

# Model making

Cycle  
Level 1 variables  
 ✓ cycle #  
 ✓ stiffness  
 ✓ damping  
 nonlinear component  
 stiffness fraction

foam  
Level 2  
 ✓ initial stress  
 ✓ strain  
 ✓ freq  
 ✓ amp  
 ✓ porosity  
 ✓ chem index  
 ✓ ID

stiffness fraction - response  
 freq, amp, chem index, cycle #, porosity

level 1:  $Y_{ij} = a_i + b_i \cdot \log(\text{cycle}) + \epsilon_{ij}$ , attach ID to cycle in R

level 2:

$$a_i = \alpha_0 + \alpha_1(\text{freq}) + \alpha_2(\text{amp}) + \alpha_3(\text{chemID}) + \alpha_4(\text{porosity}) + \alpha_5(\text{porosity} \cdot \text{chemID}) + u_i$$

$$b_i = \beta_0 + \beta_1(\text{freq}) + \beta_2(\text{amp}) + \beta_3(\text{chemID}) + \beta_4(\text{porosity}) + \beta_5(\text{porosity} \cdot \text{chemID}) + v_i$$

$$Y_{ij} = \alpha_0 + \alpha_1 \text{freq} + \alpha_2 \text{amp} + \alpha_3 \text{chemID} + \alpha_4 \text{porosity} + \alpha_5 \text{porosity} \cdot \text{chemID} + (\beta_0 + \beta_1 \text{freq} + \beta_2 \text{amp} + \beta_3 \text{chemID} + \beta_4 \text{porosity} + \beta_5 (\text{porosity} \cdot \text{chemID})) \cdot \log(\text{cycle}_i) + u_i + v_i \log(\text{cycle}) + \epsilon_{ij}$$