# **Risk Analytics - Term Project**

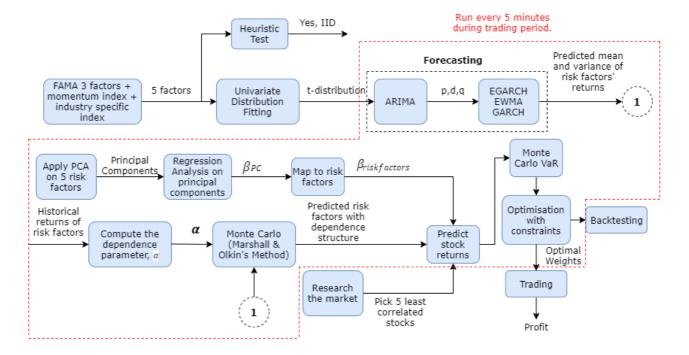
Lecturer: Dr Colin Rowat Student ID: 2031611

### **Problems**

The aim was to use Python to build a trading system that maximises relative wealth against the MSCI ACWI benchmark during its deployment period, subject to the constraint that its expected shortfall (ES) in the 1% tail is less than 1% of its value [5]. The portfolio contains 5 stocks from the Oil, Gas & Consumable Fuels (GICS code: 101020) industry.

$$\begin{aligned} \max_{w} & (w^{T}S_{stocks} - S_{benchmark}) \\ s. & t. & ES_{0.01} < 0.01 * V_{0} \\ & w^{T}S_{stocks} \leqslant V_{0} \\ & \Sigma_{i=1}^{5} w_{i} = 1 \\ & where & V_{0} = \$1 \ mil \end{aligned}$$

# **Algorithm Overview**



### **Document Structure**

- 1. Import Time Series
- 2. Research the Market
- 3. Risk Factors Model
- 4. Heuristic Test
- 5. Fit Univariate Distribution
- 6. Forecasting
- 7. Copula
- 8. Optimisation
- 9. Backtesting
- 10. Trading

# 0.0 Install the python packages

```
In [1]:
        # Installing Packages
        4 !pip install alpha_vantage
           !pip install numpy
           !pip install pandas
           !pip install arch
        8
           !pip install copulae
           !pip install matplotlib
           !pip install itertools
           !pip install seaborn
       11
           !pip install scipy
           !pip install statsmodels
       13
       14 !pip install sklearn
           !pip install warnings
           !pip install time
       17 !pip install datetime
```

```
Requirement already satisfied: alpha_vantage in c:\users\owner\anaconda3\lib\site-packages (2.1.3)
Requirement already satisfied: requests in c:\users\owner\anaconda3\lib\site-packages (from alpha_vantage) (2.22.0)
Requirement already satisfied: urllib3!=1.25.0,!=1.25.1,<1.26,>=1.21.1 in c:\users\owner\anaconda3\lib\site-packages
(from requests->alpha_vantage) (1.24.2)
Requirement already satisfied: idna<2.9,>=2.5 in c:\users\owner\anaconda3\lib\site-packages (from requests->alpha_vant
Requirement already satisfied: chardet<3.1.0,>=3.0.2 in c:\users\owner\anaconda3\lib\site-packages (from requests->alp
ha_vantage) (3.0.4)
Requirement already satisfied: certifi>=2017.4.17 in c:\users\owner\anaconda3\lib\site-packages (from requests->alpha_
vantage) (2019.9.11)
Requirement already satisfied: numpy in c:\users\owner\anaconda3\lib\site-packages (1.16.5)
Requirement already satisfied: pandas in c:\users\owner\anaconda3\lib\site-packages (0.24.2)
Requirement already satisfied: numpy>=1.12.0 in c:\users\owner\anaconda3\lib\site-packages (from pandas) (1.16.5)
Requirement already satisfied: python-dateutil>=2.5.0 in c:\users\owner\anaconda3\lib\site-packages (from pandas) (2.
8.0)
Requirement already satisfied: pytz>=2011k in c:\users\owner\anaconda3\lib\site-packages (from pandas) (2019.3)
Requirement already satisfied: six>=1.5 in c:\users\owner\anaconda3\lib\site-packages (from python-dateutil>=2.5.0->pa
ndas) (1.12.0)
Requirement already satisfied: arch in c:\users\owner\anaconda3\lib\site-packages (4.11)
```

# 0.1 Import the python libraries

```
In [2]:
            #############################
            # Importina packages
         3
            from alpha_vantage.timeseries import TimeSeries
           from alpha_vantage.techindicators import TechIndicators
            import matplotlib.pyplot as plt
            import pandas as pd
         9 import numpy as np
        10 from arch import arch_model
            import seaborn as sns
        12 from itertools import chain
        13 import scipy.stats as st
            from statsmodels.tsa.stattools import adfuller
        14
        15 | from statsmodels.tsa.statespace.sarimax import SARIMAX
        16 import statsmodels.api as sm
            from statsmodels.distributions.empirical_distribution import ECDF
        17
            plt.style.use('ggplot')
        19 | from sklearn.linear_model import LinearRegression
        20 from sklearn.preprocessing import StandardScaler
            from sklearn.decomposition import PCA
           from sklearn.pipeline import Pipeline
        22
        23 from scipy.stats import uniform
        24 | from scipy.interpolate import interp1d
        25
           from scipy.stats import t
        26 | from copulae import ClaytonCopula, GumbelCopula, FrankCopula
        27
            import warnings
            warnings.filterwarnings('ignore')
        29
           from numpy.linalg import inv
         30
            import time
```

# 1. Import Time Series Data

```
#####################
         4
           # Total stocks needed for the portfolio
         5
           PORTFOLIO_SIZE = 5
         6
           8
         9
        10
        11
           # List all the risk factors for the Fama-French Factor Model
        12
        13
           value_factors = ['SPYV', 'SPYG']
           size_factors = ['IWM', 'DJI']
        14
        15
           momentum_factors = ['MTUM']
           market_factors = ['SPY']
           sector_index = ['^SP400-101020'] # S&P 400 Oil, Gas & Consumable Fuels (Industry) Index
        17
           tot_risk_factors = market_factors + value_factors + size_factors + momentum_factors + sector_index
        18
        19
           # Benchmark
        20
           benchmark = ['ACWI']
In [4]:
           # Functions for Getting data from Alpha-Vantage
            4
         5
            def get_ticker(ticker, key='E9FYA5V9FWQ677IZ', interval='1min'):
               # Choose your output format, or default to JSON (python dict)
         6
               ts = TimeSeries(key, output_format='pandas')
         8
               ti = TechIndicators(key)
         9
               # Get ticker close time series
        10
               tick_data = ts.get_intraday(symbol=ticker, interval=interval, outputsize='full')[0]['4. close']
        11
               return tick_data.iloc[::-1]
        12
        13
           14
        15
               all_price_data = pd.concat([get_ticker(tic, key, interval)
                                         for tic in all_tickers], axis=1,
        16
        17
                                        keys=all_tickers).fillna(method='ffill', axis=0).dropna(axis=0)
        18
               return all_price_data
        19
           stock_price_data = get_all_tickers(tot_tickers)
        20
        21
           stock_price_data
Out[4]:
                  TOT
                        XOM
                                     MRO
                                                   MMP
                                                         RDS-A
                                                                NAT
                                                                      CPG
                                                                             PBR
                                                                                    CSL
                                                                                          HFC
                                                                                                 VLO
                                                                                                              PSX
           date
        2020-02-
            13
               49.0700 61.0100 28.2300 11.1300 111.5142 59.4550 51.1700 3.5701 3.1900 14.8700 161.610 44.4332 84.6982 19.8450 90.8700 34
        09:31:00
        2020-02-
               49 0968 61 0022 28 0910 10 9304 111 5900 59 2700 51 1645 3 5101 3 1801 14 9005 161 610 44 4300 84 4900 19 8107 90 8100 34
            13
        09:32:00
        2020-02-
            13
               49.0600 61.0010 28.1055 10.8452 111.7418 59.3400 51.1000 3.5000 3.1901 14.8900 161.610 44.4650 84.3200 19.8503 90.9150 34
        09:33:00
        2020-02-
               49.0500 61.0272 28.1409 10.9666 111.7436 59.3525 51.0900 3.4951 3.1900 14.8805 161.610 44.4925 84.1800
        09:34:00
        2020-02-
                                                                                        44 5100 84 2885 10 8808 QO 8400
                49 1200 61 1250 28 1512 10 9405
                                          111 8115 50 3402 51 0600 3 4000 3 1000 14 8048 161 610
```

# 2. Research the Market

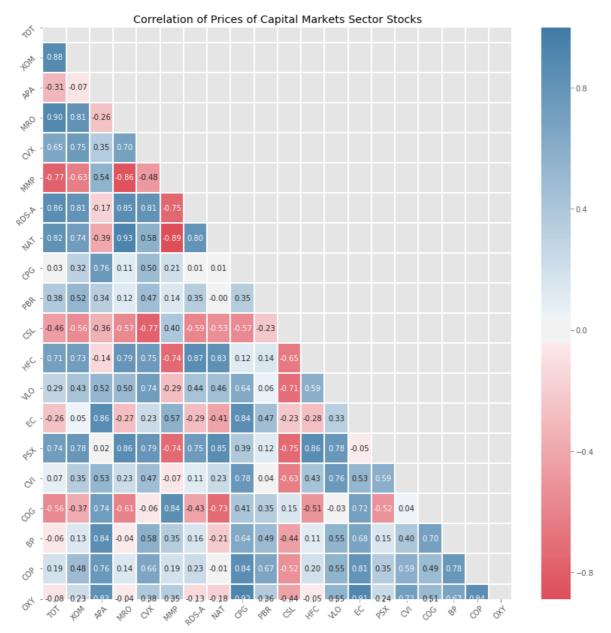
In [3]:

1

Out of the 20 top performing stocks, 5 least correlated stocks were selected because it would give the greatest diversification effect.

```
# Functions to find the least and most volatile stocks
       def get_least_risky_stocks(stock_price_data, count=PORTFOLIO_SIZE):
       6
             # Find the covariance matrix of the data
             cov_matrix = get_price_cov_stocks(stock_price_data)
       8
             # List of top 5 least volatile stocks
       9
            lvol_ticks = [cov_matrix.index[i] for v, i in
       10
                       sorted((v, i) for i, v in enumerate([cov_matrix.iloc[i, i] for i in range(len(cov_matrix))]))[
                       0:count]]
       11
            return lvol_ticks
       12
```

