# Paraphrase Identification; Numpy; Scikit-Learn

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# Paraphrase Identification

# Paraphrase Identification

- Is a sentence (A) a paraphrase of another sentence (B)?
- Do two tweets contain the same information?
- This is a difficult problem
  - What is a paraphrase?
  - ▶ Do two exact paraphrases even exist? paraphrase ⇔ strong similarity, approximately equal meaning
  - Linguistic variation
  - ▶ Even more difficult in twitter: abbreviations, spelling errors, ...
- Examples:
  - (A) I hate Mario Chalmersdont know why
  - (B) idc idc chalmers be making me mad
  - (A) It fits the larger iPhone 5
  - (B) Should I get the iPhone 5 or an Android

# SemEval-2015 Task 1: Paraphrase Similarity in Twitter

- ca. 19000 tweet pairs annotated with Amazon Mechanical Turk
- Binary classification: Pair is paraphrase (True) or not (False)
- Brainstorming: good features for recognizing paraphrases?

# Strong baseline features<sup>1</sup>

- Word overlap.
  - Most simple form: Number common words that occur in both tweets (ignore frequency).
    - "overlap"
  - Needs some normalization (so that there is no bias for longer tweets).
  - Simple solution: Extra feature for number of unique tokens in text1 and text2.

#### "union"

- Ngram overlap.
  - Accounts for some ordering information.
  - Otherwise same approach as for word overlap.
  - 3-grams perform well for this task
- Word-pair features
  - What if paraphrases use different, but semantically similar words?
  - Learn equivalences from tweets in training data!
  - ▶ Features for combinations: Word from text1 with word from text2.

<sup>&</sup>lt;sup>1</sup>Thanks to Kevin Falkner for providing extensive feature analysis. (♣) (♣) (♣) (♣)

# Example: feature representation

- (A) happy Memorial Day have a happy weekend
- (B) wishing everyone a happy Memorial Day

```
{"word_overlap":4,
"three_gram_overlap":1,
"word_union":8,
"threegram_union":8,
"happy#wishing":1,
"memorial#everyone":1,
"happy#happy":1,
...}
```

#### Implementation

• What is the result of the follwing list comprehension?

```
l=["wishing", "everyone", "a", "happy", "memorial", "day"]
n=2
[l[i:i+n] for i in range(len(1)-n+1)]
```

• How to implement word-pair features?

# Data Representation for Machine Learning

# Data Representation

- Dataset: collection of instances
- Design matrix

$$\boldsymbol{X} \in \mathbb{R}^{n \times m}$$

- n: number of instances
- m: number of features (also called feature space)
- For example:  $X_{i,j}$  count of feature j (e.g. a stem form) in document i.
- Unsupervised learning:
  - Model X, or find interesting properties of X.
  - Training data: only X.
- Supervised learning:
  - Predict specific additional properties from X.
  - ▶ Training data: Label vector  $\mathbf{y} \in \mathbb{R}^n$  (or label matrix  $\mathbf{Y} \in \mathbb{R}^{n \times k}$ ) together with  $\mathbf{X}$



ullet Use matrix  $oldsymbol{X}$  and vector  $oldsymbol{y}$  to stack instances on top of each other.

$$\mathbf{X} = \begin{bmatrix} x_{12} & x_{13} & \dots & x_{1n} \\ x_{22} & x_{23} & \dots & x_{2n} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ x_{m2} & x_{m3} & \dots & x_{mn} \end{bmatrix} \quad \mathbf{y} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_m \end{bmatrix}$$

Binary classification:

$$\mathbf{y} = \begin{bmatrix} 0 \\ 1 \\ \vdots \\ 0 \end{bmatrix} \dots \text{ or } \dots \begin{bmatrix} -1 \\ 1 \\ \vdots \\ -1 \end{bmatrix}$$

• Multi-class classification (one-hot-encoding):

$$\mathbf{Y} = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ \vdots & & & \\ 0 & 1 & 0 \end{bmatrix}$$

# Data Representation

- For performance reasons, machine-learning toolkits (scikit-learn, Keras, ...) use matrix representations (rather than e.g. string-to-count dictionaries).
- These matrix classes usually contain efficient implementations of
  - ▶ mathematical operations (matrix multiplication, vector addition ...)
  - data access and transformation (getting a certain row/column, inverting a matrix)
- What would be an appropriate underlying data-structures for the following feature sets:
  - $\blacktriangleright$  Each feature is the grey-scale value of a pixel in a 100  $\times$  100 gray-scale image?
  - ► Each feature is the indicator whether a particular word (vocab size 10000) occurs in a document or not?

