

$$\begin{aligned}
 \text{E step: For } \{HHH\}, W_0 &= \frac{k \cdot P_0^3}{k \cdot P_0^3 + (1-k) \cdot P_1^3} \\
 &= \frac{0.5 \times 0.6^3}{0.5 \times 0.6^3 + 0.5 \times 0.1^3} \\
 &= \frac{1080}{1085} \sim 0.9954
 \end{aligned}$$

$$\Rightarrow W_1 = 1 - W_0 = \frac{5}{1085} \sim 0.0046$$

$$\begin{aligned}
 \text{For } \{HHT\}, W_0 &= \frac{k \cdot P_0^2 \cdot (1-P_0)}{k \cdot P_0^2 \cdot (1-P_0) + (1-k) \cdot P_1^2 \cdot (1-P_1)} \\
 &= \frac{0.5 \times 0.6^2 \times 0.4}{0.5 \times 0.6^2 \times 0.4 + 0.5 \times 0.1^2 \times 0.9} \\
 &= \frac{720}{765} \sim 0.9412
 \end{aligned}$$

$$\Rightarrow W_1 = 1 - W_0 = \frac{45}{765} \sim 0.0588$$

$$\begin{aligned}
 \text{For } \{TTT\}, W_0 &= \frac{k \cdot (1-P_0)^3}{k \cdot (1-P_0)^3 + (1-k) \cdot (1-P_1)^3} \\
 &= \frac{0.5 \times 0.4^3}{0.5 \times 0.4^3 + 0.5 \times 0.9^3} \\
 &= \frac{320}{3965} \sim 0.0807
 \end{aligned}$$

$$\Rightarrow W_1 = 1 - W_0 = \frac{3645}{3965} \sim 0.9193$$

$$M \text{ step: } k = \frac{\frac{1080}{1085} + \frac{720}{765} + \frac{320}{3965}}{3} \sim 0.6724$$

$$p_0 = \frac{0.9954 \times 3 + 0.9412 \times 2}{9 \times 0.6724} \sim 0.8045$$

$$p_1 = \frac{0.0046 \times 3 + 0.0588 \times 2}{0.0046 \times 3 + 0.0588 \times 3 + 0.9193 \times 3} \sim 0.0455$$