Out[7]: <matplotlib.axes.\_subplots.AxesSubplot at 0x17bc02b0708>



```
In [8]:
          # Function to get the least correlated stocks from the sector and add it to the portfolio
          5
              # Get the correlation matrix of the stocks
        6
        7
              corr_matrix = get_price_corr_stocks(stock_price_data)
        8
        9
              # The greatest number of least volatile stocks to be selected
       10
              count_for_corr = int(corr_matrix.shape[0]/2 if 10 < corr_matrix.shape[0] < 30 else 5)</pre>
       11
       12
              # Removing highly correlated features
       13
              # Create positive correlation matrix
       14
              corr_df = corr_matrix.abs()
       15
              # Find the stocks with the least volatility
       17
              lvol_ticks = get_least_risky_stocks(stock_price_data, count_for_corr)
       18
              corr_list = sorted(list(chain.from_iterable(sorted((val, tic, corr_tic)))
       19
                           for val, corr_tic in
                           sorted((val, corr df.index[ind]) for ind, val in enumerate(corr df.loc[str(tic), :]))
       20
                           if tic != corr_tic) for tic in lvol_ticks)), key=lambda x: x[0])
       21
       22
             # Provides the final set of 5 tickers with least correlation among them
       23
       24
              portfolio_stocks = set()
       25
              for val, tic, corr_tic in corr_list:
       26
                 portfolio_stocks.add(tic)
       27
                 if len(portfolio_stocks) == count: break
       28
       29
              return list(portfolio_stocks)
       30
       31
          portfolio_stocks = find_least_corr_stocks(stock_price_data)
```

```
Out[8]: ['RDS-A', 'COP', 'CPG', 'NAT', 'PBR']
```

portfolio\_stocks

Then, calculate the compound returns of the stocks and risk factors. The formula is give by,

Compound Return = 
$$\ln \frac{P_t}{P_{t-1}}$$

### 3. Risk Factors Model

The FAMA-French Three Factors Model was chosen to predict stock returns. It has three factors: size of firms, book-to-market values, and excess return on the market. In other words, the three factors used are SMB (small minus big), HML (high minus low) and the market risk [5]. Two additional factors - momentum and sector specific indices were also included to improve risk evaluation.

$$r = R_f + \beta (R_m - R_f) + b_s SML + b_v HML + mMTM + sSCT + \alpha$$

Where r = rate of return,  $R_f$  = Risk free return rate,  $R_m$  = Return of the market portfolio, SMB = Small Minus Big, HML = High Minus Low i.e. book to market values, MTM = Momentum Index, SCT = Sector Specific Index and  $\alpha$ ,  $\beta$  = regression parameters. Here the risk free rate is negligible and will not be considered in the model.

- SMB refers to the differential returns of small stocks minus big stocks, where small and big refer simply to the market capitalisation of the stocks
- HML stands for the returns of a portfolio of high book-to-market stocks minus a portfolio of low book to market stocks.
- *MTM* used in this model is the *MTUM* factor index. It is to track the performance of an index that measures the performance of U.S. large- and mid-capitalization stocks exhibiting relatively higher momentum characteristics, before fees and expenses.
- *SCT* used in this model is the *S&P 400 Oil, Gas & Cnsmble Fuel(Ind)* index. It is a stock market index from *S&P* Dow Jones Indices. The index serves as a barometer for the U.S. mid-cap Oil, Gas & Cnsmble Fuel sector equities and is the most widely followed mid-cap index.

```
In [9]:
         # Function to get the returns of the stocks and risk factors
       3
         5
         def find_returns(stock_price_data):
             return np.log(stock_price_data).diff().fillna(method='ffill', axis=0).dropna(axis=0)
       6
       7
       8
       9
         def get_returns(tickers):
      10
             if isinstance(tickers, str):
               price_data = get_ticker(tickers)
      11
      12
      13
               price_data = get_all_tickers(tickers)
             return find_returns(price_data)
      14
```

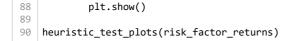
```
In [10]:
            1
            # Function to get the returns of the Fama French risk factors and create risk-factor returns dataframe
            def get_ff_risk_factors(market_factors=['SPY'],
                                  value_factors=['SPYV', 'SPYG'],
size_factors=['IWM', 'DJI'],
         6
         8
                                  momentum_factors=['MTUM'],
                                  sector_index=['^SP400-101020']):
         9
         10
                # Market factor
         11
                market_factor_returns = get_returns(market_factors)
         12
         13
                # Value factors (HML)
         14
                value_returns = get_returns(value_factors)
         15
                value_factor_returns = value_returns[value_factors[0]] - value_returns[value_factors[1]]
         17
                # Size factors (SML)
                size_returns = get_returns(size_factors)
         18
                size_factor_returns = size_returns[size_factors[0]] - size_returns[size_factors[1]]
         19
         20
         21
                # Momentum factor
         22
                momentum_factor_returns = get_returns(momentum_factors)
         23
         24
                # Sector Index factor
                sector_factor_returns = get_returns(sector_index)
         25
         26
         27
                factor_returns = pd.concat([market_factor_returns,
         28
                                         size_factor_returns,
         29
                                         value_factor_returns,
         30
                                         momentum_factor_returns,
         31
                                         sector_factor_returns], axis=1,
         32
                                         ignore_index=True).fillna(method='ffill', axis=0).dropna(axis=0)
         33
         34
                factor_returns.columns = ['Market', 'SMB', 'HML', 'Momentum', 'Sector']
         35
         36
                # Remove Outliers
         37
                factor_returns = factor_returns[(np.abs(st.zscore(factor_returns)) < 4).all(axis=1)]</pre>
         38
         39
                return factor_returns
         40
         41
            risk_factor_returns = get_ff_risk_factors()
```

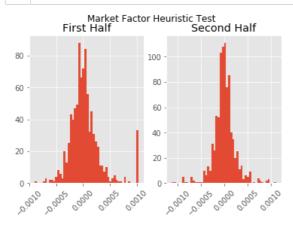
### 4. Heuristic Test

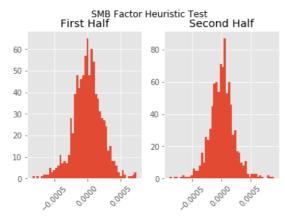
The first test is to split the compound returns time series into two halves. Then compare the respective histograms. If the compound returns are time-invariant, the two histograms should look very similar to each other [3].

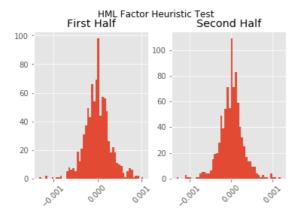
The second test consists of plotting the time series against its lagged values on a scatter plot. If the compound returns are independently identically distributed, the scatter plot must be symmetrical with respect to the reference axes and resemble a circular cloud [3].

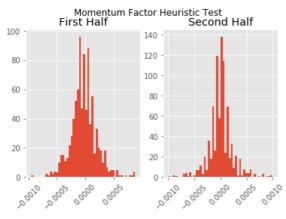
```
In [11]:
          # Function to run the heuristics test on the risk factor returns to see if they are IID
             5
             def heuristic_test_plots(risk_factor_returns):
          6
                 Performs two Heuristic tests for the risk factor returns to check if they are IID:
                     1) Split the series in two halves and plot the histogram of each half. Both the histograms
          8
          9
                        must resemble each other.
         10
                     2) Scatter-plot the time series of the total returns against the same time series lagged by
         11
                        one estimation interval. The scatter-plot must resemble a circular cloud.
         12
                 :param risk_factor_returns: Returns of all risk factors
         13
                 :return: Plot of histogram and scatter plot for each risk factor
         14
         15
                 # risk_factors = risk_factor_returns.columns
                 # number_of_factors = risk_factor_returns.shape[1]
         17
                 number_of_datapoints = risk_factor_returns.shape[0]
         18
                 first_half_df = risk_factor_returns.iloc[:int(number_of_datapoints/2), :]
                 second_half_df = risk_factor_returns.iloc[int(number_of_datapoints/2):, :]
         19
         20
                 number_of_bins = int(np.sqrt(number_of_datapoints / 0.7))
         21
         22
                 # Market Factor Histogram Heuristic Test
         23
                 fig, axes = plt.subplots(1, 2)
         24
                 fig.suptitle("Market Factor Heuristic Test")
         25
                 fig.subplots_adjust(bottom=0.2)
                 _ = first_half_df['Market'].hist(bins=number_of_bins, ax=axes[0])
                 _ = axes[0].set_title("First Half")
         27
         28
                 _ = plt.setp(axes[0].get_xticklabels(), rotation=45)
                 _ = second_half_df['Market'].hist(bins=number_of_bins, ax=axes[1])
         29
                 _ = axes[1].set_title("Second Half")
         30
         31
                 _ = plt.setp(axes[1].get_xticklabels(), rotation=45)
         33
                 # SMB Factor Histogram Heuristic Test
         34
                 fig, axes = plt.subplots(1, 2)
         35
                 fig.suptitle("SMB Factor Heuristic Test")
         36
                 fig.subplots_adjust(bottom=0.2)
                 _ = first_half_df['SMB'].hist(bins=number_of_bins, ax=axes[0])
         37
         38
                 _ = axes[0].set_title("First Half")
                 _ = plt.setp(axes[0].get_xticklabels(), rotation=45)
         39
                 = second_half_df['SMB'].hist(bins=number_of_bins, ax=axes[1])
         40
                 _ = axes[1].set_title("Second Half")
         41
                 _ = plt.setp(axes[1].get_xticklabels(), rotation=45)
         42
         43
         44
                 # HML Factor Histogram Heuristic Test
         45
                 fig, axes = plt.subplots(1, 2)
         46
                 fig.suptitle("HML Factor Heuristic Test")
         47
                 fig.subplots_adjust(bottom=0.2)
                 _ = first_half_df['HML'].hist(bins=number_of_bins, ax=axes[0])
         48
                 _ = axes[0].set_title("First Half")
         49
                 _ = plt.setp(axes[0].get_xticklabels(), rotation=45)
         50
                 _ = second_half_df['HML'].hist(bins=number_of_bins, ax=axes[1])
         51
                 _ = axes[1].set_title("Second Half")
         52
         53
                 _ = plt.setp(axes[1].get_xticklabels(), rotation=45)
         54
         55
                 # Momentum Factor Histogram Heuristic Test
         56
                 fig, axes = plt.subplots(1, 2)
         57
                 fig.suptitle("Momentum Factor Heuristic Test")
         58
                 fig.subplots_adjust(bottom=0.2)
                 _ = first_half_df['Momentum'].hist(bins=number_of_bins, ax=axes[0])
         59
                 _ = axes[0].set_title("First Half")
         60
                 _ = plt.setp(axes[0].get_xticklabels(), rotation=45)
         61
         62
                 _ = second_half_df['Momentum'].hist(bins=number_of_bins, ax=axes[1])
                 _ = axes[1].set_title("Second Half")
         63
                 _ = plt.setp(axes[1].get_xticklabels(), rotation=45)
         64
         65
         66
                 # Sector Index Factor Histogram Heuristic Test
         67
                 fig, axes = plt.subplots(1, 2)
         68
                 fig.suptitle("Sector Index Factor Heuristic Test")
         69
                 fig.subplots_adjust(bottom=0.2)
                 _ = first_half_df['Sector'].hist(bins=number_of_bins, ax=axes[0])
         70
                 _ = axes[0].set_title("First Half")
         71
         72
                 _ = plt.setp(axes[0].get_xticklabels(), rotation=45)
                 _ = second_half_df['Sector'].hist(bins=number_of_bins, ax=axes[1])
         73
                 _ = axes[1].set_title("Second Half")
         74
         75
                 _ = plt.setp(axes[1].get_xticklabels(), rotation=45)
         76
         77
                 # Scatter Plot
         78
                 factors = ['Market','SMB','HML','Momentum','Sector']
         79
                 titles = ['Market Scatter Plot','SMB Scatter Plot','HML Scatter Plot','Momentum Scatter Plot','Sector Scatter Plo
         80
                 for i in range(len(factors)):
         81
                     fig, axes = plt.subplots(1)
         82
                     fig.subplots_adjust(bottom=0.2)
         83
                     sns.scatterplot(risk_factor_returns[factors[i]][:-1],
                                 risk_factor_returns[factors[i]].shift(1).dropna(axis=0))
         84
         85
                     plt.title(factors[i])
         86
                     plt.xlabel('Risk Factors (1 time-step lagged)')
         87
                     plt.ylabel('Risk Factors')
```