# Data Representation

- What would be an appropriate underlying data-structures for the following feature sets:
  - $\blacktriangleright$  Each feature is the grey-scale value of a pixel in a  $100 \times 100$  gray-scale image?
    - Most of the features have a distinct value  $\neq 0$ . The appropriate data structure is similar to a nested list (list-of-lists).  $\Rightarrow$  Numpy Arrays
  - ► Each feature is the indicator whether a particular word (vocab size 10000) occurs in a document or not?
    - Most of the features have a value equal to 0. The appropriate data structure only stores those entries that are different than 0. (E.g with a dictionary: (row, col)  $\rightarrow$  value.)  $\Rightarrow$  SciPy Sparse Matrices

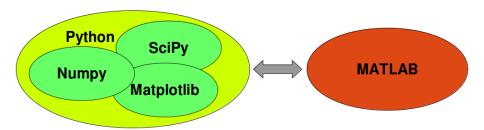
# Introduction to Numpy

# What is NumPy?

- Acronym for "Numeric Python"
- Open source extension module for Python.
- Powerful data structures for efficient computation of multi-dimensional arrays and matrices.
- Fast precompiled functions for mathematical and numerical routines.
- Used by many scientific computing and machine learning packages.
   For example
  - Scipy (Scientific Python): Useful functions for minimization, regression, Fourier-transformation and many others.
  - Similar datastructures exist in *Tensorflow*, *Pytorch*: Deep learning, mimimization of custom objective functions, auto-gradients.
- Downloading and installing numpy: www.numpy.org

# The Python Alternative to Matlab

- Python in combination with Numpy, Scipy and Matplotlib can be used as a replacement for MATLAB.
- Matplotlib provides MATLAB-like plotting functionality.



# Comparison between Core Python and Numpy

- "Core Python": Python without any special modules, i.e. especially without NumPy.
- Advantages of Core Python:
  - high-level number objects: integers, floating point
  - containers: lists with cheap insertion and append methods, dictionaries with fast lookup
- Advantages of using Numpy with Python:
  - array oriented computing
  - efficiently implemented multi-dimensional arrays
  - designed for scientific computation

# A simple numpy Example

- NumPy needs to be imported. Convention: use short name np import numpy as np
- Turn a list of temperatures in Celsius into a one-dimensional numpy array:

```
>>> cvalues = [25.3, 24.8, 26.9, 23.9]

>>> np.array(cvalues)

[ 25.3 24.8 26.9 23.9]
```

Turn temperature values into degrees Fahrenheit:

Compare to using core python only:

>>> [ 
$$x*9/5 + 32$$
 for x in cvalues] [77.54, 76.64, 80.42, 75.02]



# Creation of evenly spaced values (given stepsize)

- Useful for plotting: Generate values for x and compute y = f(x)
- Syntax:

```
arange([start ,] stop[, step ,], dtype=None)
```

- Similar to core python range, but returns ndarray rather than a list iterator.
- Defaults for start and step: 0 and 1
- dtype: If it is not given, the type will be automatically inferred from the other input arguments.
- Don't use non-integer step sizes (use linspace instead).
- Examples:

```
>>> np.arange(3.0)
array([ 0., 1., 2.])
>>> np.arange(1,5,2)
array([1, 3])
```

# Creation of evenly spaced values (given number of values)

```
\label{linspace} \begin{array}{ll} \mbox{linspace(start , stop , num=50, endpoint=True , } \\ \mbox{retstep=False)} \end{array}
```

- Creates ndarray with num values equally distributed between start (included) and stop (excluded).
- If endpoint=True, the end point is included additionally.

```
>>> np.linspace (1, 3, 5) array ([ 1. , 1.5, 2. , 2.5, 3. ]) 
>>> np.linspace (1, 3, 4, endpoint=False) array ([ 1. , 1.5, 2. , 2.5])
```

