

# Linear regression model

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## Linear regression with only one predictor.

### Student marks dataset and exploration.

The data set contain the mark scored by student in exam, hours of study and number of course they have opted for. The question we are asking in this case if, **How does number of hours of studies will impact score?**

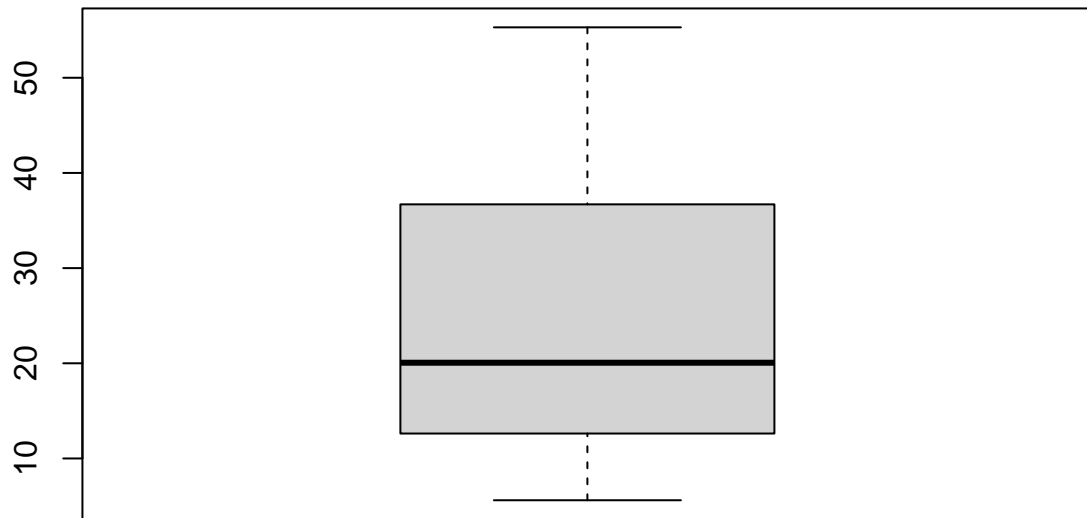
```
library(ggplot2)
library(GGally)
```

```
## Registered S3 method overwritten by 'GGally':
##   method from
##   +.gg      ggplot2
```

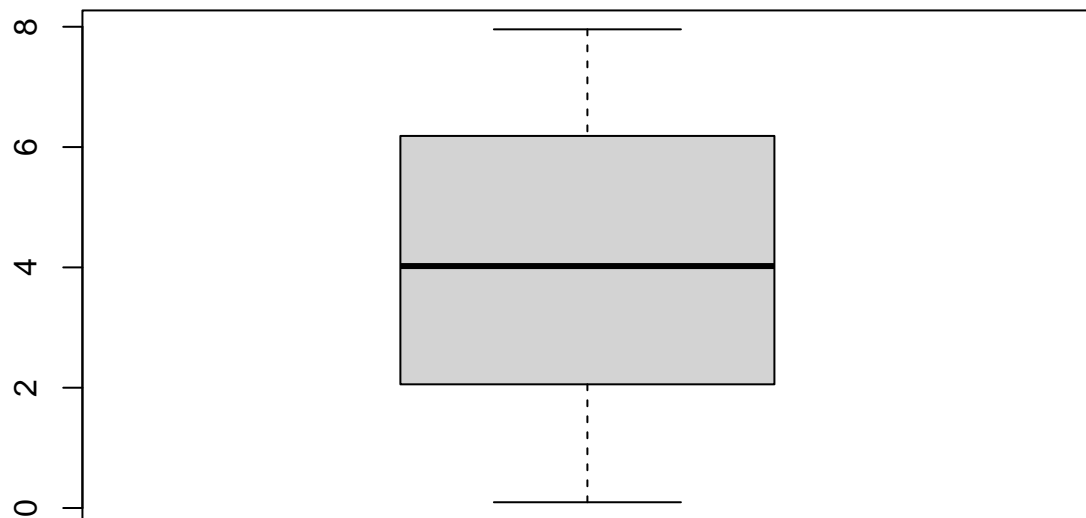
```
#Read the data set
Marks <- read.csv("data/Student_Marks.csv",header = T)
# Basic exploration of the marks data set.
summary(Marks)
```

```
##  number_courses  time_study      Marks
##  Min.    :3.00    Min.    :0.096   Min.    : 5.609
##  1st Qu.:4.00    1st Qu.:2.058   1st Qu.:12.633
##  Median :5.00    Median :4.022   Median :20.059
##  Mean   :5.29    Mean   :4.077   Mean   :24.418
##  3rd Qu.:7.00    3rd Qu.:6.179   3rd Qu.:36.676
##  Max.   :8.00    Max.   :7.957   Max.   :55.299
```

```
#graphical representations.
boxplot(Marks$Marks)
```