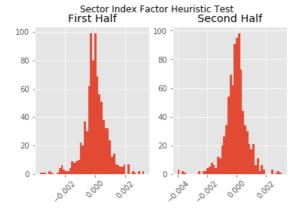


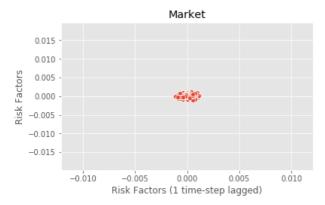


















```
0.01
        isk Factors
          0.00
In [12]:
           # Functions to create a risk factor and stock return matrix for each stock in the portfolio
           3
        5
           def join_stock_risk_factors(stock_returns, risk_factor_returns, stock):
        6
              stock_factor_data = pd.concat([stock_returns[stock], risk_factor_returns], axis=1,
                                      ignore\_index=True).fillna(method='ffill', axis=0).dropna(axis=0)
              stock_factor_data.columns = [stock, 'Market', 'SMB', 'HML', 'Momentum', 'Sector']
        8
        9
              return stock_factor_data
        10
        11
           12
        13
              total_tickers = portfolio_stocks + benchmark
        14
              risk_factor_returns = get_ff_risk_factors()
        15
              stock_returns = get_returns(total_tickers)
        16
              stock_factor_dict = {}
        17
              for stock in total_tickers:
                 stock_factor_dict[stock] = join_stock_risk_factors(stock_returns, risk_factor_returns, stock)
        18
        19
              return stock_factor_dict
        20
        21
           stock_factor_dict = get_stock_factor_df(portfolio_stocks)
          stock_factor_dict
Out[12]: {'RDS-A':
                                  RDS-A
                                                   SMB
                                                           HML
                                         Market
                                                                  Momentum \
                                                                                                     date
```

2020-02-13 09:33:00 -0.001066 0.000103 0.000459 -0.000579 -4.443786e-04 2020-02-13 09:34:00 -0.000587 0.000103 0.000459 -0.000579 -4.443786e-04 2020-02-13 09:35:00 -0.000392 -0.000713 -0.000444 0.000469 -6.665926e-04 2020-02-13 09:36:00 0.001370 -0.000713 -0.000444 0.000469 -6.665926e-04 2020-02-13 09:37:00 0.000587 -0.000059 0.000613 0.000789 2.220495e-04 2020-02-13 09:38:00 0.000586 -0.000059 0.000613 0.000789 2020-02-13 09:39:00 0.001464 0.000535 0.000239 0.000168 7.116307e-04 2020-02-13 09:40:00 -0.000683 -0.000178 -0.000401 0.000151 -3.414386e-04 2020-02-13 09:41:00 0.000029 0.000149 -0.000167 -0.000222 -2.961647e-04 2020-02-13 09:42:00 -0.000420 -0.000119 0.000119 -0.000678 -1.746960e-04 2020-02-13 09:43:00 0.000976 0.000030 0.000104 -0.000157 -1.953865e-04 2020-02-13 09:44:00 -0.000781 -0.000178 -0.000573 -0.000175 4.455962e-04 2020-02-13 09:45:00 0.000390 -0.000505 0.000282 0.000762 -1.495411e-04 2020-02-13 09:47:00 0.000780 -0.000115 0.000032 0.000310 8.660518e-05 2020-02-13 09:48:00 -0.000195 0.000594 -0.000268 -0.000381 4.442470e-04 2020-02-13 09:49:00 -0.000487 0.000059 -0.000565 0.000159 4.442470e-04

The test results suggest it is safe to assume that the compound returns are time-invariant i.i.d series.

### 5. Fit the Univariate Distribution

Sector

0.02

```
In [13]:
         # Functions to fit the univariate risk-factor distributions and plot the distributions
            # Get the distribution and parameters
         6
                distribution, param = best_fit_distribution(risk_factor_return)
         8
                if not isinstance(risk_factor_return, pd.Series):
         9
                   risk_factor_return = pd.Series(risk_factor_return)
        10
                with plt.style.context(style):
        11
                   fig = plt.figure(figsize=figsize)
         12
                   layout = (2, 2)
        13
                   dist_ax = plt.subplot2grid(layout, (0, 0), colspan=2)
        14
                   \#qq_ax = plt.subplot2grid(layout, (1, 0))
        15
                   #pp_ax = plt.subplot2grid(layout, (1, 1))
        17
                   sns.distplot(risk_factor_return, ax=dist_ax)
                   dist_ax.set_title('Distribution Plots')
        18
        19
                   #sm.qqplot(risk_factor_return, line='s', ax=qq_ax)
        20
                   #qq ax.set title('QQ Plot')
        21
                   #st.probplot(risk_factor_return, sparams=param[1:], plot=pp_ax)#, dist=eval("st."+distribution))
         22
                   plt.tight_layout()
        23
                return
        24
        25
            26
                ""Model data by finding best fit distribution to data"""
        27
               if not isinstance(risk_factor_return, pd.Series):
        28
        29
                   risk_factor_return = pd.Series(risk_factor_return)
        30
                # Get histogram of original data
        31
               y, x = np.histogram(risk_factor_return, bins=bins, density=True)
               x = (x + np.roll(x, -1))[:-1] / 2.0
        33
         34
                # Distributions to check
         35
               DISTRIBUTIONS = [st.cauchy, st.expon, st.lognorm, st.norm, st.t]
        36
        37
                # Best holders
        38
               best_distribution = st.norm
         39
                best_params = (0.0, 1.0)
        40
               best sse = np.inf
        41
        42
                # Estimate distribution parameters from data
        43
                for distribution in DISTRIBUTIONS:
        44
        45
                   # Try to fit the distribution
        46
        47
                       # Ignore warnings from data that can't be fit
                      with warnings.catch_warnings():
        48
        49
                          warnings.filterwarnings('ignore')
        50
        51
                          # fit dist to data
        52
                          params = distribution.fit(risk factor return) # Shape, Location, scale
        53
                          # Separate parts of parameters
        54
        55
                          arg = params[:-2]
        56
                          loc = params[-2]
        57
                          scale = params[-1]
        58
        59
                          # Calculate fitted PDF and error with fit in distribution
        60
                          pdf = distribution.pdf(x, loc=loc, scale=scale, *arg)
        61
                          sse = np.sum(np.power(y - pdf, 2.0))
        62
        63
                          # identify if this distribution is better
        64
                          if best_sse > sse > 0:
        65
                              best_distribution = distribution
        66
                              best_params = params
        67
                              best sse = sse
        68
        69
                   except Exception:
        70
                      pass
         71
        72
                return (best distribution.name, best params)
        73
        74
            factors = ['Market','SMB','HML','Momentum','Sector']
                                                          Degree of Freedom
        75
                                                                                               Variance')
            print(
                                                                               Mean
         76
            for i in factors:
        77
               dist = best_fit_distribution(risk_factor_returns[i])
                print('The Best Fit Distribution of ', i,'is', dist)
        78
```

```
Degree of Freedom Mean Variance

The Best Fit Distribution of The Best Fit
```

The above results shows that t-distribution is the most appropriate fit to all 5 of the compound returns.

# 6. Forecasting

While returns themselves may show little or no autocorrelation. There is a strong positive autocorrelation in squared returns. This feature is regarded as GARCH, because conditional volatility varies over time. One of the most important features of high frequency returns on equity is that volatility tends to cluster [8].

#### **ARIMA Model**

Applying the Box-Jenskins method to the ARIMA model to find the best parameters p,d and q. These parameters are then used for the forecasting models later

$$y_t = \mu + \phi_1 y_{t-1} + \ldots + \phi_p y_{t-p} - \theta_1 \epsilon_{t-1} \ldots - \theta_q \epsilon_{t-q}$$

where y = returns time series,  $\epsilon =$  lagged residuals

```
In [14]:
         # Find the parameters of the risk factors returns using the ARIMA model
            def box_jenkins_ARIMA_params(risk_factor_return):
          6
                # The Augmented Dicky-Fuller test:
                # - Tests only for trend non-stationarity
                # - Null hypothesis is time series is non-stationary
          8
         9
                if not isinstance(risk_factor_return, pd.Series):
         10
                   risk_factor_return = pd.Series(risk_factor_return)
                adf = adfuller(risk_factor_return)
         11
         12
                # print('ADF statistic: ', adf[0])
         13
                # print('p-value: ', adf[1])
         14
                if adf[1] < 0.05:</pre>
         15
                   # print("The Series is Stationary")
         16
                    # When certain orders don't work and provide value errors while fitting
         17
                    # Loop over AR order
                    order_aic_bic = []
         18
         19
                    for p in range(3):
         20
                       # Loop over MA order
         21
                       for q in range(3):
         22
                           try:
                              # Fit Model
         23
         24
                              model = SARIMAX(risk_factor_return, order=(p, 0, q))
                              results = model.fit(disp=False)
         25
         26
                               # Add order and scores to list
         27
                               # print(p, q, results.aic, results.bic)
         28
                              order_aic_bic.append((p, q, results.aic, results.bic))
         29
                           except:
         30
                              pass
         31
         32
                    order_df = pd.DataFrame(order_aic_bic, columns=['p', 'q', 'aic', 'bic'])
         33
                    order_df.sort_values('aic', inplace=True)
         34
                    if order_df.empty:
         35
                       return (1, 0, 1)
         36
                    else:
         37
                       return (order_df.iloc[0, 0], 0, order_df.iloc[0, 1])
         38
```

### **Forecasting Model**

Three forecasting methods are used to compare the estimation performance.