• If retstep=True, the stepsize is returned additionally:

```
>>> np.linspace(1, 3, 4, endpoint=False, \
    retstep=True)
(array([ 1. , 1.5, 2. , 2.5]), 0.5)
```

#### Exercise

Compare the speed of vector addition in core Python and Numpy

#### Multidimensional Arrays

- NumPy arrays can be of arbitrary dimension.
- 0 dimensions (scalar): np.array(42)
- 1 dimension (vector): np.array([3.4, 6.9, 99.8, 12.8])
- 2 dimensions (matrix):

```
np.array([ [3.4, 8.7, 9.9], [1.1, -7.8, -0.7], [4.1, 12.3, 4.8])
```

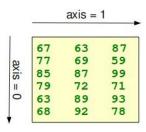
• 3 or more dimensions (tensor):

#### Question

• When can a 3 dimensional array be an appropriate representation?

# Shape of an array

```
>>> x = np.array([ [67, 63, 87],
... [77, 69, 59],
... [85, 87, 99],
... [79, 72, 71],
... [63, 89, 93],
... [68, 92, 78]])
>>> np.shape(x)
(6, 3)
```



# Changing the shape

• reshape creates new array:

```
>>> a = np.arange(12).reshape(3, 4)

>>> a

array([[ 0, 1, 2, 3],

      [ 4, 5, 6, 7],

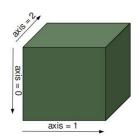
      [ 8, 9, 10, 11]])
```

Changing shape value (for existing array):

```
>>> a.shape = (2, 6)
>>> a
array([[ 0, 1, 2, 3, 4, 5],
       [ 6, 7, 8, 9, 10, 11]])
```

- Obviously, product of shape sizes must match number of elements!
- If a dimension is given as -1 in a reshaping operation, the other dimensions are automatically calculated.

# Shape of 3D Array



# Transposing an Array

• 2D case:

- Multidimensional case:
  - a.transpose(...) takes tuple of indices, indicating which axis of the old (input) array is used for each axis of the new (output) array.
  - D example:
    b = a.transpose(1,0,2)
  - $\Rightarrow$  axis 1 in a is used as axis 0 for b, axis 0 (a) becomes 1 (b), and axis 2 (a) stays axis 2 (b).

#### **Basic Operations**

• By default, arithmetic operators on arrays apply *elementwise*:

```
>>> a = np.array( [20,30,40,50] )

>>> b = np.array( [0,1,2,3] )

>>> c = a-b

array([20, 29, 38, 47])

>>> b**2

array([0, 1, 4, 9])

>>> a<35

array([ True, True, False, False], dtype=bool)
```

• In particular, the elementwise multiplication ...

```
>>> a * b
array([ 20, 60, 120, 200])
```

• ... is not to be confused with the *dot product*:

# **Unary Operators**

Numpy implements many standard unary (elementwise) operators:

```
>>> np.exp(b)
>>> np.sqrt(b)
>>> np.log(b)
```

• For some operators, an axis can be specified:

#### Indexing elements

• Indexing single elements:

```
>>> B = np.array([ [[111, 112], [121, 122]],
... [[211, 212], [221, 222]],
... [[311, 312], [321, 322]] ])
>>> B[2][1][0]
321
>>> B[2,1,0]
321
```

Indexing entire sub-array:

Indexing starting from the end:

$$>>> B[-1,-1]$$
 array ([321, 322])



# Indexing with Arrays/Lists of Indices

```
>>> a = np.arange(12)**2

>>> i = np.array([1,1,3,8,5])

>>> # This also works:

>>> # i = [1,1,3,8,5]

>>> a[i]

array([1, 1, 9, 64, 25])
```

# Indexing with Boolean Arrays

Boolean indexing is done with a boolean matrix of the *same shape* (rather than of providing a list of integer indices).

```
>>> a = np.arange(12).reshape(3,4)
>>> b = a > 4
array ([[False, False, False, False],
       [False, True, True, True],
       [ True, True, True, True]], dtype=bool)
>>> a[b]
array ([ 5, 6, 7, 8, 9, 10, 11])
>>> a[b] = 0
array([[0, 1, 2, 3],
     [4, 0, 0, 0],
       [0, 0, 0, 0]
```

