

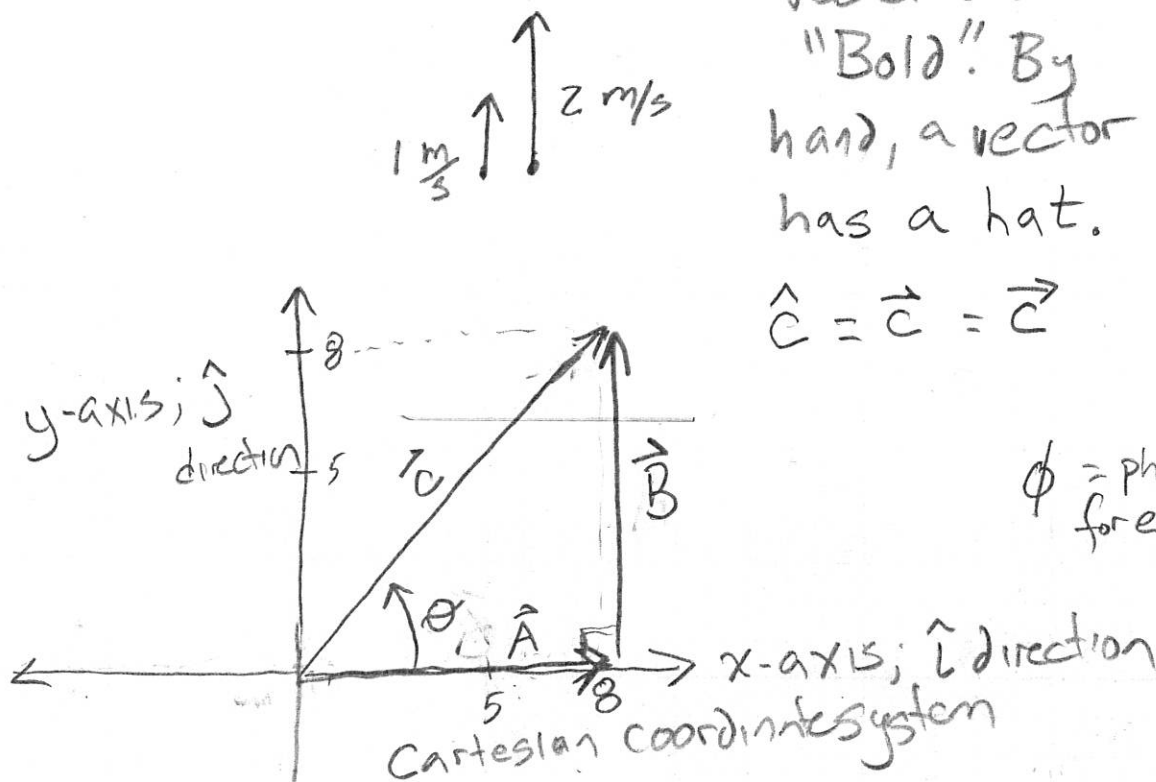
## [Chapter 3]

Vectors have direction & magnitude.

In text a vector is in "Bold". By hand, a vector has a hat.

$$\hat{c} = \vec{c} = \vec{c}$$

$\phi = \text{phi}$   
for elevation



$$\begin{aligned} \text{mag } C &= (A^2 + B^2)^{\frac{1}{2}} \\ C &= \sqrt{(A)^2 + (B)^2} \\ C &= (8^2 + 8^2)^{\frac{1}{2}} \\ C &= (64 + 64)^{\frac{1}{2}} \\ &= (128)^{\frac{1}{2}} \end{aligned}$$

$$\underline{\underline{C = 11.3}}$$

$$\vec{c} = 8\hat{i} + 8\hat{j}$$

$$\vec{c} = 8\hat{i} + 8\hat{j}$$

$$\vec{c} = \vec{A} + \vec{B} \quad \text{magnitude}$$

$$\vec{A} = 8\hat{i}; A = 8 \text{ units}$$

$$\vec{B} = 8\hat{j}; B = 8 \text{ units}$$

The magnitude of  $\vec{C}$  is 11.3 units.

