

Ridge Regression and Lasso

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```
# Set up for a Ridge Regression and a Lasso
#install.packages("glmnet")
library(glmnet) ; library(ISLR)

## Loading required package: Matrix
## Loading required package: foreach
## Loaded glmnet 2.0-16
Hitters2 = na.omit(Hitters)
x = model.matrix(Salary~., data=Hitters2)[-1] # the [-1] removes 'Salary' from 'x'
y = Hitters2$Salary
class(x) # ensuring 'x' is a matrix and not a data frame, as the glmnet function

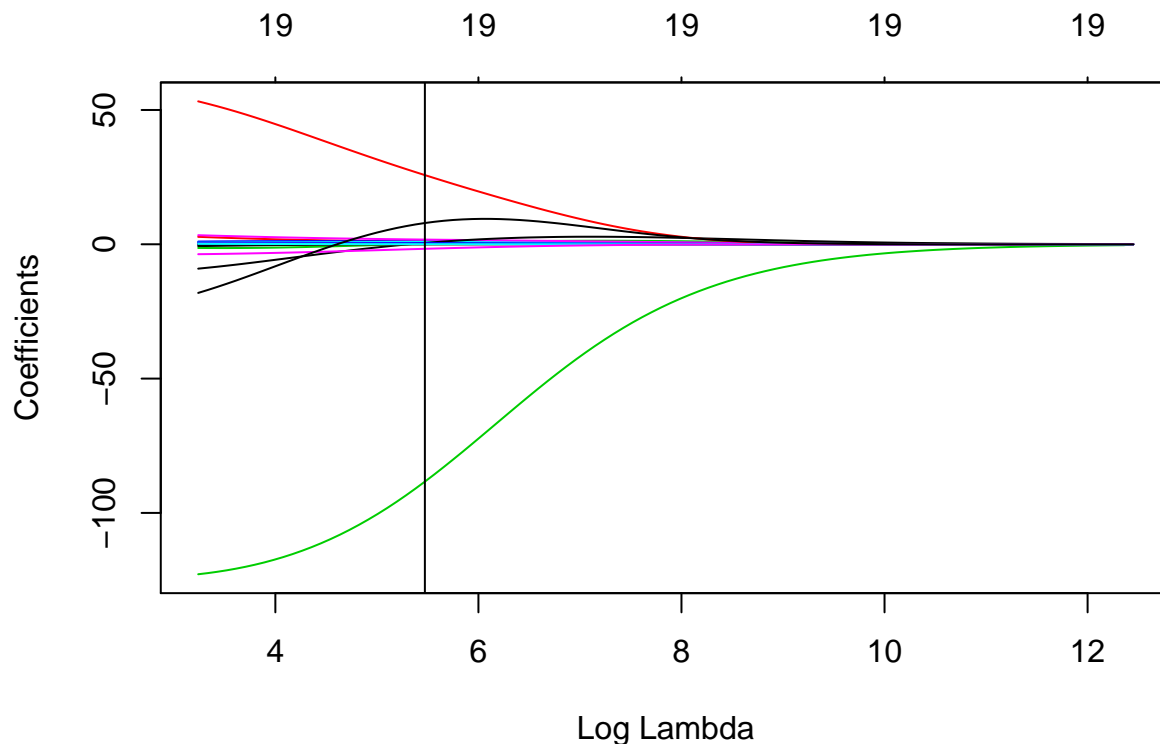
## [1] "matrix"
# requires 'x' to be a matrix
```

Ridge Regression

```
ridge_mod = glmnet(x, y, alpha=0)
#alpha = 0 performs ridge regression, and alpha = 1 performs lasso
plot(ridge_mod, xvar = "lambda")

set.seed(1)
ridge_cvfit = cv.glmnet(x, y, alpha=0)
ridge_cvfit$lambda.min #selected lambda value ; $lambda.min is that value that

## [1] 238.0769
# minimizes cross-validation error
plot(ridge_mod, xvar = "lambda") ; abline(v=log(ridge_cvfit$lambda.min))
```



```
coef(ridge_cvfit, s="lambda.min") #notice that the shrunken coefficients approach 0
```

```
## 20 x 1 sparse Matrix of class "dgCMatrix"
##              1
## (Intercept) 10.35569021
## AtBat       0.04633830
## Hits        0.96376522
## HmRun        0.27163150
## Runs         1.10118079
## RBI          0.87606196
## Walks        1.75331031
## Years        0.50454902
## CAtBat       0.01124891
## CHits        0.06274116
## CHmRun       0.43896753
## CRuns        0.12471202
## CRBI         0.13253839
## CWalks       0.03672947
## LeagueN      25.75710221
## DivisionW    -88.36043501
## PutOuts      0.18483877
## Assists      0.03847012
## Errors       -1.68470903
## NewLeagueN   7.91725605
```

Model Creation based on Ridge Regression Variable Selection

