

# Sensitivity Analyses for Decision Modeling

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June 2014

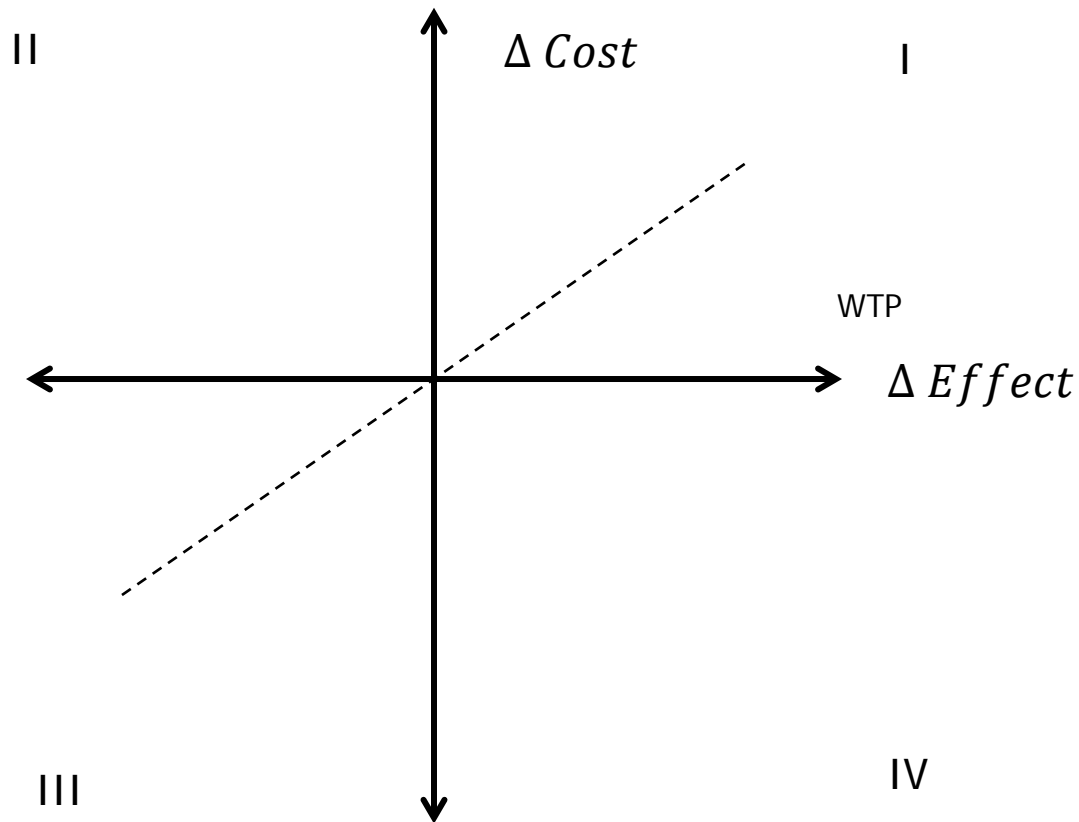
# Content

- Why sensitivity analyses?
  - Modeling Uncertainty
    - One-way sensitivity Analyses
    - Tornado Diagrams
    - Scenario Analyses
    - Probabilistic Sensitivity Analyses
-

# Output of a Decision Model

Type of Model	Output
Budget Impact Model	<i>Cost per strategy</i>
Cost Benefit Model	<i>Net social benefit = Incremental Benefit (cost) – Incremental Costs</i>
Cost-Effectiveness Model	$ICER = \frac{\Delta cost}{\Delta health\ effect}$
Cost-utility Model	$ICER = \frac{\Delta cost}{\Delta QALYs}$

# Cost-effectiveness Model quadrants



*Poll: Which quadrant represents a cost-effective strategy?*

# Cost-effectiveness Model quadrants

## Quadrant I:

- More costly and more effective  
(?)

## Quadrant II:

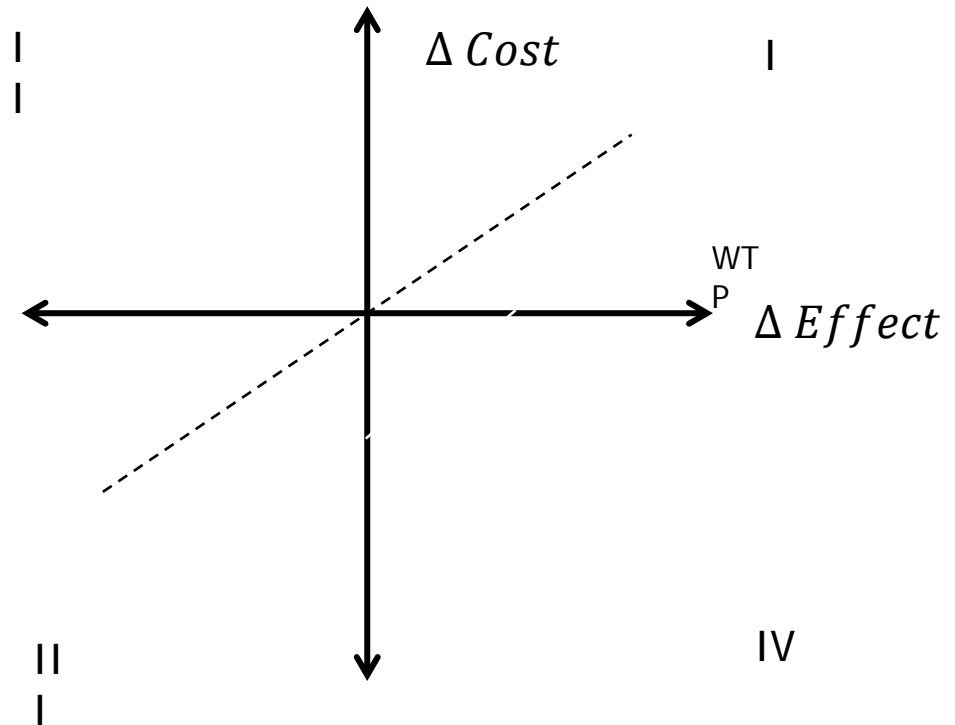
- More costly and less effective  
(No!)

## Quadrant III:

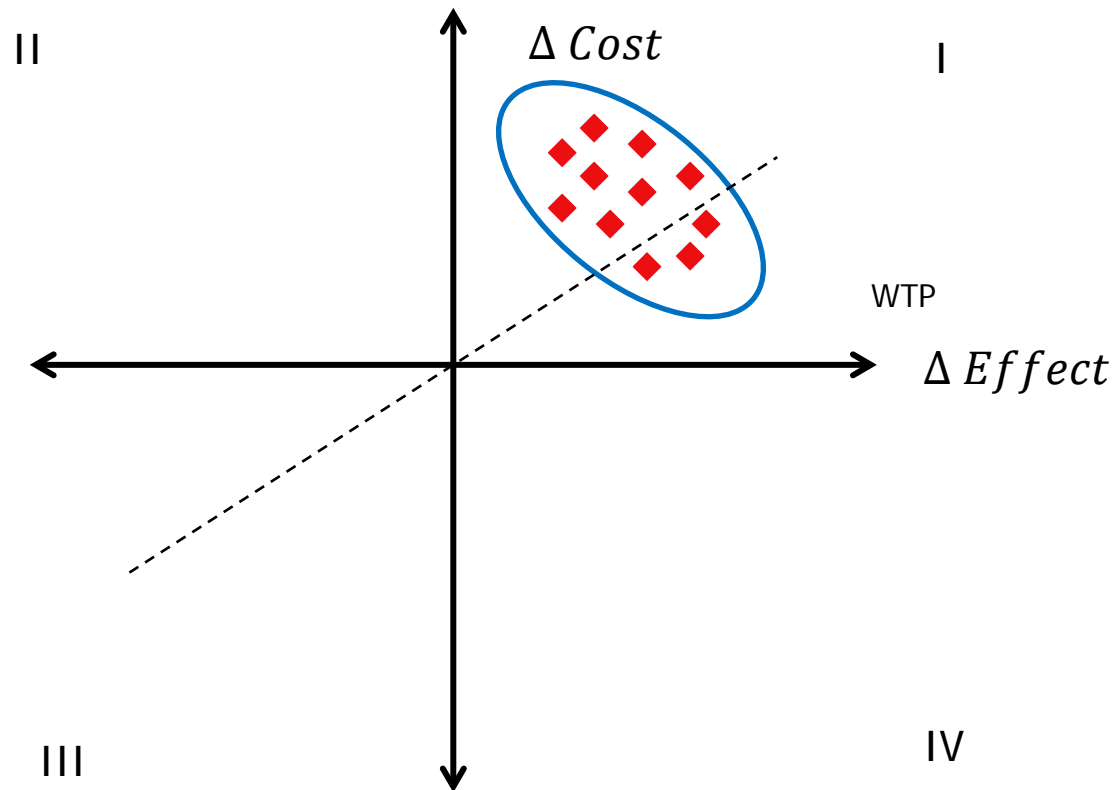
- Less costly and less effective  
(?)

## Quadrant IV:

- Less costly and more effective  
(Yes!)



# Cost-effectiveness Model output



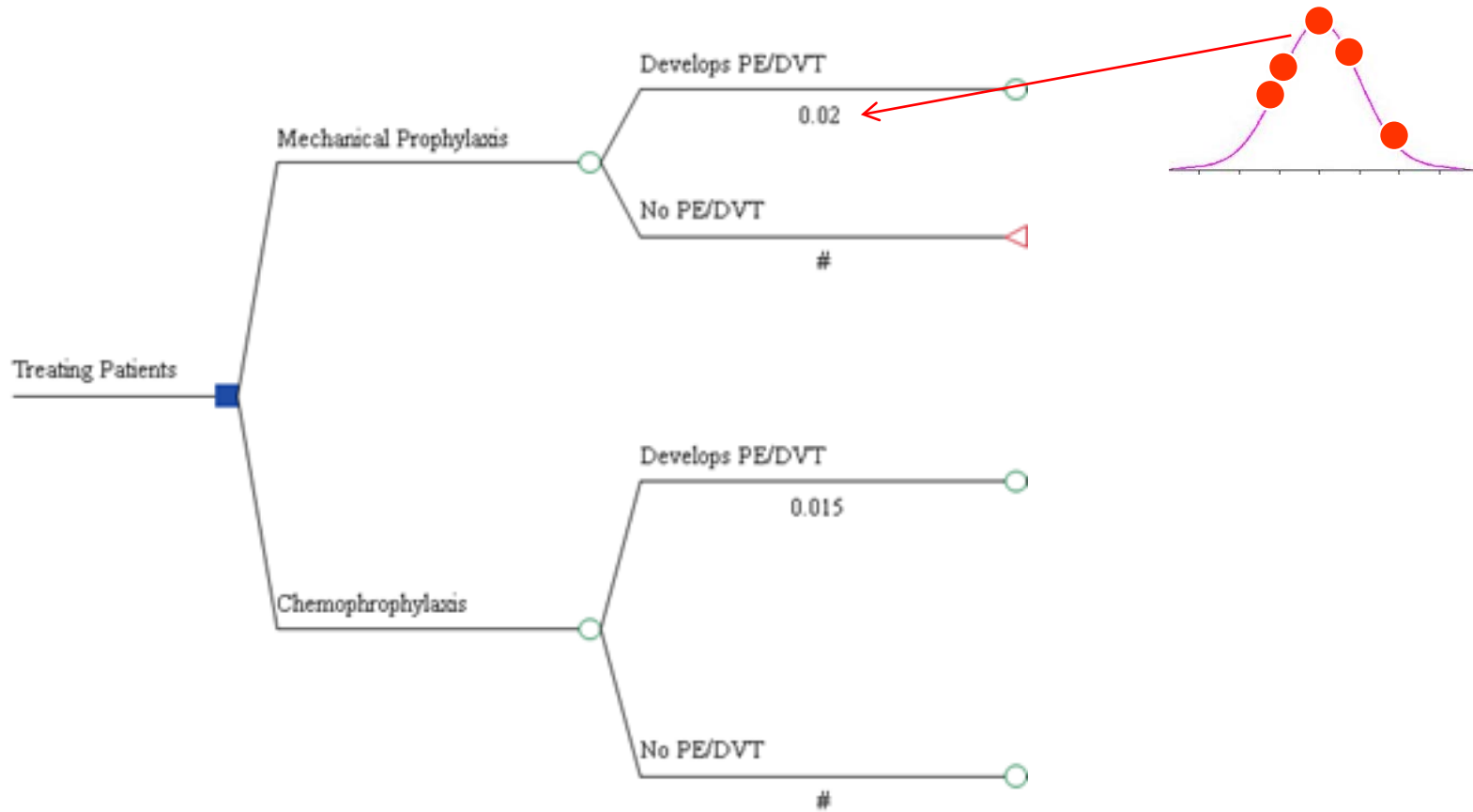
*Variation in your ICER may cause your decision to change*

# Why sensitivity analysis?

- Evaluate how uncertainty in model inputs affects the model outputs
  - Base-case model → ICERs
  - Sensitivity Analyses → Variation in ICER

Statistical Analysis	Cost-Effectiveness Analysis
Mean	ICER (Base-Case)
Variation around Mean	Variation around ICER

# Varying point estimates (TreeAge model)





# General Approach, Sensitivity Analysis

1. Change model input
2. Recalculate ICER
3. If new ICER is substantially different from old ICER → model is sensitive to that parameter
  - In this case, it is very important to be accurate about this parameter!

