Lecture 16:
Introduction to Object Recognition
and
the Nearest Neighbor Approach

READING: https://cs231n.github.io/classification/

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Stanford Vision Lab

FOR UPDATED SLIDES/NOTES CHECK: http://cs231n.stanford.edu/

What we will learn today?

- Introduction
- K-nearest neighbor algorithm
- A simple Object Recognition pipeline

What are the different visual recognition tasks?

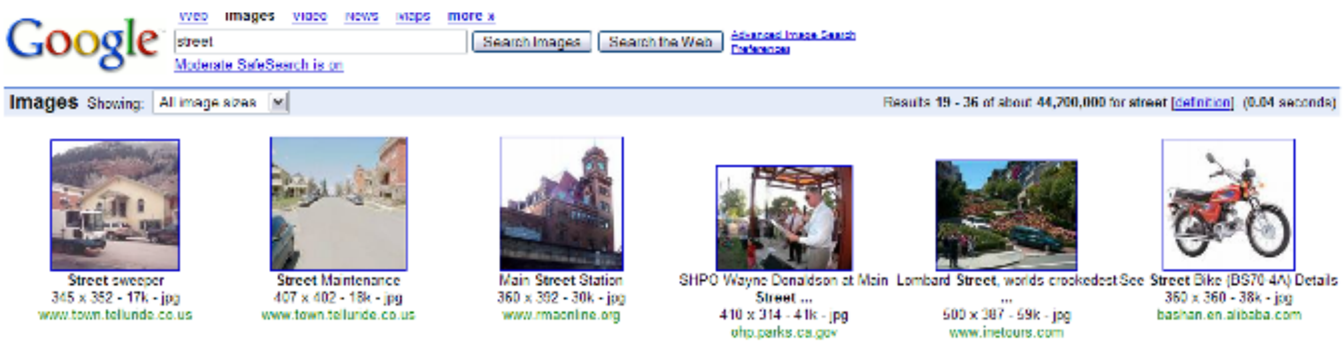
Classification:

Does this image contain a building? [yes/no]

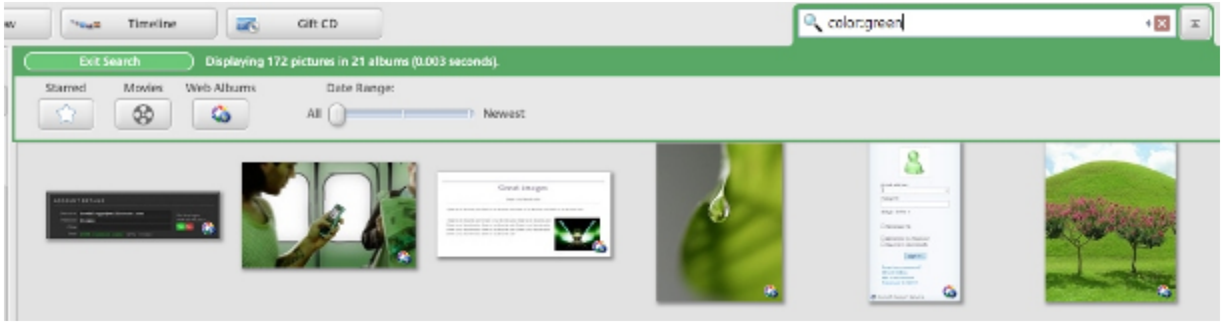
Classification:

Is this an beach?

Image Search



Organizing photo collections

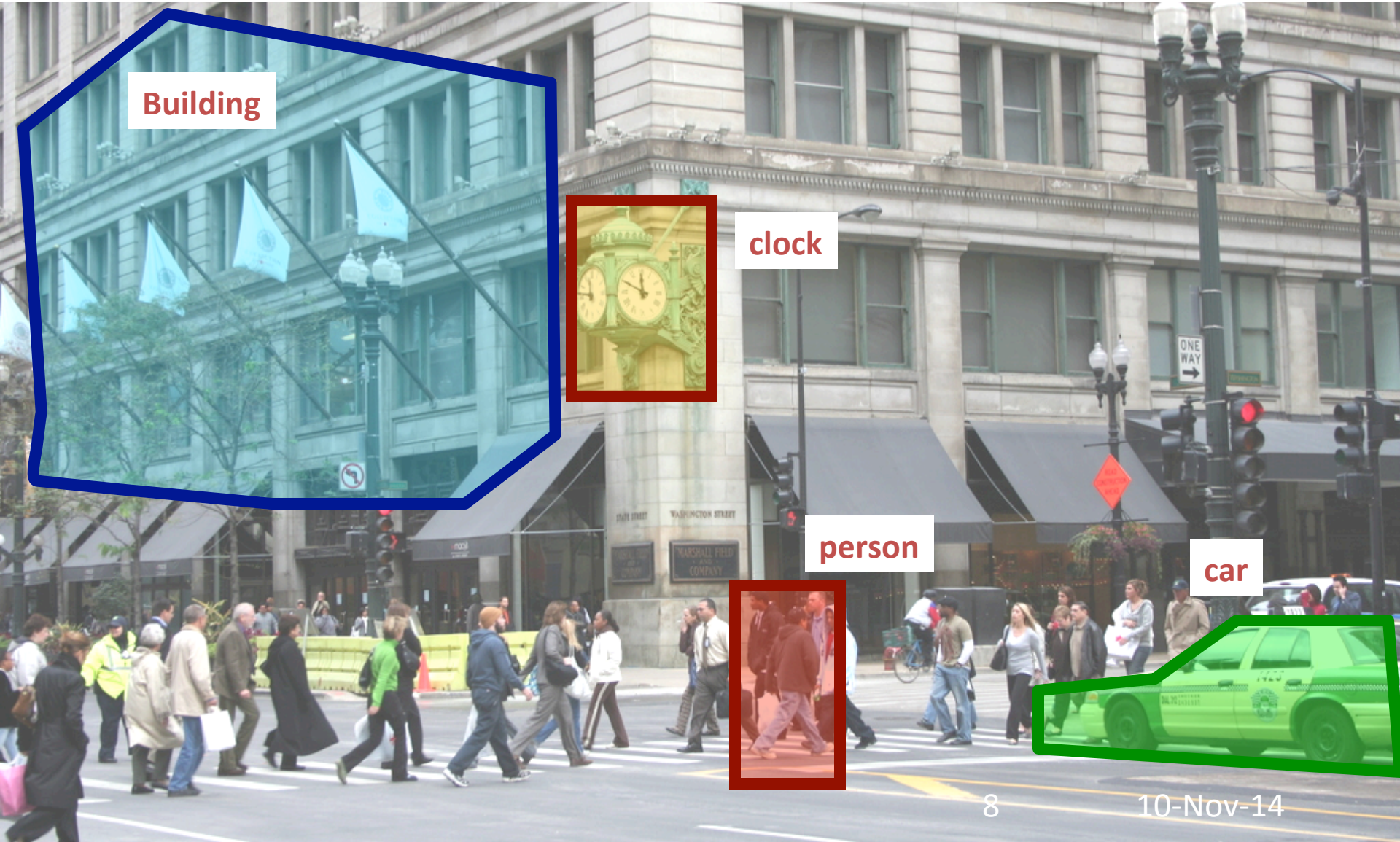


Detection:

Does this image contain a car? [where?]

Detection:

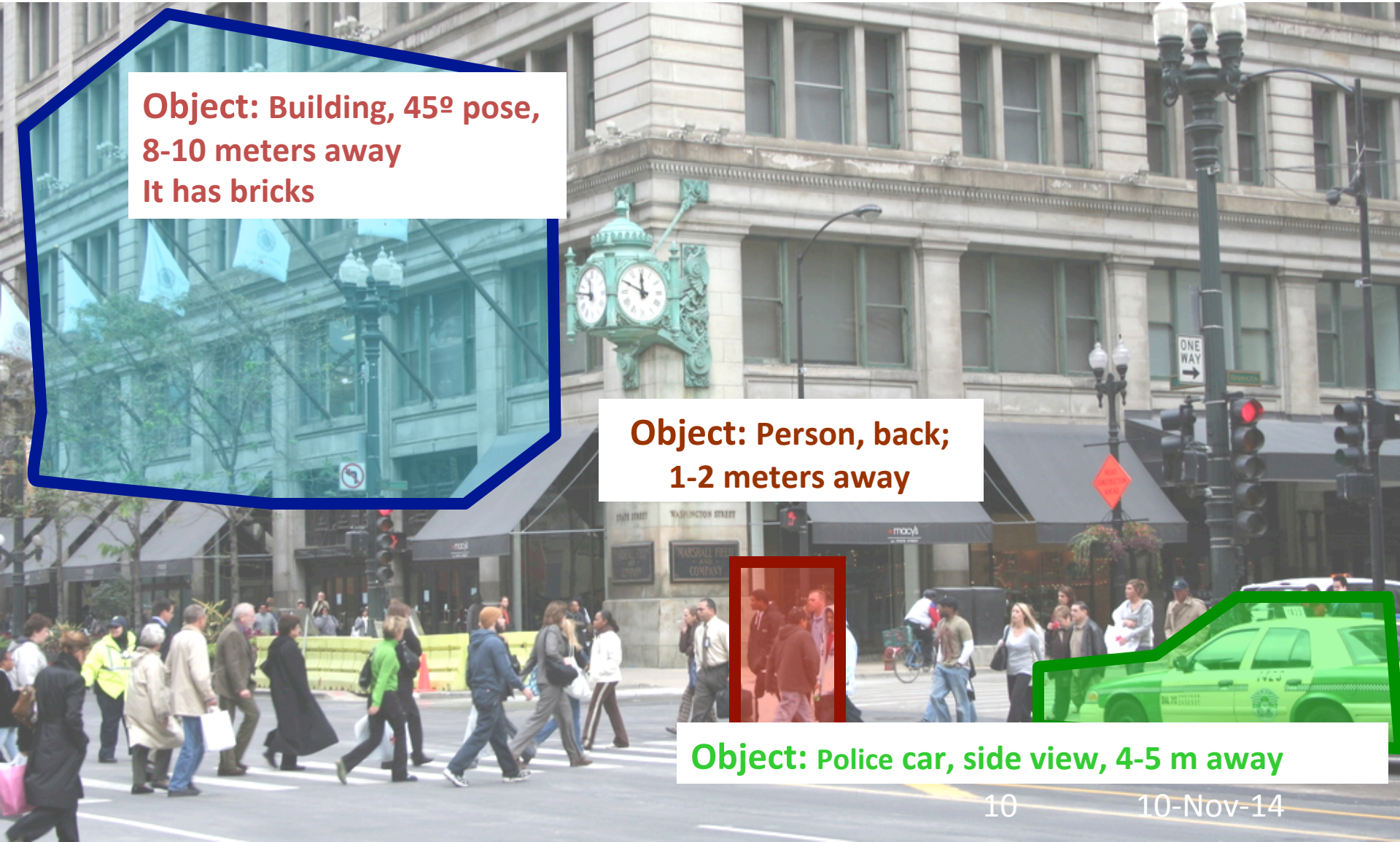
Which object does this image contain? [where?]



Detection:

Accurate localization (segmentation)

Detection: Estimating object semantic & geometric attributes



Applications of computer vision

Computational photography

Assistive technologies

Surveillance

Security

Assistive driving

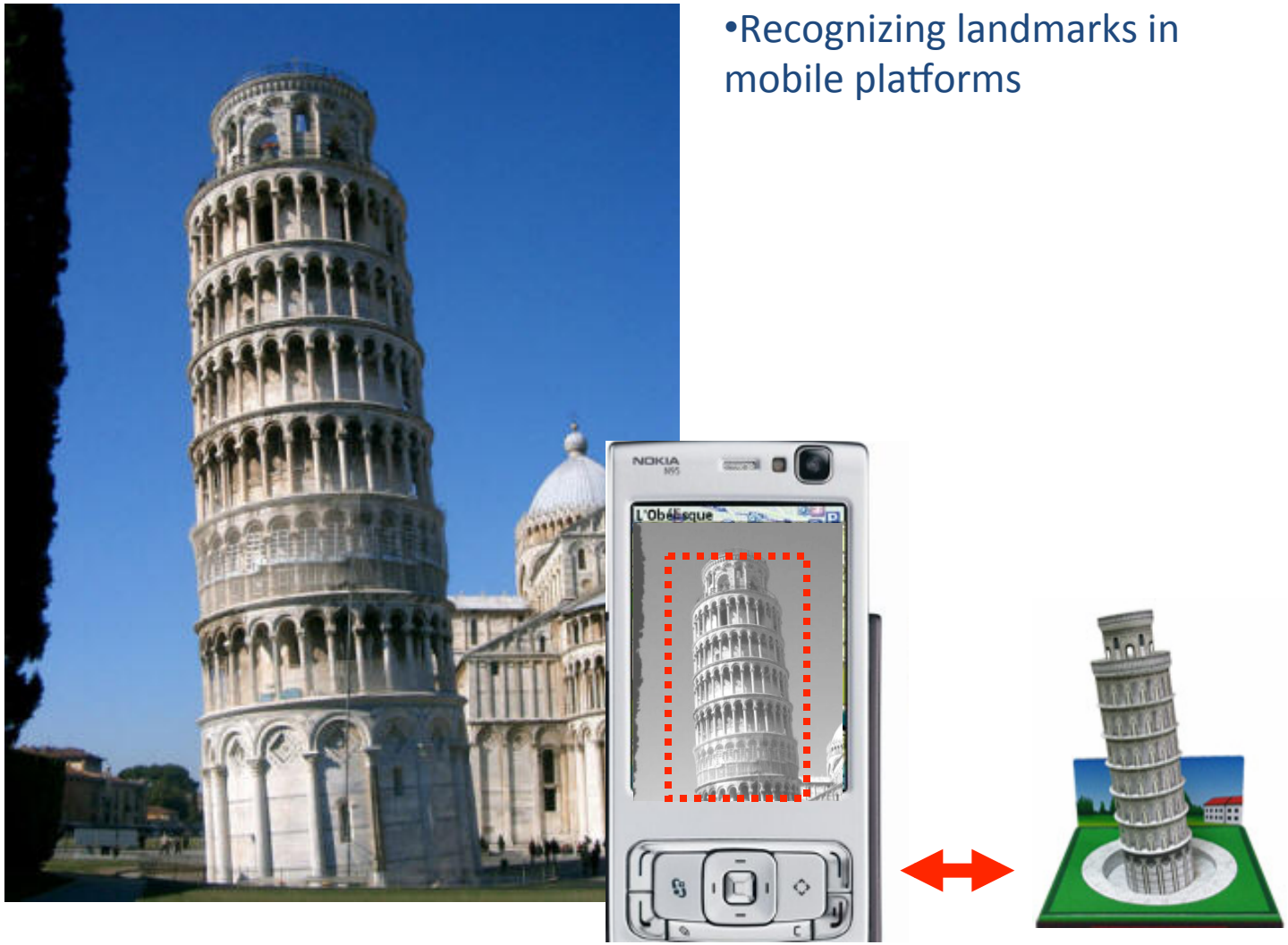
Categorization vs Single instance recognition

Does this image contain the Chicago Macy building's?

Categorization vs Single instance recognition

Where is the crunchy nut?

Applications of computer vision



- Recognizing landmarks in mobile platforms

Activity or Event recognition

What are these people doing?

Visual Recognition

- Design algorithms that are capable to
  - Classify images or videos
  - Detect and localize objects
  - Estimate semantic and geometrical attributes
  - Classify human activities and events

Why is this challenging?

How many object categories are there?