### **GARCH**

$$\sigma_t^2 = \omega + \alpha y_{t-q}^2 + \beta \sigma_{t-p}^2$$

where  $\sigma$  = volatility of returns, y = returns times series, p and q are the lags for them respectively.

#### **EGARCH**

 $\ln(\sigma_t) = \omega + \sum_{i=1}^q \alpha_i g(z_{t-i}) + \sum_{j=1}^p \gamma_j \ln(\sigma_{t-j})$  $g(z_t) = \theta z_t + \gamma(|z_t| - \mathbb{E}|z_t|)$  $z_t = \epsilon_t / \sqrt{(\sigma_t)}$  $z_t \sim t(v, 0, 1)$ 

where

where

 $\lambda = smoothing\ const, 0 < \lambda < 1$ 

```
In [15]:
             # Functions to run the GARCH and EWMA model using the parameters from the ARIMA model
            4
            def garch_fit(risk_factor_return, garch_type='EGARCH', first_obs=None, last_obs=None):
                Garch model is being calculated in 10000 * percentage rather than returns as the larger
          6
          7
                magnitude helps it to converge, hence it is multiplied by 10000.
          8
                :param risk_factor_return:
          9
                :return:
         10
                distribution, param = best_fit_distribution(risk_factor_return)
         11
         12
                p, d, q = box_jenkins_ARIMA_params(risk_factor_return)
         13
                if distribution == 't':
                    garch_model = arch_model(risk_factor_return * 10000, vol=garch_type, p=int(p), o=1, q=int(q), dist='skewt')
         14
                else:
         15
                   garch_model = arch_model(risk_factor_return * 10000, vol=garch_type, p=int(p), o=1, q=int(q), dist='normal')
         16
         17
                res = garch_model.fit(update_freq=5, disp='off', first_obs=first_obs, last_obs=last_obs)
         18
         19
            def garch_forecast(risk_factor_return, garch_type='EGARCH', horizon=5, method='simulation'):
         20
         21
                res, garch_model = garch_fit(risk_factor_return, garch_type=garch_type)
         22
                forecasts = res.forecast(horizon=horizon, method=method)
                horizon_index = 'h.' + str(horizon)
         23
                forecast_mean = forecasts.mean.iloc[-1][horizon_index]
         24
         25
                forecast_variance = forecasts.variance.iloc[-1][horizon_index]
         26
                return (forecast mean, forecast variance)
         27
         28
            def ewma_estimation(risk_factor_return, decay_param=0.9, min_periods=100):
         29
                mu_ema = risk_factor_return.ewm(decay_param, min_periods=min_periods).mean()[-1]
         30
                sigma_ema = risk_factor_return.ewm(decay_param, min_periods=min_periods).std()[-1]
         31
                return mu_ema, sigma_ema
```

### **Principal Component Analysis**

Principal component analysis is based on the spectral decomposition of a correlation matrix. It is the simplest of many orthogonalisation techniques that transform a set of correlated variables into a set of uncorrelated variables [7].

The risk factor returns covariance matrix is given by  $V = T^{-1}X'X$ , where the columns of X are denoted  $x_1, x_2, \ldots, x_5$  (individual risk factor returns) and T is the number of observations on each return.

Then, a diagonal matrix (denoted by  $\Lambda$ ) of eigenvalues of V and the orthogonal matrix (denoted by W) of eigenvectors of V. In  $\Lambda$ , order the eigenvalues (and their corresponding eigenvectors in W) from largest to smallest.

The matrix of principal components of V is a  $T \times 5$  matrix P defined as P = XW. Each principal component is the linear combination of the columns of X, where the weights are chosen in such a way that the first principal component explains the most variation and the second component explains the greatest amount of remaining variation, etc.

The total variations in X is the sum of the eigenvalues of V, i.e.  $\lambda_1 + \lambda_2 + \ldots + \lambda_5$ . Hence, the proportion of this total variation that is explained by the mth principal component is

$$\frac{\lambda_m}{\lambda_1 + \lambda_2 + \ldots + \lambda_5}$$

```
In [16]:
           # Functions to run the Linear Regression on the PCA components of the risk factors to the factor betas for each stock
           def find_all_stock_benchmark_betas(stock_factor_dict, portfolio_stocks, benchmark=['ACWI']):
               all betas dict = {}
         6
               stock_benchmark_list = portfolio_stocks + benchmark
         8
               for stock in stock benchmark list:
         9
                   factors = list(stock_factor_dict[stock].columns[1:])
        10
                   factor_data = stock_factor_dict[stock][factors]
                   stock_data = stock_factor_dict[stock][stock]
        11
        12
                   all_betas_dict[stock] = find_factor_betas(factor_data, stock_data)
        13
               return all_betas_dict
        14
        15
           def pca(factor_data, variance_ratio=0.85):
               17
        18
        19
               principal_components = pipe.fit_transform(factor_data)
        20
               variance ratio explained = pipe.steps[1][1].explained variance ratio
        21
               factor_variance_df = pd.DataFrame(zip(factor_data.columns, variance_ratio_explained),
               columns=['Factors', 'Explained Variance'])
factor_variance_df.set_index(keys='Factors', inplace=True)
        22
        23
        24
               # Select relevant principal components
        25
               number_of_components = sum(variance_ratio_explained.cumsum() < variance_ratio)</pre>
               26
        27
        28
                                                 index=factor_data.index)
        29
               return principal_components_df.iloc[:, :number_of_components], pipe.steps[1][1].components_, factor_variance_df
        30
        31
           def find_factor_betas(factor_data, stock_data):
               # Get PCA components
        33
        34
               pc, eigen_vectors, eigen_values_df = pca(factor_data)
        35
        36
               # OLS Regression
               # Fit data and find betas using OLS regression
        37
        38
               reg_all = LinearRegression()
        39
               lr_model = reg_all.fit(pc, stock_data)
        40
        41
               # From Principal Components betas find the Factor Betas
        42
               pc_betas = lr_model.coef_
        43
               factor_betas = np.dot(eigen_vectors[:, :pc.shape[1]], pc_betas)
        44
               factor_betas_df = pd.DataFrame(zip(factor_data.columns, factor_betas),
                                            columns=['Factors', 'betas'])
        45
        46
               factor_betas_df.set_index(keys='Factors', inplace=True)
```

# 7. Copula

47

After getting the marginal univariate distributions of the 5 stocks and the predicted returns at the investment horizon. Copula was used to obtain the joint density function by taking their dependence structure into account. The Clayton copula from the Archimedeans family was selected to model the compound returns as it has negative tail dependence and stock returns' negative tail dependence tends to be greater during stresful periods.

A simulation algorithm proposed by Marshall and Olkin (1988) for the compound construction of copulas was used (see pg. 189 in [6]). Clayton Case

- Generate a random variate  $\gamma$  Gamma(1,1/ $\alpha$ ) (hence  $\gamma$  has Laplace transform  $\tau(s) = (1+s)^{-1/\alpha}$
- Independently of the previous step, generate  $U_1, U_2, ..., U_n$  independent Uniform(0,1) random variables
- For  $k=1,2,\ldots,n$  calculate  $X_k=F_k^{-1}(U_k^*)$  where

