 Moderate
                       1 15 15.52667 1.702715
## X13
         3
               High
                       1 15 13.56000 1.422674
                                                13.8 13.60769 1.92738 11.0 15.5
##
      range
                  skew kurtosis
## X11
        5.3 0.2618597 -1.087983 0.4326221
## X12
        5.0 -0.3236715 -1.539690 0.4396391
        4.5 -0.3246574 -1.338458 0.3673327
## X13
```

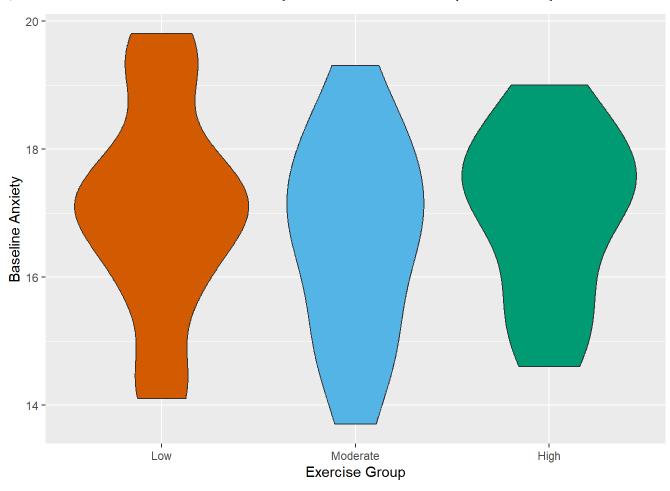
ANCOVA | EDA Visualiations

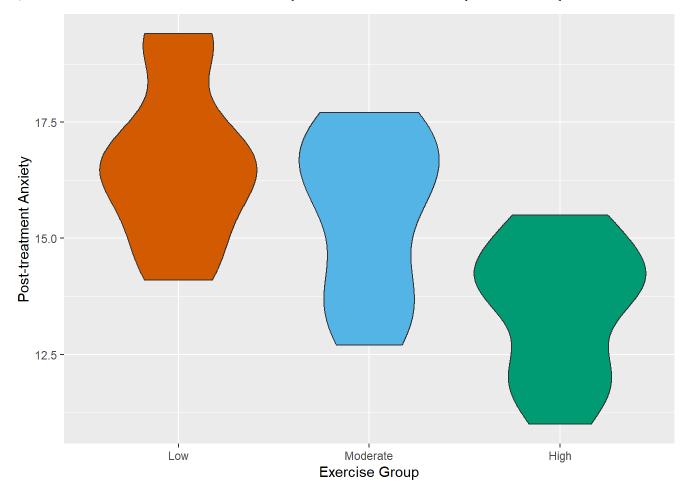








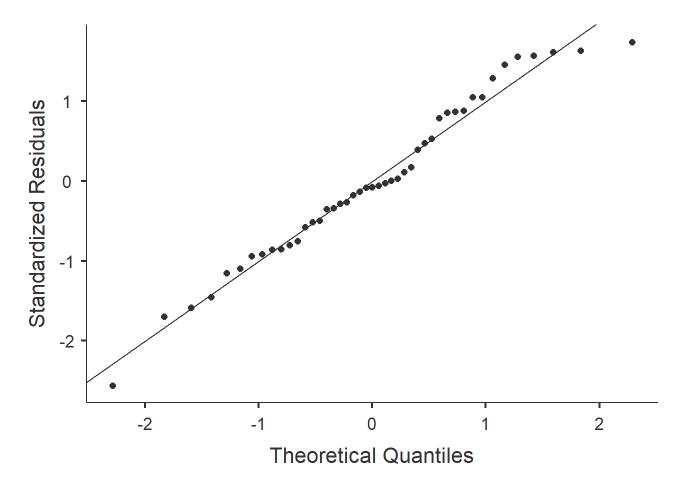




ANCOVA | Omnibus Assumption Check

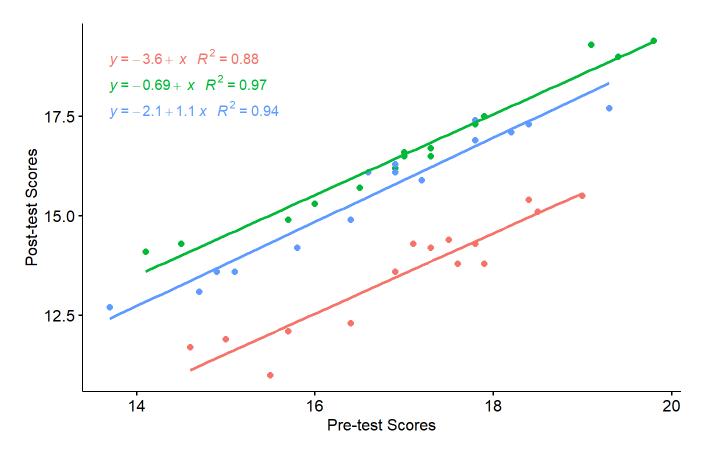
```
ancova(data = dat_anx,
    dep = posttest,
    factors = groupF,
    covs = pretest,
    effectSize = "eta",
    homo = TRUE,
    qq = TRUE,
    norm = TRUE)
```

```
##
##
    ANCOVA
##
##
    ANCOVA - posttest
##
##
                    Sum of Squares
                                        df
                                              Mean Square
                                                              F
                                                                                           η²
                                                                           р
##
                                         2
##
      groupF
                         74.022594
                                               37.0112970
                                                              218.6293
                                                                           < .0000001
                                                                                          0.4061553
##
      pretest
                        101.288528
                                         1
                                              101.2885278
                                                              598.3210
                                                                           < .0000001
                                                                                           0.5557611
##
      Residuals
                           6.940805
                                        41
                                                0.1692879
##
##
##
##
    ASSUMPTION CHECKS
##
    Homogeneity of Variances Test (Levene's)
##
##
      F
                   df1
##
                           df2
                                  p
##
##
      2.339315
                     2
                            42
                                  0.1088316
##
##
##
##
    Normality Test (Shapiro-Wilk)
##
##
      Statistic
                    р
##
      0.9753224
##
                    0.4440646
##
```



ANCOVA | Linearity Assumption Check





ANCOVA | Homogeneity of Regression Slopes Assumption Check