Challenges: viewpoint variation

Michelangelo 1475-1564

Challenges: illumination

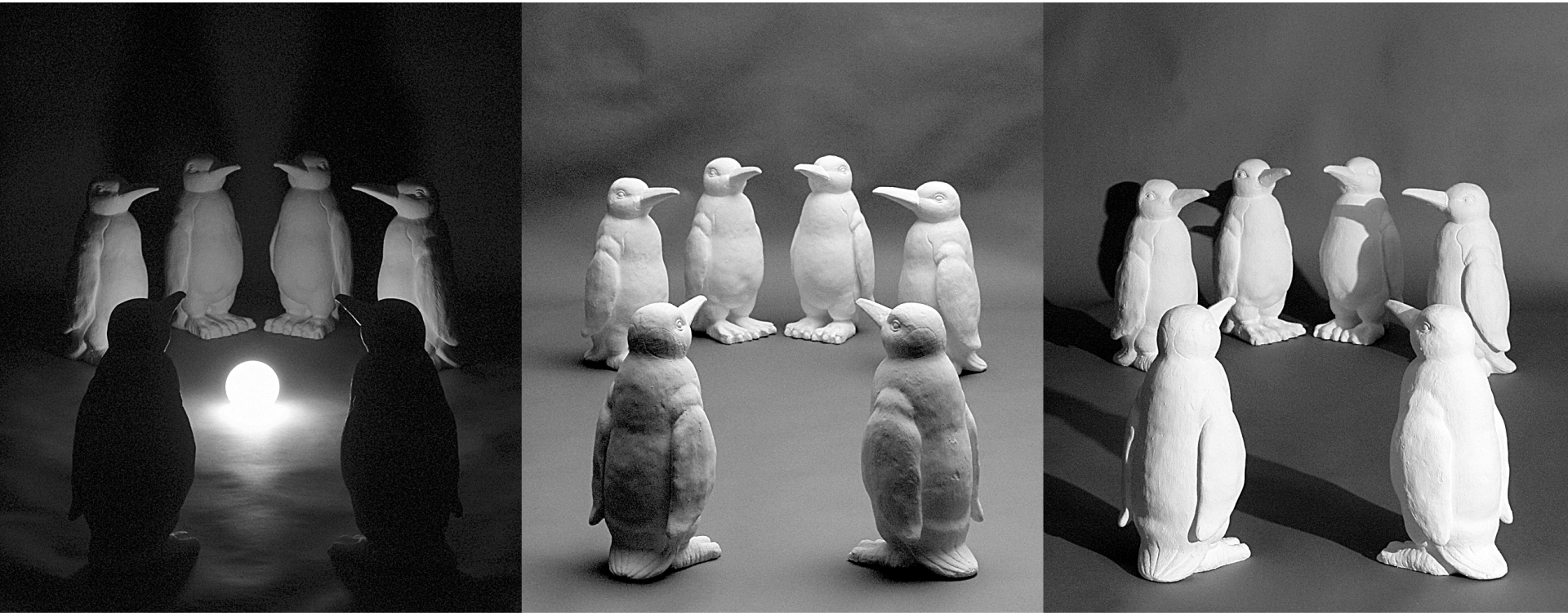


image credit: J. Koenderink

Challenges: scale

Challenges: deformation

Challenges: occlusion

Magritte, 1957

Challenges: background clutter

Kilmeny Niland. 1995

Challenges: intra-class variation

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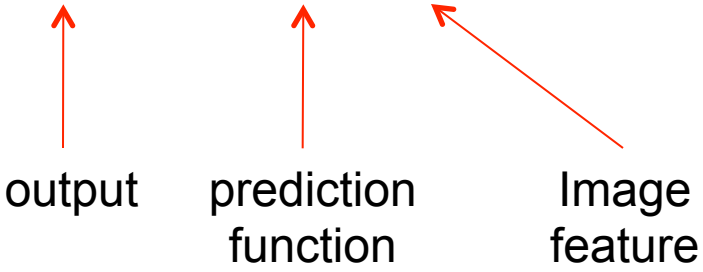
technical note

The machine learning framework

$$y = f(\mathbf{x})$$

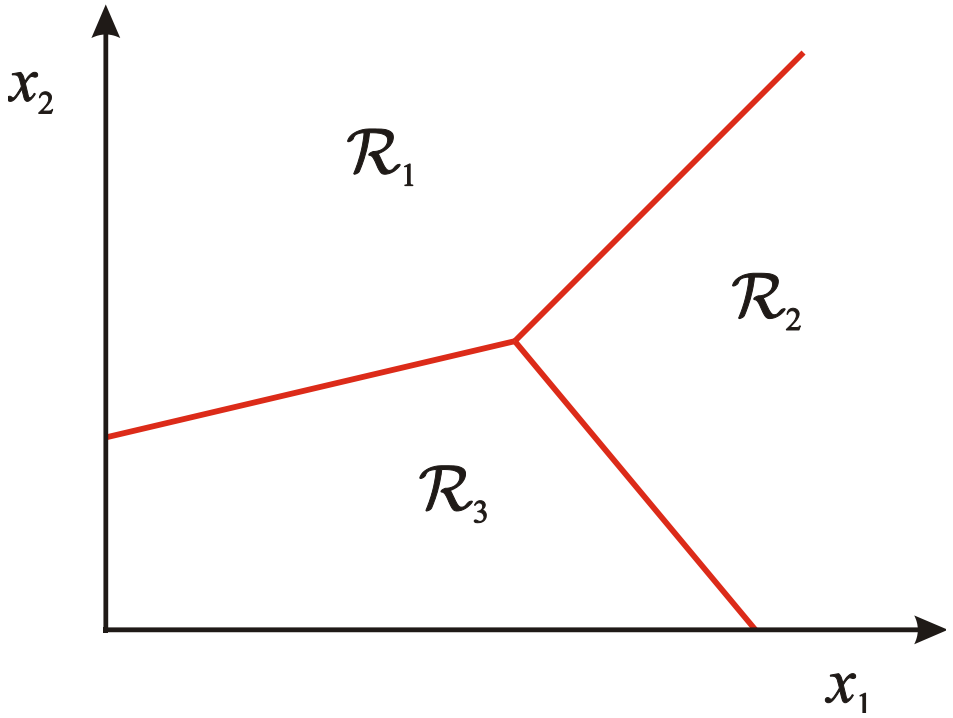


- **Training:** given a *training set* of labeled examples $\{(\mathbf{x}_1, y_1), \ldots, (\mathbf{x}_N, y_N)\}$, estimate the prediction function f by minimizing the prediction error on the training set
- **Testing:** apply f to a never before seen *test example* $\mathbf{x}$ and output the predicted value $y = f(\mathbf{x})$

Slide credit: L. Lazebnik

Classification

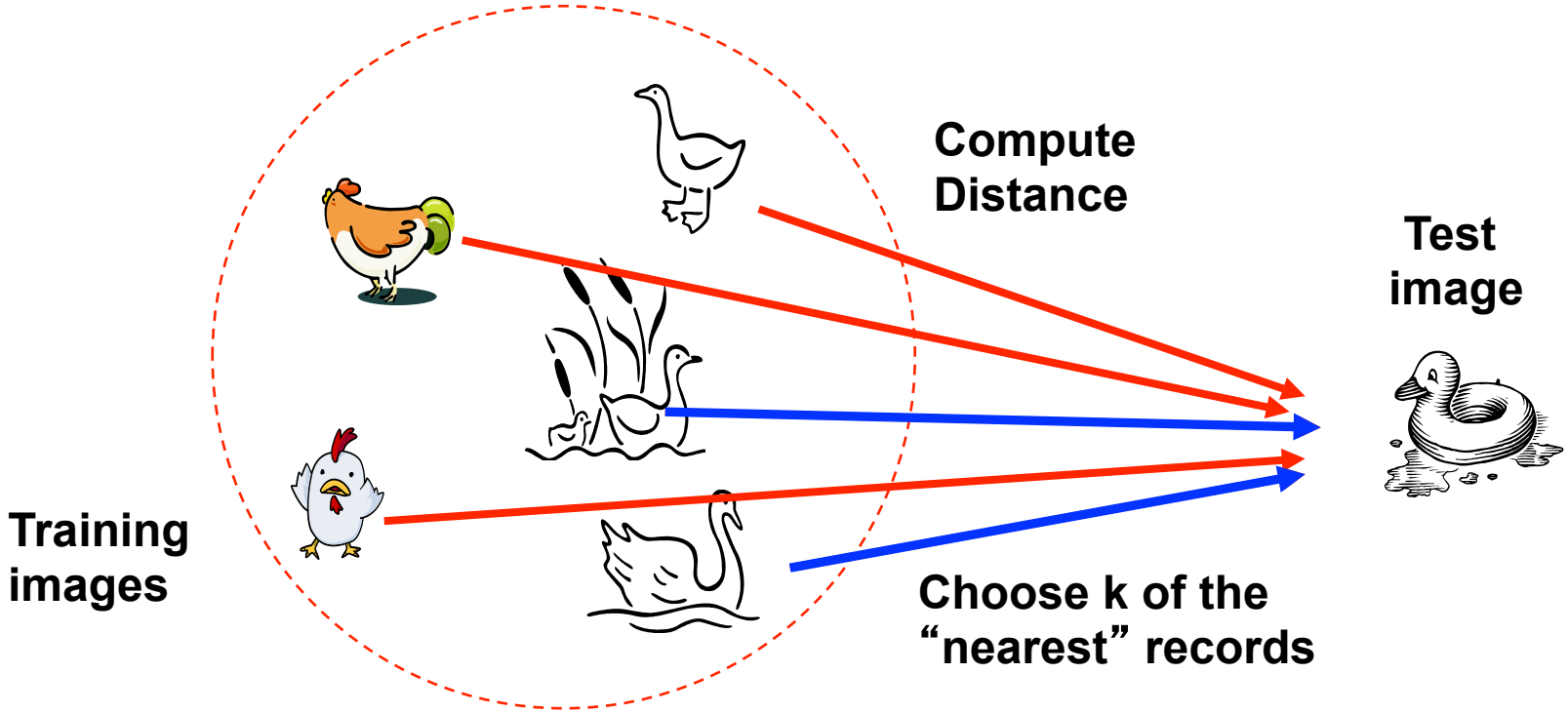
- Assign input vector to one of two or more classes
- Any decision rule divides input space into *decision regions* separated by *decision boundaries*