# Types of inputs

- Cost
  - Health Effect
    - Life Years Saved
    - Utilities
    - Cases of Disease Avoided
    - Infections Cured
  - Probabilities
  - Discount Rate
-


# Types of Uncertainty

Term	Models	AKA	Analagous term in regression	Example
Stochastic Uncertainty	Variation between identical patients	- First-order uncertainty - microsimulation	Error term	19% of Medicare beneficiaries readmitted to the hospital within 30 days. Person 1 = readmitted, Persons 2, 3, 4, 5 = not readmitted
Parameter Uncertainty	Uncertainty in estimation of parameter of interest	- Second-order uncertainty - PSA	Standard Error of the estimate	Toss a fair coin 100 times. You get 55 “heads” and 45 “tails”
Heterogeneity	Differences in patient characteristics	- Observed heterogeneity - variability	Beta-coefficients/test of sig. amongst different levels of a covariate	Drug is cost-effective for people with moderate disease, but is not cost-effective for people with mild or advanced disease

Briggs et al. 2012 Model Parameter Estimation and Uncertainty: A Report of the ISPOR-SMDM Modeling Good Research Practices Task Force – 6. *Value in Health*, 15: 835-842.

# Types of Sensitivity Analyses

# Types of Sensitivity Analyses


- One-way sensitivity Analyses
  - Tornado Diagrams
  - Scenario Analyses
  - Probabilistic Sensitivity Analyses
- 
- Often  
Deterministic
-

# Types of Sensitivity Analyses

- **Deterministic (DSA):** model input is specified as multiple point estimates and varied manually
  - **Probabilistic (PSA):** model inputs are specified as a distribution and varied
-

# DSA versus PSA

Example: Cost input, cost of outpatient visit

	DSA	PSA
Base case	\$100	\$100
Input	\$80, \$90, \$110, \$120	
Results	ICER A (when cost is \$80) ICER B (when cost is \$90) ICER C (when cost is \$110) ICER D (when cost is \$120)	The mean ICER when we vary the base-case using a normal distribution with a mean of \$100 and standard deviation of \$10 is X, using 1000 iterations

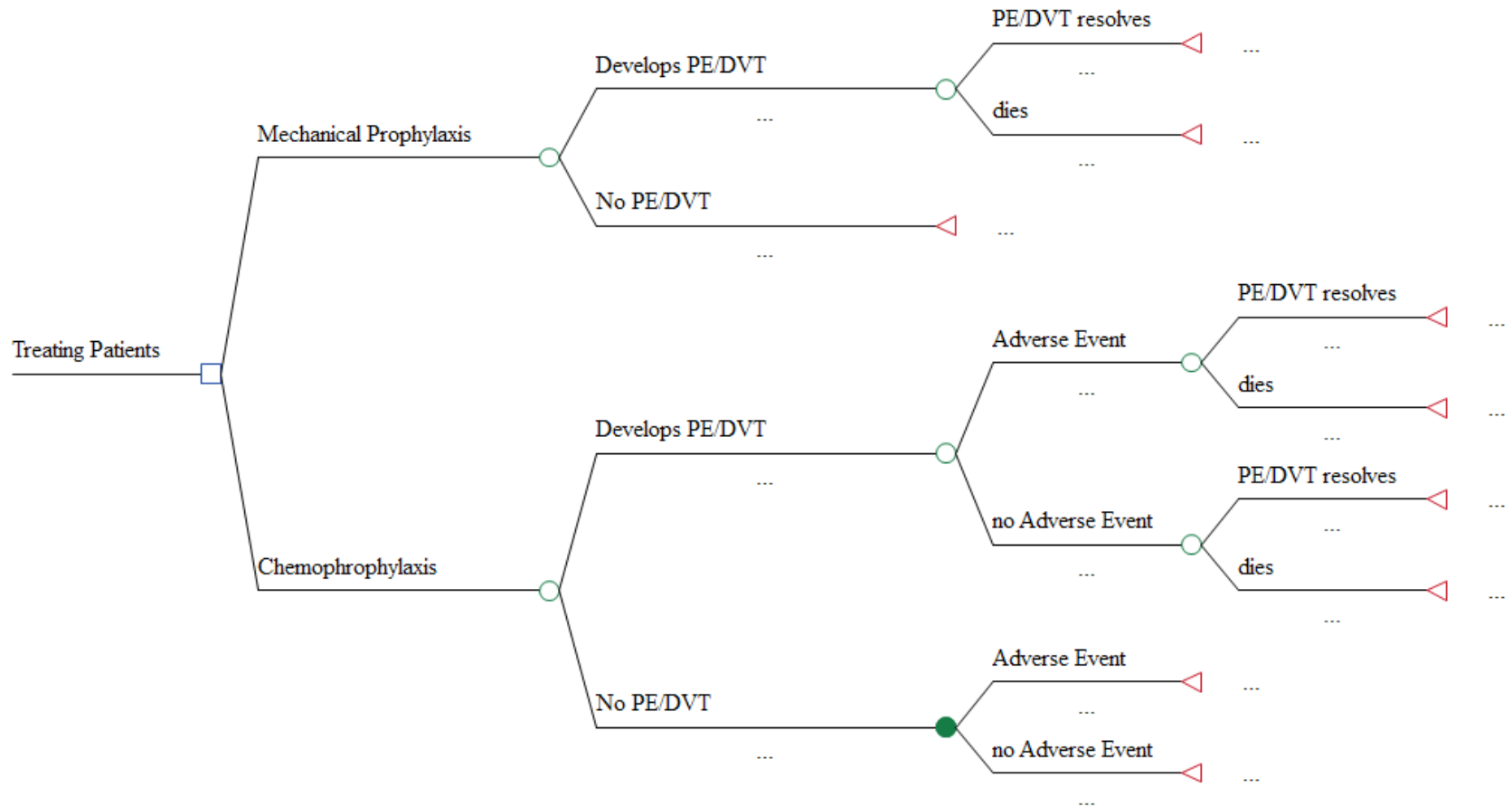
# DSA, PSA and Model structure

	DSA	PSA
Markov Cohort	X	X
Individual-level Markov Model	X	X
Discrete-Event Simulation	X	X