```
dat_anx %>%
  anova_test(posttest ~ groupF*pretest)
```

Since p > .05 for the interaction we can assume homogeneity of regression slopes

ANCOVA | Normality of Residuals

Lack of statistical significant implies that normality of residuals has been achieved

ANCOVA | Homogeneity of Variances

```
model.metrics %>%
  levene_test(.resid ~ groupF)
```

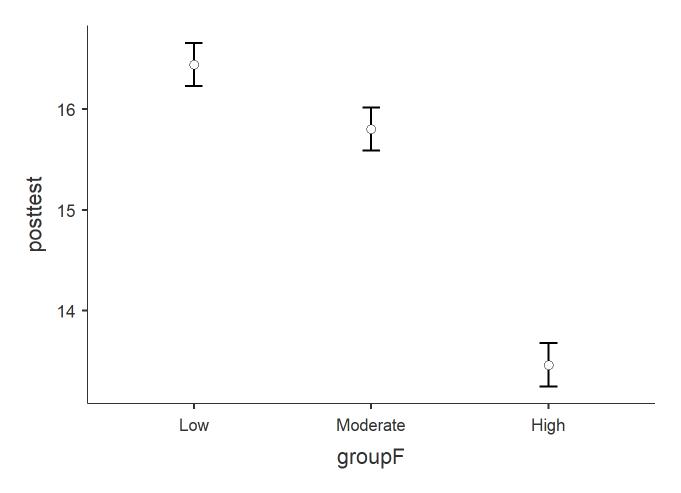
```
## # A tibble: 1 × 4
## df1 df2 statistic p
## <int> <dbl> <dbl>
## 1 2 42 2.27 0.116
```

Lack of statistical significance here implies that residual variances are homogeneous across b etween-subject groups

ANCOVA | Conducting the ANCOVA

```
options(digits = 3)
ancova(data = dat_anx,
    dep = posttest,
    factors = groupF,
    covs = pretest,
    effectSize = "eta",
    postHoc = 'groupF',
    postHocCorr = 'bonf',
    postHocES = 'd',
    postHocESCi = TRUE,
    emMeans=list(
        list('groupF')),
    emmTables=TRUE,
    emmPlots=TRUE)
```

```
##
##
    ANCOVA
##
##
    ANCOVA - posttest
##
##
                    Sum of Squares
                                        df
                                                               F
                                                                                 η²
                                              Mean Square
                                                                      р
##
                                         2
                                                                      < .001
##
      groupF
                              74.02
                                                    37.011
                                                               219
                                                                                 0.406
##
      pretest
                             101.29
                                         1
                                                   101.289
                                                               598
                                                                      < .001
                                                                                 0.556
      Residuals
                               6.94
                                        41
                                                     0.169
##
##
##
##
##
    POST HOC TESTS
##
    Post Hoc Comparisons - groupF
##
##
##
                                      Mean Difference
                                                          SE
                                                                    df
                                                                                       p-bonferroni
      groupF
                         groupF
                                                                             t
Cohen's d
              Lower
                       Upper
##
##
                        Moderate
      Low
                                                0.641
                                                          0.151
                                                                    41.0
                                                                              4.24
                                                                                       < .001
1.56
        0.738
                   2.38
##
                        High
                                                2.985
                                                          0.150
                                                                    41.0
                                                                             19.86
                                                                                       < .001
7.25
        5.476
                   9.03
##
      Moderate
                        High
                                                2.344
                                                          0.151
                                                                    41.0
                                                                             15.52
                                                                                       < .001
        4.225
5.70
                   7.17
##
##
      Note. Comparisons are based on estimated marginal means
##
##
##
    ESTIMATED MARGINAL MEANS
##
    GROUPF
##
##
    Estimated Marginal Means - groupF
##
##
##
      groupF
                            SE
                   Mean
                                      Lower
                                               Upper
##
##
      Low
                   16.4
                            0.106
                                       16.2
                                                16.7
##
      Moderate
                   15.8
                            0.107
                                       15.6
                                                 16.0
##
      High
                   13.5
                            0.106
                                       13.2
                                                13.7
##
```



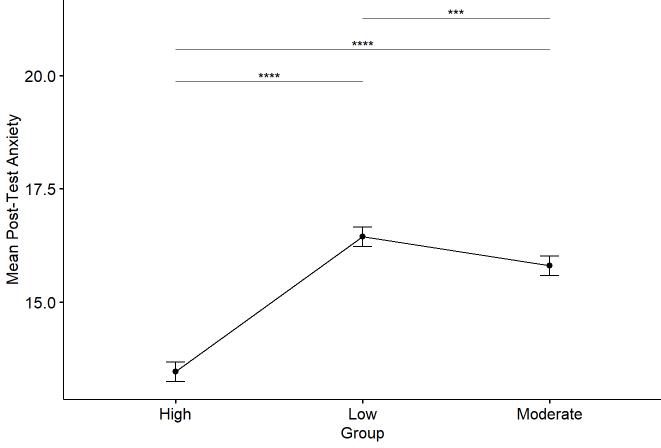
ANCOVA | Professional ANCOVA Visualization

```
## # A tibble: 3 × 13
##
     term
                 .y.
                                         df statistic
                                                                   p.adj p.adj.signif
                       group1 group2
##
     <chr>>
                 <chr> <chr> <chr> <chr> <dbl>
                                                <dbl>
                                                          <dbl>
                                                                   <dbl> <chr>
## 1 pretest*gr... post... High
                               Low
                                         41
                                               -19.9 1.19e-22 3.58e-22 ****
                                               -15.5 9.21e-19 2.76e-18 ****
## 2 pretest*gr... post... High
                                         41
                               Moder...
## 3 pretest*gr... post... Low
                               Moder...
                                         41
                                                 4.24 1.26e- 4 3.77e- 4 ***
## # i 4 more variables: y.position <dbl>, groups <named list>, xmin <dbl>,
```

ANCOVA | Professional ANCOVA Visualization

