

Supplementary material

pyisotopomer: A Python package for obtaining nitrous oxide isotopocules from isotope ratio mass spectrometry

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Table S1: Different pairings of reference materials. Pooled standard deviations of γ and κ calculated from different pairings of reference materials, and the corresponding pooled standard deviations of $\delta^{15}\text{N}^\alpha$, $\delta^{15}\text{N}^\beta$, and SP, are shown for tests performed on the Lab 1 and Lab 2 IRMS. Pooled standard deviations are also shown for scrambling and isotopomer calculations done in the MATLAB and Python versions of the software.

Test	Pooled standard deviations				
	γ (% uncertainty*)	κ (% uncertainty*)	$\delta^{15}\text{N}^\alpha$ (‰ <i>vs. AirN₂</i>)	$\delta^{15}\text{N}^\beta$ (‰ <i>vs. AirN₂</i>)	SP (‰ <i>vs. AirN₂</i>)
Lab 1 three ref. pairings, no extreme values	0.39	0.16	0.47	0.44	0.91
Lab 2 three ref. pairings, incl. extreme values	0.77	1.17	2.54	2.29	4.83
Lab 2 one ref. pairing, excl. extreme values	0.15	0.61	(see section 4.7 for precision between replicates)		
MATLAB vs. Python	0.44	0.93	0.028	0.026	0.054

*Percent uncertainties represent pooled SD as a percentage of the mean

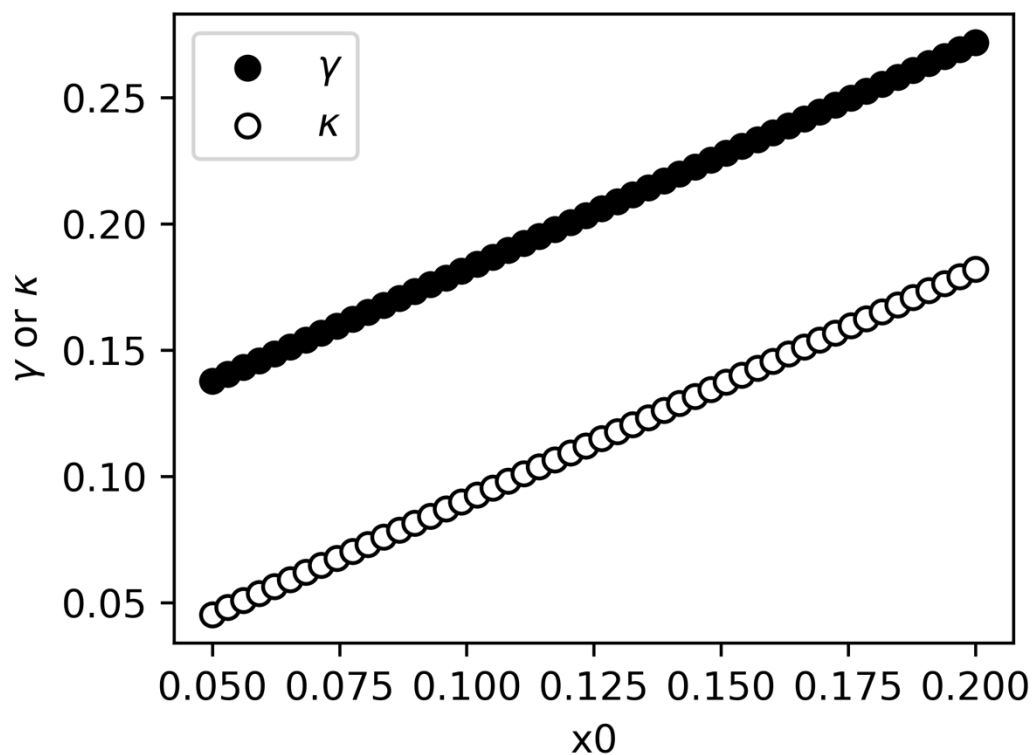


Figure S1. Solutions for γ and κ calculated across a range of initial guesses (x_0) for the least squares solver function at the core of pyisotopomer. The default values for x_0 are $\gamma=0.17$ and $\kappa=0.08$, based on the performance of the ThermoFinnigan Delta V mass spectrometer at Lab 1.