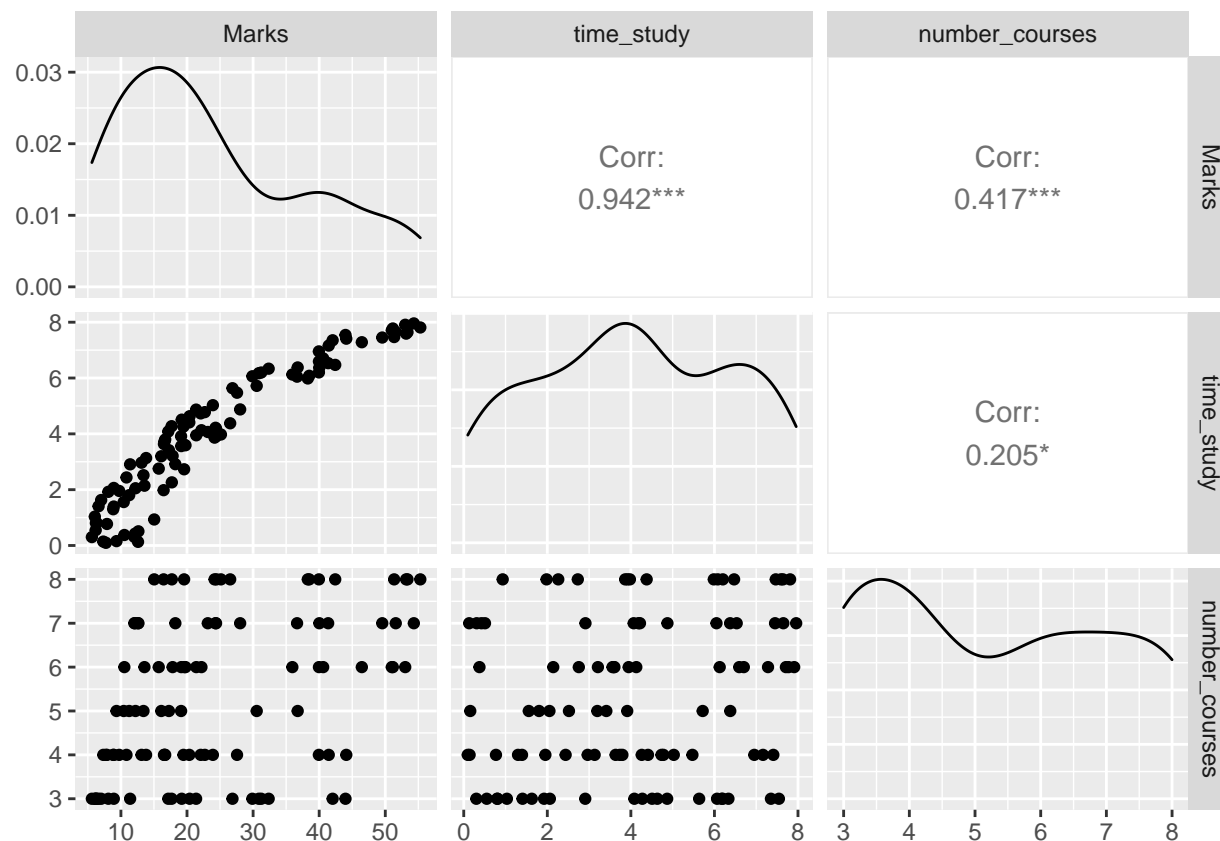
```
boxplot(Marks$time_study)
```



```
str(Marks)
```

```
## 'data.frame':  100 obs. of  3 variables:
## $ number_courses: int  3 4 4 6 8 6 3 5 4 3 ...
## $ time_study    : num  4.508 0.096 3.133 7.909 7.811 ...
## $ Marks         : num  19.2 7.73 13.81 53.02 55.3 ...
```

```
# The first set of data exploration is pair plot which check for
#correlation among predictor and repose.
ggpairs(Marks[,c(3,2,1)])
```



### Linear regression fitting.

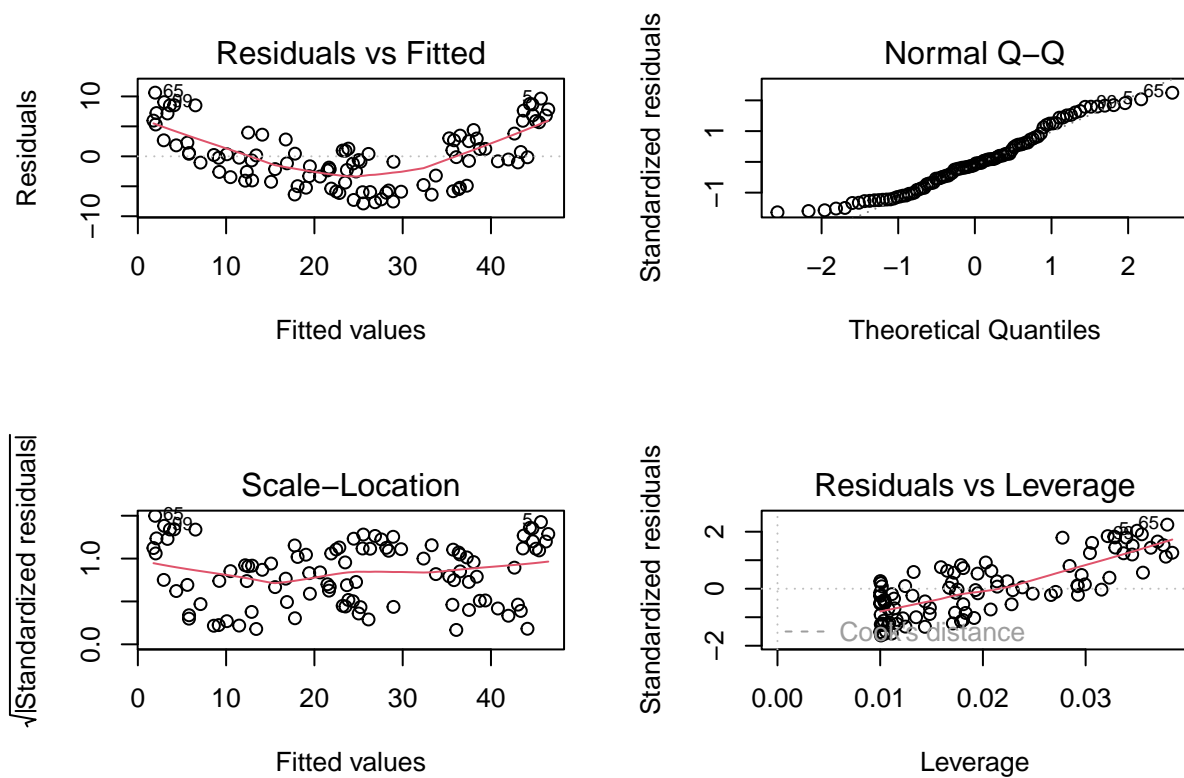
Based on Pairwise plot it is clear that Marks do follow a linear trend with time of study. In the next step we will model the linear regression

$$y = \beta_0 + \beta_1 X + \epsilon$$

where

$$\epsilon = N(\mu, \sigma)$$

```
model <- lm(Marks~time_study,data = Marks)
#model's assumptions validation.
par(mfrow=c(2,2))
plot(model)
```