```
get_emmeans(pwc)
```

```
## # A tibble: 3 × 8
##
    pretest group
                                     df conf.low conf.high method
                     emmean
                               se
##
       <dbl> <fct>
                     <dbl> <dbl> <dbl>
                                           <dbl>
                                                     <dbl> <chr>>
## 1
       16.9 High
                       13.5 0.106
                                            13.2
                                                      13.7 Emmeans test
## 2
       16.9 Low
                       16.4 0.106
                                     41
                                            16.2
                                                      16.7 Emmeans test
       16.9 Moderate 15.8 0.107
                                            15.6
## 3
                                     41
                                                      16.0 Emmeans test
```



pwc: Emmeans test; p.adjust: Bonferroni

ANCOVA | Factorial Research Context Prompt

Your local sports psychologist and stress research enthusiast found out you were learning various quantitative statistical methods and reached out to offer you a consulting/analytics opportunity. They gathered data from 60 participants to attempt to evaluate the effect of a new protein treatment and exercise on experienced stress levels in a group of older adults. The data set (dat_stress) contains five variables:

- id Participant identification number
- score Stress score collected from each participant
- treatment Treatment variable with two levels (yes Received protein treatment; no Received placebo treatment)
- exercise Level of exercise employed by participants (low, moderate, high)
- age Age of participant when data was collected

The goal for this final research question was: Does adjusting for the age of participants impact how stress scores fluctuate across treatment and exercise variables?

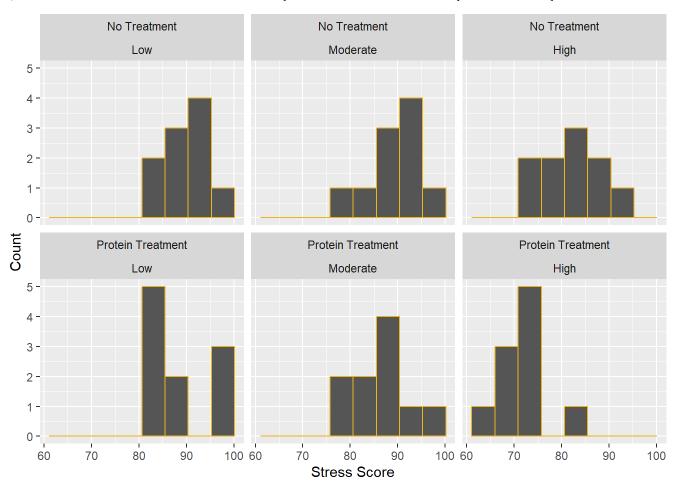
Factorial ANCOVA | Data

dat_stress <- read.csv("ancova2.csv")</pre>

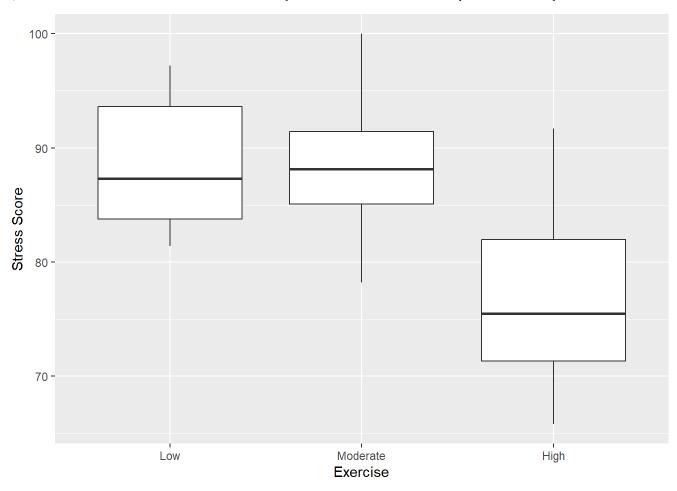
Factorial ANCOVA | Descriptive Stats (Baseline-test)

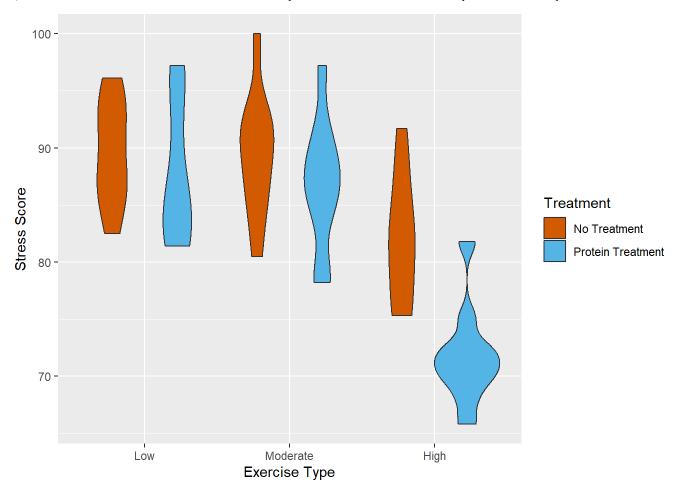
```
##
      item
                     group1
                             group2 vars n mean
                                                 sd median trimmed mad min
                                                     89.2
                                                             89.7 5.49 82.5
## X11
         1
               No Treatment
                                      1 10 89.6 4.49
## X12
        2 Protein Treatment
                               Low 1 10 87.9 6.29 84.8
                                                             87.5 4.37 81.4
## X13
               No Treatment Moderate 1 10 89.4 5.42 89.8
                                                            89.2 4.23 80.5
        4 Protein Treatment Moderate 1 10 86.8 5.69 87.1
## X14
                                                             86.6 4.23 78.2
## X15
               No Treatment
                              High 1 10 82.0 5.58 82.1
                                                             81.6 7.56 75.3
        6 Protein Treatment
## X16
                              High 1 10 71.8 4.33 71.2 71.3 1.93 65.8
##
        max range
                    skew kurtosis se
## X11 96.1 13.6 -0.0335 -1.565 1.42
## X12 97.2 15.8 0.4837
                         -1.702 1.99
## X13 100.0 19.5 0.2159 -0.670 1.72
## X14 97.2 19.0 0.0618
                         -0.916 1.80
                         -1.345 1.77
## X15 91.7 16.4 0.2737
## X16 81.8 16.0 0.9351
                         0.303 1.37
```

Factorial ANCOVA | EDA Visualizations





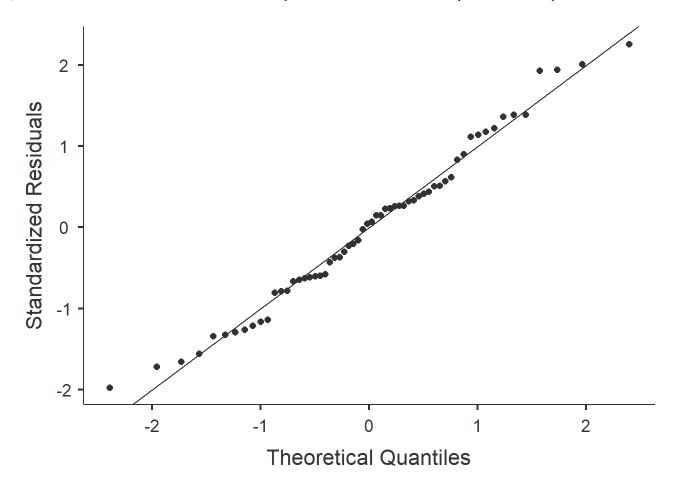




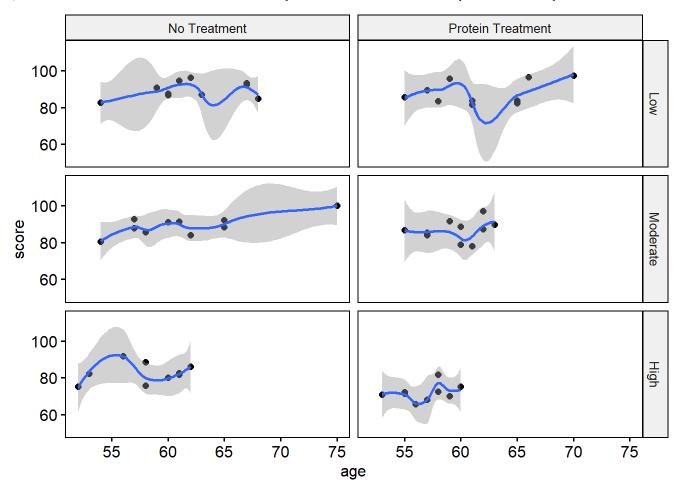
Factorial ANCOVA | Assumption Check: Omnibus and Grouped Level