Slide credit: L. Lazebnik

Nearest Neighbor Classifier

- Assign label of nearest training data point to each test data point

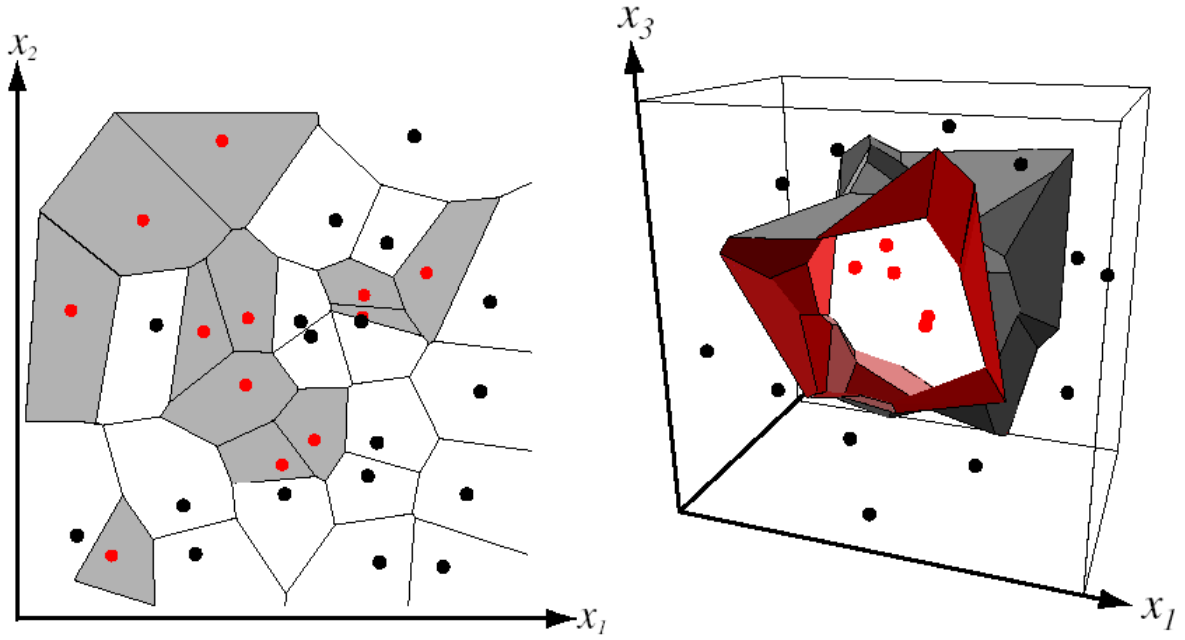


Source: N. Goyal

technical note

Nearest Neighbor Classifier

- Assign label of nearest training data point to each test data point



from Duda *et al.*

partitioning of feature space
for two-category 2D and 3D data

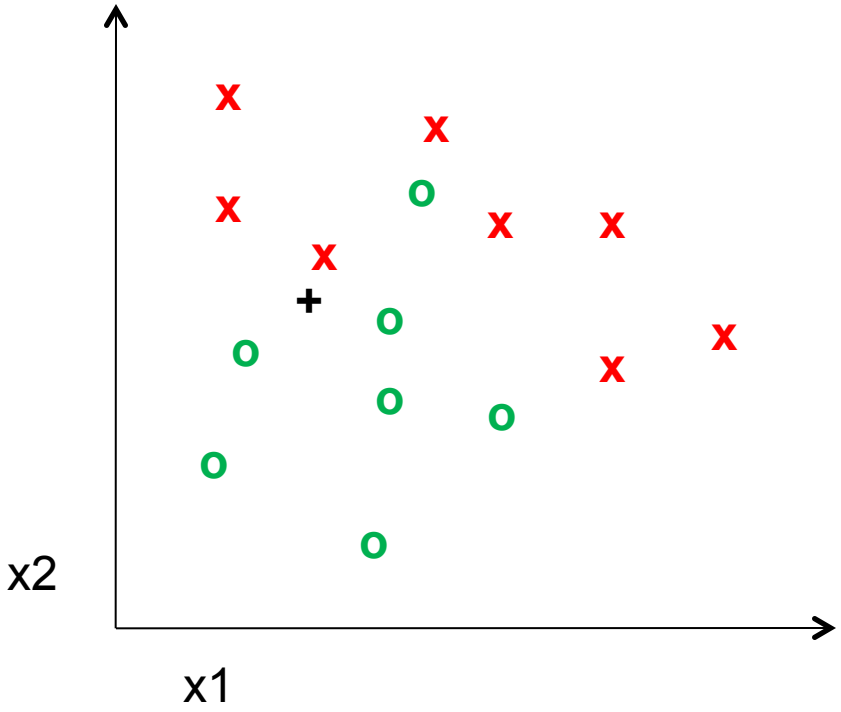
Source: D. Lowe

K-nearest neighbor

Distance measure - Euclidean

$$Dist(X^n, X^m) = \sqrt{\sum_{i=1}^{D} (X_i^n - X_i^m)^2}$$

Where X^n and X^m are the n-th and m-th data points

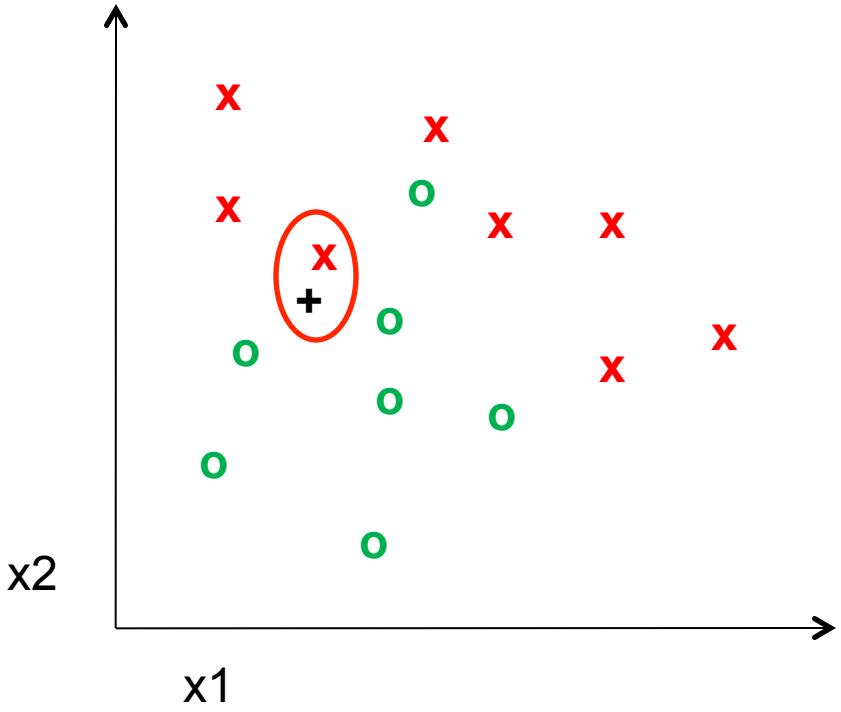


1-nearest neighbor

Distance measure - Euclidean

$$Dist(X^n, X^m) = \sqrt{\sum_{i=1}^{D} (X_i^n - X_i^m)^2}$$

Where X^n and X^m are the n-th and m-th data points

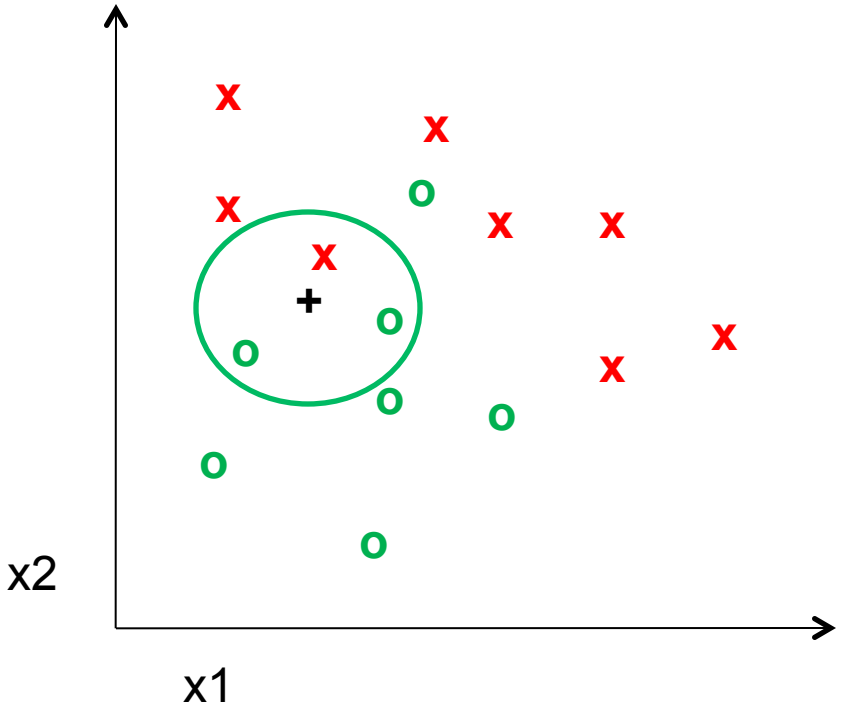


3-nearest neighbor

Distance measure - Euclidean

$$Dist(X^n, X^m) = \sqrt{\sum_{i=1}^{D} (X_i^n - X_i^m)^2}$$

Where X^n and X^m are the n-th and m-th data points

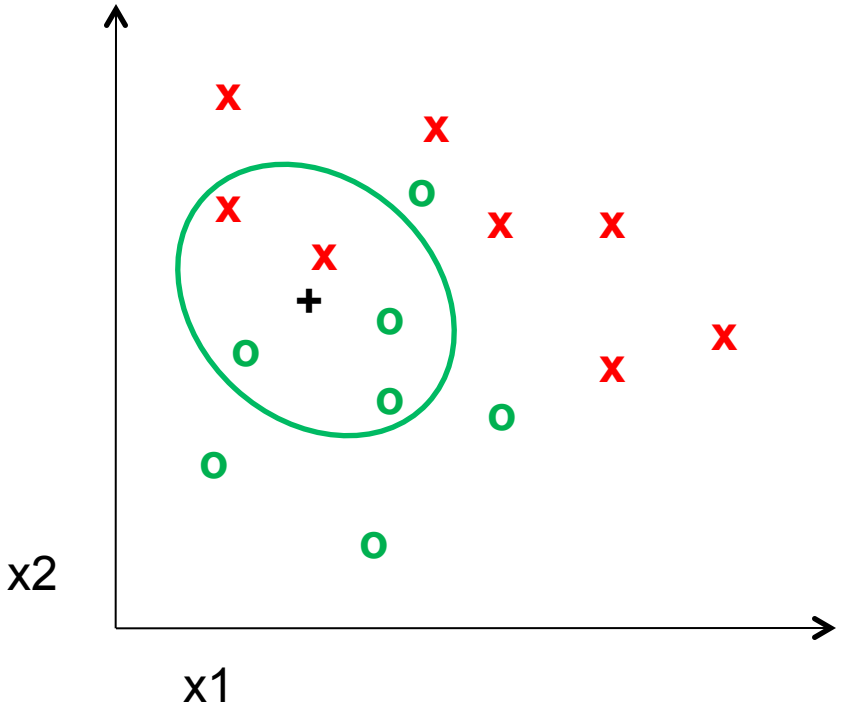


5-nearest neighbor

Distance measure - Euclidean

$$Dist(X^n, X^m) = \sqrt{\sum_{i=1}^{D} (X_i^n - X_i^m)^2}$$

Where X^n and X^m are the n-th and m-th data points

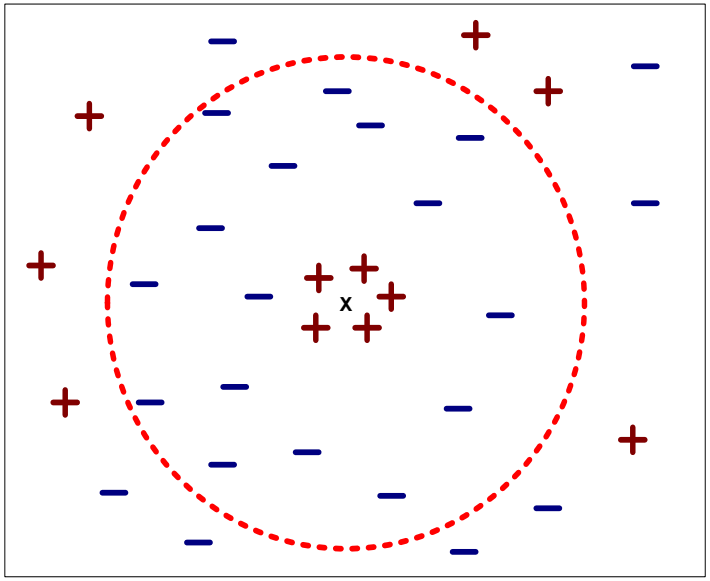


K-NN: a very useful algorithm

- Simple, a good one to try first
- Very flexible decision boundaries
- With infinite examples, 1-NN provably has error that is at most twice Bayes optimal error

K-NN: issues to keep in mind

- Choosing the value of k:
  - If too small, sensitive to noise points
  - If too large, neighborhood may include points from other classes



