

Boston Housing Price Prediction using Linear Regression

■ Abstract

This project predicts median housing prices in the Boston area using **Linear Regression**. The model analyzes various socio-economic and environmental factors that influence housing prices. By applying regression techniques, the project demonstrates how statistical learning can be used for price forecasting and real-estate analysis.

■ Dataset Information

- **Source:** [Boston Housing Dataset on Kaggle](https://www.kaggle.com/datasets/vikrishnan/boston-house-prices)
- **Attributes:**
 - `CRIM`: Per capita crime rate by town
 - `ZN`: Proportion of residential land zoned for large lots
 - `INDUS`: Proportion of non-retail business acres per town
 - `CHAS`: Charles River dummy variable (1 if tract bounds river; 0 otherwise)
 - `NOX`: Nitric oxide concentration (ppm)
 - `RM`: Average number of rooms per dwelling
 - `AGE`: Proportion of owner-occupied units built before 1940
 - `DIS`: Weighted distances to employment centers
 - `RAD`: Accessibility index to radial highways
 - `TAX`: Property tax rate per \$10,000
 - `PTRATIO`: Pupil-teacher ratio
 - `B`: Proportion of Black population
 - `LSTAT`: % lower status of the population
 - `MEDV`: Median value of owner-occupied homes (target variable)

■■ Project Workflow

1. **Data Loading and Exploration**
 - Import dataset, inspect missing values, and examine feature distribution.
2. **Data Preprocessing**
 - Handle missing data, feature scaling, and correlation analysis using a heatmap.
3. **Feature Selection**
 - Select important features influencing `MEDV` based on correlation values.
4. **Model Training**
 - Train a **Linear Regression** model using Scikit-learn.
5. **Model Evaluation**
 - Evaluate using **R² Score**, **Mean Absolute Error (MAE)**, **Mean Squared Error (MSE)**, and **Root Mean Squared Error (RMSE)**.
6. **Visualization**
 - Compare actual vs. predicted prices and plot residual errors.

■ Mathematical Explanation

Linear Regression is modeled as:

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n + \epsilon$$

Cost Function (MSE):

$$J(\beta) = \frac{1}{2m} \sum_{i=1}^m (h_{\beta}(x^{(i)}) - y^{(i)})^2$$

Gradient Descent:

$$\beta_j := \beta_j - \alpha \frac{\partial}{\partial \beta_j} J(\beta)$$

Where:

- α = learning rate
- m = number of training examples

The model minimizes the cost function iteratively to find the best-fit line.

■ Results and Analysis

- **R² Score:** ~0.73 (model explains 73% of variance)
- **MAE:** Low average error between predicted and actual prices
- **Observation:** Features like `RM`, `LSTAT`, and `PTRATIO` have the strongest influence on house prices.

The predicted vs. actual plot demonstrates a strong linear relationship, validating model performance.

■ Conclusion

The Linear Regression model effectively predicts Boston housing prices, providing insights into key factors affecting home values. Further improvements could include polynomial regression or ensemble methods for enhanced accuracy.

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