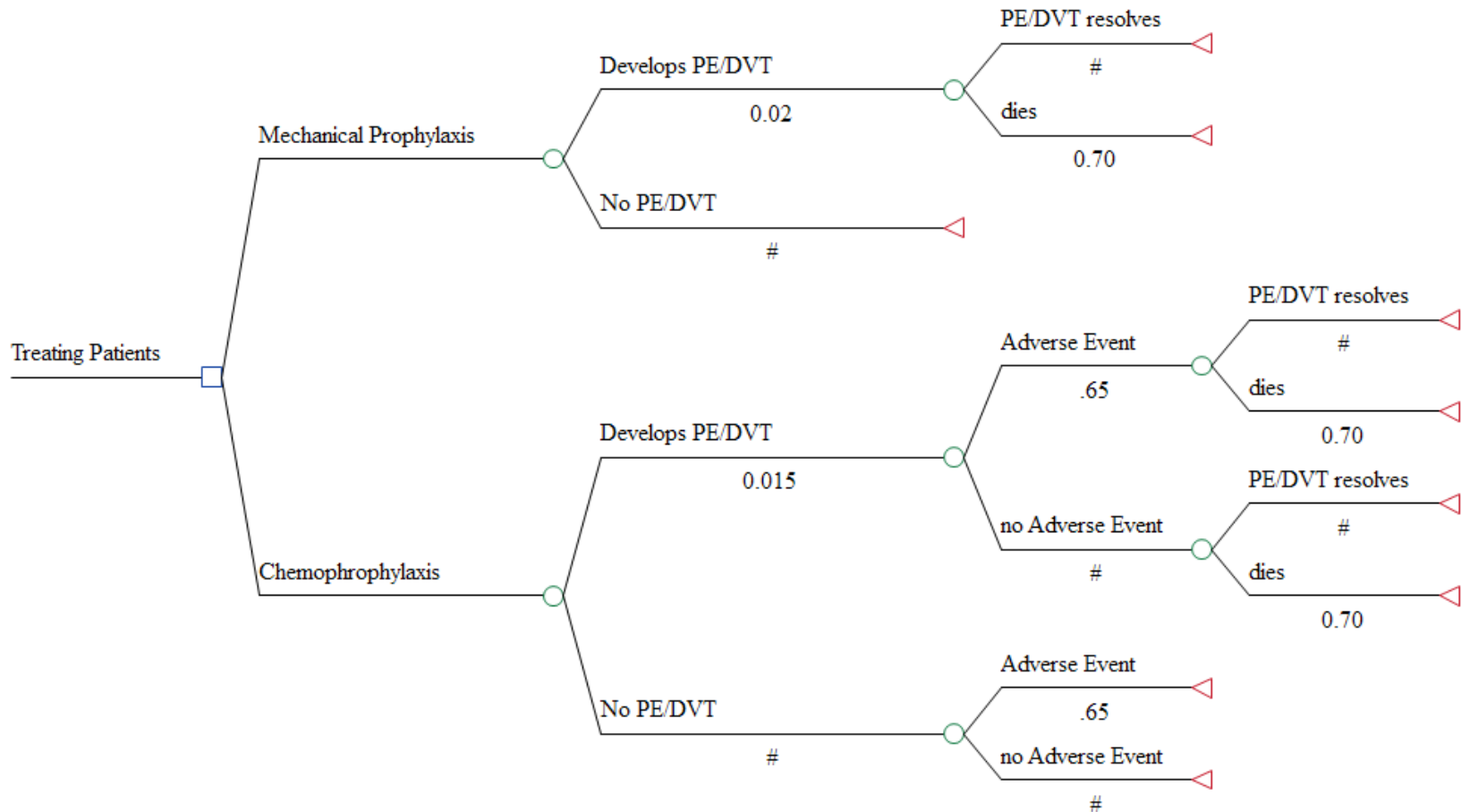


# Sensitivity Analyses in TreeAge

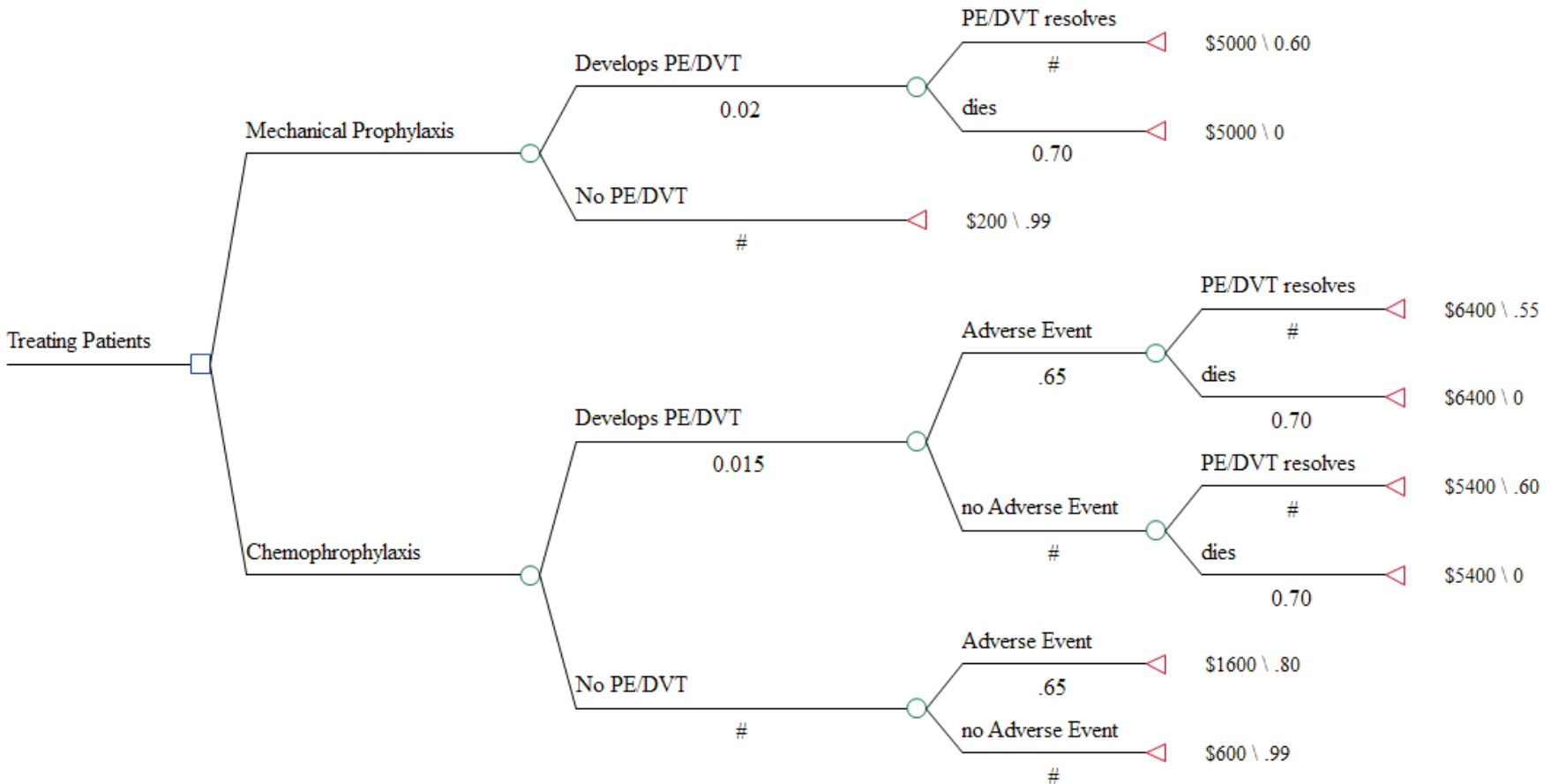
# PE/DVT example



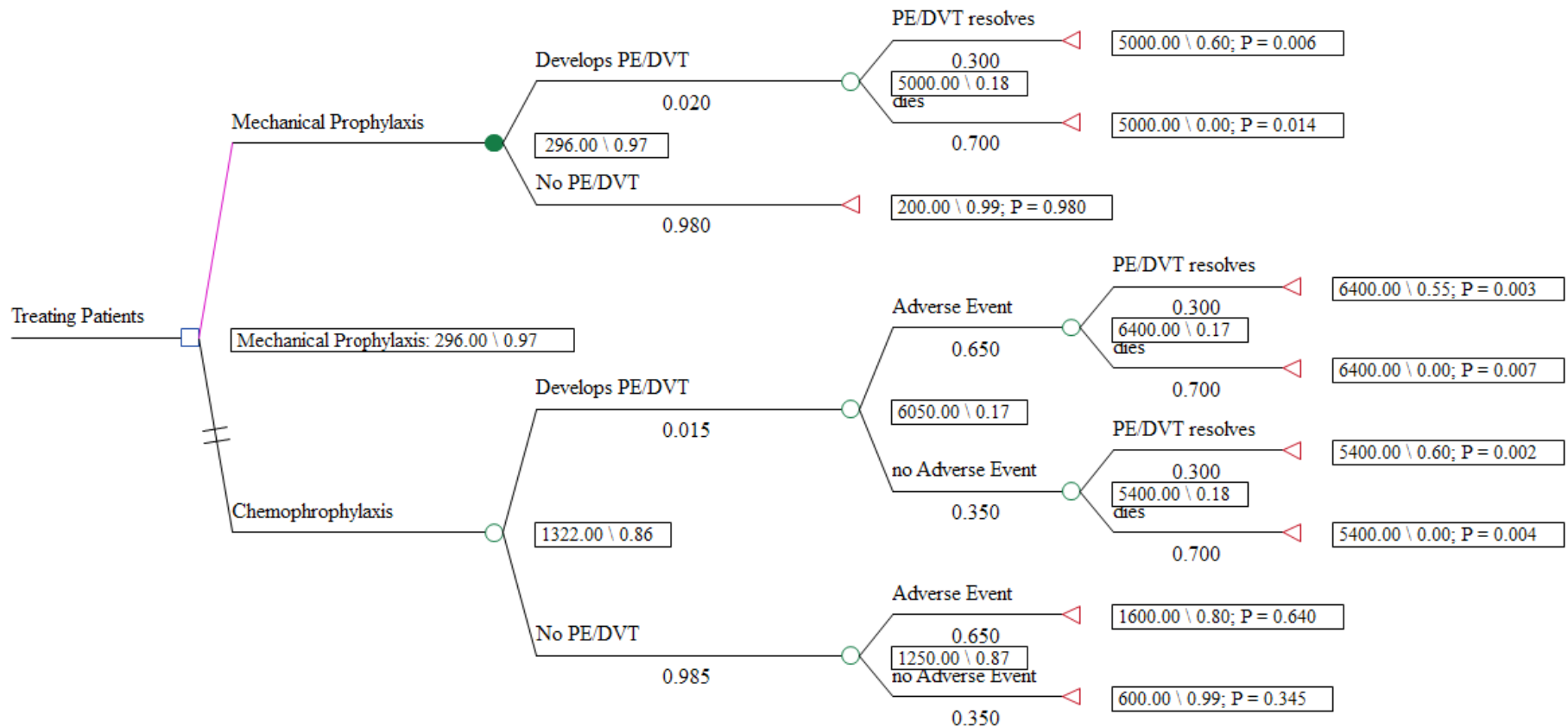
# PE/DVT example – Hypothetical Probabilities



# PE/DVT example – Hypothetical full inputs



# Model results, with point estimates



# One-Way Sensitivity Analyses

# One-way sensitivity analysis

- Vary one input (parameter) at a time, and see how model results are affected
- Example: probability of AE\_chemo
  - Base-case: 0.65
  - Sensitivity analysis: range from 40-80%
    - Run 5 models, each with the following input:
      - .040, 0.50, 0.60, 0.70, 0.80

# Inputting variables to run a sensitivity analysis

- Best practice:

1. **Insert variables, not point estimates**

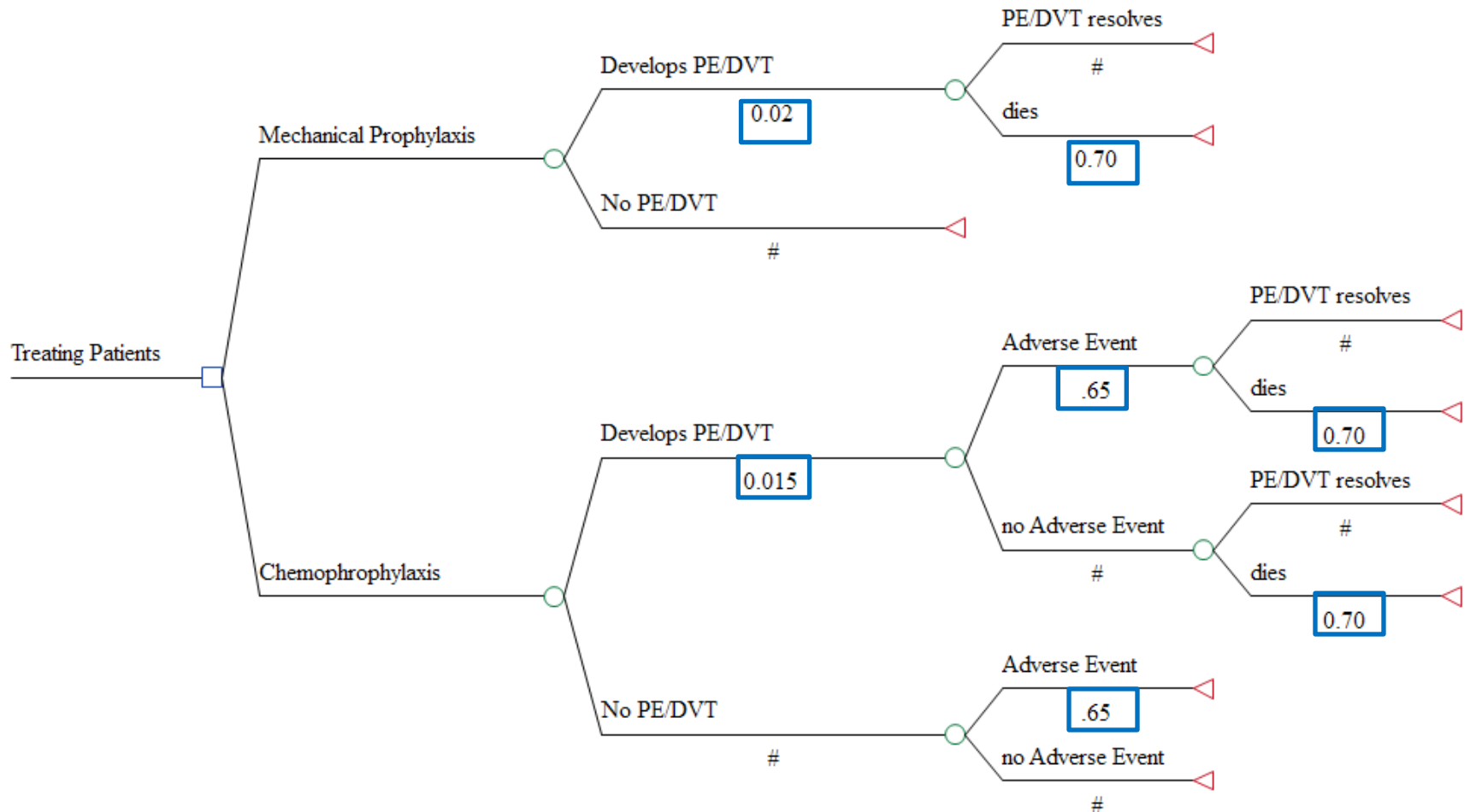
- Example: probability of AE, chemoprophylaxis
  - “0.65” (Point estimate)
  - “p\_AE\_chemo” (Variable)