return factor\_betas\_df

$$U_k^* = \tau(-\frac{1}{\gamma}lnU_k)$$

```
In [17]:
             # Functions to find the copula and generate multivariate simulations from the selected copula for Monte Carlo calcula
             def get_copula_theta(risk_factor_returns, dim = PORTFOLIO_SIZE):
                 theta = []
          6
                 log_lik = []
          8
          9
                 # Clayton Copula
                 clay_cop = ClaytonCopula(dim=dim)
         10
         11
                     clay_cop.fit(risk_factor_returns)
         12
                 theta.append(clay_cop.params)
         13
                 log_lik.append(-clay_cop.log_lik(risk_factor_returns))
         14
         15
                 # Gumbel Copula
                 gum_cop = GumbelCopula(dim=dim)
         17
                   = gum_cop.fit(risk_factor_returns)
         18
                 theta.append(gum_cop.params)
         19
                 log_lik.append(-gum_cop.log_lik(risk_factor_returns))
         20
         21
                 # Frank Copula
         22
                 frank_cop = FrankCopula(dim=dim)
         23
                   = frank cop.fit(risk factor returns)
         24
                 theta.append(frank_cop.params)
         25
                 log_lik.append(-frank_cop.log_lik(risk_factor_returns))
         27
                 copula_df = pd.DataFrame(zip(theta, log_lik),
                                         columns=['theta', 'log likelihood'],
index=['Clayton', 'Gumbel', 'Frank'])
         28
         29
         30
                 copula_df.sort_values('log likelihood', inplace=True)
         31
                 return copula_df
         33
         34
             def copula_returns(number_simulations, theta, number_factors=5):
         35
                 copula_sims_list = []
         36
                 unif_rv_df = uniform.rvs(size=number_simulations * number_factors).reshape(number_simulations, number_factors)
         37
                 for i in range(number_simulations):
         38
                     gamma_rv = np.random.gamma(shape=1, scale=1. / theta)
         39
                     copula_sims_list.append([((1. + (-np.log(u) / gamma_rv)) ** (-1. / theta)) for u in unif_rv_df[i, :]])
         40
                 return copula sims list
         41
         42
             def generate_garch_sim_copula(risk_factor_return, garch_type='EGARCH', horizon=5, size=1000):
         43
         44
                 dist, param = best_fit_distribution(risk_factor_return)
                 if garch_type == 'EWMA':
         45
         46
                     mean, variance = ewma_estimation(risk_factor_return)
         47
                     return t.rvs(df=param[0],
                                 size=size,
         48
         49
                                 loc=mean.
         50
                                 scale=np.sqrt(variance))
         51
         52
                     mean, variance = garch forecast(risk factor return, garch type=garch type, horizon=horizon)
         53
                     return t.rvs(df=param[0],
                                 size=size,
         55
                                 loc=mean/10000.
         56
                                 scale=np.sqrt(variance)/10000)
         57
         58
         59
             def copula_factor_sims(risk_factor_returns, garch_type='EGARCH', number_simulations=1000):
                 number_simulations = number_simulations if number_simulations < risk_factor_returns.shape[0] else risk_factor_ret
         60
         61
                 copula_df = get_copula_theta(risk_factor_returns)
         62
                 theta = copula df.iloc[0, 0]
         63
                 copula_unif_rv = pd.DataFrame(copula_returns(number_simulations, theta))
         64
                 ppf = pd.DataFrame()
         65
                 for i in range(5):
         66
                     # Get fore-casted simulations
         67
                     risk_factor_simulations = generate_garch_sim_copula(risk_factor_returns.iloc[:, i],
         68
                                                                       garch_type=garch_type,
         69
                                                                       size=number_simulations)
         70
                     ppf[i] = inverted(risk_factor_simulations)(copula_unif_rv[i])
         71
                     if any(np.isinf(ppf.iloc[:, i])) or any(np.isnan(ppf.iloc[:, i])):
                         ppf[i] = np.array(risk_factor_returns.iloc[:number_simulations, i])
         72
         73
                 ppf.columns = ['Market', 'SMB', 'HML', 'Momentum', 'Sector
         74
                 return ppf
         75
         76
         77
             def inverted(data):
         78
                 sample = data
         79
                 sample_edf = ECDF(sample)
         80
                 slope_changes = sorted(set(sample))
         81
                 sample_edf_values_at_slope_changes = [sample_edf(item) for item in slope_changes]
                 inverted_edf = interp1d(sample_edf_values_at_slope_changes, slope_changes, fill_value="extrapolate")
         82
         83
                 return inverted edf
```

```
In [18]:
           # Function to get the stock returns from the factor returns
           def get stock from factor_returns(stock_factor_dict, garch_type='EGARCH', number_stocks=PORTFOLIO_SIZE, number_simula
              risk_factor_returns = list(stock_factor_dict.values())[0].iloc[:, 1:]
         6
              number_simulations = number_simulations if number_simulations < risk_factor_returns.shape[0] else risk_factor_ret</pre>
         8
         9
                  ppf = copula_factor_sims(risk_factor_returns, garch_type=garch_type, number_simulations=number_simulations)
        10
              except:
                  11
        12
                  # print(ValueError)
        13
                  ppf = risk_factor_returns.iloc[:number_simulations, :]
              betas_dict = find_all_stock_benchmark_betas(stock_factor_dict, list(stock_factor_dict.keys())[:number_stocks])
        14
        15
              stock_returns_dict = {}
              for stock, betas in betas_dict.items():
        17
                  stock_returns_dict[stock] = np.dot(ppf, betas).flatten()
        18
                  stock_returns_dict[stock] = np.dot(ppf, betas).flatten()
        19
              stock_returns_df = pd.DataFrame(stock_returns_dict)
        20
              return stock returns df
```

# 8. Optimisation

# **Optimisation Algorithm**

- · Generate some random weights, they can be negative to represent short selling.
- Using Monte Carlo, simulate the risk factor returns from the Copula Multivariate distribution and generate the corresponding stock returns.
- Multiply the weights with the generated stock returns to generate the portfolio returns and get the portfolio returns distribution.
- Subtract the simulated forecasted benchmark returns from the generated portfolio returns to obtain active returns distribution.
- From the active returns distribution, get the negative 1% tail and find its mean to get the Expected shortfall.
- Repeat this procedure for each set of weights and select the weight which provides the maximum expected active return over the benchmark for which the expected shortfall falls below the 1% portfolio cutoff.

```
In [19]:
         # Function to optimize over the weights to maximum active returns over the benchmark for 1% Expected shortfall
            5
             def optimize(stock_factor_dict, garch_type='EGARCH', number_simulations=1000):
          6
                # generate a sets of weight
                random_weight_df = pd.DataFrame(np.random.uniform(0, 2, 5 * number_simulations).reshape(number_simulations, 5))
          8
                final_random_weight_df = random_weight_df.divide(np.array(random_weight_df.sum(axis=1)).reshape(-1, 1), axis=1)
          9
         10
                for row_index in range(np.random.randint(final_random_weight_df.shape[0])):
                    indx = list(np.random.choice([0, 1, 2, 3, 4], size=4, replace=False))
         11
         12
                    final_random_weight_df.iloc[row_index, indx[0]] = final_random_weight_df.iloc[row_index, indx[0]] + 0.2
         13
                    final_random_weight_df.iloc[row_index, indx[1]] = final_random_weight_df.iloc[row_index, indx[1]] - 0.2
         14
                    final_random_weight_df.iloc[row_index, indx[2]] = final_random_weight_df.iloc[row_index, indx[2]] + 0.2
         15
                    final_random_weight_df.iloc[row_index, indx[3]] = final_random_weight_df.iloc[row_index, indx[3]] - 0.2
         17
                tail_loss_limit = -(1 + 0.01) ** (1 / 420) - 1 # 1% ES annualized to be converted to minutely
         18
                max_return = 0
         19
                record = 0
         20
         21
                # calculate porfolio's expected return of porfolio under different weight
         22
                stock_benchmark_return = get_stock_from_factor_returns(stock_factor_dict, garch_type=garch_type, number_simulation
         23
                if garch_type == 'EWMA':
         24
                    stock_return = stock_benchmark_return.iloc[:, :-1]
         25
                    benchmark_return = stock_benchmark_return.iloc[:, -1]
         26
                else:
         27
                    stock_return = stock_benchmark_return.iloc[:, :-1] * 10000
         28
                    benchmark_return = stock_benchmark_return.iloc[:, -1] * 10000
         29
                portfolio_return = np.dot(final_random_weight_df, stock_return.T)
         30
                active_return = np.array([portfolio_return[i, :]-np.array(benchmark_return) for i in range(len(benchmark_return))
         31
                mean_return = active_return.mean(axis=1)
         33
                # calculate cvar
         34
                active_return.sort(axis=1)
         35
                one_percent_index = int(active_return.shape[1]/100)
         36
                value_tail = active_return[:, :one_percent_index]
         37
                expected_shortfall = np.mean(value_tail, axis=1)
         38
         39
                # find out the maximum return rate portfolio under constraint
         40
                for i in range(len(expected_shortfall)):
         41
                    if expected_shortfall[i] < tail_loss_limit:</pre>
         42
                        continue
         43
                    else.
         44
                        if mean_return[i] < max_return:</pre>
         45
                            continue
         46
                        else:
         47
                           max_return = mean_return[i]
         48
                            record = i
         49
         50
                # print(max return)
         51
                weight_df = pd.DataFrame(zip(list(stock_return.columns), final_random_weight_df.iloc[record, :]),
                                        columns=['stocks', 'weights'])
         52
         53
                weight_df.set_index(keys='stocks', inplace=True)
         54
                return weight_df.T, expected_shortfall[record]
```