#### Slicing

- Syntax for slicing lists and tuples can be applied to multiple dimensions in NumPy.
- Syntax:

```
A[start0:stop0:step0, start1:stop1:step1, ...]
```

• Example in 1 dimension:

```
>>> S = np.array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> S[3:6:2]
array([3, 5])
>>> S[:4]
array([0, 1, 2, 3])
>>> S[4:]
array([4, 5, 6, 7, 8, 9])
>>> S[:]
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

# Slicing 2D

$$A = np.arange(25).reshape(5,5)$$
  
 $B = A[:3,2:]$ 

$$B = A[3:,:]$$

$$X = np.arange(28).reshape(4,7)$$
  
 $V = X[...2 ...3]$ 

$$Y = X[::2, ::3]$$

$$Y = X[:, ::3]$$









# Slicing: Caveat

 Slicing only creates a new view: the underlying data is shared with the original array.

```
>>> A = np.array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9]) 
>>> S = A[2:6] 
>>> S[0] = 22 
>>> S[1] = 23 
>>> A 
array([ 0, 1, 22, 23, 4, 5, 6, 7, 8, 9])
```

If you want a deep copy that does not share elements with A, use:
 A[2:6].copy()

#### Quiz

• What is the value of b?

```
>>> a = np.arange(4)
>>> b = a[:]
>>> a *= b
```

# Arrays of Ones and of Zeros

```
>>> np.ones((2,3))
array([[ 1., 1., 1.],
      [1., 1., 1.]
>>> a = np.ones((3,4),dtype=int)
array ([[1, 1, 1, 1],
       [1, 1, 1, 1],
       [1, 1, 1, 1]
>>> np.zeros((2,4))
array([[ 0., 0., 0., 0.],
       [0., 0., 0.. 0.11)
>>> np.zeros_like(a)
array([[0, 0, 0, 0].
       [0, 0, 0, 0]
       [0.0.0.0]
```

#### Creating Random Matrices

• Array of floats uniformly drawn from the interval [0, 1):

• Generate floats drawn from standard normal distribution  $\mathcal{N}(0,1)$ :

- For repeatability of your experiment, initialize the seed at the beginning of your script:
  - $\triangleright$  >>> np.random.seed = 0
  - Otherwise, it will be initialized differently at every run (from system clock).
  - ▶ If you use core python random numbers, also initialize the seed there:

```
>>> import random >>> random.seed (9001)
```

#### Creating Diagonal Matrices

- eye(N, M=None, k=0, dtype=float)
  - N Number of rows.
  - M Number of columns.
  - k Diagonal position.
    - 0: main diagonal, starting at (0,0)+n, -n: move diagonal n up/down

dtype Data type (e.g. int or float)



•  $\Rightarrow$  To create an identity matrix (symmetric  $N=M,\ k=1$ ) the size N is the only argument.

#### Iterating

Iterating over rows:

```
>>> for row in b:
... print(row)
...
[0 1 2 3]
[10 11 12 13]
[20 21 22 23]
[30 31 32 33]
[40 41 42 43]
```

•  $\Rightarrow$  but (!) prefer matrix operations over iterating, if possible.

## Stacking of arrays

Vertical stacking:

```
>>> a = np.array([[1,2],[3,4]])

>>> b = np.array([[11,22],[33,44]])

>>> np.vstack((a,b))