2. **Then, define variables as:**

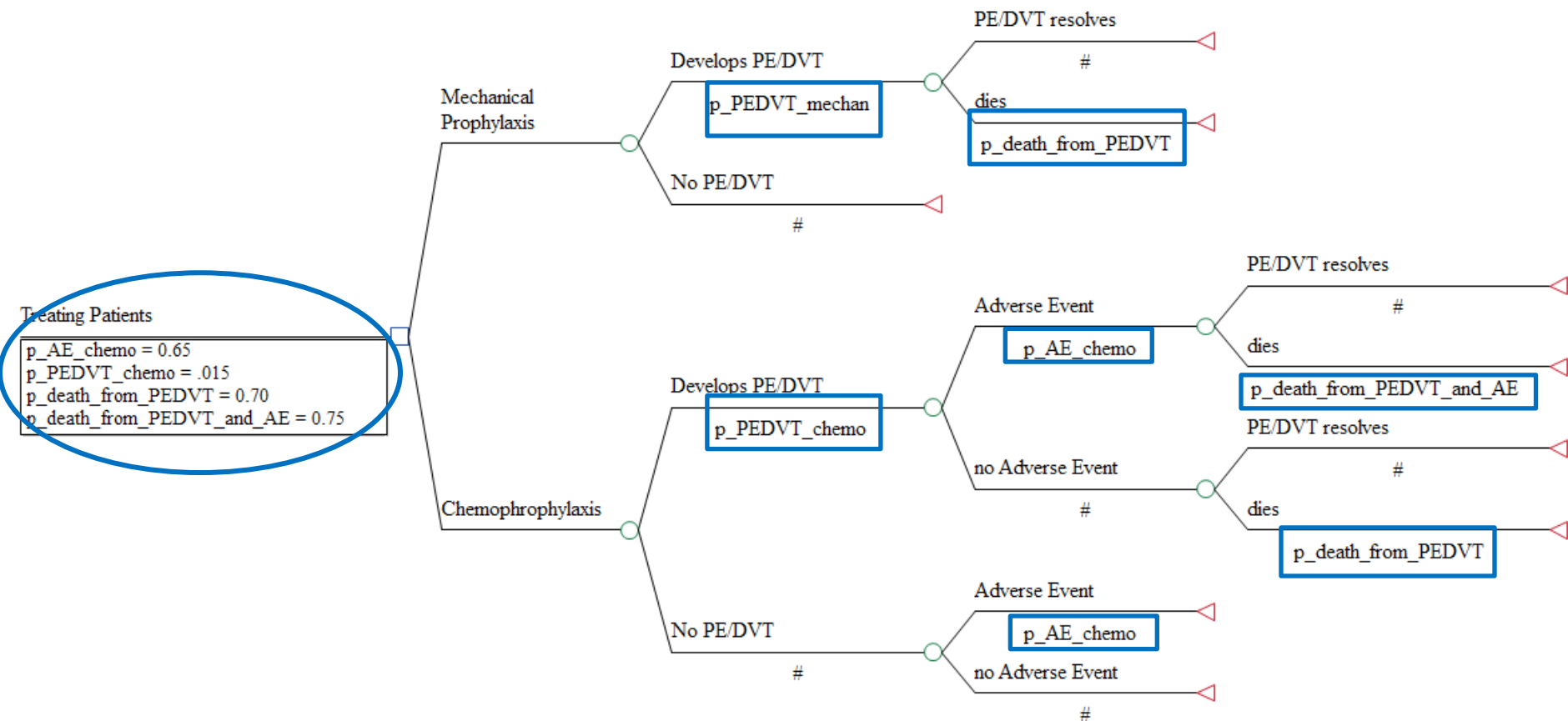
- Point estimates (DSA) or
  - Distributions (PSA)
  - Example: definition of probability of Adverse Event, chemoprophylaxis
    - Defining variable as a point estimate: “p\_AE\_chemo” = 0.65”
    - Defining variable as a distribution: “p\_AE\_chemo” = dist\_AE\_chemo”
-



# PE/DVT example – Probabilities as Point Estimates

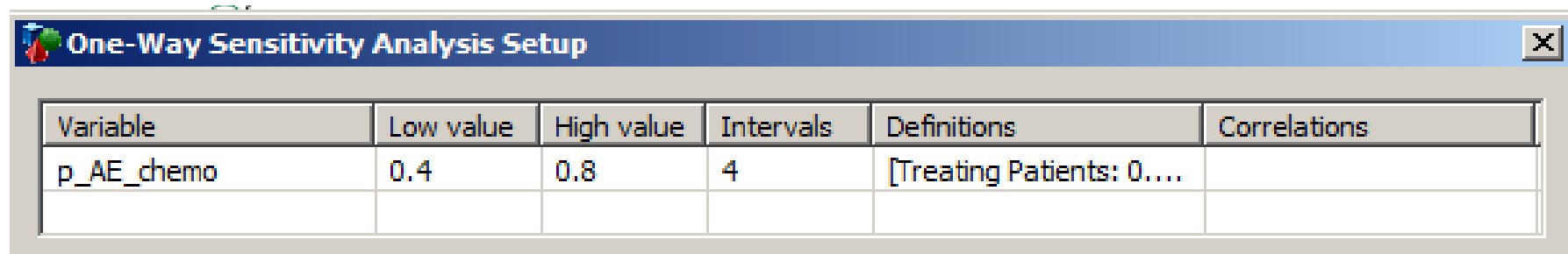


# PE/DVT example – Probabilities as Variables and Variables defined as Point Estimates



# One-way sensitivity analyses

- Define your range



Variable	Low value	High value	Intervals	Definitions	Correlations
p_AE_chemo	0.4	0.8	4	[Treating Patients: 0....	

# Output, one-way sensitivity analyses

## Sensitivity Cost Effectiveness Analysis

p_AE_chemo	Strategy	Cost	Incr cost	Eff	Incr Eff	C/E	Incr C/E (ICER)	Dominance
0.4	Mechanical Prophylaxis	296.00	0.00	0.97	0.00	303.96	0.00	
	Chemoprophylaxis	1072.00	776.00	0.90	-0.07	1187.50	-10919.58	(Dominated)
0.5	Mechanical Prophylaxis	296.00	0.00	0.97	0.00	303.96	0.00	
	Chemoprophylaxis	1172.00	876.00	0.88	-0.09	1325.86	-9750.26	(Dominated)
0.6	Mechanical Prophylaxis	296.00	0.00	0.97	0.00	303.96	0.00	
	Chemoprophylaxis	1272.00	976.00	0.87	-0.11	1470.22	-8985.25	(Dominated)
0.7	Mechanical Prophylaxis	296.00	0.00	0.97	0.00	303.96	0.00	
	Chemoprophylaxis	1372.00	1076.00	0.85	-0.13	1620.99	-8445.76	(Dominated)
0.8	Mechanical Prophylaxis	296.00	0.00	0.97	0.00	303.96	0.00	
	Chemoprophylaxis	1472.00	1176.00	0.83	-0.15	1778.59	-8044.88	(Dominated)

# Inputs for a one-way sensitivity analysis

- Can get range from 95% Confidence Interval reported
  - Varying a parameter an arbitrary range, such as  $\pm 50\%$  -- not a great practice
    - This will demonstrate model sensitivity, but does not reflect uncertainty
  - Expert Opinion
-

# Series of One-way Sensitivity Analyses

1. Vary probability of chemoprophylaxis-related adverse event
    - a. Compare these ICERs to base-case ICER
  2. Vary cost of treating adverse event
    - a. Compare these ICERs to base-case ICER
  3. Vary probability of death from PE/DVT
    - a. Compare these ICERs to base-case ICER
  4. Etc.
-

# Caution

- Generally, a series of one-way sensitivity analyses will underestimate uncertainty in a cost-effectiveness ratio:
    - The ICER is based off of multiple parameters, not just one
    - Here, you are assuming that uncertainty exists only in one parameter
    - Solution: Probabilistic Sensitivity Analyses!
-

# But...

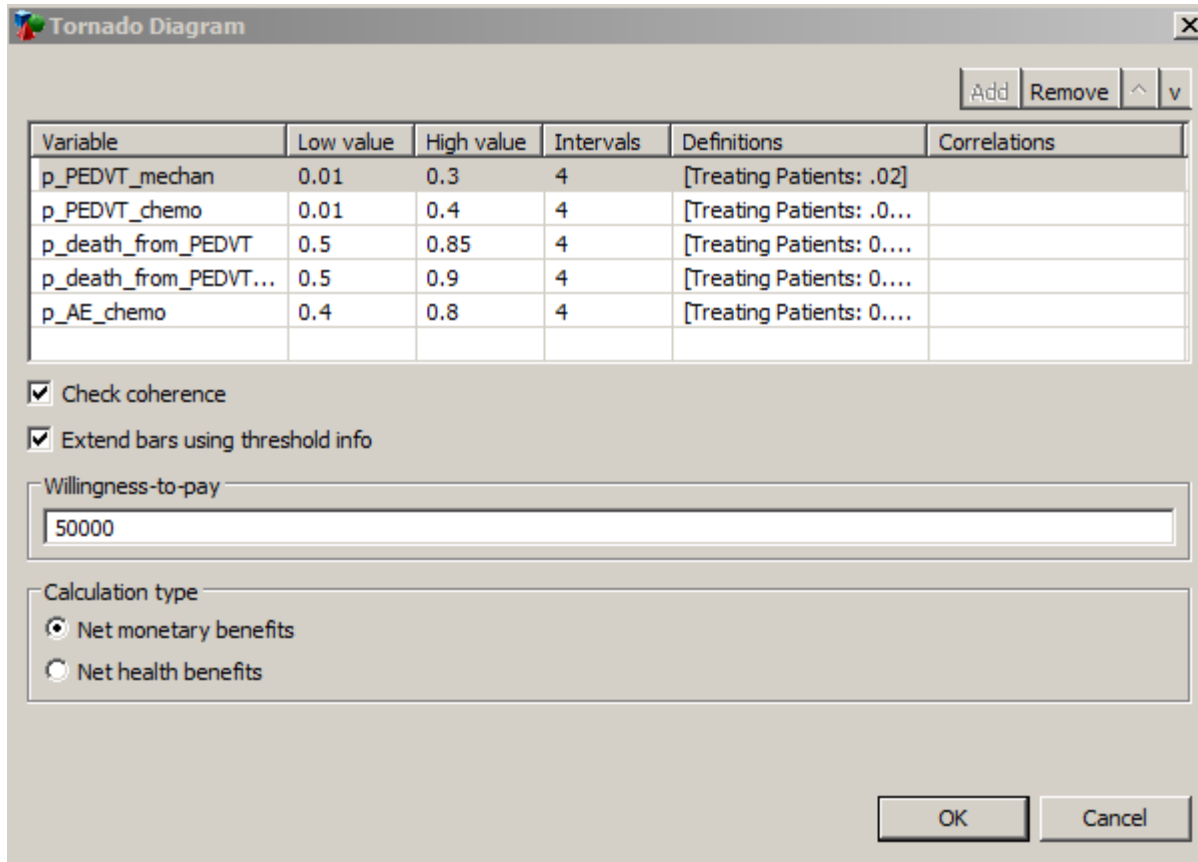
- You should still do one-way sensitivity analyses!
  - Easy way to understand which parameters matter
-



# Tornado diagrams

- Tell you which of your one-way sensitivity analyses had the greatest impact on model results
  - Bar: a one-way sensitivity analysis
  - Width of bar represents impact on model results
-