# 9. Backtesting

```
In [20]:
          # Function for Backtesting the E-GARCH, GARCH and EWMA
          4
             def backtesting():
                 # Get the stock prices
                all_stock_price = get_all_tickers(tot_tickers)
          6
          7
                portfolio_stocks = find_least_corr_stocks(all_stock_price)
          8
                portfolio_stock_price = all_stock_price[portfolio_stocks]
          9
                 stock_factor_dict = get_stock_factor_df(portfolio_stocks)
         10
                 # General variables for bl
         11
         12
                 initial fund = 1000000 # Initial investment, 1million dollars
         13
                 trading_interval = 1 # in minute
         14
         15
                 # Starter variables for EGARCH
                num_shares_egarch = dict((stock, []) for stock in portfolio_stocks)
         16
         17
                 remaining_fund_egarch = []
         18
                 port_valuelist_egarch = []
         19
                 tot_assets_egarch = []
         20
                expected shortfall egarch = []
         21
                 profit_per_trade_egarch = []
         22
                 # Starter variables for GARCH
         23
         24
                 num_shares_garch = dict((stock, []) for stock in portfolio_stocks)
         25
                 remaining_fund_garch = []
         26
                 port_valuelist_garch = []
         27
                 tot_assets_garch = []
         28
                 expected_shortfall_garch = []
         29
                 profit_per_trade_garch = []
         30
         31
                 # Starter variables for EWMA
                num_shares_ewma = dict((stock, []) for stock in portfolio_stocks)
         32
                remaining_fund_ewma = []
         33
                 port_valuelist_ewma = []
         34
         35
                 tot_assets_ewma = []
         36
                 expected_shortfall_ewma = []
         37
                profit_per_trade_ewma = []
         38
         39
                 # Trading Algorithm
         40
                k = 1
         41
                 while k <= 13:
         42
                    start = time.time()
         43
         44
                    # Trading ended
         45
                    if k == 13:
         46
                        print('###################"--Trading Terminated---##############")
         47
                        print('----EGARCH Estimation Gives----')
         48
         49
                        print('The Final Asset Value is ' + str(np.round(port_valuelist_egarch[-1] + remaining_fund_egarch[-1],2)
                        print('Profit/Loss = ' + str(port_valuelist_egarch[-1] + remaining_fund_egarch[-1] - initial_fund) +
         50
         51
         52
                        print('----GARCH Estimation Gives----')
                        print('The Final Asset Value is ' + str(np.round(port_valuelist_garch[-1] + remaining_fund_garch[-1],2))
         53
                        print('Profit/Loss = ' + str(port_valuelist_garch[-1] + remaining_fund_garch[-1] - initial_fund) +
         54
         55
                        # EWMA
         56
                        print('----EWMA Estimation Gives----')
                        print('The Final Asset Value is ' + str(np.round(port_valuelist_ewma[-1] + remaining_fund_ewma[-1],2)) +
         57
         58
                        print('Profit/Loss = ' + str(port_valuelist_ewma[-1] + remaining_fund_ewma[-1] - initial_fund) + ' USD')
         59
                    print('##############Trade', k, 'starts###########")
         60
         61
         62
         63
                    #####BACKTESTING USE THIS########
         64
                    # Get the minutely price data (start)-----
         65
                    price_df = portfolio_stock_price.iloc[100 * (k - 1):100 * k, :] # rolling to simulate live data
                    # Get the minutely price data (end)------
         66
                    #####BACKTESTING USE THIS########
         67
         68
         69
                    # Compute the log returns (start)-----
         70
                    # compound_returns = (1 + find_returns(price_df)).cumprod()
         71
                    # Compute the Log returns (end)----
         72
         73
                    # The weights supposed to be generated by optimisation function, but I use random weights here.
         74
                    weights egarch, es egarch = optimize(stock factor dict)
         75
                    weights_garch, es_garch = optimize(stock_factor_dict, garch_type='GARCH')
         76
                    weights_ewma, es_ewma = optimize(stock_factor_dict, garch_type='EWMA')
         77
         78
                    # Expected Shortfalls
         79
                    expected_shortfall_egarch.append(es_egarch)
         80
                    expected_shortfall_garch.append(es_garch)
                    expected_shortfall_ewma.append(es_ewma)
         81
         82
         83
                    # Calculate the current portfolio value(start)-----
         84
         85
                    if k == 1:
         86
                        # EGARCH
         87
                        remaining_fund_egarch.append(0)
```

```
88
                 tot_assets_egarch.append(initial_fund + remaining_fund_egarch[-1])
 89
                 # GARCH
90
                 remaining_fund_garch.append(0)
 91
                 tot_assets_garch.append(initial_fund + remaining_fund_garch[-1])
92
                 # FWMA
93
                 remaining_fund_ewma.append(0)
                 tot_assets_ewma.append(initial_fund + remaining_fund_ewma[-1])
94
                 print('The initial investment amount is: ' + str(np.round(initial_fund,2)) + ' USD')
95
96
             else:
97
                 # EGARCH
98
                 port_value_egarch = 0 # reset the portfolio value to zero
99
                 for stock in portfolio_stocks:
                     # Re-evaluate portfolio value after receiving new price
100
101
                     port_value_egarch += num_shares_egarch[stock][-1] * stock_price_data.iloc[-1, portfolio_stocks.index(
102
                 # Re-evalute total assets (previous remaining fund + updated portfolio value)
                 tot_assets_egarch.append(remaining_fund_egarch[-1] + port_value_egarch)
103
104
                 profit_per_trade_egarch.append(tot_assets_egarch[-1] - tot_assets_egarch[-2])
105
106
                 port_value_garch = 0 # reset the portfolio value to zero
107
                 for stock in portfolio_stocks:
                     # Re-evaluate portfolio value after receiving new price
109
110
                     port_value_garch += num_shares_garch[stock][-1] * stock_price_data.iloc[-1, portfolio_stocks.index(st
111
                 # Re-evalute total assets (previous remaining fund + updated portfolio value)
                 tot_assets_garch.append(remaining_fund_garch[-1] + port_value_garch)
112
113
                 profit_per_trade_garch.append(tot_assets_garch[-1] - tot_assets_garch[-2])
114
115
116
                 port value ewma = 0 # reset the portfolio value to zero
117
                 for stock in portfolio_stocks:
118
                     # Re-evaluate portfolio value after receiving new price
                     port_value_ewma += num_shares_ewma[stock][-1] * stock_price_data.iloc[-1, portfolio_stocks.index(stock)]
119
                 # Re-evalute total assets (previous remaining fund + updated portfolio value)
120
121
                 tot_assets_ewma.append(remaining_fund_ewma[-1] + port_value_ewma)
122
                 profit_per_trade_ewma.append(tot_assets_ewma[-1] - tot_assets_ewma[-2])
123
124
125
126
             # Calculate the current portfolio value(end)-----
127
             # Reset portfolio value before trading.
128
             # EGARCH
129
             port_value_egarch = 0
130
             for stock in portfolio_stocks:
                 num_shares_egarch[stock].append(int(float(weights_egarch[stock]) * tot_assets_egarch[-1] / stock_price_da
131
132
                 port_value_egarch += num_shares_egarch[stock][-1] * stock_price_data.iloc[-1, portfolio_stocks.index(stock)]
133
             port_valuelist_egarch.append(port_value_egarch)
134
             remaining_fund_egarch.append(tot_assets_egarch[-1] - port_valuelist_egarch[-1])
             print('----EGARCH Estimation Gives----')
135
             print('The Current Asset Value is ' + str(np.round(port_valuelist_egarch[-1], 2)) + ' USD')
136
137
             for stock in portfolio_stocks:
138
                 print('The portfolio currently holds ' + str(np.round(num_shares_egarch[stock][-1], 2)) + ' shares of '
139
             # GARCH
140
141
             port_value_garch = 0
             for stock in portfolio_stocks:
142
                 num_shares_garch[stock].append(int(float(weights_garch[stock]) * tot_assets_garch[-1] /stock_price_data.i
143
144
                 port_value_garch += num_shares_garch[stock][-1] * stock_price_data.iloc[-1, portfolio_stocks.index(stock)
145
             port_valuelist_garch.append(port_value_garch)
146
             remaining_fund_garch.append(tot_assets_garch[-1] - port_valuelist_garch[-1])
147
             print('----GARCH Estimation Gives----')
             print('The Current Asset Value is ' + str(np.round(port_valuelist_garch[-1], 2)) + ' USD')
148
149
             for stock in portfolio_stocks:
                 print('The portfolio currently holds ' + str(np.round(num_shares_garch[stock][-1], 2)) + ' shares of ' +
150
151
152
             # EWMA
153
             port value ewma = 0
154
             for stock in portfolio_stocks:
155
                 num_shares_ewma[stock].append(int(float(weights_ewma[stock]) * tot_assets_ewma[-1] / stock_price_data.ile
156
                 port_value_ewma += num_shares_ewma[stock][-1] * stock_price_data.iloc[-1, portfolio_stocks.index(stock)]
157
             port_valuelist_ewma.append(port_value_ewma)
158
             remaining_fund_ewma.append(tot_assets_ewma[-1] - port_valuelist_ewma[-1])
159
             print('----EWMA Estimation Gives----')
             print('The Current Asset Value is ' + str(np.round(port_valuelist_ewma[-1], 2)) + ' USD')
160
161
             for stock in portfolio_stocks:
162
                 print('The portfolio currently holds ' + str(np.round(num_shares_ewma[stock][-1], 2)) + ' shares of ' + s
163
164
165
             k += 1
166
167
             # Pause after each trade to gather data
168
             end = time.time()
             print('Analysis runtime: ' + str(np.round((end - start),2)) + ' s')
169
             time.sleep(trading_interval*60- (end - start))
170
```



```
In [21]:
          # Function for Trading the E-GARCH, GARCH and EWMA
          # Get the stock prices
             all_stock_price = get_all_tickers(tot_tickers)
          6
             portfolio_stocks = find_least_corr_stocks(all_stock_price)
          8
             portfolio_stock_price = all_stock_price[portfolio_stocks]
         10 # General variables for bl
         11 initial fund = 1000000 # Initial investment, 1million dollars
             trading interval = 5 # in minute
         12
         13
         14 # Starter variables for EGARCH
         num_shares_egarch = dict((stock, []) for stock in portfolio_stocks)
         16 remaining_fund_egarch = []
         17 port_valuelist_egarch = []
         18 tot_assets_egarch = []
         19 | expected_shortfall_egarch = []
         20 profit_per_trade_egarch = []
         21
         22 # Starter variables for GARCH
         23 num_shares_garch = dict((stock, []) for stock in portfolio_stocks)
         24 remaining_fund_garch = []
         25 port_valuelist_garch = []
         26 tot_assets_garch = []
         27 expected_shortfall_garch = []
         28 profit_per_trade_garch = []
         29
         30 # Starter variables for EWMA
         num_shares_ewma = dict((stock, []) for stock in portfolio_stocks)
         32 remaining_fund_ewma = []
         33 port_valuelist_ewma = []
         34 tot_assets_ewma = []
         35 expected_shortfall_ewma = []
         36 profit_per_trade_ewma = []
         37
         38 # Trading Algorithm
         39 k = 1
         40 while k <= 13:
         41
                start = time.time()
         42
                 # Trading ended
         43
         44
                 if k == 13:
         45
                    print('#################---Trading Terminated---###############")
         46
         47
                    print('----EGARCH Estimation Gives----')
                    print('The Final Asset Value is ' + str(np.round(port_valuelist_egarch[-1] + remaining_fund_egarch[-1],2)) +
         48
         49
                    print('Profit/Loss = ' + str(port_valuelist_egarch[-1] + remaining_fund_egarch[-1] - initial_fund) + ' USD')
         50
                    # GARCH
         51
                    print('----GARCH Estimation Gives----')
                    print('The Final Asset Value is ' + str(np.round(port valuelist garch[-1] + remaining fund garch[-1],2)) + '
         52
                    print('Profit/Loss = ' + str(port_valuelist_garch[-1] + remaining_fund_garch[-1] - initial_fund) + ' USD')
         53
         54
         55
                    print('----EWMA Estimation Gives----')
                    print('The Final Asset Value is ' + str(np.round(port_valuelist_ewma[-1] + remaining_fund_ewma[-1],2)) + ' US
         56
                    print('Profit/Loss = ' + str(port_valuelist_ewma[-1] + remaining_fund_ewma[-1] - initial_fund) +
         57
         58
                 print('#################Trade', k, 'starts############")
         59
         60
         61
         62
                 #####BACKTESTING USE THIS########
         63
                 # Get the minutely price data (start)-----
                 # price_df = portfolio_stock_price.iloc[100 * (k - 1):100 * k, :] # rolling to simulate live data
         64
         65
                 stock_price_data = get_all_tickers(portfolio_stocks)
                 stock_factor_dict = get_stock_factor_df(portfolio_stocks)
         66
         67
                 # Get the minutely price data (end)------
         68
         69
         70
                 # The weights supposed to be generated by optimisation function, but I use random weights here.
         71
                 weights_egarch, es_egarch = optimize(stock_factor_dict)
         72
                 weights_garch, es_garch = optimize(stock_factor_dict, garch_type='GARCH')
         73
                 weights_ewma, es_ewma = optimize(stock_factor_dict, garch_type='EWMA')
         74
                 # Expected Shortfalls
         75
         76
                 expected_shortfall_egarch.append(es_egarch)
         77
                 expected_shortfall_garch.append(es_garch)
         78
                 expected_shortfall_ewma.append(es_ewma)
         79
         80
                 # Calculate the current portfolio value(start)------
         81
         82
                 if k == 1:
                    # EGARCH
         83
         84
                    remaining_fund_egarch.append(0)
                    tot_assets_egarch.append(initial_fund + remaining_fund_egarch[-1])
         85
         86
                    # GARCH
         87
                    remaining_fund_garch.append(0)
```

```
88
                   tot_assets_garch.append(initial_fund + remaining_fund_garch[-1])
 89
 90
                   remaining_fund_ewma.append(0)
                   tot_assets_ewma.append(initial_fund + remaining_fund_ewma[-1])
 91
                   print('The initial investment amount is: ' + str(np.round(initial_fund,2)) + ' USD')
 92
             else:
 93
 94
                   port_value_egarch = 0 # reset the portfolio value to zero
 95
 96
                   for stock in portfolio_stocks:
 97
                          # Re-evaluate portfolio value after receiving new price
                   port_value_egarch += num_shares_egarch[stock][-1] * stock_price_data.iloc[-1, portfolio_stocks.index(stoc
# Re-evalute total assets (previous remaining fund + updated portfolio value)
 98
 99
100
                   tot_assets_egarch.append(remaining_fund_egarch[-1] + port_value_egarch)
101
                   profit_per_trade_egarch.append(tot_assets_egarch[-1] - tot_assets_egarch[-2])
102
                   # GARCH
103
                   port_value_garch = 0 # reset the portfolio value to zero
104
105
                    for stock in portfolio_stocks:
                          # Re-evaluate portfolio value after receiving new price
106
                          port_value_garch += num_shares_garch[stock][-1] * stock_price_data.iloc[-1, portfolio_stocks.index(stock)
107
                    # Re-evalute total assets (previous remaining fund + updated portfolio value)
                   tot_assets_garch.append(remaining_fund_garch[-1] + port_value_garch)
109
110
                   profit_per_trade_garch.append(tot_assets_garch[-1] - tot_assets_garch[-2])
111
112
                   # EWMA
113
                   port_value_ewma = 0 # reset the portfolio value to zero
114
                   for stock in portfolio_stocks:
115
                          # Re-evaluate portfolio value after receiving new price
                         port_value_ewma += num_shares_ewma[stock][-1] * stock_price_data.iloc[-1, portfolio_stocks.index(stock)]
116
117
                   # Re-evalute total assets (previous remaining fund + updated portfolio value)
118
                   tot_assets_ewma.append(remaining_fund_ewma[-1] + port_value_ewma)
119
                   profit_per_trade_ewma.append(tot_assets_ewma[-1] - tot_assets_ewma[-2])
120
121
122
123
             # Calculate the current portfolio value(end)-----
             # Reset portfolio value before trading.
124
125
             # EGARCH
126
             port_value_egarch = 0
127
             for stock in portfolio_stocks:
128
                    129
                    port_value_egarch += num_shares_egarch[stock][-1] * stock_price_data.iloc[-1, portfolio_stocks.index(stock)]
130
             port_valuelist_egarch.append(port_value_egarch)
131
             remaining\_fund\_egarch.append(tot\_assets\_egarch[-1] - port\_valuelist\_egarch[-1]) \\
             print('----EGARCH Estimation Gives----')
132
             print('The Current Asset Value is ' + str(np.round(port_valuelist_egarch[-1], 2)) + ' USD')
133
134
             for stock in portfolio_stocks:
                    print('The portfolio currently holds ' + str(np.round(num_shares_egarch[stock][-1], 2)) + ' shares of ' + ste
135
136
137
             # GARCH
138
             port_value_garch = 0
139
             for stock in portfolio_stocks:
                   num\_shares\_garch[stock]. append(int(float(weights\_garch[stock]) * tot\_assets\_garch[-1] / stock\_price\_data.ilock]) * tot\_assets\_garch[-1] / stock\_price\_data.ilock] * tot\_assets\_garch[-1] / stock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilock\_price\_data.ilo
140
                   port_value_garch += num_shares_garch[stock][-1] * stock_price_data.iloc[-1, portfolio_stocks.index(stock)]
141
142
             port_valuelist_garch.append(port_value_garch)
143
             remaining\_fund\_garch.append(tot\_assets\_garch[-1] - port\_valuelist\_garch[-1])
144
             print('----GARCH Estimation Gives----')
145
             print('The Current Asset Value is ' + str(np.round(port_valuelist_garch[-1], 2)) + ' USD')
146
             for stock in portfolio_stocks:
147
                   print('The portfolio currently holds ' + str(np.round(num_shares_garch[stock][-1], 2)) + ' shares of ' + stock
148
149
             # EWMA
150
             port value ewma = 0
151
             for stock in portfolio_stocks:
                    num_shares_ewma[stock].append(int(float(weights_ewma[stock]) * tot_assets_ewma[-1] / stock_price_data.iloc[-1
152
                   port_value_ewma += num_shares_ewma[stock][-1] * stock_price_data.iloc[-1, portfolio_stocks.index(stock)]
153
154
             port_valuelist_ewma.append(port_value_ewma)
155
             remaining\_fund\_ewma.append(tot\_assets\_ewma[-1] - port\_valuelist\_ewma[-1])
156
             print('----EWMA Estimation Gives----')
             print('The Current Asset Value is ' + str(np.round(port_valuelist_ewma[-1], 2)) + ' USD')
157
158
             for stock in portfolio_stocks:
159
                   print('The portfolio currently holds ' + str(np.round(num_shares_ewma[stock][-1], 2)) + ' shares of ' + stock
160
161
162
             k += 1
163
             # Pause after each trade to gather data
164
165
             end = time.time()
             print('Analysis runtime: ' + str(np.round((end - start),2)) + ' s')
166
167
             time.sleep(trading_interval*60- (end - start))
```

```
The portfolio currently holds 12 shares of COP
The portfolio currently holds 23315 shares of CPG
The portfolio currently holds 173691 shares of NAT
The portfolio currently holds 37488 shares of PBR
----GARCH Estimation Gives---
The Current Asset Value is 999960.49 USD
The portfolio currently holds 804 shares of RDS-A
The portfolio currently holds 1974 shares of COP
The portfolio currently holds 23833 shares of CPG
The portfolio currently holds 148034 shares of NAT
The portfolio currently holds 18962 shares of PBR
----EWMA Estimation Gives---
The Current Asset Value is 1000010.51 USD
The portfolio currently holds -2011 shares of RDS-A
The portfolio currently holds -2621 shares of COP
The portfolio currently holds 46300 shares of CPG
The portfolio currently holds 169683 shares of NAT
The portfolio currently holds 37269 shares of PBR
Analysis runtime: 65.1 s
----EGARCH Estimation Gives--
The Current Asset Value is 998684.15 USD
The portfolio currently holds -3484 shares of RDS-A
The portfolio currently holds 70 shares of COP
The portfolio currently holds 45690 shares of CPG
The portfolio currently holds 215901 shares of NAT
The portfolio currently holds 20855 shares of PBR
----GARCH Estimation Gives---
The Current Asset Value is 999168.67 USD
The portfolio currently holds -2716 shares of RDS-A
The portfolio currently holds -2433 shares of COP
The portfolio currently holds 111633 shares of CPG
The portfolio currently holds 235749 shares of NAT
The portfolio currently holds 8798 shares of PBR
----EWMA Estimation Gives---
The Current Asset Value is 998407.08 USD
The portfolio currently holds 1278 shares of RDS-A
The portfolio currently holds 594 shares of COP
The portfolio currently holds 35891 shares of CPG
The portfolio currently holds 210261 shares of NAT
The portfolio currently holds 5809 shares of PBR
Analysis runtime: 68.18 s
----EGARCH Estimation Gives--
The Current Asset Value is 999361.44 USD
The portfolio currently holds -538 shares of RDS-A
The portfolio currently holds -2823 shares of COP
The portfolio currently holds 83772 shares of CPG
The portfolio currently holds 179468 shares of NAT
The portfolio currently holds 22199 shares of PBR
----GARCH Estimation Gives---
The Current Asset Value is 999883.47 USD
The portfolio currently holds -884 shares of RDS-A
The portfolio currently holds -3203 shares of COP
The portfolio currently holds 69215 shares of CPG
The portfolio currently holds 170835 shares of NAT
The portfolio currently holds 30301 shares of PBR
 ---EWMA Estimation Gives---
The Current Asset Value is 998775.56 USD
The portfolio currently holds -1680 shares of RDS-A
The portfolio currently holds -2531 shares of COP
The portfolio currently holds 150172 shares of CPG
The portfolio currently holds 141138 shares of NAT
The portfolio currently holds 18526 shares of PBR
Analysis runtime: 78.66 s
----EGARCH Estimation Gives----
The Current Asset Value is 1002379.99 USD
The portfolio currently holds -3331 shares of RDS-A
The portfolio currently holds -3045 shares of COP
The portfolio currently holds 87338 shares of CPG
The portfolio currently holds 184356 shares of NAT
The portfolio currently holds 30768 shares of PBR
----GARCH Estimation Gives---
The Current Asset Value is 1002758.83 USD
The portfolio currently holds 1252 shares of RDS-A
The portfolio currently holds -2618 shares of COP
The portfolio currently holds 111598 shares of CPG
The portfolio currently holds 212885 shares of NAT
The portfolio currently holds 1122 shares of PBR
----EWMA Estimation Gives----
The Current Asset Value is 1002047.51 USD
The portfolio currently holds -3799 shares of RDS-A
The portfolio currently holds -2150 shares of COP
The portfolio currently holds 63707 shares of CPG
The portfolio currently holds 233174 shares of NAT
The portfolio currently holds 22859 shares of PBR
```