array([[1, 2],

       [3, 4],

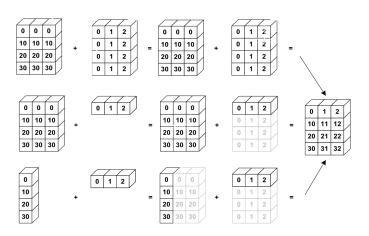
       [11, 22],

       [33, 44]])
```

Horizontal stacking:

#### **Broadcasting**

Operations can work on arrays of different sizes if Numpy can **transform** them so that they all have the **same size**!

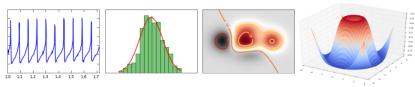


#### Plotting data

- Often it is a good idea to plot some properties of the data.
  - Verify expectations that you have about the data.
  - ► Spot trends, maxima/minima, (ir-)regularities and outliers.
  - similiratities / dissimilarities between two data sets.
- Recommended package: Matplotlib/Pyplot

#### **Pyplot**

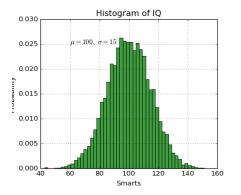
Plotting data and functions with Python.



- Package of the matplotlib library.
- Uses numpy data structures
- Inspired by the matlab plotting commands
- Import pyplot as: import matplotlib.pyplot as plt

#### Example: Histograms

- Show the empirical distribution of one variable.
- Frequency of values with equally-spaced intervals.



x = 100 + 15 \* np.random.randn(10000)
plt.hist(x, 50)

#### Ressources

• NumPy Quickstart:
http:
//docs.scipy.org/doc/numpy-dev/user/quickstart.html

• http://www.python-course.eu/numpy.php

# Scipy Sparse Matrices

#### Scipy Sparse Matrices

- SciPy is another package of the Python scientific computing stack. (NumPy+SciPy+Matplotlib~Matlab)
- scipy.sparse contains a range of sparse matrix implementations
  - Different underlying datastructures
  - slightly different use-cases
- All implementations
  - inherit from the same base class
  - provide basic matrix operations, e.g.:

get_shape()	Get shape of a matrix.
getnnz()	Number of stored values, including
	explicit zeros.
transpose ([axes, copy])	Reverses the dimensions of the sparse
	matrix.
$+$ , $_{-add_{-}}(other)$	Add two matrices.
*,mul(other), dot(other)	Matrix (vector) multiplication
	4 11 12 42 14 14 14 14 14 14 14 14 14 14 14 14 14

# Types of Sparse Matrices

scipy . sparse . csr_matrix	Compressed Sparse Row matrix (default).
	Very efficient format for arithmetic operations.
scipy . sparse . lil_matrix	Row-based linked list sparse matrix.
	Efficient changes to matrix structure.
	Less efficient for arithmetic.
scipy . sparse . coo_matrix	A sparse matrix in COOrdinate format.
	Triples of row, column and value.
scipy . sparse . dia_matrix	Sparse matrix with DIAgonal storage

#### What is the result?

```
import numpy as np
from scipy.sparse import csr_matrix
A = csr_matrix([[1, 2, 0], [0, 0, 3], [4, 0, 5]])
v = np.array([1, 0, -1])
A.dot(v)
```

# **Memory Saving**

- Given:
  - ▶ 1000 docs
  - ▶ 100 unique words per doc
  - ► 10000 vocabulary size
- What is the expected percentage of memory used by sparse matrix (compared to dense)?

#### Time Saving

```
from timeit import default_timer as timer
from scipy import sparse
import numpy as np
rnd = np.random.RandomState(seed=123)
X = \text{rnd.uniform(low=0.0, high=1.0, size=(200000, 1000))}
v = rnd.uniform(low=0.0, high=1.0, size=(1000,1))
X[X<0.99]=0
v [v < 0.99] = 0
X_csr = sparse.csr_matrix(X)
v_csr = sparse.csr_matrix(v)
start = timer()
X 2 = X.dot(v)
time_dense = timer() - start
start = timer()
X_2 = X_csr.dot(v_csr)
time_sparse = timer() - start
```

 $\Rightarrow$  0.16 seconds (time\_dense) vs. 0.01 seconds (time\_sparse)

# Scikit-learn Data Structures

 Now that we know about Numpy (dense) matrices, and Scipy (sparse) matrices, let's see how we can use them for machine learning with Scikit-learn.

#### Scikit-learn Vectorizers

- For efficiency, Scikit-learn uses matrices for its algorithms.
- However, data is often present in different forms (text; dictionaries: feature → count; ...)
- Scikit-learn provides Vectorizers to convert other data-types into matrices.
- A vectorizer object provides a mapping (e.g. from vocabulary to column indices): it is important that the same mapping is used for training, test and dev data!
- For most vectorizers, one can choose whether Dense or Sparse representation is preferred.

#### Loading features from dicts

- DictVectorizer can be used to convert feature arrays represented as lists of dict objects to the NumPy/SciPy representation
- Input: one dict per instance (feature counts)
  - key: feature
  - value: observed value of that feature
- Output: Design matrix
- The vectorizer constructs a feature map use the same feature map for new data! (I.e. do not create a new feature map).
- Values of the dictionary can be:
  - Numerical: the numarical value is stored in the resulting matrix in the column for that feature.
  - **Boolean**: two columns are created in the matrix for that feature.
  - String: several columns are created in the matrix, one for each possible value for that feature.

#### DictVectorizer: Example