orelei = +1

$$\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{8}{8} = 1$$

$$\sin \theta = \frac{\text{opp}}{\text{hyp}} =$$

$$\cos \theta = \frac{\text{adj}}{\text{hyp}}$$

$$\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{8}{8}$$

$$\theta = \arctan\left(\frac{8}{8}\right)$$

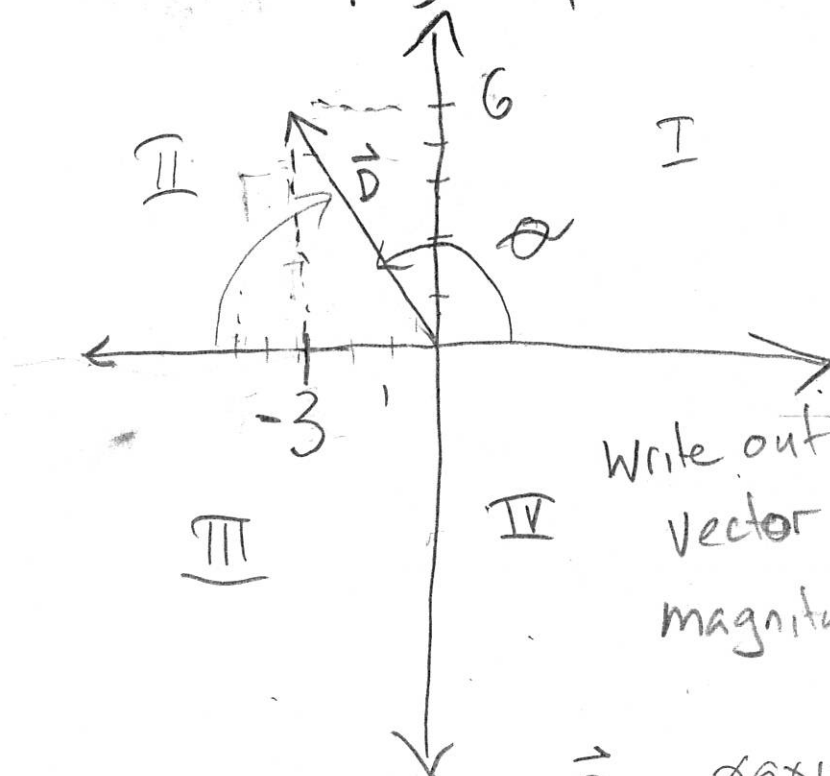
$$\theta = \arctan\left(\frac{8}{8}\right)$$

$$\theta = \tan^{-1}\left(\frac{8}{8}\right) = 45^\circ$$

$$= 0.785398$$

radians

$$= \boxed{\phantom{0.785398}}$$



Write out  $\vec{D}$  in  
vector notation,  
magnitude & angle

$$\begin{aligned}\vec{D} &= x\text{axis}, y\text{axis} \\ &= -3\hat{i} + 6\hat{j} \\ \text{mag } \vec{D} &= (-3^2 + 6^2)^{\frac{1}{2}} \\ &= (9 + 36)^{\frac{1}{2}} \\ &= (45)^{\frac{1}{2}} \\ &= 3\sqrt{5} \\ &\approx 6.7\end{aligned}$$

$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$\tan \theta = \frac{6}{-3}$$