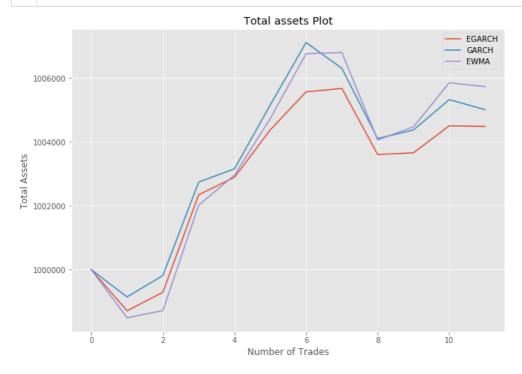
```
Analysis runtime: 68.9 s
----EGARCH Estimation Gives--
The Current Asset Value is 1002925.66 USD
The portfolio currently holds -2469 shares of RDS-A
The portfolio currently holds -2947 shares of COP
The portfolio currently holds 134028 shares of CPG
The portfolio currently holds 196996 shares of NAT
The portfolio currently holds 13779 shares of PBR
----GARCH Estimation Gives---
The Current Asset Value is 1003193.04 USD
The portfolio currently holds -3460 shares of RDS-A
The portfolio currently holds -2774 shares of COP
The portfolio currently holds 146920 shares of CPG
The portfolio currently holds 135728 shares of NAT
The portfolio currently holds 27716 shares of PBR
----EWMA Estimation Gives----
The Current Asset Value is 1003019.16 USD
The portfolio currently holds -4023 shares of RDS-A
The portfolio currently holds -2622 shares of COP
The portfolio currently holds 157153 shares of CPG
The portfolio currently holds 173183 shares of NAT
The portfolio currently holds 18013 shares of PBR
Analysis runtime: 64.78 s
----EGARCH Estimation Gives--
The Current Asset Value is 1004452.07 USD
The portfolio currently holds -2589 shares of RDS-A
The portfolio currently holds -641 shares of COP
The portfolio currently holds 156829 shares of CPG
The portfolio currently holds 162848 shares of NAT
The portfolio currently holds 7485 shares of PBR
----GARCH Estimation Gives---
The Current Asset Value is 1005209.54 USD
The portfolio currently holds -2941 shares of RDS-A
The portfolio currently holds -3215 shares of COP
The portfolio currently holds 108255 shares of CPG
The portfolio currently holds 223670 shares of NAT
The portfolio currently holds 16289 shares of PBR
----EWMA Estimation Gives----
The Current Asset Value is 1004761.82 USD
The portfolio currently holds -1704 shares of RDS-A
The portfolio currently holds -66 shares of COP
The portfolio currently holds 98462 shares of CPG
The portfolio currently holds 150963 shares of NAT
The portfolio currently holds 18249 shares of PBR
Analysis runtime: 66.94 s
----EGARCH Estimation Gives---
The Current Asset Value is 1005564.47 USD
The portfolio currently holds -373 shares of RDS-A
The portfolio currently holds -1025 shares of COP
The portfolio currently holds 52706 shares of CPG
The portfolio currently holds 195800 shares of NAT
The portfolio currently holds 17616 shares of PBR
----GARCH Estimation Gives----
The Current Asset Value is 1007129.17 USD
The portfolio currently holds -3815 shares of RDS-A
The portfolio currently holds -2706 shares of COP
The portfolio currently holds 209535 shares of CPG
The portfolio currently holds 187224 shares of NAT
The portfolio currently holds 2513 shares of PBR
----EWMA Estimation Gives----
The Current Asset Value is 1006809.68 USD
The portfolio currently holds -2622 shares of RDS-A
The portfolio currently holds -1715 shares of COP
The portfolio currently holds 55401 shares of CPG
The portfolio currently holds 198339 shares of NAT
The portfolio currently holds 26976 shares of PBR
Analysis runtime: 80.53 s
---EGARCH Estimation Gives--
The Current Asset Value is 1005686.36 USD
The portfolio currently holds 200 shares of RDS-A
The portfolio currently holds -1128 shares of COP
The portfolio currently holds 122940 shares of CPG
The portfolio currently holds 224273 shares of NAT
The portfolio currently holds -6477 shares of PBR
----GARCH Estimation Gives----
The Current Asset Value is 1006305.82 USD
The portfolio currently holds 278 shares of RDS-A
The portfolio currently holds -2868 shares of COP
The portfolio currently holds 18896 shares of CPG
The portfolio currently holds 264461 shares of NAT
The portfolio currently holds 14750 shares of PBR
----EWMA Estimation Gives----
The Current Asset Value is 1006829.82 USD
```

```
The portfolio currently holds -1499 shares of RDS-A
The portfolio currently holds -3110 shares of COP
The portfolio currently holds 142934 shares of CPG
The portfolio currently holds 212455 shares of NAT
The portfolio currently holds 5606 shares of PBR
Analysis runtime: 82.19 s
----EGARCH Estimation Gives---
The Current Asset Value is 1003615.0 USD
The portfolio currently holds 130 shares of RDS-A
The portfolio currently holds -2393 shares of COP
The portfolio currently holds 215962 shares of CPG
The portfolio currently holds 164597 shares of NAT
The portfolio currently holds -8484 shares of PBR
---GARCH Estimation Gives---
The Current Asset Value is 1004148.48 USD
The portfolio currently holds -2317 shares of RDS-A
The portfolio currently holds -2922 shares of COP
The portfolio currently holds 154564 shares of CPG
The portfolio currently holds 209384 shares of NAT
The portfolio currently holds 5712 shares of PBR
---EWMA Estimation Gives-
The Current Asset Value is 1004110.81 USD
The portfolio currently holds -1620 shares of RDS-A
The portfolio currently holds -2780 shares of COP
The portfolio currently holds 113546 shares of CPG
The portfolio currently holds 195752 shares of NAT
The portfolio currently holds 15230 shares of PBR
Analysis runtime: 73.6 s
----EGARCH Estimation Gives---
The Current Asset Value is 1003584.26 USD
The portfolio currently holds 252 shares of RDS-A
The portfolio currently holds 2364 shares of COP
The portfolio currently holds 3332 shares of CPG
The portfolio currently holds 189959 shares of NAT
The portfolio currently holds 14312 shares of PBR
----GARCH Estimation Gives---
The Current Asset Value is 1004442.24 USD
The portfolio currently holds -2017 shares of RDS-A
The portfolio currently holds -1554 shares of COP
The portfolio currently holds 93755 shares of CPG
The portfolio currently holds 201978 shares of NAT
The portfolio currently holds 14680 shares of PBR
----EWMA Estimation Gives----
The Current Asset Value is 1004458.07 USD
The portfolio currently holds -3617 shares of RDS-A
The portfolio currently holds 3469 shares of COP
The portfolio currently holds 25680 shares of CPG
The portfolio currently holds 285727 shares of NAT
The portfolio currently holds -4042 shares of PBR
Analysis runtime: 73.26 s
----EGARCH Estimation Gives--
The Current Asset Value is 1004557.64 USD
The portfolio currently holds -3843 shares of RDS-A
The portfolio currently holds -1860 shares of COP
The portfolio currently holds 86575 shares of CPG
The portfolio currently holds 197445 shares of NAT
The portfolio currently holds 24799 shares of PBR
----GARCH Estimation Gives--
The Current Asset Value is 1005399.56 USD
The portfolio currently holds -1333 shares of RDS-A
The portfolio currently holds -74 shares of COP
The portfolio currently holds 18537 shares of CPG
The portfolio currently holds 200724 shares of NAT
The portfolio currently holds 23739 shares of PBR
----EWMA Estimation Gives---
The Current Asset Value is 1005876.81 USD
The portfolio currently holds -3312 shares of RDS-A
The portfolio currently holds -3138 shares of COP
The portfolio currently holds 123722 shares of CPG
The portfolio currently holds 205899 shares of NAT
The portfolio currently holds 17845 shares of PBR
Analysis runtime: 66.62 s
----EGARCH Estimation Gives---
The Current Asset Value is 1004443.68 USD
The portfolio currently holds 1205 shares of RDS-A
The portfolio currently holds 5162 shares of COP
The portfolio currently holds 168353 shares of CPG
The portfolio currently holds -2353 shares of NAT
The portfolio currently holds 6561 shares of PBR
----GARCH Estimation Gives---
The Current Asset Value is 1004999.65 USD
The portfolio currently holds 10714 shares of RDS-A
The portfolio currently holds 7011 shares of COP
```

```
The portfolio currently holds 116901 shares of CPG
The portfolio currently holds -48473 shares of NAT
The portfolio currently holds -11072 shares of PBR
----EWMA Estimation Gives--
The Current Asset Value is 1005715.04 USD
The portfolio currently holds 12258 shares of RDS-A
The portfolio currently holds 5490 shares of COP
The portfolio currently holds 132119 shares of CPG
The portfolio currently holds -58831 shares of NAT
The portfolio currently holds -11218 shares of PBR \,
Analysis runtime: 70.61 s
----EGARCH Estimation Gives----
The Final Asset Value is 1004482.78 USD
Profit/Loss = 4482.780499999761 USD
----GARCH Estimation Gives----
The Final Asset Value is 1005005.04 USD
Profit/Loss = 5005.03619999974 USD
----EWMA Estimation Gives---
The Final Asset Value is 1005725.31 USD
Profit/Loss = 5725.311399999773 USD
```