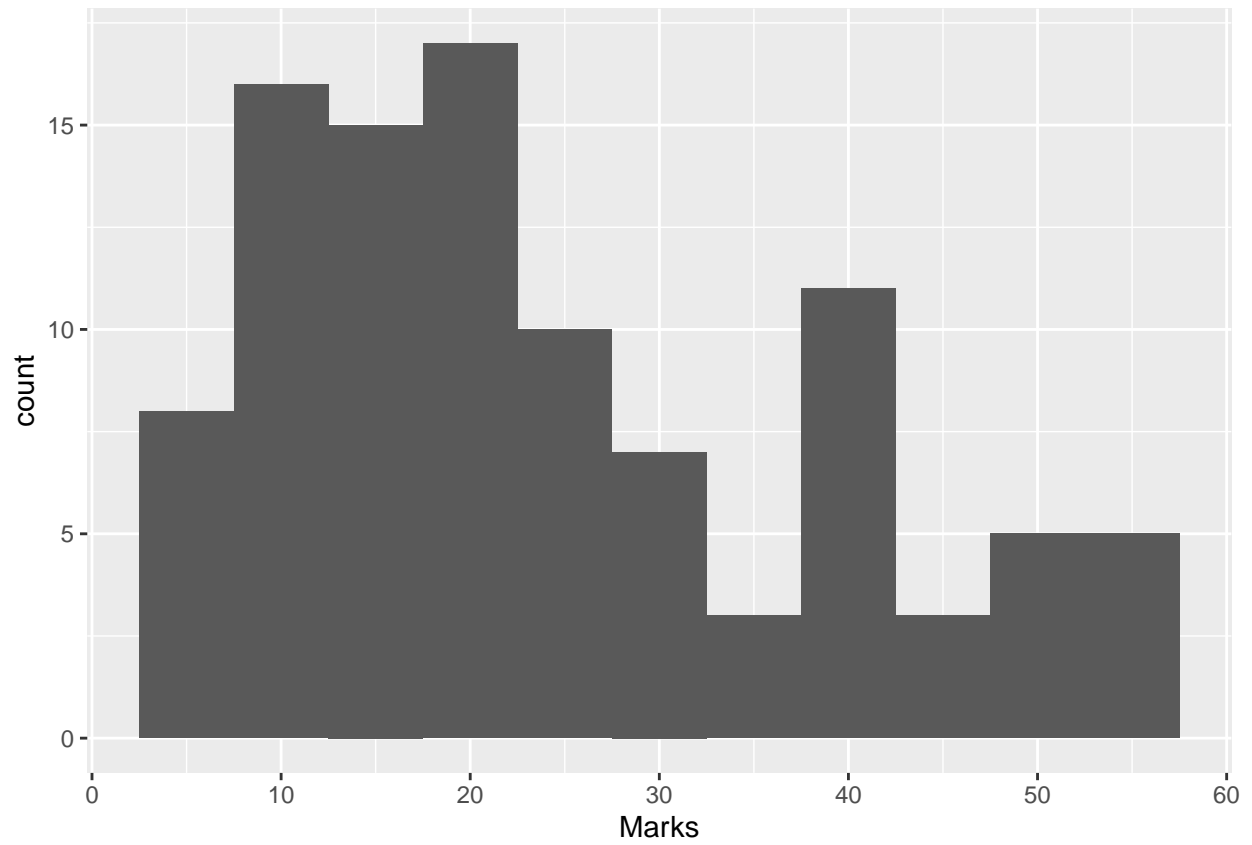


### Assumption of linear regression.

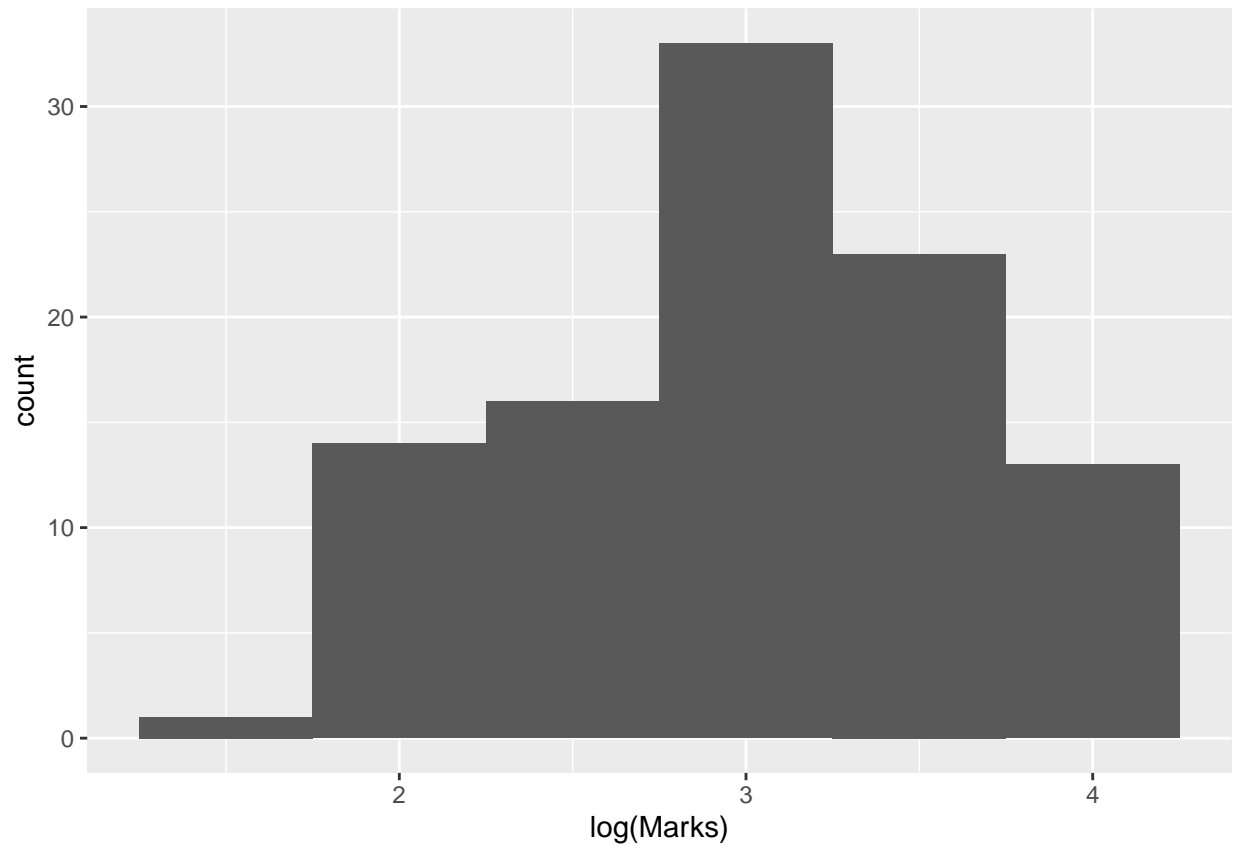
1. Linear relation.
2. Normality
3. Homogeneity of residuals variance