```
# Check Assumptions using techniques described in class
ancova(data = dat_stress,
    dep = score,
    factors = c(Treatment, Exercise),
    covs = age,
    effectSize = "partEta",
    homo = TRUE,
    qq = TRUE,
    norm = TRUE)
```

ANCOVA								
ANCOVA - scor	e							
		Sum of	Squares	df	Mean Square	F	р	η²p
Treatment			275	1	275.0	11.07	0.002	0.173
Exercise			1029	2	514.7	20.71	< .001	0.439
age			226	1	226.4	9.11	0.004	0.147
Treatment:E	xercise		221	2	110.5	4.45	0.016	0.144
Residuals			1317	53	24.8			
		es Test <i>(</i>	levene's)					
		es Test (Levene's)					
	f Varianc	es Test (p	Levene's)					
	f Varianc		Levene's)					
Homogeneity o	f Varianco 1 df2	р	Levene's)					
Homogeneity o F df 0.955	f Variance 1 df2 5 54	p 0.453	Levene's)					
Homogeneity o	f Variance 1 df2 5 54	p 0.453	Levene's)					
Homogeneity o F df 0.955	f Variance 1 df2 5 54	p 0.453	Levene's)					



```
## `geom_smooth()` using formula = 'y ~ x'
```



```
# Homogeneity of Regression slopes

dat_stress %>%
  anova_test(score ~ age + Treatment + Exercise + Treatment*Exercise + age*Treatment + age*Exercise + age*Exercise*Treatment)
```

```
## ANOVA Table (type II tests)
##
##
                     Effect DFn DFd
                                                    p p<.05
                                                                 ges
                                      8.359 6.00e-03
                                                          * 0.148000
## 1
                                  48
                         age
                               1
## 2
                  Treatment
                                      9.907 3.00e-03
                                                          * 0.171000
## 3
                   Exercise
                                  48 18.197 1.31e-06
                                                          * 0.431000
## 4
         Treatment:Exercise
                               2
                                 48
                                      3.303 4.50e-02
                                                          * 0.121000
## 5
                                      0.009 9.25e-01
                                                            0.000189
              age:Treatment
                               1
                                 48
## 6
               age:Exercise
                                  48
                                      0.235 7.91e-01
                                                            0.010000
## 7 age:Treatment:Exercise
                               2 48
                                      0.073 9.30e-01
                                                            0.003000
```

```
# Normality assessments
lm<-lm(score~age + Exercise*Treatment, dat_stress)
model.metrics <- augment(lm)
shapiro_test(model.metrics$.resid)</pre>
```

```
# Homogeneity of variance assessments
model.metrics %>%
levene_test(.resid ~ Exercise*Treatment)
```

Factorial ANCOVA | Conducting the ANCOVA