```
newfitlm=lm(Salary ~ Runs + Walks + Years + League + Division + Errors + NewLeague, data=Hitters2)
summary(newfitlm) #reduced model
```

```
##
## Call:
## lm(formula = Salary ~ Runs + Walks + Years + League + Division +
##     Errors + NewLeague, data = Hitters2)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -733.23 -205.03  -50.05  126.57 2124.43
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -122.185     79.524  -1.536  0.12567
## Runs           5.436       1.289   4.218 3.43e-05 ***
## Walks          3.662       1.468   2.495  0.01322 *
## Years          35.385       4.777   7.407 1.89e-12 ***
## LeagueN        81.920     89.211   0.918  0.35935
## DivisionW     -124.950     44.577  -2.803  0.00545 **
## Errors         -1.881       3.505  -0.537  0.59204
## NewLeagueN    -16.321     87.969  -0.186  0.85296
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 359 on 255 degrees of freedom
## Multiple R-squared:  0.3837, Adjusted R-squared:  0.3668
## F-statistic: 22.68 on 7 and 255 DF,  p-value: < 2.2e-16
```

```
newfitlm2=lm(Salary ~ Runs + Walks + Years + League + Division + Errors, data=Hitters2)
summary(newfitlm2) #further reduction
```

```
##
## Call:
## lm(formula = Salary ~ Runs + Walks + Years + League + Division +
##     Errors, data = Hitters2)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -731.72 -205.11  -49.08  126.17 2122.66
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -122.728     79.320  -1.547  0.12304
## Runs           5.432       1.286   4.223 3.35e-05 ***
## Walks          3.654       1.464   2.496  0.01320 *
## Years          35.387       4.768   7.421 1.71e-12 ***
## LeagueN        67.755     46.062   1.471  0.14253
## DivisionW     -124.998     44.492  -2.809  0.00535 **
## Errors         -1.855       3.496  -0.531  0.59619
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 358.3 on 256 degrees of freedom
```

```
## Multiple R-squared:  0.3836, Adjusted R-squared:  0.3692
## F-statistic: 26.56 on 6 and 256 DF,  p-value: < 2.2e-16

newfitlm3=lm(Salary ~ Runs + Walks + Years + League + Division, data=Hitters2)
summary(newfitlm3) #further reduction

##
## Call:
## lm(formula = Salary ~ Runs + Walks + Years + League + Division,
##     data = Hitters2)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -724.35 -207.07  -56.97   123.35  2125.45
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -133.927     76.353  -1.754  0.08062 .
## Runs           5.297       1.259   4.207 3.58e-05 ***
## Walks          3.702       1.459   2.537  0.01178 *
## Years         35.737       4.716   7.578 6.39e-13 ***
## LeagueN        64.333      45.545   1.413  0.15901
## DivisionW    -125.515     44.419  -2.826  0.00509 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 357.8 on 257 degrees of freedom
## Multiple R-squared:  0.383, Adjusted R-squared:  0.371
## F-statistic: 31.9 on 5 and 257 DF,  p-value: < 2.2e-16

notdoneyetlm=lm(Salary ~ Runs + Hits + Walks + Years + Division, data=Hitters2)
summary(notdoneyetlm) #final model ; all significant factors, but

##
## Call:
## lm(formula = Salary ~ Runs + Hits + Walks + Years + Division,
##     data = Hitters2)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -731.62 -209.29  -56.61   103.52  2203.93
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -147.802     71.254  -2.074  0.03905 *
## Runs          -1.093       2.407  -0.454  0.65025
## Hits           3.431       1.194   2.873  0.00441 **
## Walks          4.698       1.455   3.229  0.00140 **
## Years         33.885       4.679   7.242 5.13e-12 ***
## DivisionW    -132.246     43.910  -3.012  0.00286 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 353.5 on 257 degrees of freedom
## Multiple R-squared:  0.3975, Adjusted R-squared:  0.3858
```