Based on our graphs above, the plot of Residuals vs Fitted value we can see that our data is not homogeneous. We can later confirm this by plotting a histogram of Marks. **One way to overcome this problem is to do transformation.**

```
library(ggplot2)
ggplot(data = Marks, aes(x=Marks))+geom_histogram(binwidth = 5)
```



```
##Log transformation  
ggplot(data = Marks,aes(x=log(Marks)))+geom_histogram(binwidth = 0.5)
```



```
##lets check the normality by using shapiro test
shapiro.test(Marks$Marks)
```

```
##
## Shapiro-Wilk normality test
##
## data: Marks$Marks
## W = 0.91427, p-value = 7.082e-06
```

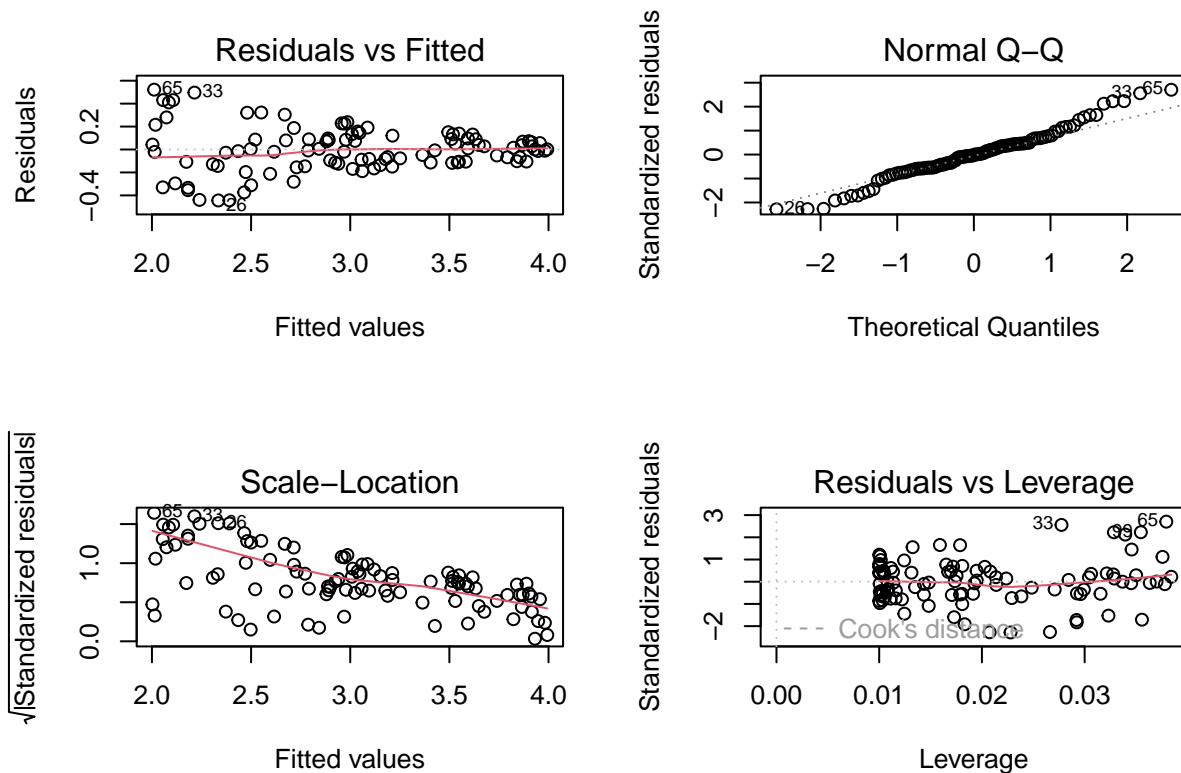
```
shapiro.test(log(Marks$Marks))
```

```
##
## Shapiro-Wilk normality test
##
## data: log(Marks$Marks)
## W = 0.96222, p-value = 0.005805
```

```
## The value p-value have increase but not to significant level that
## distribution become normal.
```

The value p-value have increase but not to significant level that distribution become normal. However, given with data the model will improve significantly

```
model1 <- lm(log(Marks)~time_study,data = Marks)
#model's assumptions validation.
par(mfrow=c(2,2))
plot(model1)
```



```
summary(model1)
```

```
##
## Call:
## lm(formula = log(Marks) ~ time_study, data = Marks)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.44413 -0.11272 -0.00365  0.09239  0.52174
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  1.978317   0.039250   50.4   <2e-16 ***
## time_study   0.253277   0.008331   30.4   <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1967 on 98 degrees of freedom
## Multiple R-squared:  0.9041, Adjusted R-squared:  0.9032
## F-statistic: 924.3 on 1 and 98 DF, p-value: < 2.2e-16
```