```
options(digits=3)
ancova(data = dat_stress,
    dep = score,
    factors = c(Treatment, Exercise),
    covs = age,
    effectSize = "partEta",
    postHoc = ~Exercise + Treatment: Exercise,
    postHocCorr = 'bonf',
    postHocES = 'd',
    postHocEsCi = TRUE,
    emMeans= ~ Exercise + Treatment + Exercise: Treatment,
    emmTables=TRUE,
    emmPlots=TRUE)
```

NOTE: Results may be misleading due to involvement in interactions

Sum of Squares df Mean Square F p η ² p Treatment 275 1 275.0 11.07 0.002 0.173 Exercise 1029 2 514.7 20.71 < .001 0.439 age 226 1 226.4 9.11 0.004 0.147 Treatment:Exercise 221 2 110.5 4.45 0.016 0.144 Residuals 1317 53 24.8 POST HOC TESTS	#								
Sum of Squares df Mean Square F p n²p	# ANCOVA	- score							
Treatment 275 1 275.0 11.07 0.002 0.173	# #		Sum of Squa	res	df Me	an Square	F	р	 η²p
Exercise 1029 2 514.7 20.71 < .001 0.439 age 226.1 226.4 9.11 0.004 0.147 The Treatment:Exercise 221 2 110.5 4.45 0.016 0.144 Residuals 1317 53 24.8 POST HOC TESTS FOR THOC Comparisons - Exercise Exerc	# ———— # Tnoat	-mont			1	275 0	11 07		2 0 172
# age									
Treatment: Exercise		.136							
Residuals 1317 53 24.8 POST HOC TESTS Post Hoc Comparisons - Exercise Resolver Upper Low - Moderate -0.0950 1.59 53.0 -0.0596 1.000 0.0191 -0.660 0.622 Moderate - High 9.5942 1.74 53.0 5.5063 < .001 Moderate - High 9.6892 1.66 53.0 5.8495 < .001 Moderate - High 9.6892 1.66 53.0 5.8495 < .001 Note. Comparisons are based on estimated marginal means Moderate - High 9.6892 1.66 53.0 5.8495 < .001 Note. Comparisons - Treatment: Exercise Note. Comparisons - Treatment High 5.4851 Note. Comparisons - Treatment Low 1.5286	•	ment·Exercise							
Post Hoc Comparisons - Exercise Exercise								0.01	0.144
POST HOC TESTS Post Hoc Comparisons - Exercise Exercise									
Post Hoc Comparisons - Exercise Exercise									
Post Hoc Comparisons - Exercise		OC TESTS							
Exercise Exercise Mean Difference SE df t p-bonferroni shen's d Lower Upper E Low - Moderate -0.0950 1.59 53.0 -0.0596 1.000 20.0191 -0.660 0.622 E - High 9.5942 1.74 53.0 5.5063 <.001 247 1.130 2.720 E Moderate - High 9.6892 1.66 53.0 5.8495 <.001 238 1.177 2.710 E Note. Comparisons are based on estimated marginal means E Post Hoc Comparisons - Treatment: Exercise E Treatment Exercise Treatment Exercise Mean Difference E df t p-bonferroni Cohen's d Lower Upper E No Treatment Low - No Treatment High 5.4851 23 53.0 -0.07727 1.000 -0.03460 -0.933 0.864 E No Treatment High 5.4851 34 53.0 2.34727 0.340 1.10037 0.136 2.065 E Protein Treatment Moderate 1.5111 27 53.0 0.66538 1.000 0.30315 -0.611 1.218	t Post Ho	oc Companicons	Evoncico						
Low									
Note Comparisons are based on estimated marginal means	Exerc	rise Fx	ercise Mean	Differ	ence	SE d	f t		n-honferroni
Low				DITTE	CIICC	JL u			p boili ci i olii
Low - Moderate -0.0950 1.59 53.0 -0.0596 1.000 .0191 -0.660 0.622 - High 9.5942 1.74 53.0 5.5063 < .001 47 1.130 2.720 - Moderate - High 9.6892 1.66 53.0 5.8495 < .001 38 1.177 2.710 Note. Comparisons are based on estimated marginal means Post Hoc Comparisons - Treatment: Exercise Treatment Exercise Treatment Exercise Mean Difference df t p-bonferroni Cohen's d Lower Upper No Treatment Low - No Treatment High 5.4851 34 53.0 2.34727 0.340 1.1007 0.136 2.065 - Protein Treatment Low 1.5286 23 53.0 0.68538 1.000 0.30665 -0.593 1.206 - Protein Treatment Moderate 1.5111 27 53.0 0.66630 1.000 0.30315 -0.611 1.218									
1.130 2.720 1.130 2.720 1.130 2.720 1.130 2.720 1.130 2.720 1.130 2.720 1.130 2.710 1.130 2.710 1.130 2.710 1.130 2.710 1.130 2.710 1.130 2.710 1.130 2.710 1.130 2.710 1.140 1.15									