technical note

K-NN: issues to keep in mind

- Choosing the value of k:
  - If too small, sensitive to noise points
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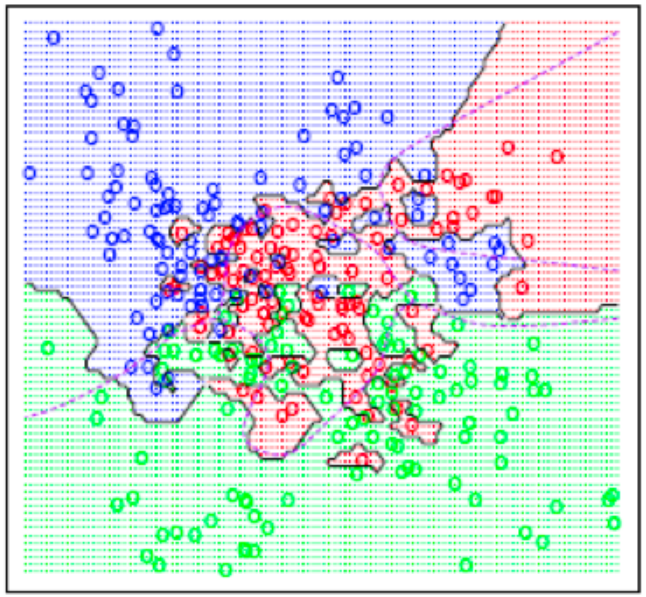
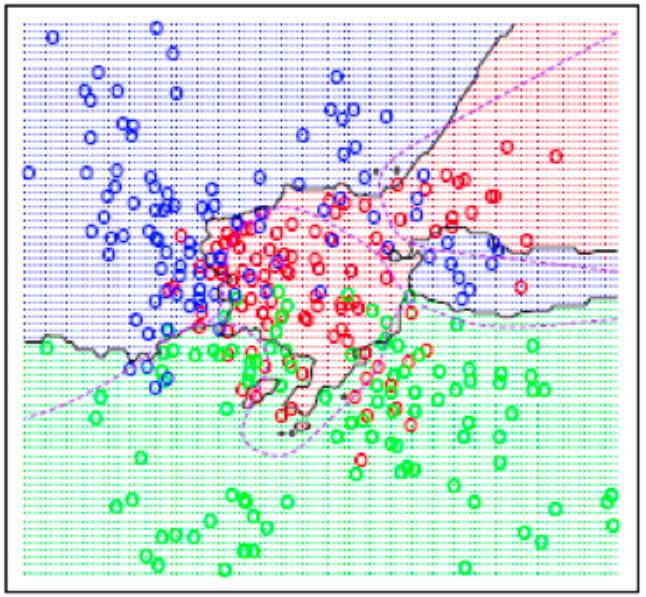
K=1

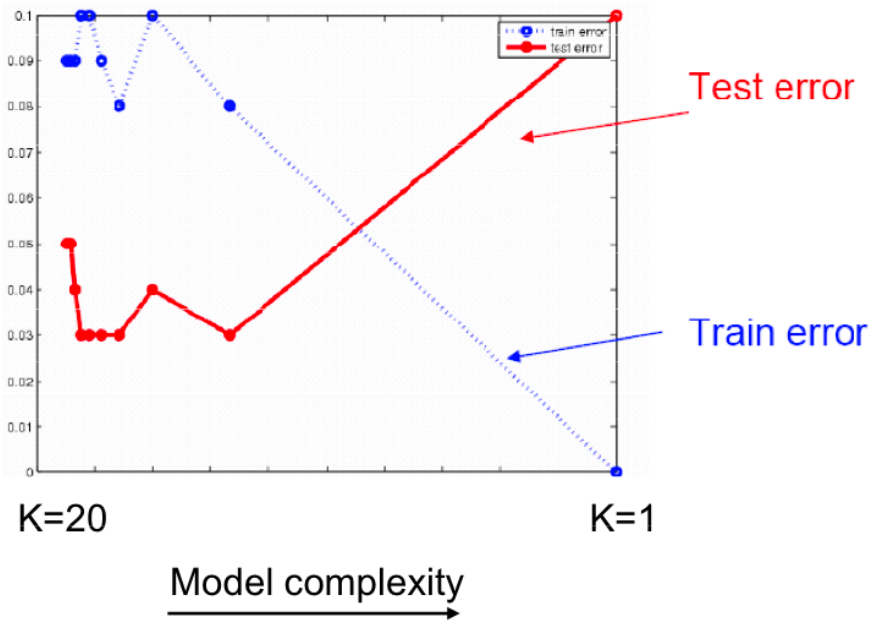


K=15



K-NN: issues to keep in mind

- Choosing the value of k:
  - If too small, sensitive to noise points
  - If too large, neighborhood may include points from other classes
  - Solution: cross validate!



Setting Hyperparameters

Idea #1: Choose hyperparameters that work best on the data

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BAD: K = 1 always works perfectly on training data

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Idea #2: Split data into **train** and **test**, choose hyperparameters that work best on test data

Setting Hyperparameters

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Idea #2: Split data into **train** and **test**, choose hyperparameters that work best on test data

BAD: No idea how algorithm will perform on new data

Slide composited from Andrej Karpathy and Fei-Fei Li http://vision.stanford.edu/teaching/cs231n/

Setting Hyperparameters

Idea #1: Choose hyperparameters that work best on the data

BAD: K = 1 always works perfectly on training data

Idea #2: Split data into **train** and **test**, choose hyperparameters that work best on test data

BAD: No idea how algorithm will perform on new data

Idea #3: Split data into **train**, **val**, and **test**; choose hyperparameters on val and evaluate on test

Better!