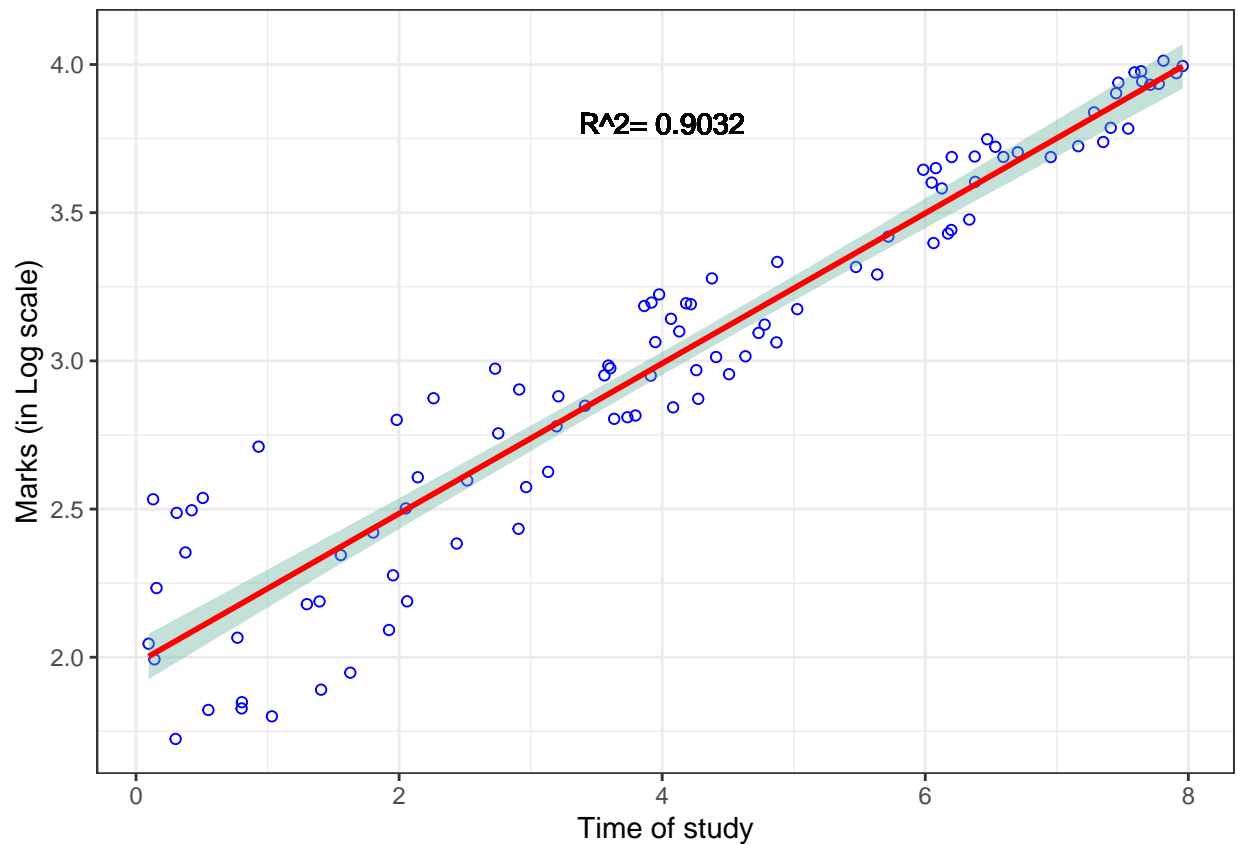


interpretation of model with log transformation.

$$\log(\text{Marks}) = 1.978 + 0.253 * \text{studytime} + \epsilon$$

```
plot_model2 <- ggplot(data = Marks, aes(x=time_study, y=log(Marks)))
plot_model2+geom_point(pch=1, col="blue")+
  geom_smooth(method=lm, color="red", fill="#69b3a2", se=TRUE)+
  theme_bw()+
  labs(x="Time of study", y="Marks (in Log scale)")+
  geom_text(mapping = aes(x=4, y=3.8,
                          label=paste("R^2=", round(summary(model1)$adj.r.squared, 4))))
```

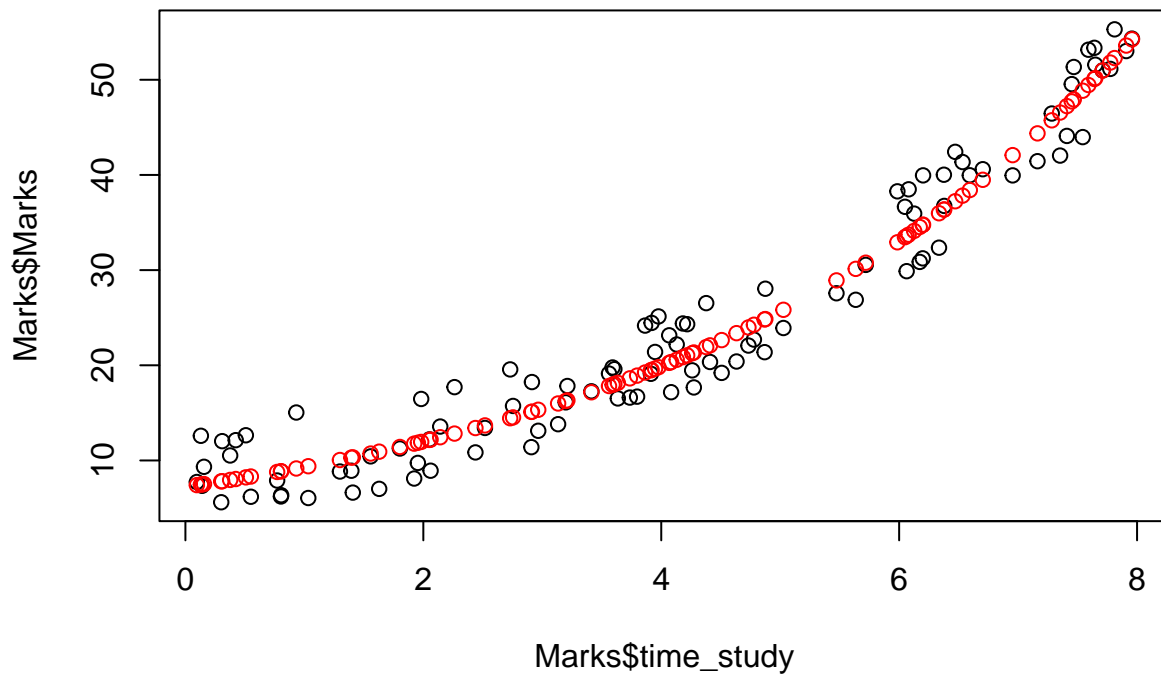
## 'geom\_smooth()' using formula 'y ~ x'