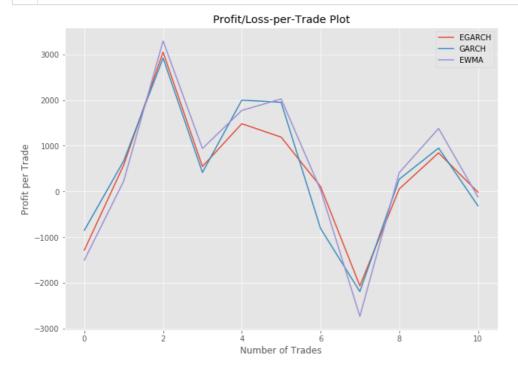
### Results

```
In [22]:
            1 # Plotting total assets for each Method
               tot_assets_egarch_series = pd.Series(tot_assets_egarch)
               tot_assets_garch_series = pd.Series(tot_assets_garch)
               tot_assets_ewma_series = pd.Series(tot_assets_ewma)
                fig = plt.figure(figsize=(10, 7))
               ax = fig.add_axes([0.1, 0.1, 0.8, 0.8]) # main axes
                _ = ax.plot(np.arange(len(tot_assets_egarch_series)), tot_assets_egarch_series.values, label='EGARCH')
               = ax.plot(np.arange(len(tot_assets_garch_series)), tot_assets_garch_series.values, label='GARCH')
= ax.plot(np.arange(len(tot_assets_garch_series)), tot_assets_ewma_series.values, label='EWMA')
            8
               _ = ax.set_xlabel("Number of Trades")
               _ = ax.set_ylabel("Total Assets")
           11
               _ = ax.set_title("Total assets Plot")
           12
               _ = ax.legend()
```



~

```
In [23]:
               # Plotting the Profit/Loss values per trade for each method
               profit_per_trade_egarch_series = pd.Series(profit_per_trade_egarch)
               profit_per_trade_garch_series = pd.Series(profit_per_trade_garch)
               profit_per_trade_ewma_series = pd.Series(profit_per_trade_ewma)
               fig = plt.figure(figsize=(10, 7))
               ax = fig.add_axes([0.1, 0.1, 0.8, 0.8]) # main axes
               _ = ax.plot(np.arange(len(profit_per_trade_egarch_series)), profit_per_trade_egarch_series.values, label='EGARCH')
               = ax.plot(np.arange(len(profit_per_trade_garch_series)), profit_per_trade_garch_series.values, label='GARCH')
= ax.plot(np.arange(len(profit_per_trade_ewma_series)), profit_per_trade_ewma_series.values, label='EWMA')
            8
               _ = ax.set_xlabel("Number of Trades")
               _ = ax.set_ylabel("Profit per Trade")
           11
               _ = ax.set_title("Profit/Loss-per-Trade Plot")
           12
               _ = ax.legend()
           13
```



# References

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