# Conducting a tornado diagram



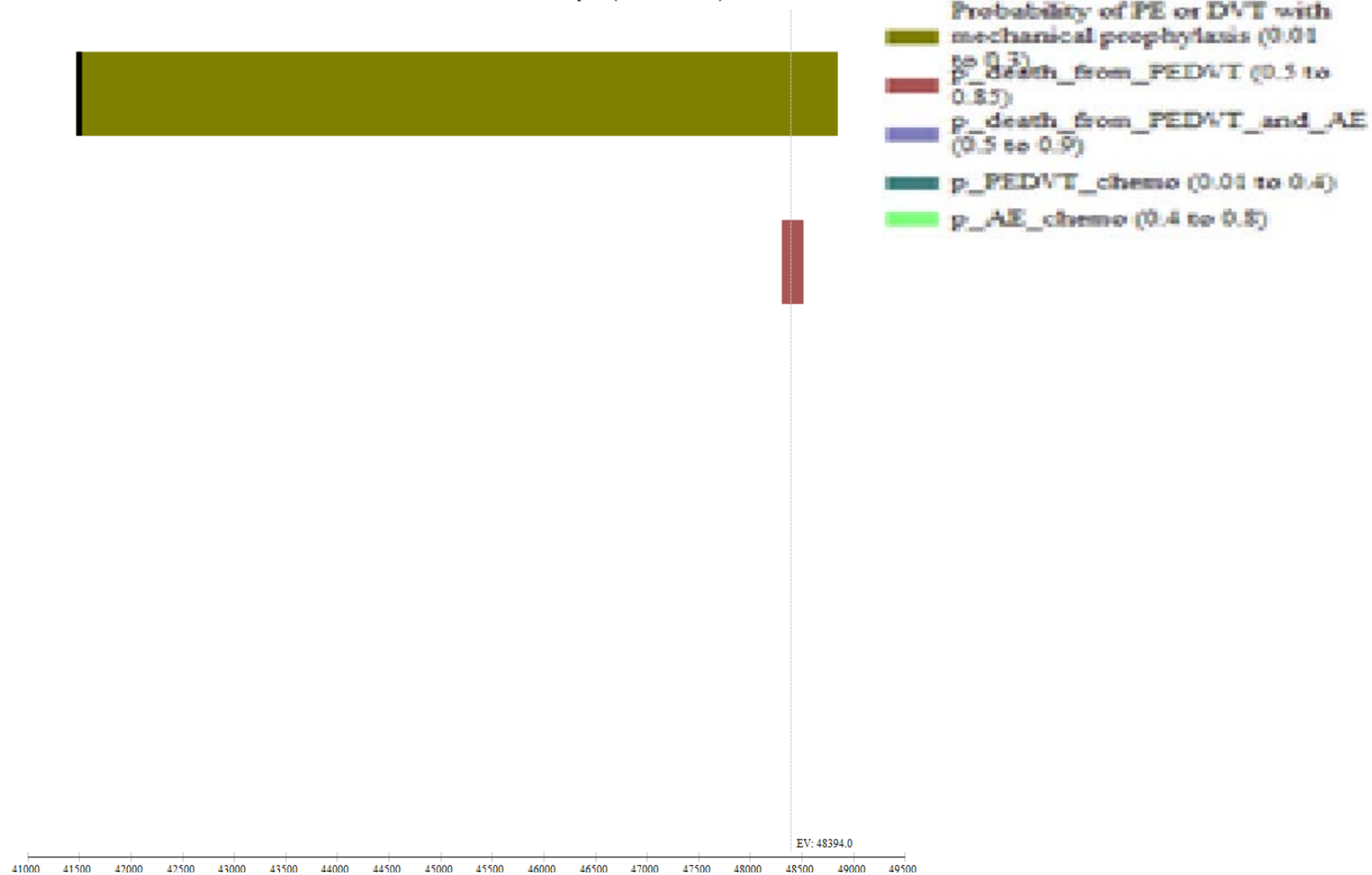
The screenshot shows the 'Tornado Diagram' window. It contains a table with the following data:

Variable	Low value	High value	Intervals	Definitions	Correlations
p_PEDVT_mechan	0.01	0.3	4	[Treating Patients: .02]	
p_PEDVT_chemo	0.01	0.4	4	[Treating Patients: .0...	
p_death_from_PEDVT	0.5	0.85	4	[Treating Patients: 0....	
p_death_from_PEDVT...	0.5	0.9	4	[Treating Patients: 0....	
p_AE_chemo	0.4	0.8	4	[Treating Patients: 0....	

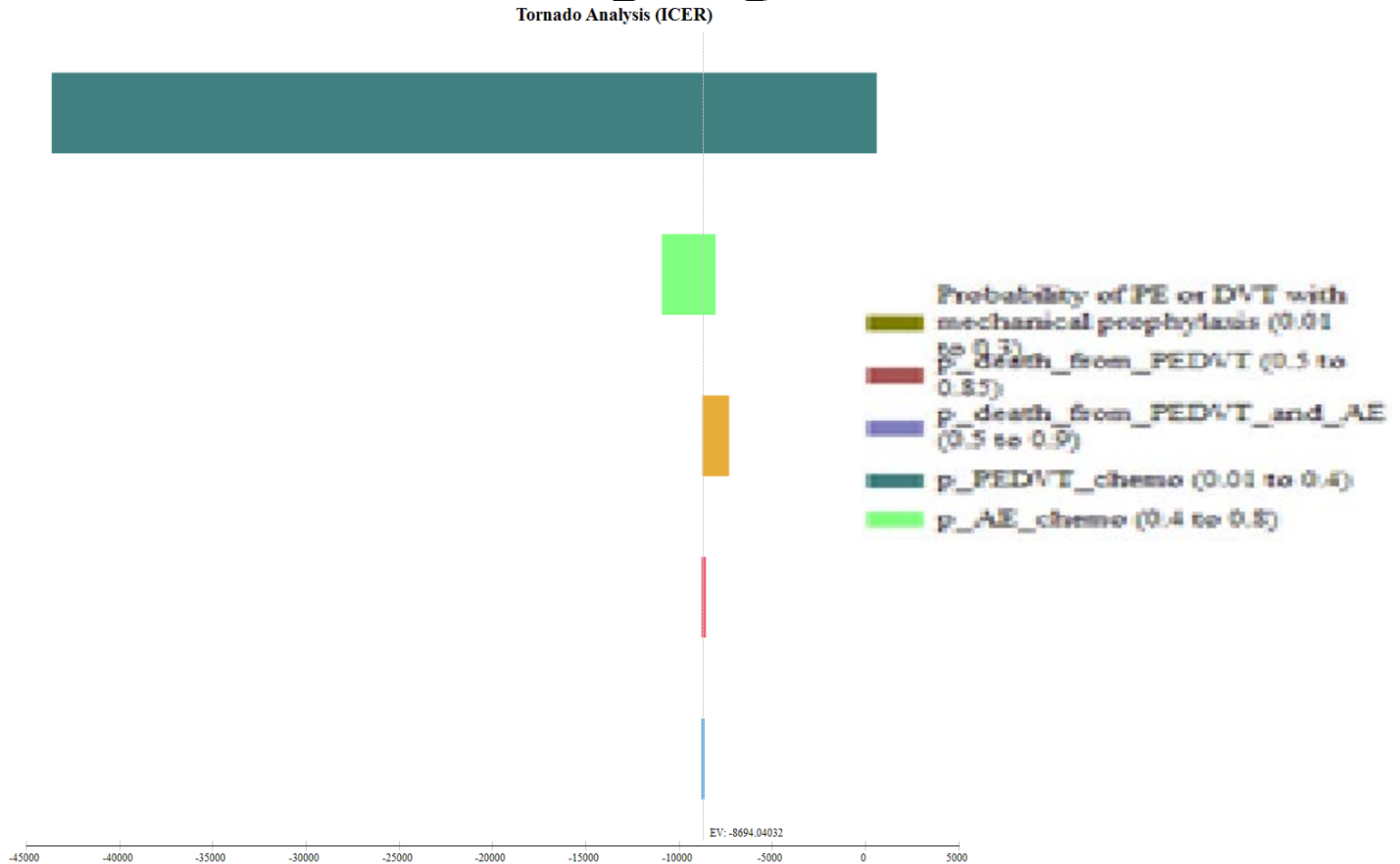
Below the table, there are two checked options: 'Check coherence' and 'Extend bars using threshold info'. A 'Willingness-to-pay' section has a text box containing '50000'. A 'Calculation type' section has two radio buttons: 'Net monetary benefits' (selected) and 'Net health benefits'. At the bottom right are 'OK' and 'Cancel' buttons.

# Tornado Diagram (Net Benefits)

Tornado Analysis (Net Benefits)



# Tornado Results (ICER) – *recommended graph to view*



# Tornado diagram, text report -

**Tornado Sensitivity Analysis - ICER Report**

VARIABLE_NAME	VARIABLE_RANGE	LOW_VALUE	HIGH_VALUE	SPREAD	SPREAD_SQR	RISK_PCT	CUMUL_PCT
p_PEDVT_mechan	0.01 to 0.3	-43639.51223	599.24346	44238.75569	1957067504.59758	35.90785	35.90785
p_AE_chemo	0.4 to 0.8	-10919.58067	-8044.87618	2874.70449	8263925.87916	0.15162	36.09902
p_PEDVT_chemo	0.01 to 0.4	-8755.5842	-7313.90762	1441.67658	2078431.34776	0.03813	35.94598
p_death_from_PEDVT	0.5 to 0.85	-8792.95107	-8565.56971	227.38136	51702.28401	0.00095	35.94693
p_death_from_PEDVT_and_AE	0.5 to 0.9	-8793.94024	-8635.18248	158.75776	25204.02665	0.00046	35.94739

- The high value for p\_PEDVT\_mechan results in chemoprophylaxis now being the preferred strategy
- Tells us we need to be more precise with our estimate of PE/DVT associated with mechanical prophylaxis
- Other variables don't impact our model conclusions

# Limitations of Tornado diagrams

- Just a series of one-way sensitivity analyses, with results presented on top of one another
  - There is not just uncertainty in one parameter – there is uncertainty in most, if not all, parameters
-

# Scenario Analyses

# Scenario analyses

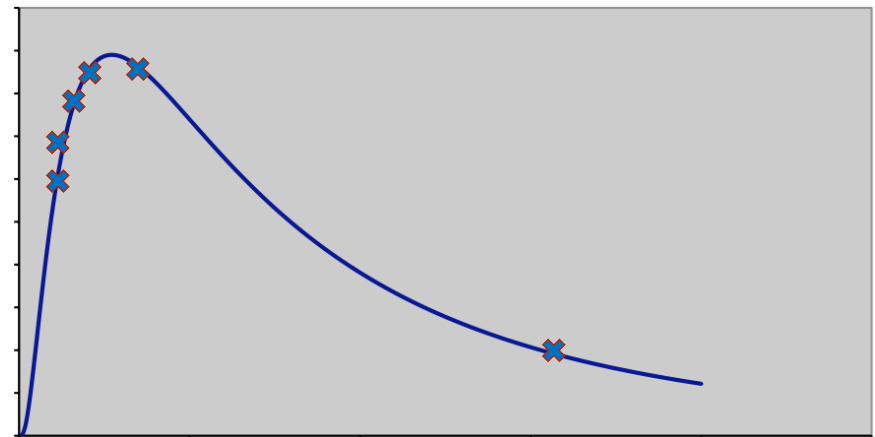
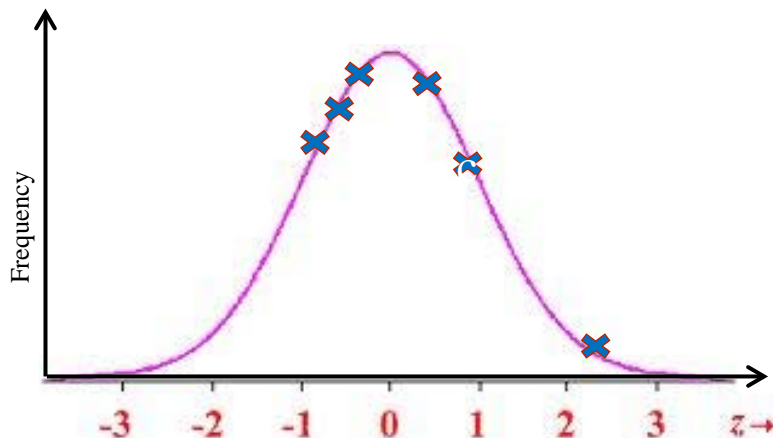
- Interested in subgroups
    - Cost-effectiveness of chemical versus mechanical prophylaxis in 85+ only
      - Change risk of PE/DVT, risk of AE, risk of death from PE/DVT/AE
  - Changes the point estimate of multiple parameters
  - Do not incorporate uncertainty !
-



# Probabilistic Sensitivity Analyses

# Probabilistic sensitivity analysis

- Vary multiple parameters simultaneously
- Each variable comes from a *distribution*
- Model is run many times (1,000, 10,000, etc.)
  - Each model iteration plucks a value from that distribution and uses it as the model input