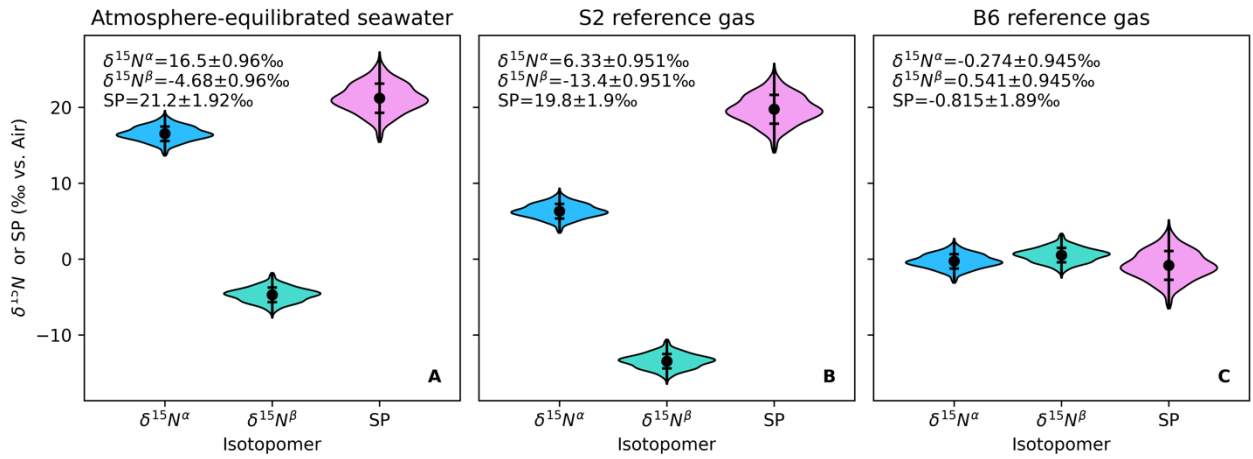


Figure S2: Isotopocule values and error associated with an uncertainty of $\pm 6.83 \times 10^{-4}$ in γ and $\pm 1.48 \times 10^{-4}$ in κ , based on Monte Carlo simulation results. The violin plots are based on a kernel density estimate of the distribution and show the mean value $\pm 1\sigma$.