In order to back transform from log scale to linear scale we need to look in the use the formula

$$\text{Marks} = \exp^{B1 * \text{time} + B0}$$

```
exp_pred <- exp(predict(model1, newdata = Marks))
plot(Marks$Marks ~ Marks$time_study)
points(exp_pred ~ Marks$time_study, col="red")
```



Model with more than one parameter.

$$y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \epsilon$$

where

$$\epsilon = N(\mu, \sigma)$$

Let us use the fish morphometric data and ask question is fish length can predict its weight.

```
fish <- read.csv("data/Fish_morphometrics.csv", header = T)
# Summary and str of data
summary(fish)
```

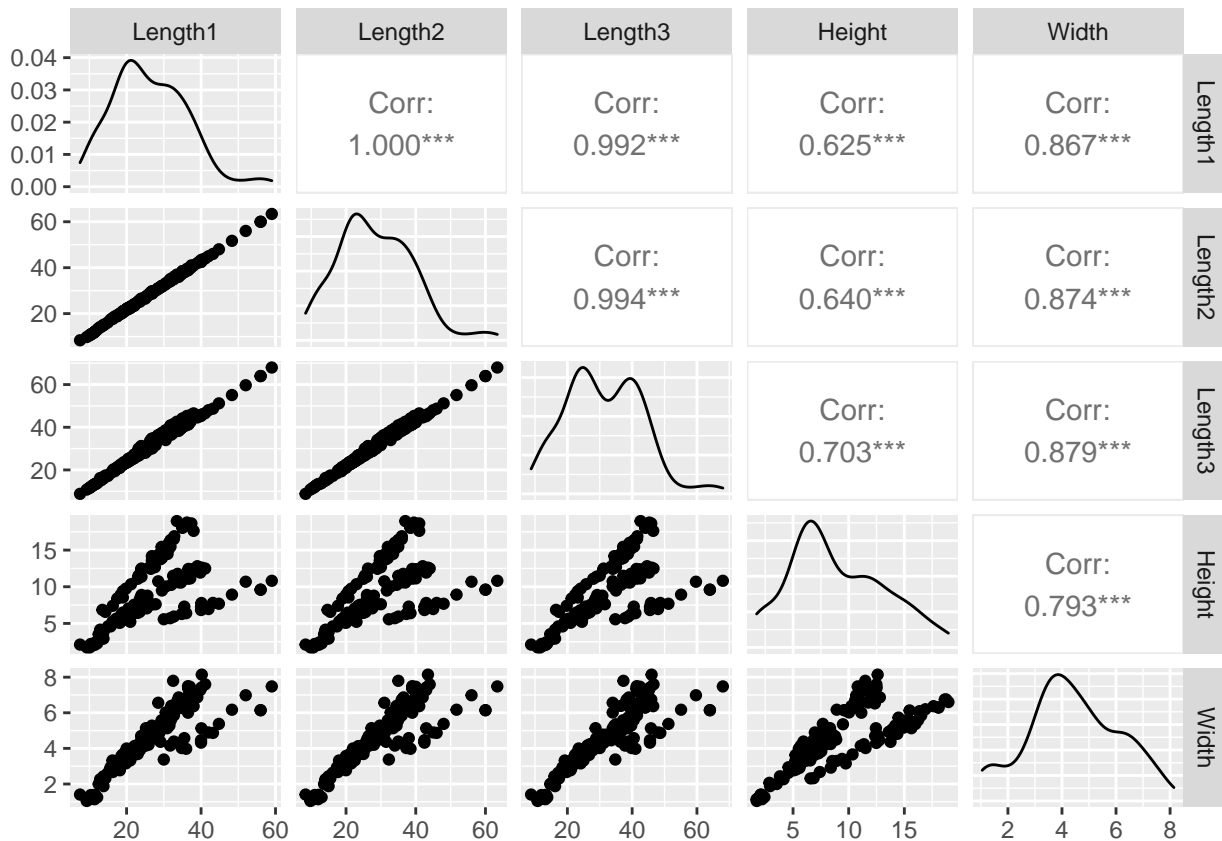
```
## Species           Weight           Length1           Length2
## Length:159      Min.      : 0.0      Min.      : 7.50      Min.      : 8.40
## Class :character 1st Qu.: 120.0    1st Qu.:19.05     1st Qu.:21.00
## Mode  :character Median : 273.0    Median :25.20     Median :27.30
##                Mean   : 398.3    Mean   :26.25     Mean   :28.42
##                3rd Qu.: 650.0    3rd Qu.:32.70     3rd Qu.:35.50
##                Max.   :1650.0    Max.   :59.00     Max.   :63.40
## Length3          Height           Width
## Min.      : 8.80    Min.      : 1.728    Min.      :1.048
## 1st Qu.:23.15    1st Qu.: 5.945    1st Qu.:3.386
## Median :29.40    Median : 7.786    Median :4.248
## Mean   :31.23    Mean   : 8.971    Mean   :4.417
```

```
## 3rd Qu.:39.65 3rd Qu.:12.366 3rd Qu.:5.585
## Max. :68.00 Max. :18.957 Max. :8.142
```

```
str(fish)
```

```
## 'data.frame': 159 obs. of 7 variables:
## $ Species: chr "Bream" "Bream" "Bream" "Bream" ...
## $ Weight : num 242 290 340 363 430 450 500 390 450 500 ...
## $ Length1: num 23.2 24 23.9 26.3 26.5 26.8 26.8 27.6 27.6 28.5 ...
## $ Length2: num 25.4 26.3 26.5 29 29 29.7 29.7 30 30 30.7 ...
## $ Length3: num 30 31.2 31.1 33.5 34 34.7 34.5 35 35.1 36.2 ...
## $ Height : num 11.5 12.5 12.4 12.7 12.4 ...
## $ Width : num 4.02 4.31 4.7 4.46 5.13 ...
```

```
# pairwise plot
ggpairs(fish[,3:7])
```



```
library(dplyr)
```