Slide composited from Andrej Karpathy and Fei-Fei Li http://vision.stanford.edu/teaching/cs231n/

Setting Hyperparameters

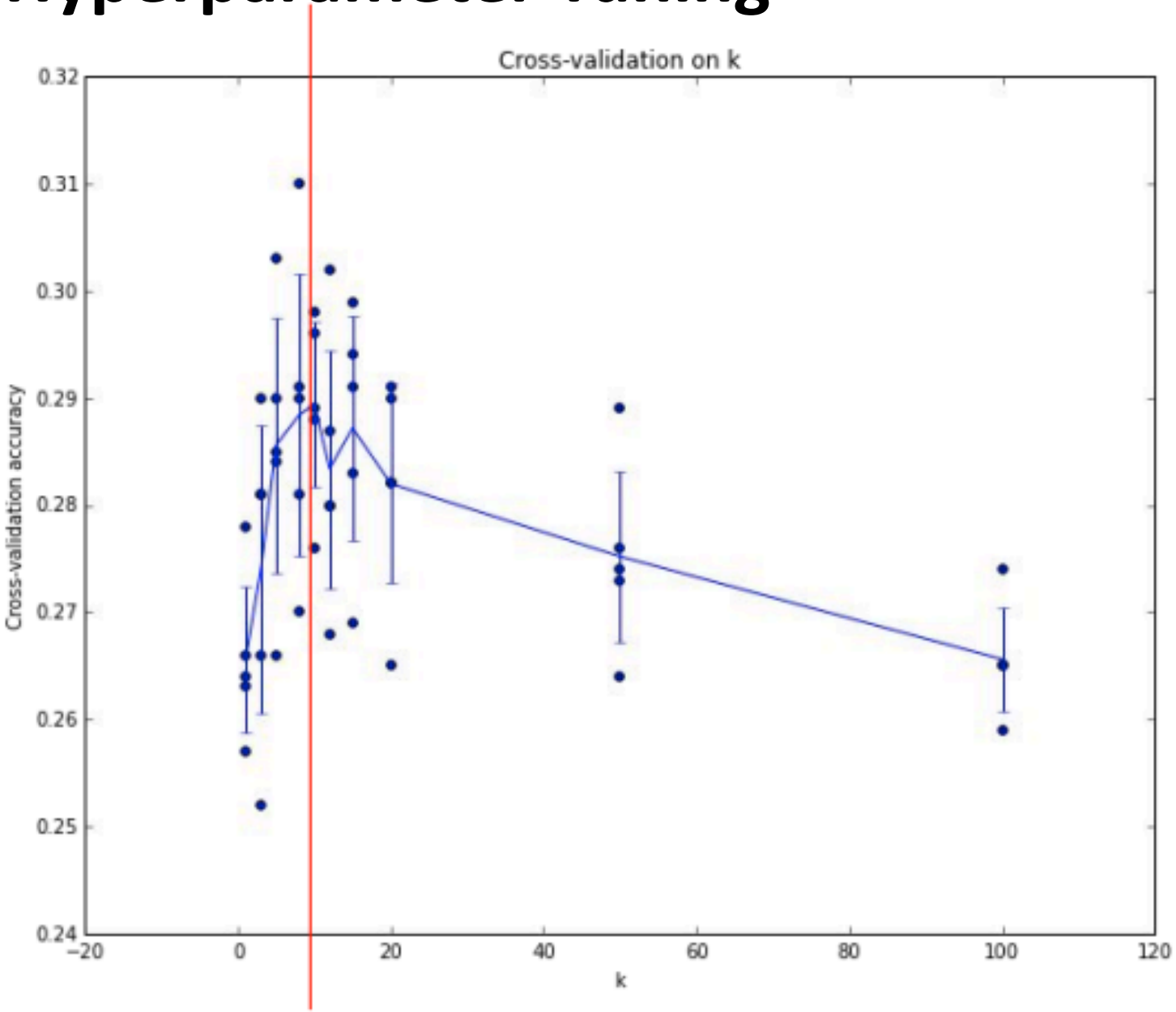
Your Dataset

Idea #4: **Cross-Validation**: Split data into **folds**,
try each fold as validation and average the results

fold 1	fold 2	fold 3	fold 4	fold 5	test
fold 1	fold 2	fold 3	fold 4	fold 5	test
fold 1	fold 2	fold 3	fold 4	fold 5	test

Useful for small datasets, but not used too frequently in deep learning

Hyperparameter Tuning



Example of
5-fold cross-validation
for the value of **k.**

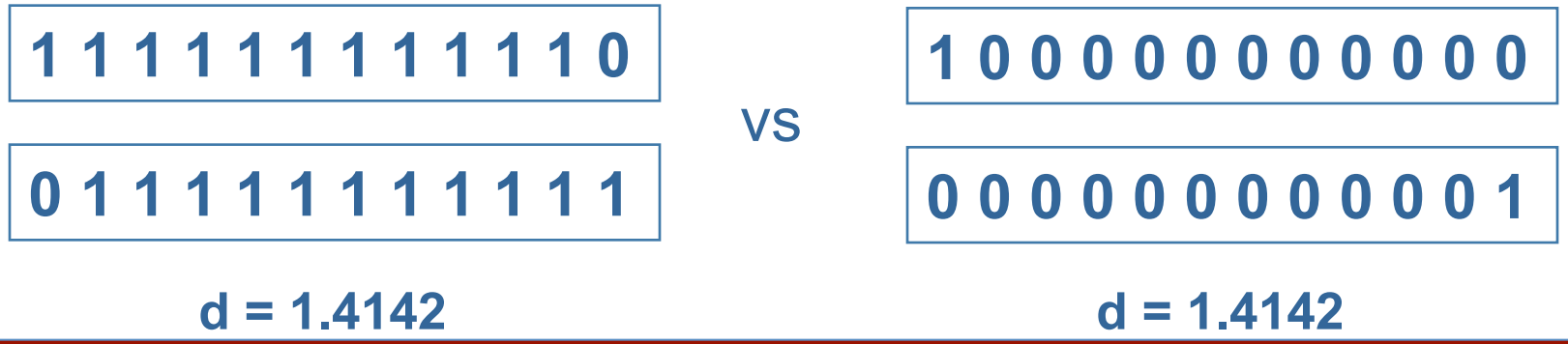
Each point: single
outcome.

The line goes
through the mean, bars
indicated standard
deviation

(Seems that k ~= 7 works best
for this data)

K-NN: issues to keep in mind

- Choosing the value of k:
  - If too small, sensitive to noise points
  - If too large, neighborhood may include points from other classes
  - Solution: cross validate!
- Can produce counter-intuitive results (using Euclidean measure)



K-NN: issues to keep in mind

- Choosing the value of k:
  - If too small, sensitive to noise points
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  - Solution: cross validate!
- Can produce counter-intuitive results (using Euclidean measure)
  - Solution: normalize the vectors to unit length

1 1 1 1 1 1 1 1 1 1 1 0

0 1 1 1 1 1 1 1 1 1 1 1

d = 1.4142

vs

1 0 0 0 0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0 0 0 0 1

d = 1.4142

K-NN: issues to keep in mind

- Choosing the value of k:
  - If too small, sensitive to noise points
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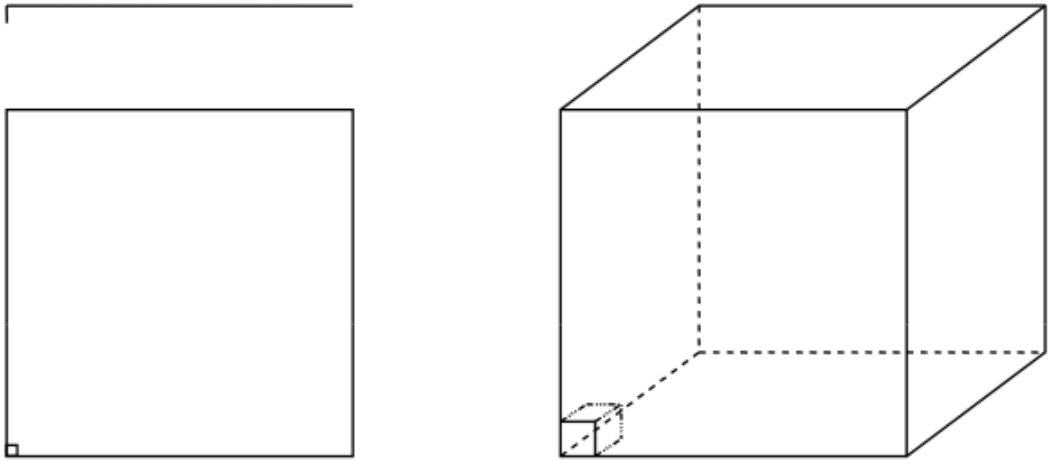
  - Solution: normalize the vectors to unit length
- Curse of Dimensionality

Curse of dimensionality

- Assume 5000 points uniformaly distributed in the unit hypercube and we want to apply 5-NN. Suppose our query point is at the origin.
  - In 1-dimension, we must go a distance of 5/5000=0.001 on the average to capture 5 nearest neighbors.
  - In 2 dimensions, we must go $\sqrt{0.001}$ to get a square that contains 0.001 of the volume.
  - In d dimensions, we must go $(0.001)^{1/d}$



K-NN: issues to keep in mind

- Choosing the value of k:
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  - If too large, neighborhood may include points from other classes
  - Solution: cross validate!
- Can produce counter-intuitive results (using Euclidean measure)
  - Solution: normalize the vectors to unit length
- Curse of Dimensionality
  - Solution: no good one

Many classifiers to choose from

- **K-nearest neighbor**
- SVM
- Neural networks
- Naïve Bayes
- Bayesian network
- Logistic regression
- Randomized Forests
- Boosted Decision Trees
- RBMs
- Etc.