- High 9.5942 1.74 53.0 5.5063 < .001 47 1.130 2.720 Moderate - High 9.6892 1.66 53.0 5.8495 < .001 Note. Comparisons are based on estimated marginal means Post Hoc Comparisons - Treatment: Exercise Treatment Exercise Treatment Cohen's d Lower Upper No Treatment Low - No Treatment High 5.4851 Sand 9.68538 1.000 0.30665 -0.593 1.206 Protein Treatment Low 1.5211 7 53.0 0.66630 1.000 0.30315 -0.6611 1.218	Low	- Mo	derate	-0.	0950	1.59 5	3.0 -0	.0596	1.000
1.130 2.720	.0191								
Moderate			gh	9.	5942	1.74 5	3.0 5	5.5063	< .001
Note. Comparisons are based on estimated marginal means Post Hoc Comparisons - Treatment: Exercise Treatment									
Note. Comparisons are based on estimated marginal means Post Hoc Comparisons - Treatment:Exercise			gh	9.	6892	1.66 5	3.0 5	.8495	< .001
Note. Comparisons are based on estimated marginal means Post Hoc Comparisons - Treatment:Exercise Post Hoc Comparisons - Treatment:Exercise Treatment Exercise Treatment Cohen's d Lower Upper		177 2.710							
Post Hoc Comparisons - Treatment:Exercise Treatment									
Post Hoc Comparisons - Treatment:Exercise Treatment		Companicanc		+:	l manaina	1 maans			
Post Hoc Comparisons - Treatment:Exercise Treatment		. Comparisons a	re based on est	cimated	ı margına	ı means			
Post Hoc Comparisons - Treatment:Exercise									
Treatment df t p-bonferroni Cohen's d Lower Upper									
df t p-bonferroni Cohen's d Lower Upper No Treatment Low - No Treatment Moderate -0.1725 23 53.0 -0.07727 1.000 -0.03460 -0.933 0.864 - No Treatment High 5.4851 34 53.0 2.34727 0.340 1.10037 0.136 2.065 - Protein Treatment Low 1.5286 23 53.0 0.68538 1.000 0.30665 -0.593 1.206 - Protein Treatment Moderate 1.5111 27 53.0 0.66630 1.000 0.30315 -0.611 1.218	:	oc Comparisons	- Treatment:Eye	arcise					
df t p-bonferroni Cohen's d Lower Upper No Treatment Moderate -0.1725 23 53.0 -0.07727 1.000 -0.03460 -0.933 0.864 - No Treatment High 5.4851 34 53.0 2.34727 0.340 1.10037 0.136 2.065 - Protein Treatment Low 1.5286 23 53.0 0.68538 1.000 0.30665 -0.593 1.206 - Protein Treatment Moderate 1.5111 27 53.0 0.66630 1.000 0.30315 -0.611 1.218	Post Ho	oc Comparisons	- Treatment:Exe	ercise					
No Treatment Low - No Treatment Moderate -0.1725 23 53.0 -0.07727 1.000 -0.03460 -0.933 0.864 - No Treatment High 5.4851 34 53.0 2.34727 0.340 1.10037 0.136 2.065 - Protein Treatment Low 1.5286 23 53.0 0.68538 1.000 0.30665 -0.593 1.206 - Protein Treatment Moderate 1.5111 27 53.0 0.66630 1.000 0.30315 -0.611 1.218	Post Ho	·					Evancis	Maan	Difference
23 53.0 -0.07727	# Post Ho	ment	Exercise	Tr		Lower			Difference
23 53.0 -0.07727 1.000 -0.03460 -0.933 0.864 - No Treatment High 5.4851 34 53.0 2.34727 0.340 1.10037 0.136 2.065 - Protein Treatment Low 1.5286 23 53.0 0.68538 1.000 0.30665 -0.593 1.206 - Protein Treatment Moderate 1.5111 27 53.0 0.66630 1.000 0.30315 -0.611 1.218	Post Ho	ment	Exercise	Tr		Lower			Difference
- No Treatment High 5.4851 34 53.0 2.34727 0.340 1.10037 0.136 2.065 - Protein Treatment Low 1.5286 23 53.0 0.68538 1.000 0.30665 -0.593 1.206 - Protein Treatment Moderate 1.5111 27 53.0 0.66630 1.000 0.30315 -0.611 1.218	: Post Ho	t t	Exercise p-bonferron:	Tr i Co	ohen's d		Upper	. 	
34 53.0 2.34727 0.340 1.10037 0.136 2.065 - Protein Treatment Low 1.5286 23 53.0 0.68538 1.000 0.30665 -0.593 1.206 - Protein Treatment Moderate 1.5111 27 53.0 0.66630 1.000 0.30315 -0.611 1.218	Post Ho Treat df No Tr	t reatment	Exercise p-bonferron: Low	Tr i Co	ohen's d	nt	Upper	 :e	