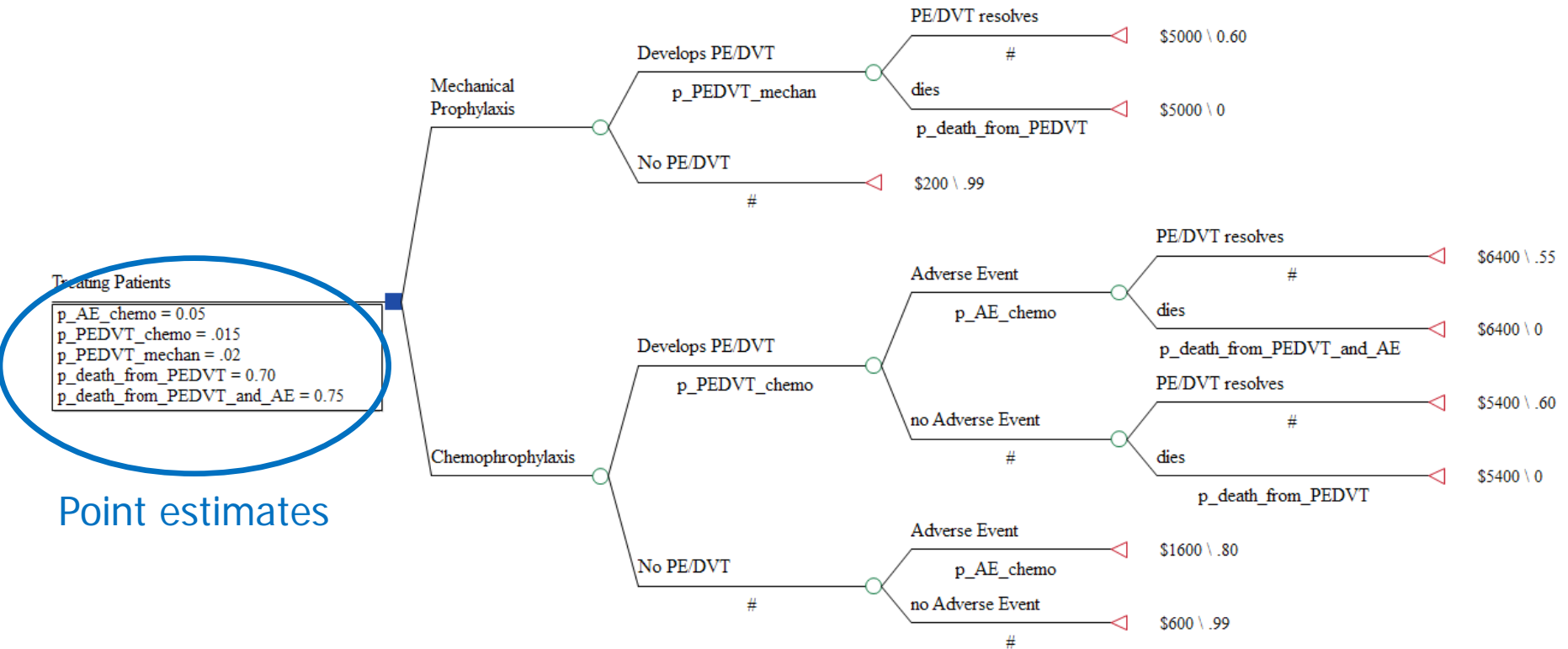
# PSA

- Values are sampled with replacement!
  - Values sampled based on their likelihood of occurrence
  - Results (comparing strategy A to B):
    - Mean  $\text{Cost}_A$  & variation in  $\text{Cost}_A$
    - Mean  $\text{Cost}_B$  & variation in  $\text{Cost}_B$
    - Mean  $\text{Health Effect}_A$  & variation in  $\text{Health Effect}_A$
    - Mean  $\text{Health Effect}_B$  & variation in  $\text{Health Effect}_B$
-

# Choosing distributions for your PSA – general guidance

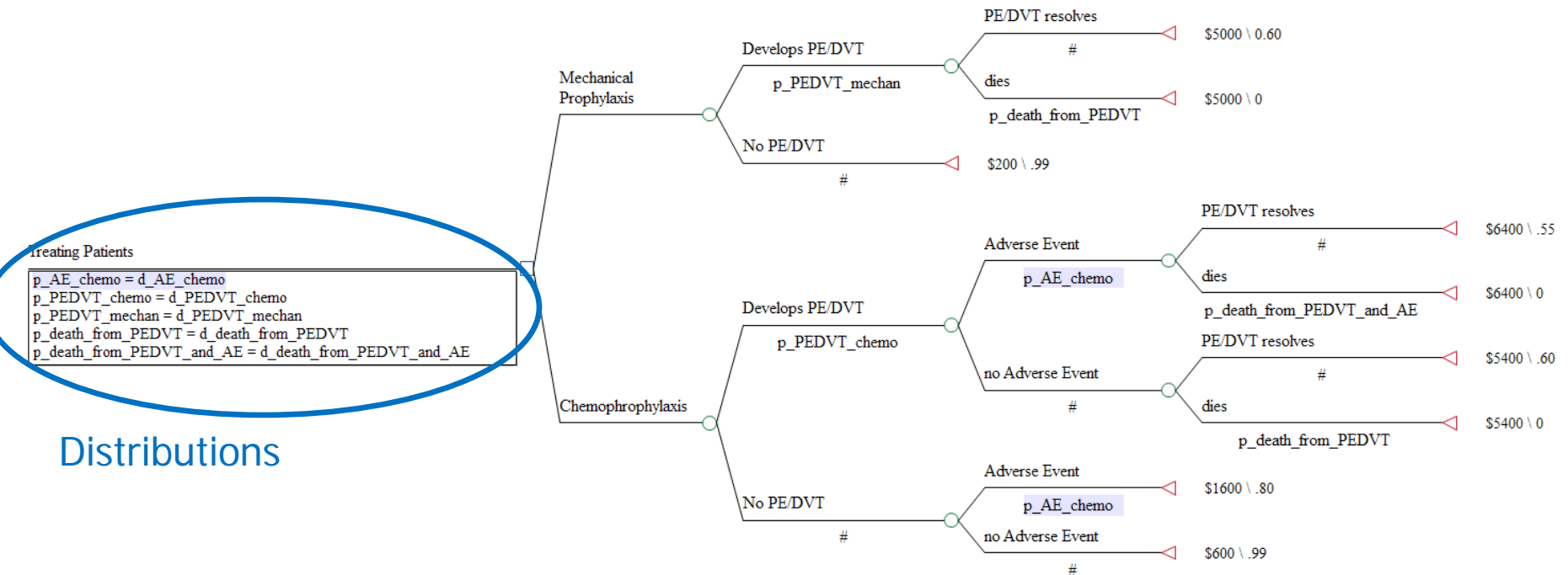
- Costs: log-normal, normal
  - Probabilities: beta
  - Utilities: beta
-

# Inputting variables into your PSA



- Need to define variables in terms of distributions, rather than point estimates

# Defining distributions in a PSA



# Creating distribution-based definitions

## 1. Create the distribution: `d_AE_chemo`

Define the distribution in terms of its shape

- normal, beta, etc
- Define the parameters for that distribution
  - mean/variance, alpha/beta, etc.

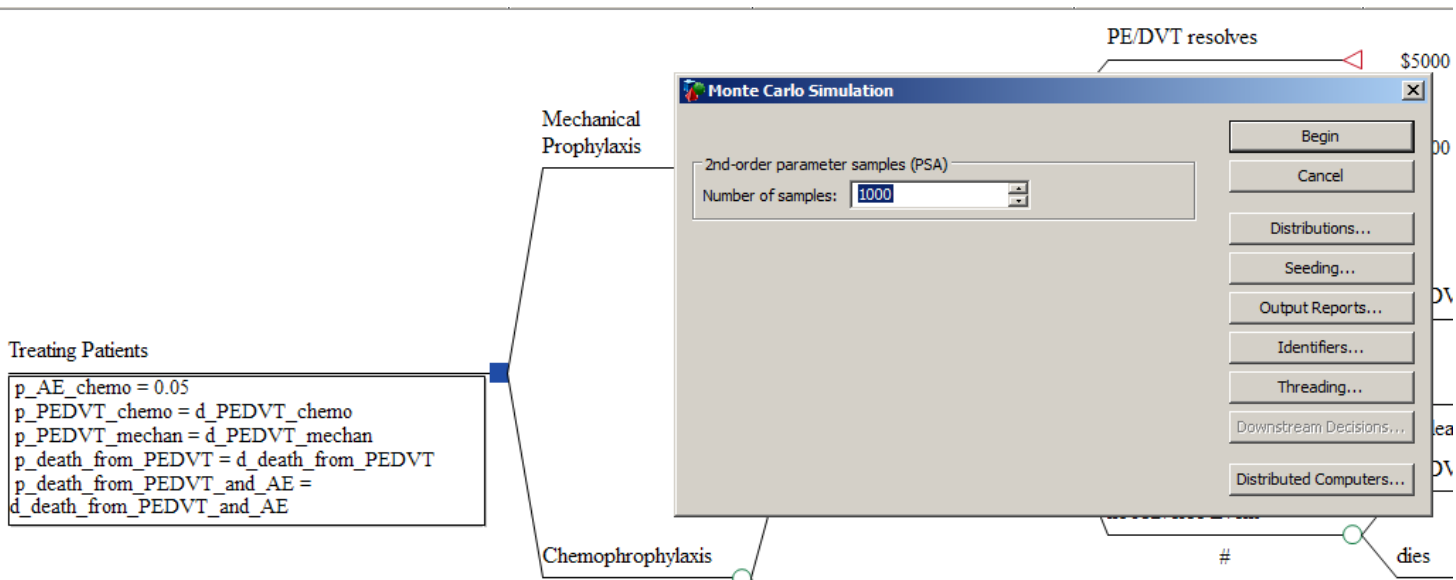
## 2. Assign the distribution to a variable:

```
prob_AE_chemo = d_AE_chemo
```

---

# Running a PSA

- Define all variables (model inputs) as distributions
- Determine your number of iterations