$$\tan \theta = -2$$

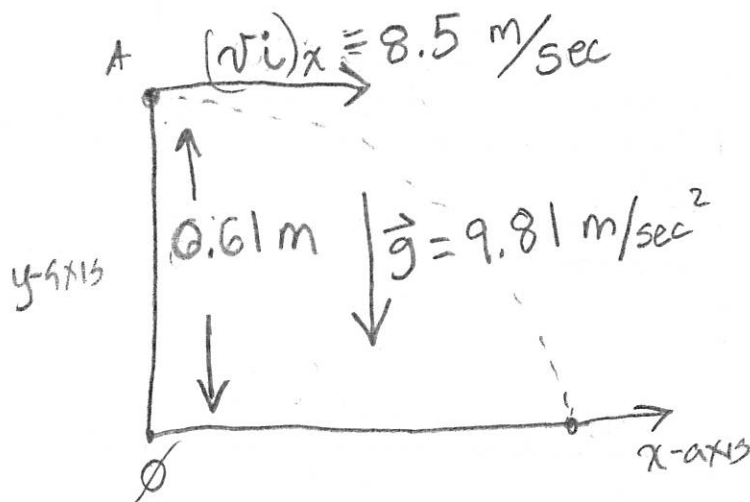
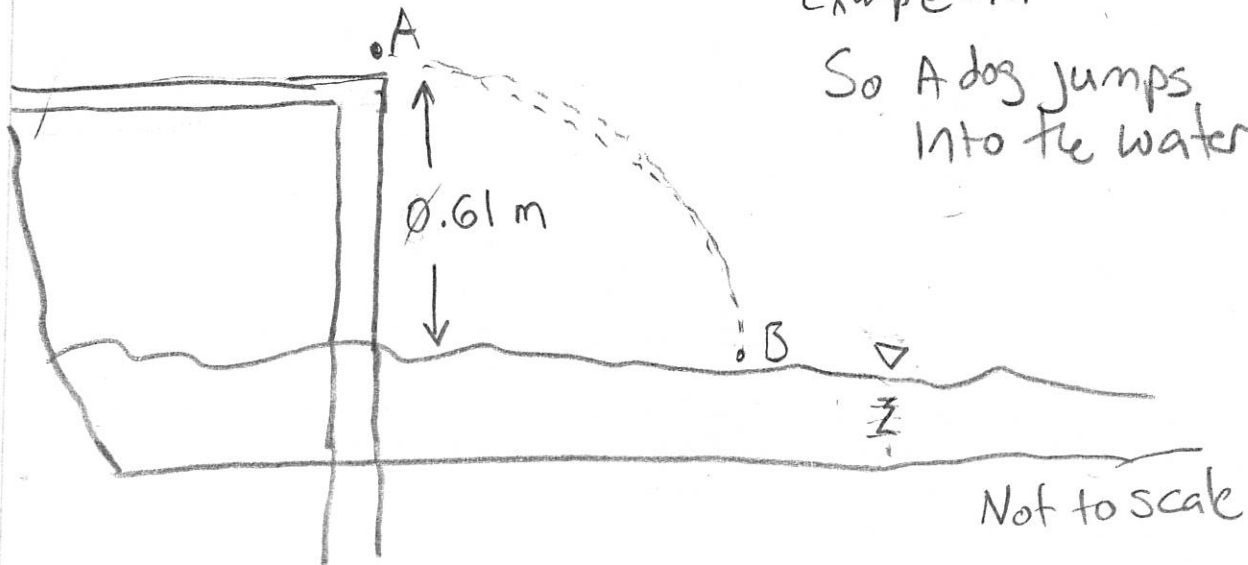
$$\theta = \tan^{-1}(-2)$$

$$= -63.4^\circ + 180$$

$$= 116.6^\circ \text{ or } -1.107 \text{ rad}$$

## Example 3.11

So A dog jumps  
into the water...



$$x_f = x_i + v_x \Delta t$$

$$[m] + \left[ \frac{m}{\text{sec}} \right] \cdot \text{sec}$$

$$x_f = 0 + v_x \Delta t$$

$$x_f = 8.5 \cdot \Delta t$$

Given

$$x_i = 0$$

$$y_i = 0.61 \text{ m}$$

$$(v_i)_x = 8.5 \text{ m/sec}$$

$$(v_i)_y = 0 \text{ m/sec}$$

$$\vec{a}_x = 0 \text{ m/sec}^2$$

$$\vec{a}_y = \vec{g} = 9.81 \text{ m/sec}^2$$

Find:

Displacement  
How far did the  
dog jump?