Which is the best one?

Slide credit: D. Hoiem

Generalization

Training set (labels known)

Test set (labels unknown)

- How well does a learned model generalize from the data it was trained on to a new test set?

Slide credit: L. Lazebnik

Generalization

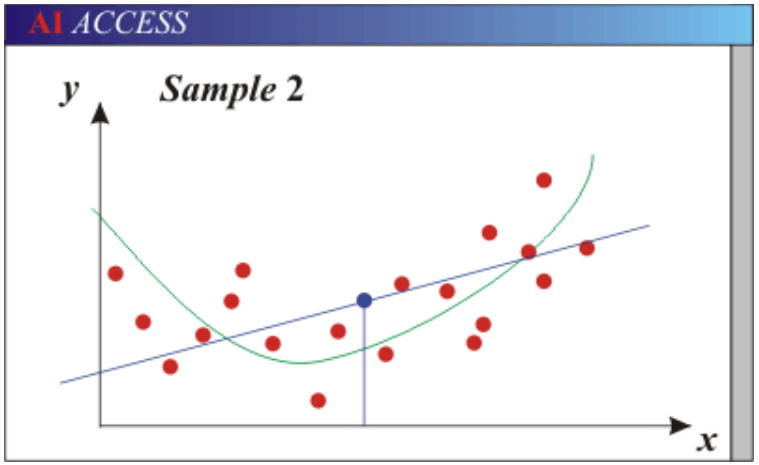
- Components of generalization error
  - **Bias:** how much the average model over all training sets differ from the true model?
    - Error due to inaccurate assumptions/simplifications made by the model
  - **Variance:** how much models estimated from different training sets differ from each other
- **Underfitting:** model is too "simple" to represent all the relevant class characteristics
  - High bias and low variance
  - High training error and high test error
- **Overfitting:** model is too "complex" and fits irrelevant characteristics (noise) in the data
  - Low bias and high variance
  - Low training error and high test error

Slide credit: L. Lazebnik

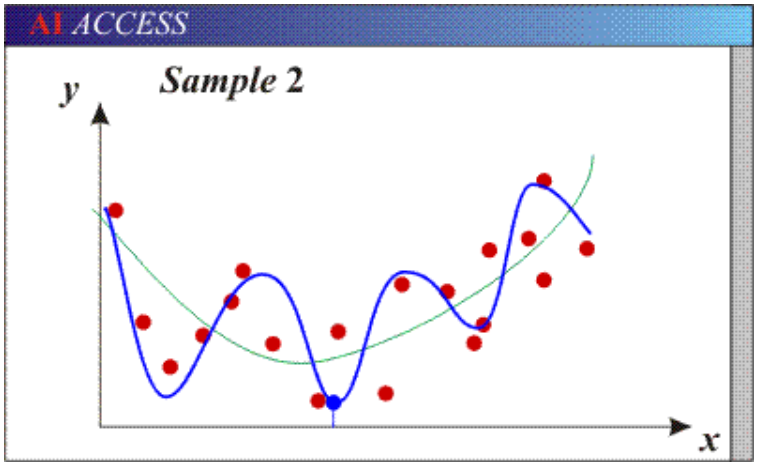
No Free Lunch Theorem

Slide credit: D. Hoiem

Bias-Variance Trade-off



- Models with too few parameters are inaccurate because of a large bias (not enough flexibility).



- Models with too many parameters are inaccurate because of a large variance (too much sensitivity to the sample).

Slide credit: D. Hoiem

technical note

Remember…

- No classifier is inherently better than any other: you need to make assumptions to generalize

- Three kinds of error
  - Inherent: unavoidable
  - Bias: due to over-simplifications
  - Variance: due to inability to perfectly estimate parameters from limited data

Slide credit: D. Hoiem

How to reduce variance?

- Choose a simpler classifier
- Regularize the parameters
- Get more training data

Slide credit: D. Hoiem

Last remarks about applying machine learning methods to object recognition

- There are machine learning algorithms to choose from
- Know your data:
  - How much supervision do you have?
  - How many training examples can you afford?
  - How noisy?
- Know your goal (i.e. task):
  - Affects your choices of representation
  - Affects your choices of learning algorithms
  - Affects your choices of evaluation metrics
- Understand the math behind each machine learning algorithm under consideration!

What we will learn today?

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- K-nearest neighbor algorithm
- A simple Object Recognition pipeline

Object recognition: a classification framework

- Apply a prediction function to a feature representation of the image to get the desired output:

f() = “apple”

f() = “tomato”

f() = “cow”

Dataset: ETH-80, by B. Leibe Slide credit: L. Lazebnik

A simple pipeline

Training

Training Images

Training Labels

Image Features

Training

Learned Classifier

Testing

Test Image

Image Features

Learned Classifier

Prediction

Dataset: ETH-80, by B. Leibe Slide credit: D. Hoiem, L. Lazebnik

A simple pipeline

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Learned Classifier

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Test Image

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Learned Classifier

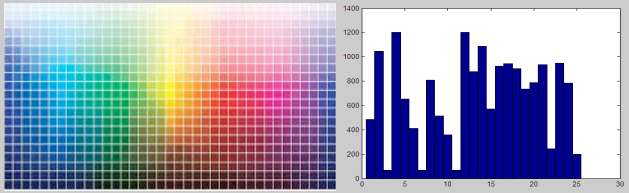
Prediction

Dataset: ETH-80, by B. Leibe Slide credit: D. Hoiem, L. Lazebnik

Image features

Input image

Color: Quantize RGB values



Invariance?

? Translation

? Scale

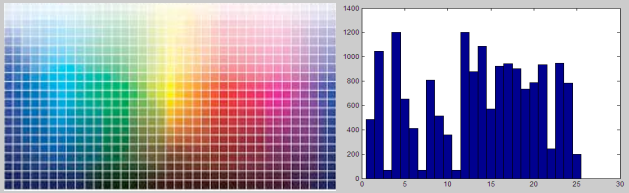
? Rotation

? Occlusion

Image features

Input image

Color: Quantize RGB values



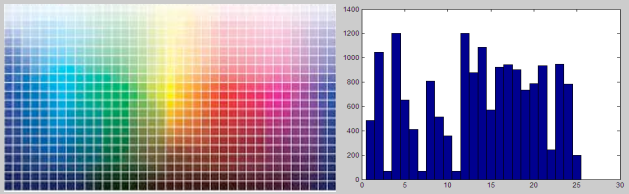
Invariance?

- Translation
- ? Scale
- Rotation (in-planar)
- Occlusion

Image features

Input image

Color: Quantize RGB values



Invariance?
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Global shape: PCA space

Invariance?
- ? Translation
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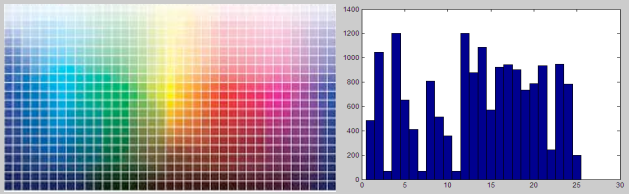

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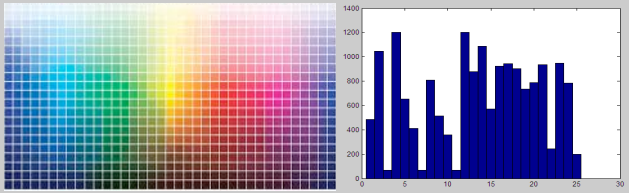

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Global shape: PCA space

Invariance?
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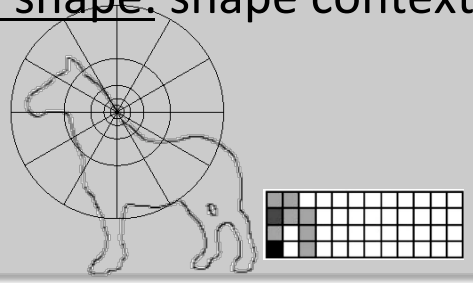
Local shape: shape context



Invariance?
- ? Translation
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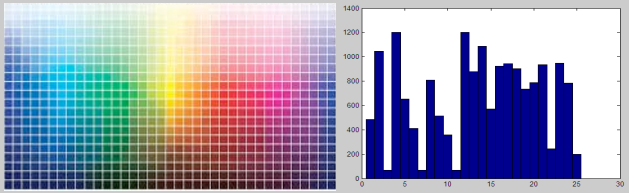
Image features

Input image

Color: Quantize RGB values



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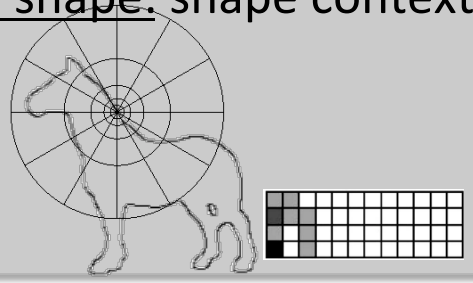
- Occlusion