```
## F-statistic: 33.91 on 5 and 257 DF, p-value: < 2.2e-16
```

```
# shouldn't "Hits" and "HmRun" be significant, by intuition?
```

```
cor(Hitters2$Hits, Hitters2$Runs) # Multicollinearity
```

```
## [1] 0.9106301
```

```
cor(Hitters2$Runs, Hitters2$HmRun) ; cor(Hitters2$Hits, Hitters2$HmRun)
```

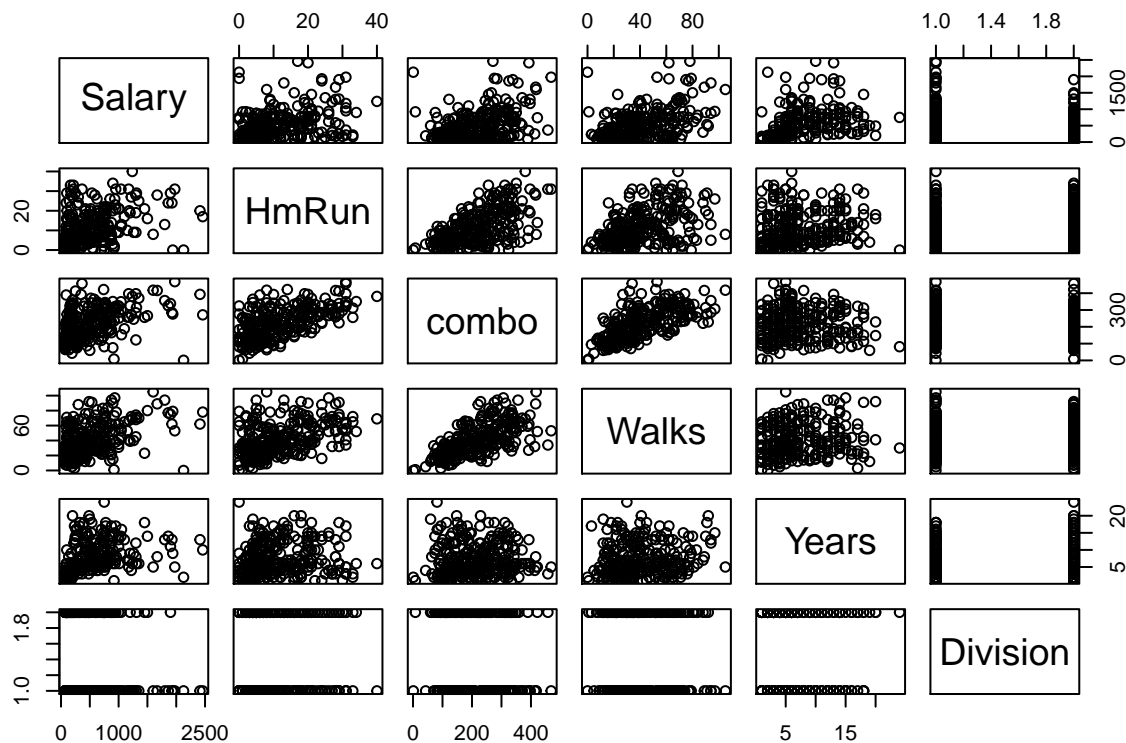
```
## [1] 0.6310759
```

```
## [1] 0.5306274
```

```
div=mean(Hitters2$Hits)/mean(Hitters2$Runs)
```

```
Hitters2$combo=(Hitters2$Hits + div*Hitters2$Runs)
```

```
pairs(Salary ~ HmRun + combo + Walks + Years + Division, data=Hitters2)
```



```
# No extreme correlations
```

```
combolm=lm(Salary ~ HmRun + combo + Walks + Years + Division, data=Hitters2)
```

```
summary(combolm)
```

```
##
```

```
## Call:
```

```
## lm(formula = Salary ~ HmRun + combo + Walks + Years + Division,  
##     data = Hitters2)
```

```
##
```

```
## Residuals:
```

```
##      Min       1Q   Median       3Q      Max  
## -750.20 -208.47  -44.86  126.50 2177.96
```

```
##
```

```
## Coefficients:
```

```
##              Estimate Std. Error t value Pr(>|t|)  
## (Intercept)  -120.924     70.932  -1.705 0.089441 .  
## HmRun           2.813       3.159   0.891 0.373984
```