```
>>> measurements = \Gamma
... {'city': 'Dubai', 'temperature': 33.},
... {'city': 'London', 'temperature': 12.},
... {'city': 'San Fransisco', 'temperature': 18.},
. . . ]
>>> from sklearn.feature_extraction import DictVectorizer
>>> vec = DictVectorizer()
>>> vec.fit_transform(measurements).toarray()
array([[ 1., 0., 0., 33.],
      [ 0., 1., 0., 12.],
      [ 0., 0., 1., 18.]])
>>> vec.get_feature_names()
['city=Dubai', 'city=London', 'city=San Fransisco', 'temperature']
```

#### **DictVectorizer**

- Creates sparse matrices by default, can be changed to dense.
- fit\_transform (some\_dict) creates the mapping to matrix columns
- Apply to new dictionaries with fit\_transform ( other\_dict )

## Feature hashing

- Hash function (not a rigorous definition, but sufficient for our purposes):
  - ► Function that maps every object from input space to an integer in pre-specified range
  - Regularities (e.g. sequential order) from input space are not preserved in output space, assignment looks random (for properties of interest)
- Hash collision: Two different values from input space are mapped to same output
- Applications of hash functions?

#### Feature hashing

- Large amounts of features also means many model parameters to learn and store (no sparsity here)
- One way of fighting amount of features: sort and take most frequent.
- Another way: use hash function to "randomly" group features together
- Hashing trick:
  - Input space: features
  - Output space: columns in design matrix
- FeatureHasher: Vectorizer that uses the hashing trick.
  - ⇒ inverse\_transform is not possible

#### Transforming text into a design matrix

- SciPy provides some functionality to create feature matrices from raw text
  - tokenization
  - lowercasing
  - ngram creation
  - occurrence counting
  - filtering by minimum word length (default=2)
  - filtering by minimum and maximum document frequency.
  - **.**..
- Very convenient!
- Note: you have more control if you create the features yourself and use DictVectorizer

#### **CountVectorizer**

```
>>> from sklearn.feature_extraction.text import CountVectorizer
>>> corpus = [
       'This is the first document.',
... 'This is the second second document.',
... 'And the third one.',
... 'Is this the first document?',
. . . 1
>>> vectorizer = CountVectorizer()
>>> X = vectorizer.fit_transform(corpus)
>>> vectorizer.get_feature_names()
['and', 'document', 'first', 'is', 'one', 'second', 'the', 'third',
 'this'l
>>> X.toarray()
array([[0, 1, 1, 1, 0, 0, 1, 0, 1],
       [0. 1. 0. 1. 0. 2. 1. 0. 1].
       [1, 0, 0, 0, 1, 0, 1, 1, 0].
       [0, 1, 1, 1, 0, 0, 1, 0, 1]], dtype=int64)
```

# CountVectorizer: unigrams, bigrams, document frequency

#### Summary

- Features for Paraphrase identification
  - Number of overlapping words and ngrams
  - Normalization for tweet length
  - Word pair features
- Dense and Sparse Matrices
  - Numpy arrays docs.scipy.org/doc/numpy-dev/user/quickstart.html
  - Scipy sparse matrices docs.scipy.org/doc/scipy-0.18.1/reference/sparse.html
- Scikit-learn Vecorizers
   http://scikit-learn.org/stable/modules/feature\_extraction.html
- Questions?