$$\vec{v}_y [\text{m/sec}] = \vec{a}_y [\text{m/sec}^2] \Delta t$$

$$y_f = y_i + (v_i)_y \Delta t - \frac{1}{2} \vec{g} (\Delta t)^2$$

$$[m] = [m] + \left[ \frac{m}{\text{sec}} \cdot \text{sec} \right] + \left[ \frac{m}{\text{sec}^2} \cdot \text{sec}^2 \right]$$

$$0 = 0.61 + 0 \cdot \Delta t - \frac{1}{2} (9.81) \Delta t^2$$

$$-0.61 = -\frac{1}{2} (9.81) \Delta t^2$$

$$0.61 = \frac{1}{2} (9.81) \Delta t^2$$

$$0.61 = \left( \frac{9.81}{2} \right) \Delta t^2$$

$$\left( \frac{2 \cdot 0.61}{9.81} \right) = \Delta t^2$$

$$\left( \frac{2 \cdot 0.61}{9.81} \right)^{\frac{1}{2}} = \Delta t$$

$$\left( \frac{1.22}{9.81} \right)^{\frac{1}{2}} = \Delta t$$

$$\underline{\underline{0.353 = \Delta t}}$$

$$x_f = 8.5 \Delta t$$

$$x_f = 8.5 (0.353)$$

$$\underline{\underline{x_f = 3.0 \text{ m}}}$$

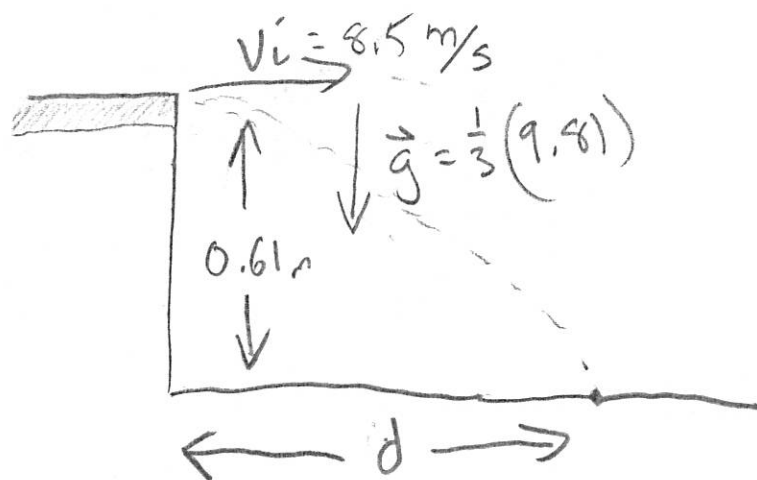
Imagine dog jumping on mars

Assume  $\vec{g}_{\text{mars}} = \frac{1}{3} \vec{g}_{\text{earth}}$

If everything else is the same

how long is the dog Airborne

and what is  $d$  = displacement of the dog



[Given is as above]

$$y_f = y_i + (v_f)_y \Delta t - \frac{1}{2} \vec{g}_{\text{mars}} \Delta t^2$$

$$0 = 0.61 \text{ m} + 0 - \frac{1}{2} \left[ \frac{1}{3} \cdot 9.81 \text{ m/s}^2 \right] \Delta t^2$$

$$0.61 = \frac{9.81}{6} \Delta t^2$$

$$\left( \frac{6 \cdot 0.61}{9.81} \right)^{\frac{1}{2}} = \Delta t$$

$$\underline{\underline{0.612 = \Delta t}}$$

$$x_f = x_i + v \Delta t$$

$$x_f = 0 + 8.5 \cdot 0.612$$

$$\underline{\underline{x_f = 5.2 \text{ m}}}$$

A <sup>typical</sup> regulation dock jumping dog on Mars  
will be airborne for 0.61 sec and  
have a displacement of 5.2 m

On Earth the dog will be airborne  
for 0.35 sec and will have a  
displacement of 3 m

W.F.] Good class, following last semester  
Right speed

D.T.] Good review of magnitude & vectors  
Kinematics. Right speed.

T.D.] Good, Improve graphs to  
show vector lengths

L.L.] Fine. Still fresh. Should be interesting.  
Took in feedback.

B.B.] Good. Felt comfortable. Visual learner.

Homework: send me a text msg  
605-209-9974  
with your Name