```
## combo          1.315      0.357    3.682 0.000282 ***
## Walks          3.751      1.368    2.742 0.006532 **
## Years         34.492      4.689    7.356 2.54e-12 ***
## DivisionW     -129.066    44.036   -2.931 0.003684 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 355 on 257 degrees of freedom
## Multiple R-squared:  0.3926, Adjusted R-squared:  0.3807
## F-statistic: 33.22 on 5 and 257 DF,  p-value: < 2.2e-16
```

*# HmRun is not statistically significant, but the researcher opted to keep it in due to
the intuitive relationship between salary and number of homeruns.
Therefore, 'combolm' is our final model*

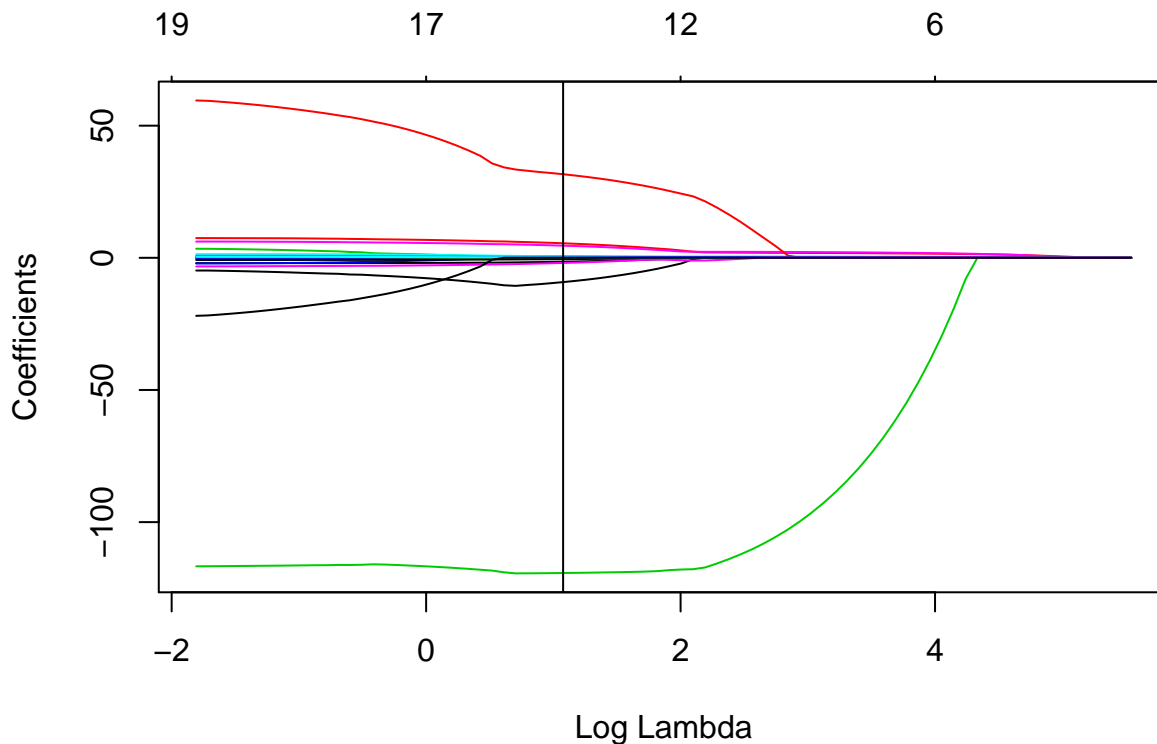
Lasso

```
lasso_mod = glmnet(x, y, alpha=1)
plot(lasso_mod, xvar = "lambda")
set.seed(1)
lasso_cvfit = cv.glmnet(x, y, alpha=1)
lasso_cvfit$lambda.min #selected lambda value ; $lambda.min is that value that
```

```
## [1] 2.935124
```

minimizes cross-validation error

```
plot(lasso_mod, xvar = "lambda") ; abline(v=log(lasso_cvfit$lambda.min))
```



```
coef(lasso_cvfit, s="lambda.min")
```

```
## 20 x 1 sparse Matrix of class "dgCMatrix"
##              1
## (Intercept) 117.5258436
## AtBat      -1.4742901
## Hits       5.4994256
## HmRun      .
## Runs       .
## RBI        .
## Walks      4.5991651
## Years     -9.1918308
## CAtBat     .
## CHits      .
## CHmRun     0.4806743
## CRuns      0.6354799
## CRBI       0.3956153
## CWalks    -0.4993240
## LeagueN    31.6238173
## DivisionW -119.2516409
## PutOuts    0.2704287
## Assists    0.1594997
## Errors    -1.9426357
## NewLeagueN .

# 6 variables have been shrunk towards 0 by the Lasso method

lasso_coefs = as.numeric(coef(lasso_cvfit, s="lambda.min"))
sum(abs(lasso_coefs)==0)

## [1] 6

# 6 additional variables have been set = 0 by the Lasso method
```