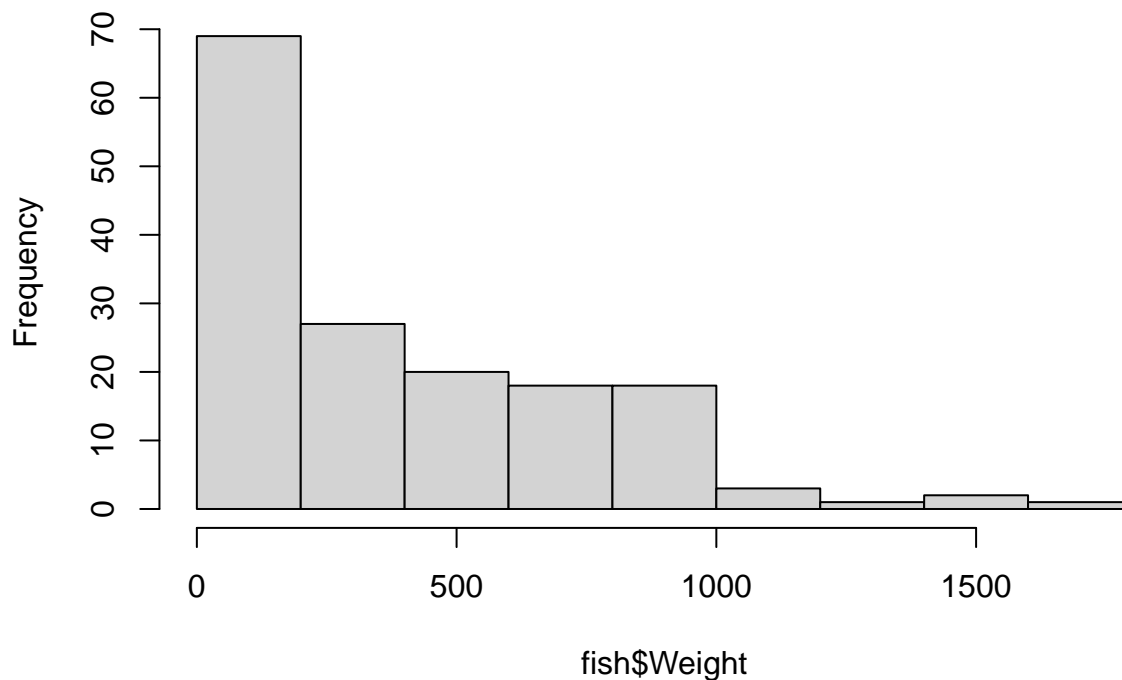
```
##
## Attaching package: 'dplyr'

## The following objects are masked from 'package:stats':
##
## filter, lag
```

```
## The following objects are masked from 'package:base':
##
## intersect, setdiff, setequal, union

fish_group<-fish%>%group_by(Species)%>%summarise(count=n(),mean(Weight),mean(Length3),sd(Weight))
fish<-fish%>%mutate(avg_length = (Length1+Length2+Length3)/3)
hist(fish$Weight)
```

## Histogram of fish\$Weight



```
#Install.packages("devtools")
devtools::install_github("cardiomoon/ggiraphExtra")
```

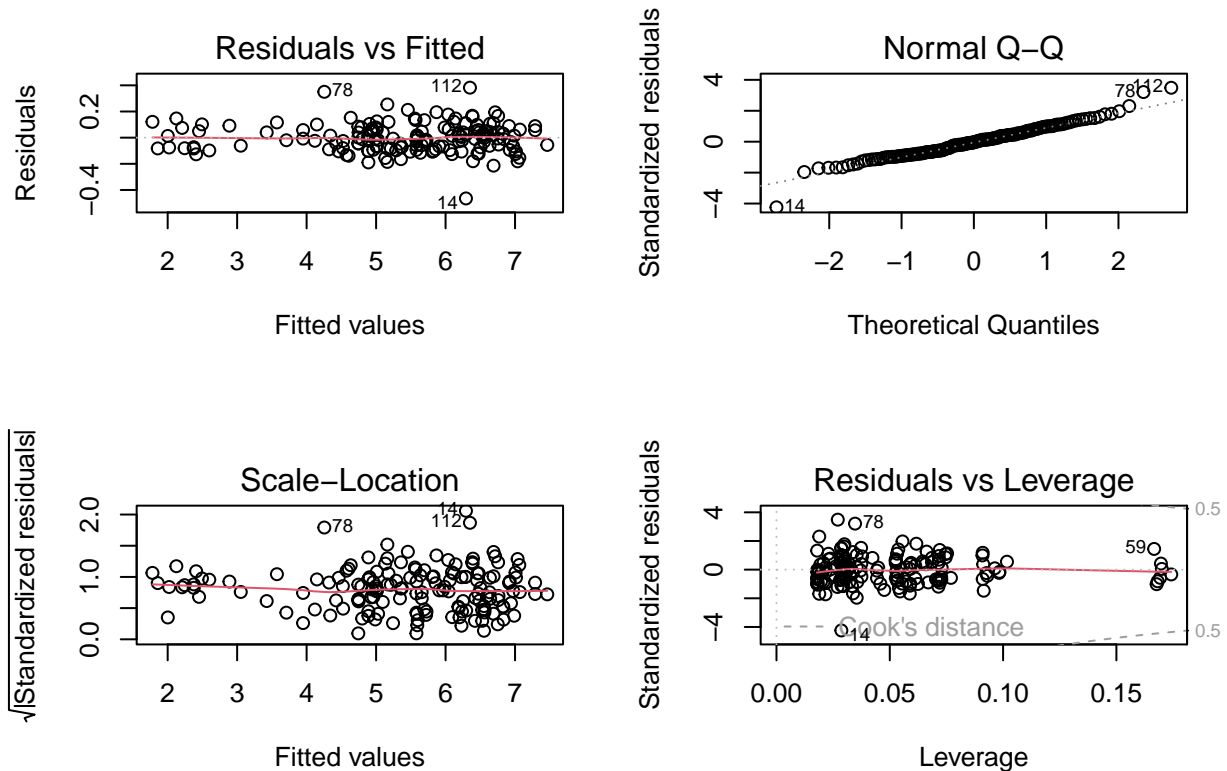
```
## Skipping install of 'ggiraphExtra' from a github remote, the SHA1 (c2c1ce81) has not changed since 1.
## Use 'force = TRUE' to force installation
```

```
library(ggiraphExtra)
require(ggiraph)
```

```
## Loading required package: ggiraph
```

```
model_fish1 <- lm(Weight~avg_length+Species,data = fish)
fish <- fish[fish$Weight!=0,] ## wrong data point
model_log <- lm(log(Weight)~avg_length+Species,data = fish)
#we make log log transformation
```

```
fish <- fish%>%mutate(log_w = log(Weight),log_avg_len=log(avg_length))
model_log_log <- lm(log_w~log_avg_len+Species,data = fish)
par(mfrow=c(2,2))
plot(model_log_log)
```



```
summary.lm(model_log_log)
```

```
##
## Call:
## lm(formula = log_w ~ log_avg_len + Species, data = fish)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.46466 -0.07484 -0.00418  0.06379  0.38221
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -4.57249    0.13214  -34.603  < 2e-16 ***
## log_avg_len     3.10950    0.03718   83.625  < 2e-16 ***
## SpeciesParkki    0.12178    0.04276    2.848  0.00502 **
## SpeciesPerch   -0.12573    0.02569   -4.894  2.53e-06 ***
## SpeciesPike    -0.86944    0.03447  -25.226  < 2e-16 ***
## SpeciesRoach   -0.14879    0.03510   -4.239  3.91e-05 ***
## SpeciesSmelt   -0.79600    0.05204  -15.295  < 2e-16 ***
## SpeciesWhitefish 0.02280    0.04919    0.464  0.64362
```