- Protein Treatment Low 1.5286 23 53.0 0.68538 1.000 0.30665 -0.593 1.206 - Protein Treatment Moderate 1.5111 27 53.0 0.66630 1.000 0.30315 -0.611 1.218	Post Ho Treat df No Tr	t reatment	Exercise p-bonferron: Low 1.000	Tr i Co - No	Treatme	nt -0.933	Upper Moderat 0.864	 :e	-0.1725
23 53.0 0.68538 1.000 0.30665 -0.593 1.206 - Protein Treatment Moderate 1.5111 27 53.0 0.66630 1.000 0.30315 -0.611 1.218	Post Ho Treat df No Tr 23 53.	reatment 0 -0.07727	Exercise p-bonferron: Low 1.000	Tr i Co - No 0 -	Treatme 0.03460 Treatme	nt -0.933 nt	Upper Moderat 0.864 High		-0.1725
- Protein Treatment Moderate 1.5111 27 53.0 0.66630 1.000 0.30315 -0.611 1.218	Post Ho Treat df No Tr 23 53.	reatment 0 -0.07727	Exercise p-bonferron: Low 1.000	Tr i Co - No 0 - - No	Treatme 0.03460 Treatme 1.10037	nt -0.933 nt 0.136	Moderat 0.864 High 2.065		-0.1725 5.4851
27 53.0 0.66630 1.000 0.30315 -0.611 1.218	Post Ho Treat No Tr No Tr 34 53.	reatment .0 -0.07727 .0 2.34727	Exercise p-bonferron: Low 1.000	Tr i Co - No 0 - - No 0	Treatme 0.03460 Treatme 1.10037 Otein Tr	nt -0.933 nt 0.136 eatment	Moderat 0.864 High 2.065 Low	ee	-0.1725 5.4851
	# Post Ho # Treat # Mo Tr 23 53. # 34 53. # 23 53.	reatment .0 -0.07727 .0 2.34727	Exercise p-bonferron: Low 1.000	Tr i Co - No 0 - - No 0	Treatme 0.03460 Treatme 1.10037 Totein Tr 0.30665	nt -0.933 nt 0.136 eatment -0.593	Moderat 0.864 High 2.065 Low 1.206	re	-0.1725 5.4851 1.5286
- Protein treatment from 15 /210	# Post Ho # Treat # Mo Tr 23 53. # 34 53. # 23 53.	reatment .0 -0.07727 .0 2.34727 .0 0.68538	Exercise p-bonferron: Low 1.000 0.340	Tr i Co - No 0 - No 0 - Pr 0 - Pr	Treatme 0.03460 Treatme 1.10037 Otein Tr 0.30665	nt -0.933 nt 0.136 eatment -0.593 eatment	Moderat 0.864 High 2.065 Low 1.206	re i	-0.1725 5.4851 1.5286

##			Moderate -	No Treatment	High	5.6576
2.30	53.0	2.45505	0.261	1.13497 0.182	2.088	
##			-	Protein Treatment	Low	1.7011
2.23	53.0	0.76287	1.000	-0.34125 -1.241	0.558	
##			-	Protein Treatment	Moderate	1.6836
2.25	53.0	0.74847	1.000	0.33775 -0.570	1.245	
##			-	Protein Treatment	High	15.4044
2.35	53.0	6.56340	< .001 3.	09029 1.970 4.	210	
##			High -	Protein Treatment	Low	-3.9565
2.32	53.0	-1.70712	1.000	0.79372 -0.152	1.739	
##			-	Protein Treatment	Moderate	-3.9740
2.25	53.0	-1.76839	1.000	0.79722 -0.120	1.715	
##			-	Protein Treatment	High	9.7468
2.23	53.0	4.36234	< .001 1.	95532 0.979 2.	932	
##	Protein	Treatment	Low -	Protein Treatment	Moderate	-0.0175
2.26	53.0	-0.00774	1.000	-0.00350 -0.912	0.905	
##			-	Protein Treatment	High	13.7033
2.36	53.0	5.79876	< .001 2.	74904 1.658 3.	840	
##			Moderate -	Protein Treatment	High	13.7208
2.27	53.0	6.04155	< .001 2.	75254 1.693 3.	812	

Note. Comparisons are based on estimated marginal means

##

ESTIMATED MARGINAL MEANS

##

##

EXERCISE

Estimated Marginal Means - Exercise

##					
## ##	Exercise	Mean	SE	Lower	Upper
##					
##	Low	87.7	1.16	85.4	90.1
##	Moderate	87.8	1.12	85.6	90.1
##	High	78.1	1.19	75.8	80.5
##					

##

TREATMENT

##

Estimated Marginal Means - Treatment

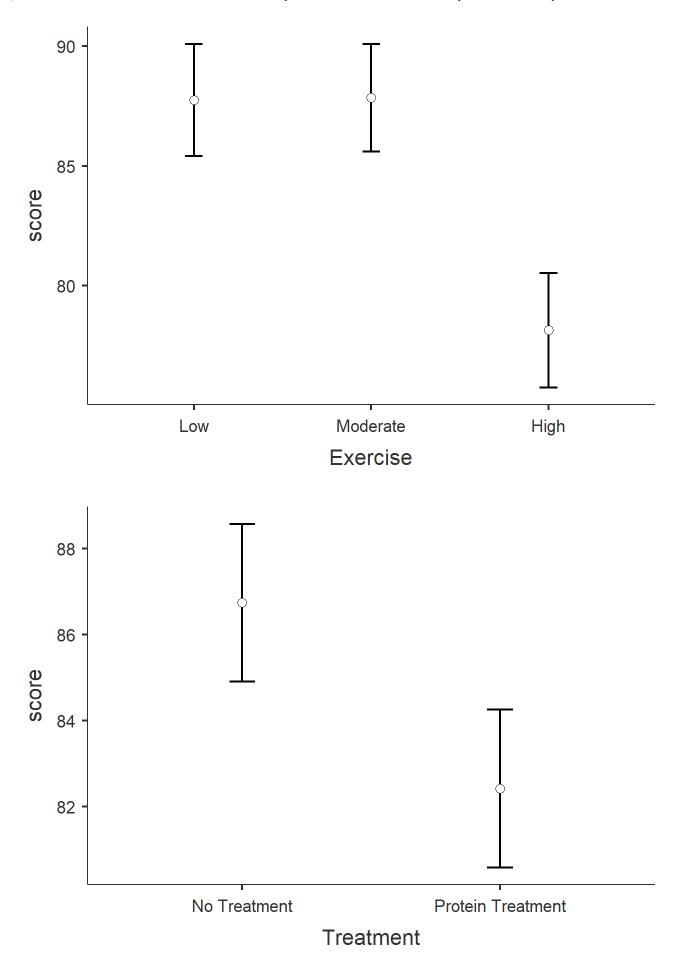
##					
##	Treatment	Mean	SE	Lower	Upper
##					
##	No Treatment	86.7	0.914	84.9	88.6
##	Protein Treatment	82.4	0.914	80.6	84.3
##					

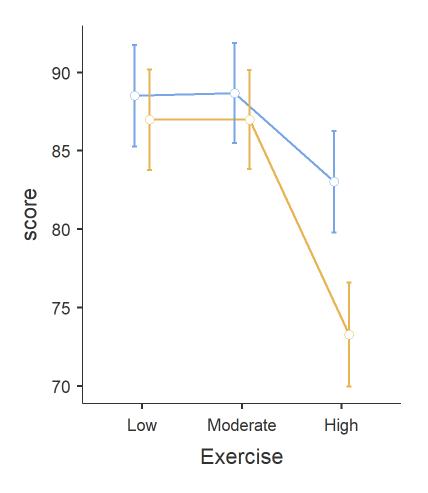
##

EXERCISE: TREATMENT

##

## Treatment ##	Exercise	Mean	SE	Lower	Upper
## No Treatment	Low	88.5	1.62	85.3	91.7
##	Moderate	88.7	1.59	85.5	91.9
##	High	83.0	1.61	79.8	86.3
## Protein Treatm	ent Low	87.0	1.60	83.8	90.2
##	Moderate	87.0	1.58	83.8	90.2
##	High	73.3	1.65	70.0	76.6





Treatment

- No Treatment
- Protein Treatment