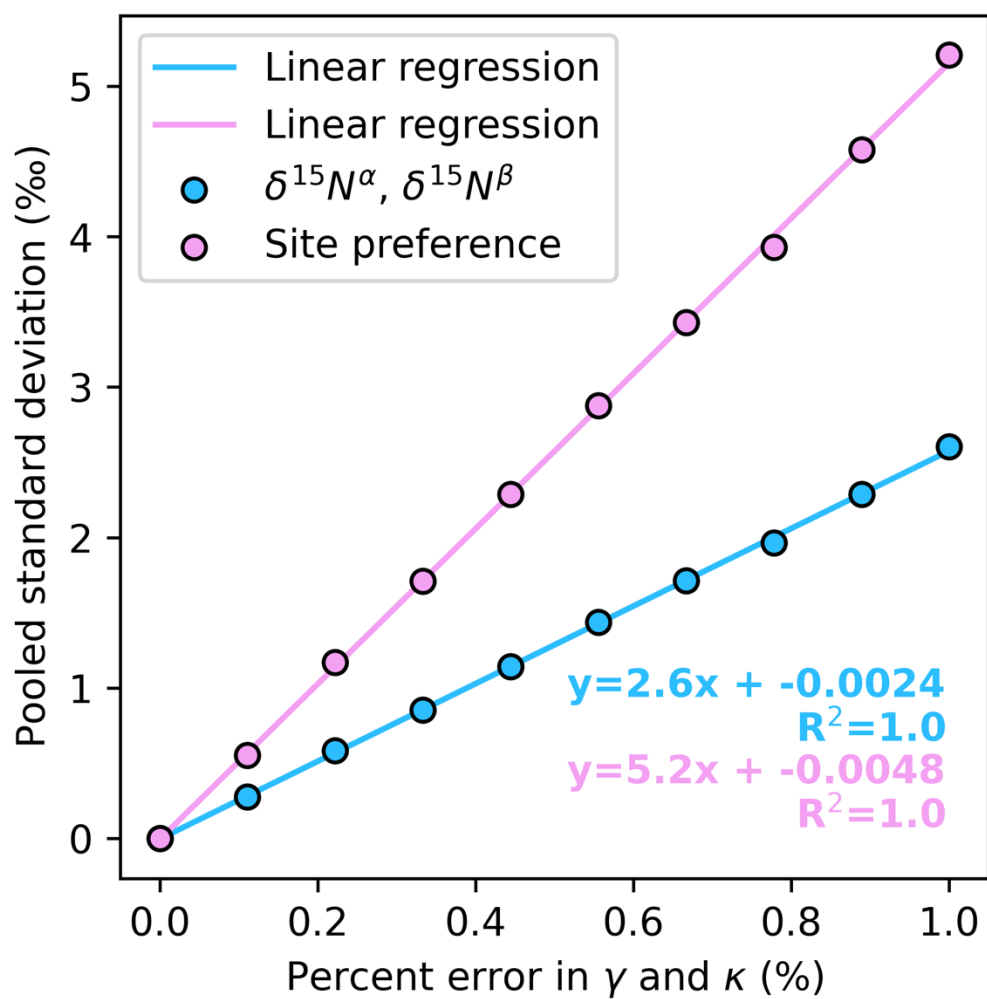


Figure S3: Pooled standard deviation of $\delta^{15}\text{N}^\alpha$, $\delta^{15}\text{N}^\beta$, and SP resulting from increasing relative uncertainties in γ and κ . Each point corresponds to 1,000 values of γ and κ sampled from a distribution with standard deviation equal to the given level of uncertainty, and the corresponding pooled standard deviation of 1,000 simulated values of $\delta^{15}\text{N}^\alpha$, $\delta^{15}\text{N}^\beta$, and SP.

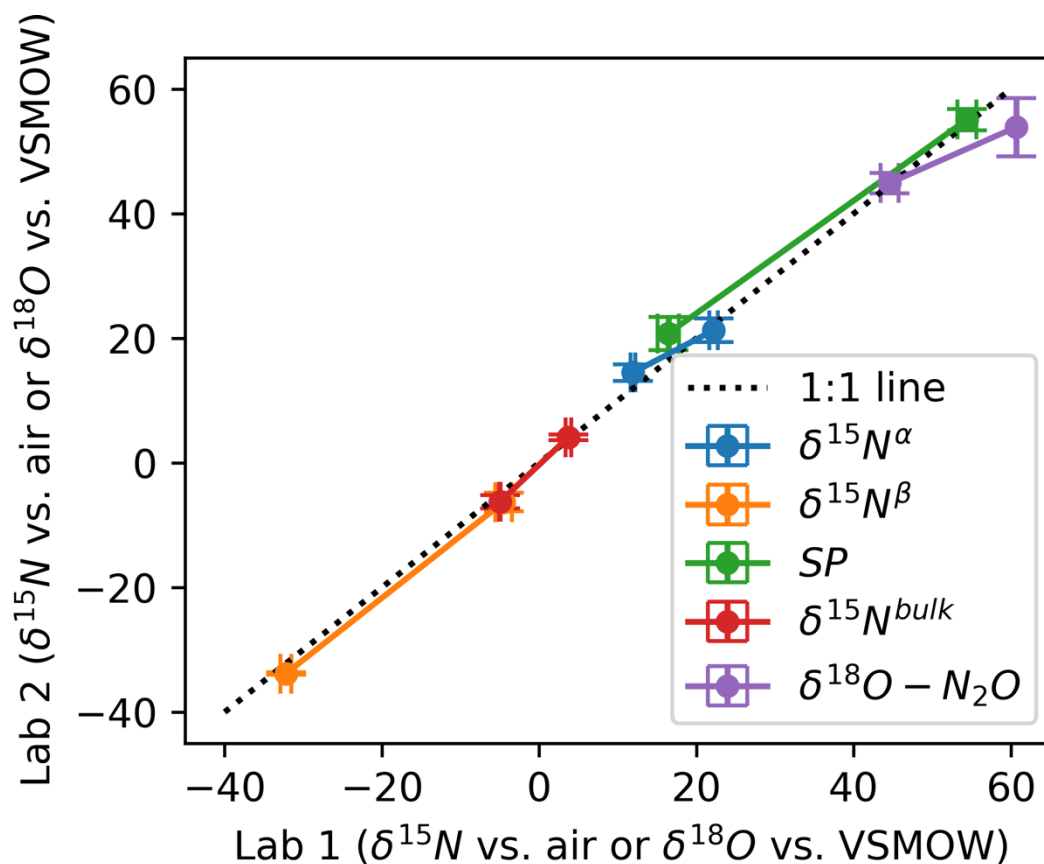


Figure S4: Intercalibration results for lake water unknowns taken at 10 meters and 90 meters depth from lake Lugano in Switzerland. Independent measurements of the isotopic composition of N_2O in each sample, performed by Lab 1 and Lab 2, respectively, are plotted against each other. Data points represent the mean from replicate bottles taken at the same depth ($n=2-5$) and error bars represent one standard deviation. A one-to-one line (black dashed line) is plotted for comparison.