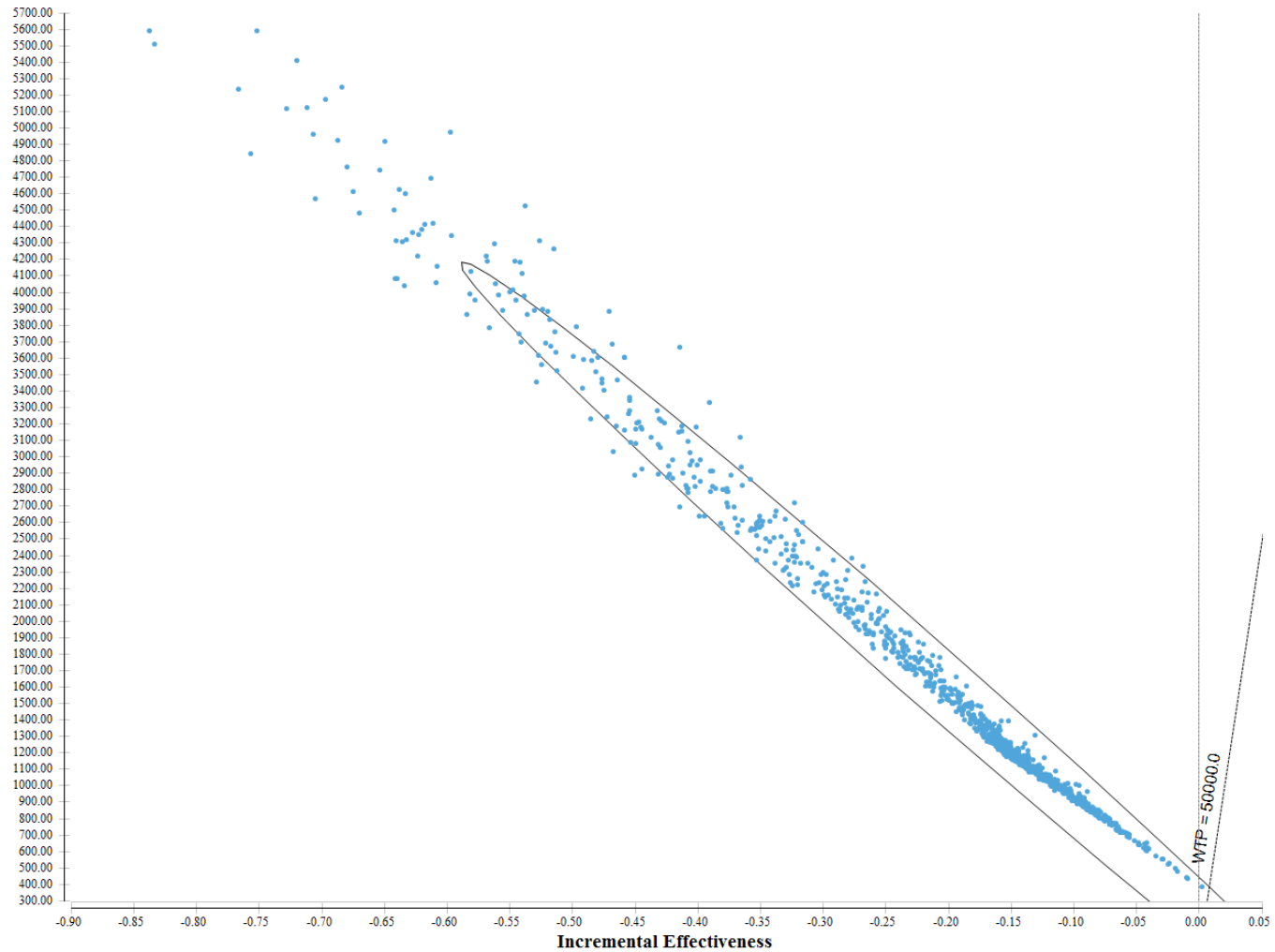


# Ways to show uncertainty in the ICER

- Cost-effectiveness planes (CE scatterplot)
  - Cost-effectiveness acceptability curve
  - Net benefits
-

# CE Scatter Plot

Incremental Cost-Effectiveness, Chemoprophylaxis v. Mechanical Prophylaxis

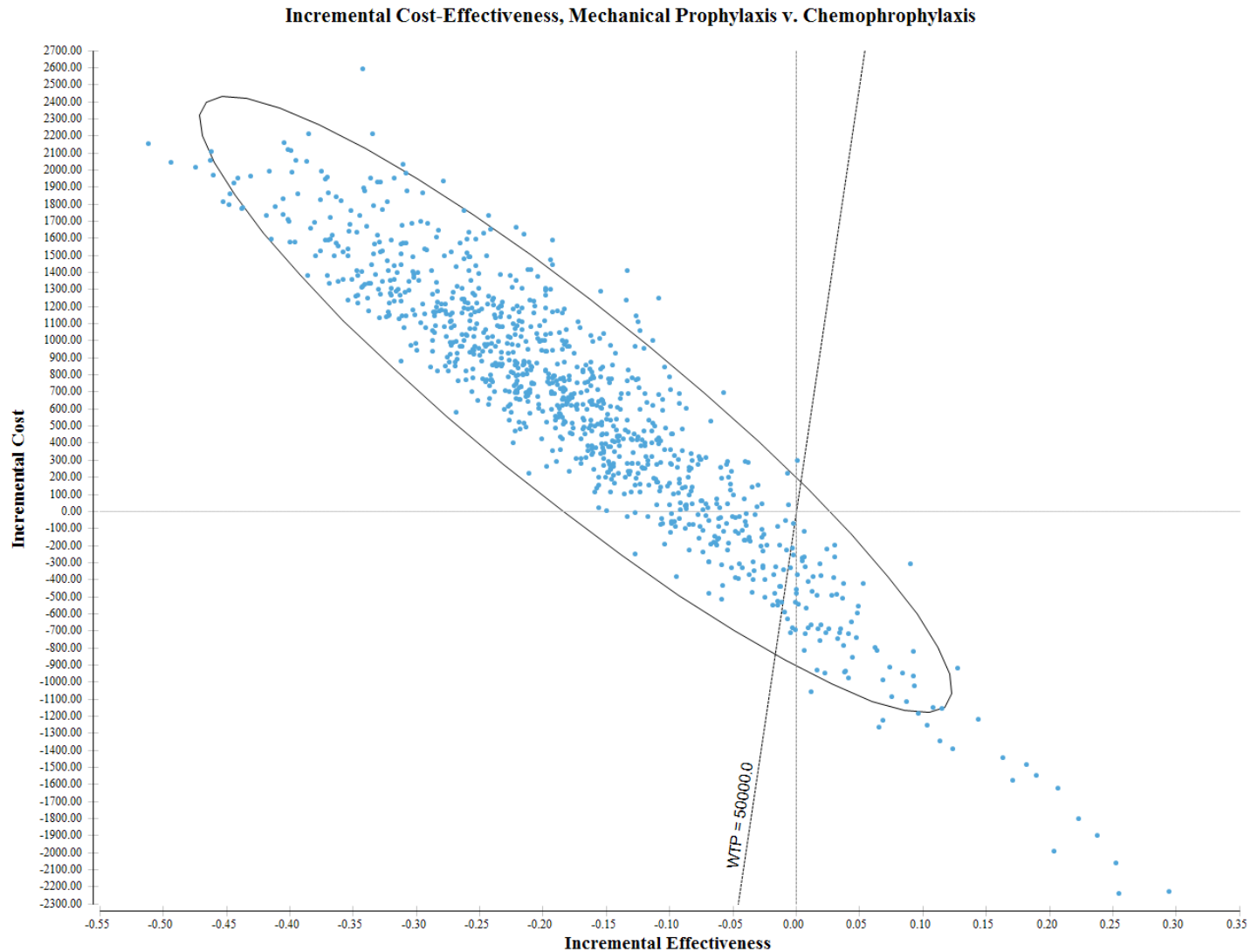


# “ICE Report”

Incremental CE Plot Report Chemoprophylaxis v. Mechanical Prophylaxis						
COMPONENT	QUADRANT	INCREFF	INCR COST	INCRCE	FREQUENCY	PROPORTION
C1	IV	IE>0	IC<0	Superior	0	0
C2	I	IE>0	IC>0	ICER<50000.0	0	0
C3	III	IE<0	IC<0	ICER>50000.0	0	0
C4	I	IE>0	IC>0	ICER>50000.0	1	0.001
C5	III	IE<0	IC<0	ICER<50000.0	0	0
C6	II	IE<0	IC>0	Inferior	999	0.999
Indiff	origin	IE=0	IC=0	0/0	0	0

- In this hypothetical example (with entirely made-up data) Mechanical Prophylaxis is cost-effective compared to Chemo Prophylaxis 99.9% of the time
  - Costs less AND provides more health benefit

# Cost-Effectiveness Plane, if in multiple quadrants

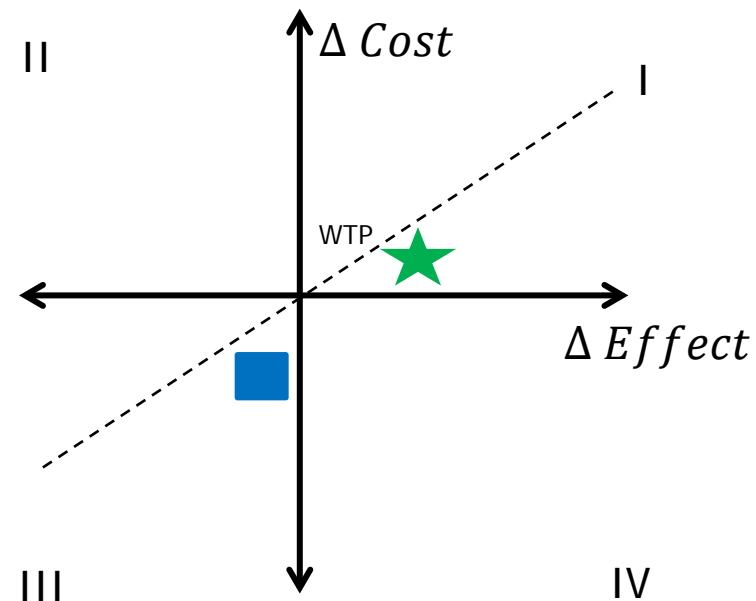


# Ways one should not show uncertainty in the ICER

- Show only the numeric value of the ICER and Confidence Interval

- $ICER = \frac{Cost\ A - Cost\ B}{Effect\ A - Effect\ B} = \frac{-40,000}{-1} = \$40,000 / QALY$

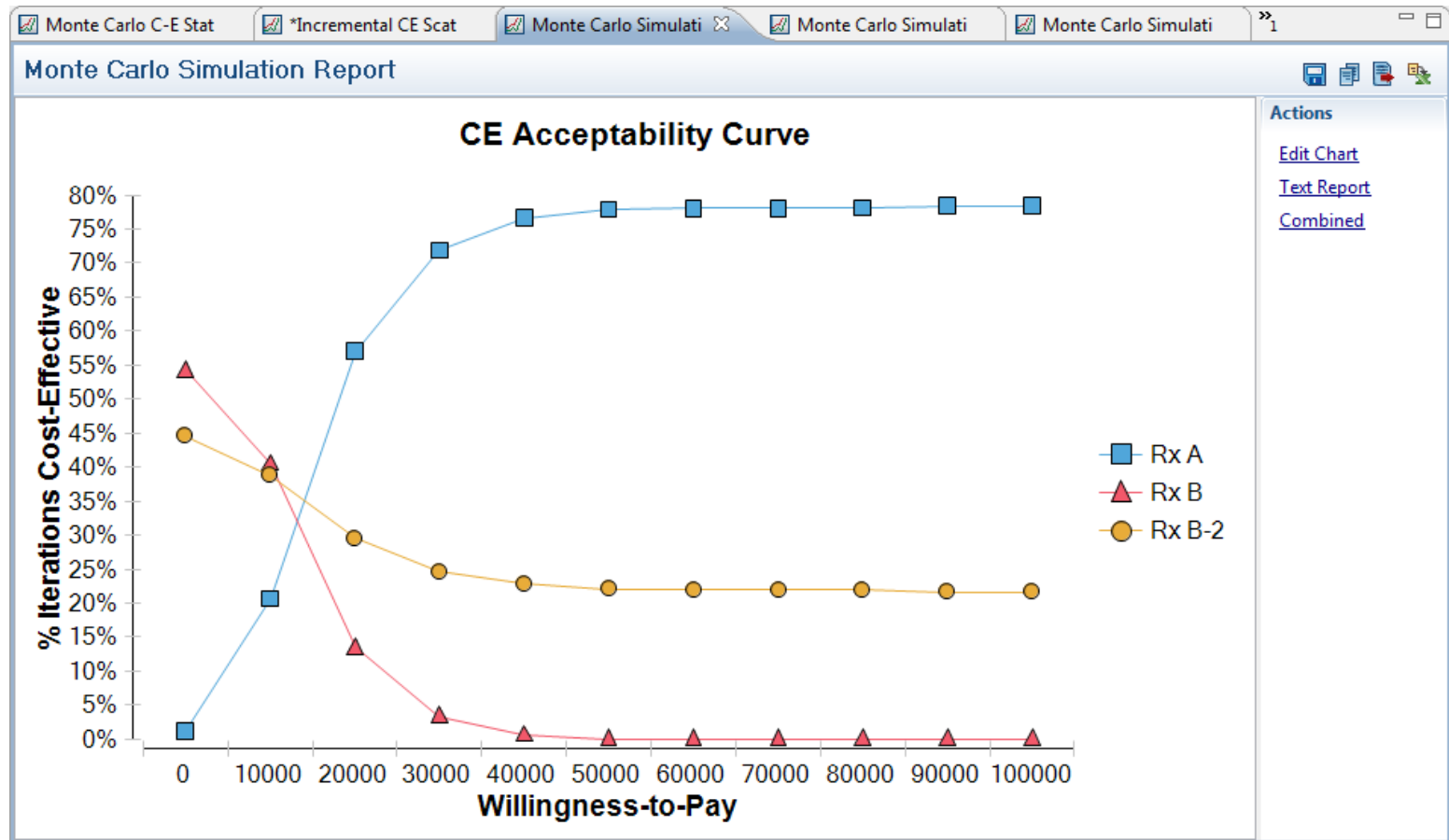
- $ICER = \frac{Cost\ A - Cost\ B}{Effect\ A - Effect\ B} = \frac{40,000}{1} = \$40,000 / QALY$