```
# Assessment of Simple Main Effects
dat_stress %>%
  group_by(Exercise) %>%
  anova_test(score ~ age + Treatment)
```

```
## # A tibble: 6 × 8
     Exercise Effect
                           DFn
                                  DFd
                                                     p `p<.05`
                                                                  ges
## * <fct>
               <chr>>
                         <dbl> <dbl>
                                       <dbl>
                                                 <dbl> <chr>>
                                                                <dbl>
## 1 Low
                                       2.25 0.152
                                                                0.117
               age
                                                                0.025
## 2 Low
               Treatment
                                       0.437 0.517
                              1
                                   17
                                                                0.281
## 3 Moderate age
                                       6.65
                                            0.02
## 4 Moderate Treatment
                                       0.419 0.526
                                                                0.024
                                       0.794 0.385
## 5 High
               age
                              1
                                   17
                                                                0.045
## 6 High
                                   17 18.7
                                              0.000455
                                                                0.524
               Treatment
                              1
```

```
dat_stress %>%
  group_by(Treatment) %>%
  anova_test(score ~ age + Exercise)
```

```
## # A tibble: 4 × 8
    Treatment
                      Effect
                                 DFn
                                       DFd
                                                         p `p<.05`
                                                                     ges
## * <fct>
                      <chr>
                               <dbl> <dbl> <dbl>
                                                     <dbl> <chr>>
                                                                   <dbl>
                                                           "*"
## 1 No Treatment
                                        26 7.26 0.012
                                                                   0.218
                      age
                                                           "*"
## 2 No Treatment
                                   2
                                        26 3.99 0.031
                                                                   0.235
                      Exercise
## 3 Protein Treatment age
                                   1
                                        26 2.37 0.136
                                                                   0.083
## 4 Protein Treatment Exercise
                                        26 17.3 0.0000164 "*"
                                                                   0.572
```

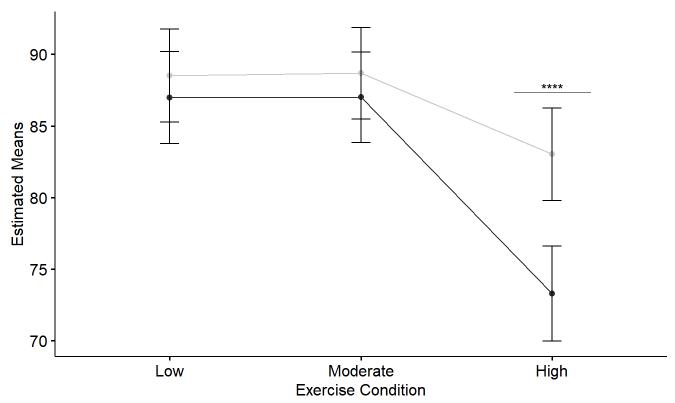
Factorial ANCOVA | Professional ANCOVA Visualization

```
## # A tibble: 1 × 10
    Exercise term
##
                           .y.
                                group1
                                           group2
                                                    df statistic
                                                                          p.adj
    <fct>
            <chr>
                          <chr> <chr>
                                           <chr> <dbl>
                                                        <dbl>
                                                                   <dbl>
                                                                          <dbl>
## 1 High
             age*Treatment score No Treatm... Prote...
                                                    53
                                                          4.36 5.97e-5 5.97e-5
## # i 1 more variable: p.adj.signif <chr>
```

```
## # A tibble: 3 × 10
   Treatment
##
                                                        df statistic
                       term
                                      group1 group2
                                .y.
                                                                               p.adj
     <fct>
                       <chr>>
                                <chr> <chr> <chr> <chr> <dbl>
                                                               <dbl>
                                                                               <dbl>
## 1 Protein Treatment age*Exe... score Low
                                             Moder...
                                                        53 -0.00774 9.94e-1 1
## 2 Protein Treatment age*Exe... score Low
                                                        53 5.80
                                                                     3.78e-7 1.13e-6
                                             High
## 3 Protein Treatment age*Exe... score Moder... High
                                                                     1.55e-7 4.66e-7
                                                        53 6.04
## # i 1 more variable: p.adj.signif <chr>
```

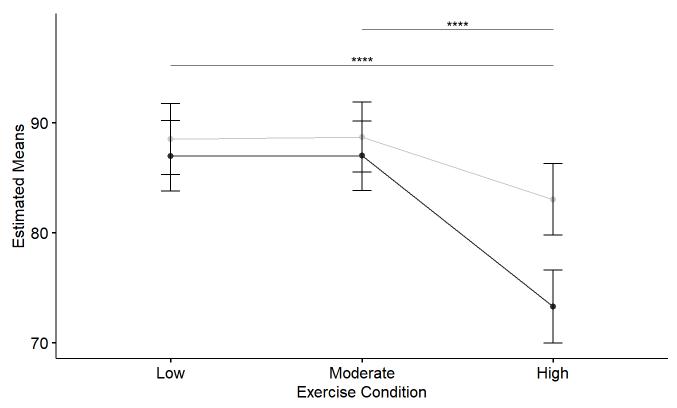
```
lp <- ggline(
  get_emmeans(pwc),
  x = "Exercise",
  y = "emmean",
  color = "Treatment",
  palette = "grey") +
  geom_errorbar(
   aes(ymin = conf.low,
      ymax = conf.high),
  width = 0.1)</pre>
```

Treatment - No Treatment - Protein Treatment



pwc: Emmeans test; p.adjust: Bonferroni

Treatment → No Treatment → Protein Treatment



pwc: Emmeans test; p.adjust: Bonferroni