Local shape: shape context

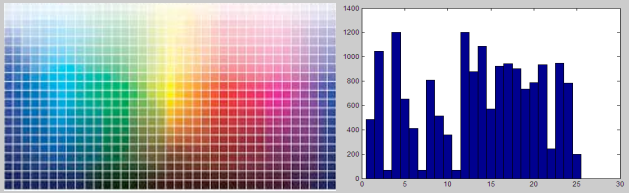


Invariance?
- Translation
- Scale
- ? Rotation (in-planar)
- Occlusion

Image features

Input image

Color: Quantize RGB values



Invariance?
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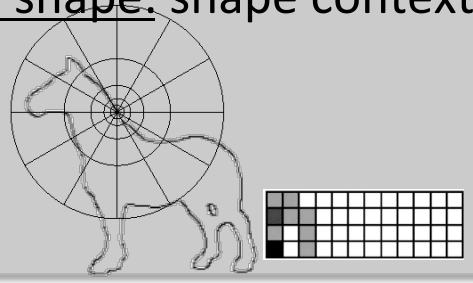
- Rotation
- Occlusion

Global shape: PCA space

Invariance?
- Translation
- ? Scale
- Rotation
- Occlusion

Local shape: shape context



Invariance?
- Translation
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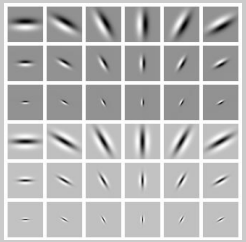
- Occlusion

Texture: Filter banks



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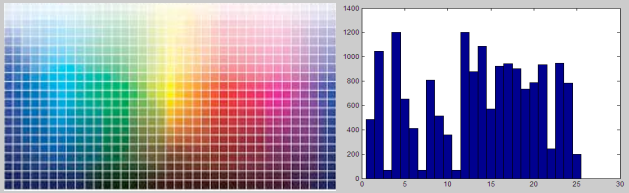

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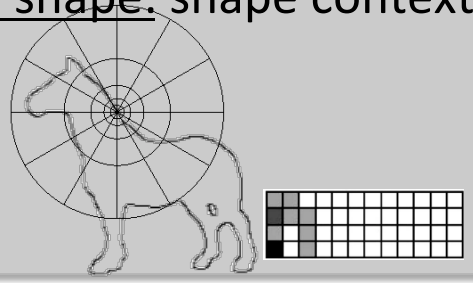

Invariance?
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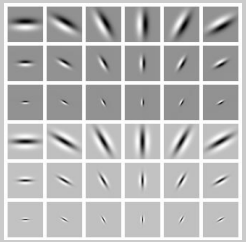
Texture: Filter banks



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A simple pipeline

Training

Training Images

Training Labels

Image Features

Training

Learned Classifier

Testing

Test Image

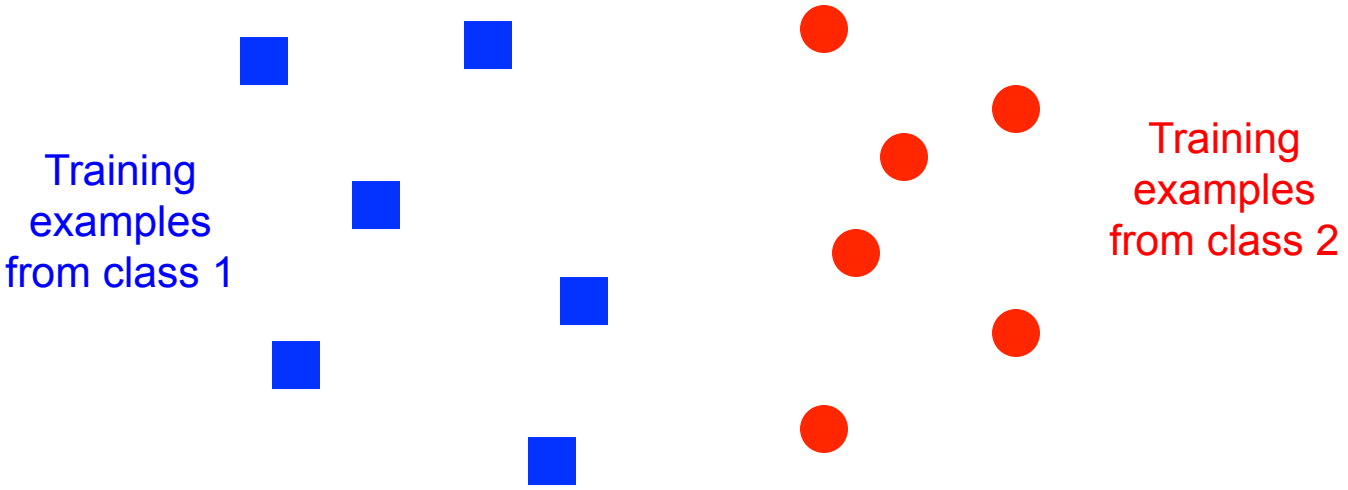
Image Features

Learned Classifier

Prediction

Dataset: ETH-80, by B. Leibe Slide credit: D. Hoiem, L. Lazebnik

Classifiers: Nearest neighbor



Slide credit: L. Lazebnik

A simple pipeline

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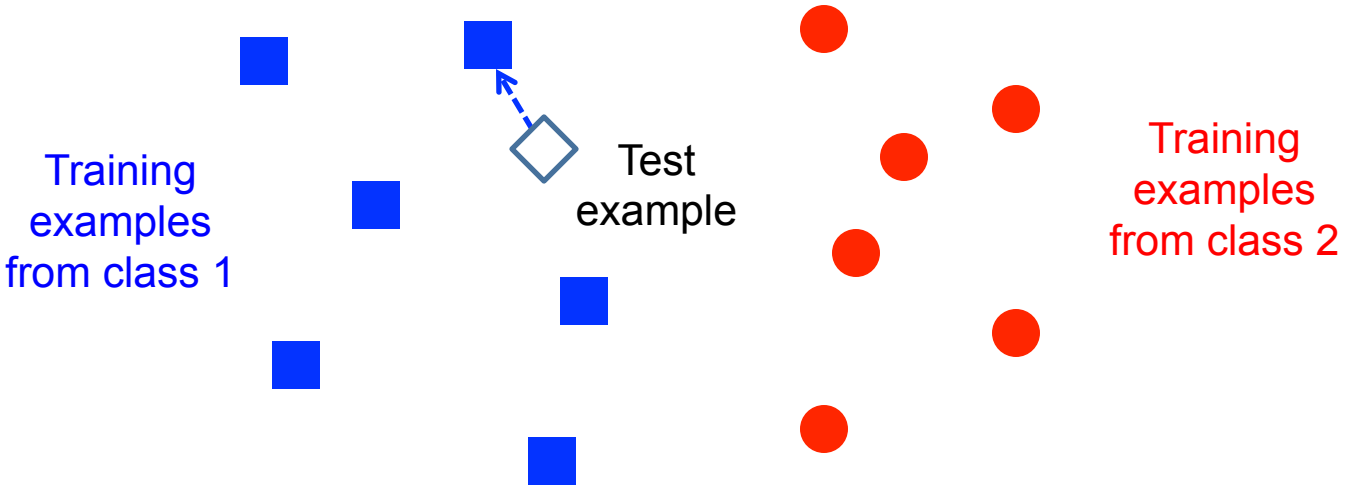

Slide credit: L. Lazebnik

Results

	Color	$D_x D_y$	Mag-Lap	PCA Masks	PCA Gray	Cont. Greedy	Cont. DynProg	Avg.
apple	57.56%	**85.37%**	80.24%	78.78%	**88.29%**	77.07%	76.34%	77.66%
pear	66.10%	90.00%	85.37%	**99.51%**	**99.76%**	90.73%	91.71%	89.03%
tomato	**98.54%**	94.63%	**97.07%**	67.80%	76.59%	70.73%	70.24%	82.23%
cow	86.59%	82.68%	**94.39%**	75.12%	62.44%	86.83%	86.34%	82.06%
dog	34.63%	62.44%	74.39%	72.20%	66.34%	**81.95%**	**82.93%**	67.84%
horse	32.68%	58.78%	70.98%	77.80%	77.32%	**84.63%**	**84.63%**	69.55%
cup	79.76%	66.10%	77.80%	**96.10%**	**96.10%**	**99.76%**	**99.02%**	87.81%
car	62.93%	**98.29%**	77.56%	**100.0%**	**97.07%**	**99.51%**	**100.0%**	90.77%
total	64.85%	79.79%	82.23%	83.41%	82.99%	86.40%	86.40%	80.87%

Dataset: ETH-80, by B. Leibe, 2003

Results

Category	Primary feature(s)	Secondary feature(s)
apple	PCA Gray	Texture $D_x D_y$
pear	PCA Gray / Masks	
tomato	Color	Texture Mag-Lap
cow	Texture Mag-Lap	Contour / Color
dog	Contour	
horse	Contour	
cup	Contour	PCA Gray / Masks
car	PCA Masks / Contour	Texture $D_x D_y$

Dataset: ETH-80, by B. Leibe, 2003

What we have learned today?

- Introduction
- K-nearest neighbor algorithm
- A simple Object Recognition pipeline