# Willingness to pay (WTP)

- Previously, I had to specify my WTP
  - What if you don't know what that is?
    - Or different decision makers have different WTP?
  - Use a Cost-Effectiveness Acceptability Curve
    - Percentage of iterations that favor each strategy, over a range of WTP
-

# Cost-effectiveness acceptability curves – hypothetical



# Net Benefits

- Combine information on costs, outcomes, and willingness to pay
    - Net Monetary Benefits
  - Positive number indicates technology is cost-effective
  - *Use when you are very certain about your WTP*
-



# Net Monetary benefits

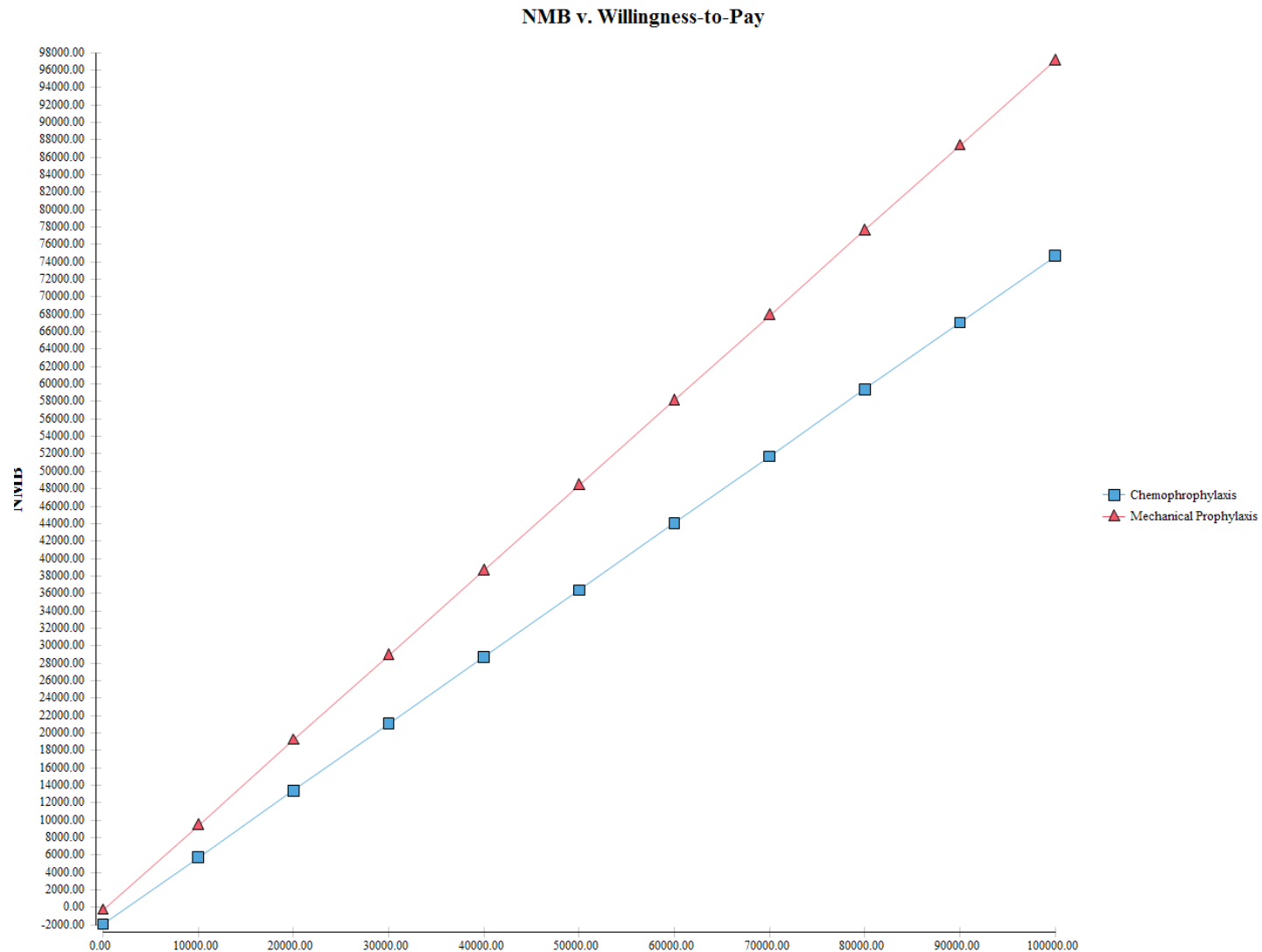
- Net Monetary Benefits

$$\text{NMB} = (\Delta \text{ Effect} * \text{WTP}) - \Delta \text{ Cost}$$

$$(-0.11 * \$50,000) - \$1,057 = \$-6,557$$

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# TreeAge- Net Monetary benefits



# **3 ways to show uncertainty in the ICER**

1. Cost-effectiveness planes/quadrant
  2. Cost-effectiveness acceptability curve
  3. Net monetary benefits (only if you are certain on your WTP)
-

# How many iterations in a PSA?

- More distributions = more iterations
- Stop when the simulations generate mean values (without seeding) that are very similar

Monte Carlo C-E Statistics

Attribute	Statistic	Mechanical Prophylaxis	Chemophrophyl...
[-] Cost	Mean	295.98	1371.17
	Std Deviation	14.14	966.99
	Minimum	258.19	614.93
	2.5%	270.26	625.63
	10%	278.24	645.27
	Median	295.36	944.17
	90%	315.24	2839.58
	97.5%	325.44	4053.16
	Maximum	338.22	5235.56
	Size (n)	1000.00	1000.00
	Variance	199.99	935077.00
	Variance/Size	0.20	935.08
	SQRT[Varianc...	0.45	30.58
[-] Eff	Mean	0.97	0.86

Monte Carlo C-E Statistics

Attribute	Statistic	Mechanical Prophylaxis	Chemophrophyl...
[-] Cost	Mean	295.92	1351.17
	Std Deviation	13.87	900.21
	Minimum	258.06	613.43
	2.5%	270.30	631.42
	10%	277.89	651.39
	Median	294.83	950.08
	90%	313.93	2682.31
	97.5%	322.97	3850.64
	Maximum	347.62	5115.89
	Size (n)	1000.00	1000.00
	Variance	192.33	810375.85
	Variance/Size	0.19	810.38
	SQRT[Varianc...	0.44	28.47
[-] Eff	Mean	0.97	0.86

# 100 iterations

Monte Carlo C-E Statistics			
Attribute	Statistic	Mechanical Prophylaxis	Chemophrophyl...
Cost	Mean	297.80	1413.88
	Std Deviation	13.17	919.06
	Minimum	269.18	613.56
	2.5%	278.24	620.09
	10%	281.11	654.41
	Median	295.40	1056.64
	90%	315.54	2697.37
	97.5%	324.32	3593.22
	Maximum	336.49	5047.80
	Size (n)	100.00	100.00
	Variance	173.49	844673.03
	Variance/Size	1.73	8446.73
	SQRT[Varianc...	1.32	91.91
Eff	Mean	0.97	0.85

Monte Carlo C-E Statistics			
Attribute	Statistic	Mechanical Prophylaxis	Chemophrophyl...
Cost	Mean	296.30	1274.05
	Std Deviation	14.44	891.76
	Minimum	260.79	614.87
	2.5%	261.01	626.80
	10%	280.79	641.58
	Median	296.48	929.81
	90%	315.42	2678.31
	97.5%	322.91	3994.27
	Maximum	335.50	4528.79
	Size (n)	100.00	100.00
	Variance	208.37	795237.48
	Variance/Size	2.08	7952.37
	SQRT[Varianc...	1.44	89.18
Eff	Mean	0.97	0.88

# PSA Summary

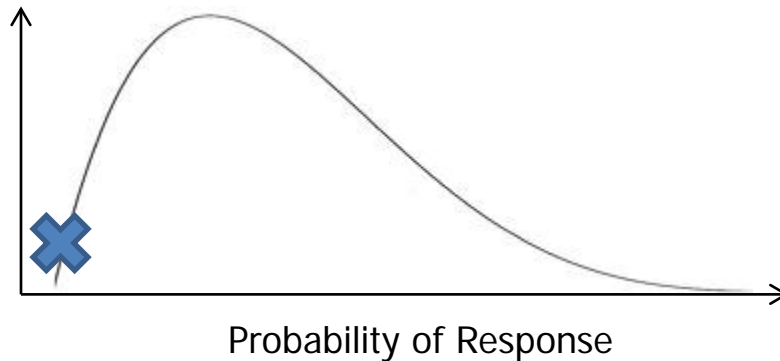
- Looks at model results when multiple sources of uncertainty are evaluated simultaneously
  - Results presented in terms of:
    - C-E planes (quadrants)
    - C-E acceptability curves
    - Net Monetary Benefits
  - Required in order to publish in a peer-reviewed journal!
-

# Joint Parameter Uncertainty

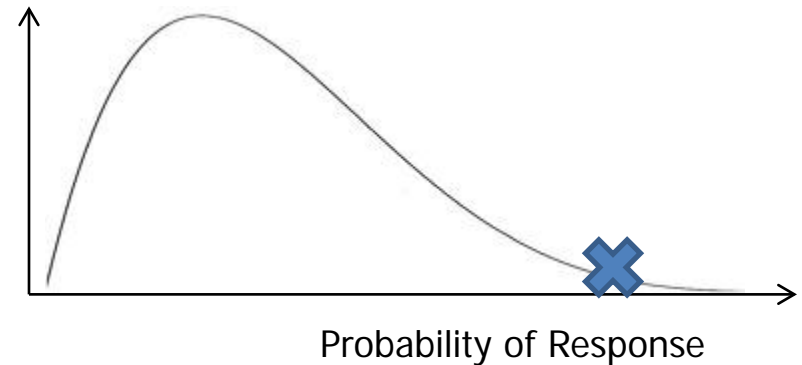
# Joint Parameter uncertainty

**The model will assume no covariance between parameters unless you specify otherwise**

**Probability of response at  
26 weeks**



**Probability of response at  
52 weeks**





# Accommodating Joint Parameter uncertainty

- Define one variable in terms of the other

$$X = Y + (Y * 0.2)$$

- Use a table to link variables, have PSA identify Index

- Variable X = if(PSA = 1; Table 1[Index; 1]; 0.55)
- Variable Y = if(PSA = 1; Table 1[Index; 2]; 0.65)

Index	X	Y
1	0.60	0.67
2	0.480	0.89
3	0.89	0.93

- If the PSA indicator is turned on:
  - go to Table 1, choose the row (Index) corresponding with the model cycle we are in and use the value in column 1
- otherwise, use a value of 0.55

# SUMMARY

# Summary

- All model inputs have uncertainty
- Test how this uncertainty affects model results
  - Do so by varying model inputs
- Tornado diagrams: first-pass understanding of the most important variables in your model
- Need to run a PSA in order to fully evaluate the combination of uncertainty in all/most model inputs on robustness of model results
  - Be careful to accommodate joint parameter uncertainty

# References

## ■ General Overview:

- Hunink M, Glasziou P, Siegel J, et al. “Chapter 11: Variability and Uncertainty” in Decision Making in Health and Medicine: Integrating Evidence and Values. Cambridge, UK: Cambridge Press, 2004. 339-363.

## ■ Best Practices:

- Briggs et al. Model Parameter Estimation and Uncertainty: A Report of the ISPOR-SMDM Modeling Good Research Practices Task Force – 6. *Value in Health*, 2012, 15: 835-842.

**QUESTIONS?**