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1111 on 150 degrees of freedom
## Multiple R-squared:  0.9933, Adjusted R-squared:  0.993
## F-statistic: 3174 on 7 and 150 DF,  p-value: < 2.2e-16
```

```
summary.aov(model_log_log)
```

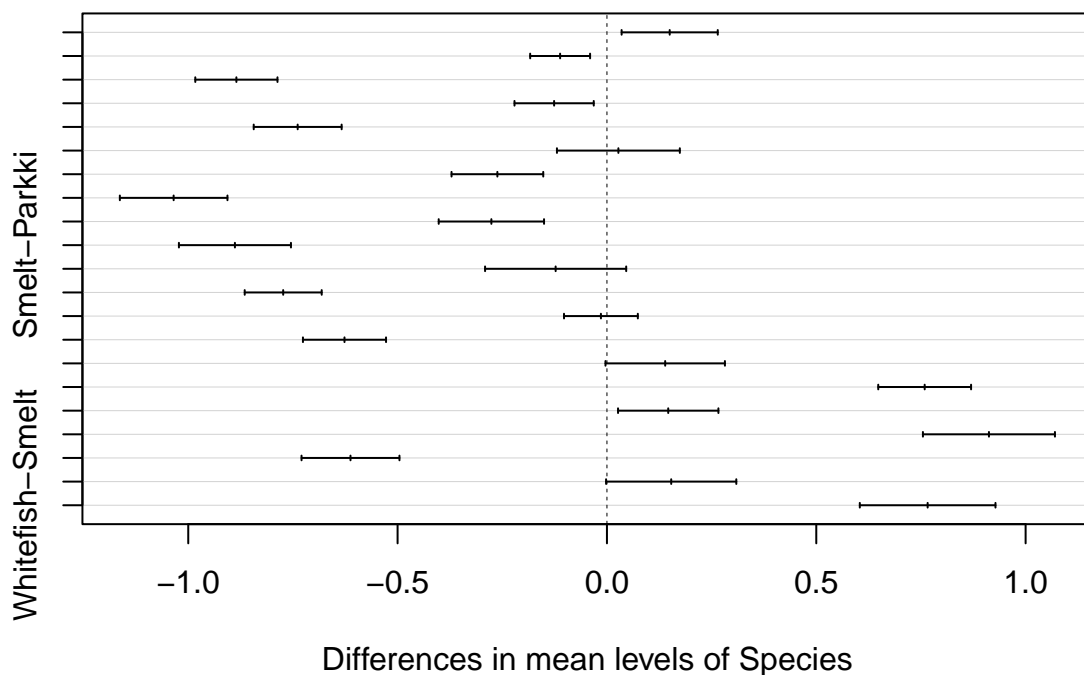
```
##           Df Sum Sq Mean Sq F value Pr(>F)
## log_avg_len  1 258.61  258.61 20949.4 <2e-16 ***
## Species      6  15.66    2.61   211.4 <2e-16 ***
## Residuals   150   1.85    0.01
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
model_log_log_aov <- aov(log_w~log_avg_len+Species,data = fish)
par(mfrow=c(1,1))
#posthoc
Tuk <-TukeyHSD(model_log_log_aov, "Species",data = fish)
```

```
## Warning in replications(paste("~", xx), data = mf): non-factors ignored:
## log_avg_len
```

```
plot(Tuk)
```

## 95% family-wise confidence level



```

#predicting the values
pred_value<-predict.lm(model_log_log,interval = "confidence")
pred_value <- as.data.frame(pred_value)
fish <- cbind(fish,pred_value)
## plotting the model
plot <- ggplot(data = fish, aes(x=log_avg_len,y=log_w,col=Species))
plot+geom_point()+
  geom_line(aes(y=fit))+
  geom_ribbon(aes(ymin=lwr,ymax=upr),alpha=0.05)

```

